Characterization of SiC Power Transistors for Power Conversion Circuits Based on C-V Measurement

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## Abstract

Power switching devices are required for power electronics to regulate and distribute the power and energy from power conversion circuits. Silicon carbide (SiC) as a wide band gap semiconductor is the promising material for power switching device applications due to their inherent material characteristics. In present, SiC power transistors, especially SiC power MOSFETs and JFETs, are the most possible power switches for high switching frequency power conversion circuits due to fast turn-off capability. Transient behavior in switching operation of SiC power transistors responds to charge/discharge phenomenon of terminal capacitances in the devices. The differential capacitance in a semiconductor device varies with the applied voltage in accordance with the depleted region thickness.

In this dissertation, we developed the C-V characterization system for high-voltage power transistors, which realizes the selective measurement of a specified capacitance from among several capacitances integrated in one device. Three terminal capacitances are evaluated to specify device characteristics—the capacitance for gate-source, gate-drain, and drain-source. The input, output, and reverse transfer capacitances are also evaluated to assess the switching behavior of the power transistors in the circuit. Next, we characterized the voltage dependence of terminal capacitances of the SiC power MOSFET, lateral-type SiC JFET, and vertical-type SiC JFET, and also characterized the static I-V characteristics of the power devices. Then, we evaluated the switching operation of the power devices with considering the charge/discharge behavior of terminal capacitances of the devices. Their device structures decide the voltage dependence of the capacitance characteristics, so that the C-V characteristics govern their switching behaviors. The results give us a clue to understand the switching dynamics of the power devices. The simulated switching behavior of the power devices is validated with the experimental results. It is clearly shown that the simulated results in switching behavior of the power devices coincided with experimental results suitably.

In the end, we demonstrated the operation of the SiC power MOSFET in a high frequency switching converter circuit for evaluating its performances The experiment results showed smooth waveforms of the current and voltage. Therefore, the SiC power MOSFET can be suitably used in the high frequency switching converter circuit to regulate the output voltage.

**Keywords:** SiC, MOSFET, JFET, C-V characteristics, Switching behavior, Device structure

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# Chapter 1

# Introduction

The purpose of this introductory chapter is to present motivations and overviews of the works done in this dissertation. A more in-depth introduction is given in each of main chapters of this dissertation.

## 1.1 SiC power devices

Silicon carbide (SiC) has several properties such as high breakdown voltage, high temperature operation capability, and high thermal conductivity, making them potentially superior to Silicon (Si) semiconductors and thus making them attractive for power devices [1–5]. Among the other SiC semiconductors, 4H-SiC is the most promising material for power switching device applications due to their inherent material characteristics, quality of the crystal growth, and the maturity of manufacturing process. Some of the electrical and material properties of Si and 4H-SiC are summarized and compared in Tab. 1.1, which are pertinent for power device applications [2,6,7].

For the great advantages of SiC power devices, SiC diodes have studied well [9–13] and Schottky Barrier Diodes (SBDs) made of 4H-SiC with sufficiently high current and voltage ratings have already been commercialized by some manufactures [14]. The advantages of SiC SBDs in power conversion circuits have been reported in [15–18]; e.g., no reverse recovery current, no temperature influence on the switching behavior, no forward recovery, fast switching, and so on. Various types of controllable switching

Table 1.1 A comparison of the electrical and material properties of Si and 4H-SiC for power device applications at room temperature 300 K.

Parameters	Si	4H-SiC
Energy band gap $E_{\rm G}$ (eV)	1.11	3.26
Intrinsic carrier concentration $n_{\rm i} \ ({\rm cm}^{-3})$	$1.4{\times}10^{10}$	$6.7{\times}10^{-11}$
Electron mobility $\mu_n \ (cm^{-3})$	1400	947
Hole mobility $\mu_{\rm p} \ ({\rm cm}^{-3})$	450	124
Relative dielectric constant $\epsilon_{\rm s}$	11.7	9.7
Saturation drift velocity $v_{\rm sat}$ (cm/s)	$1 \times 10^7$	$2.1{ imes}10^7$
Critical electric field for breakdown $E_{\rm crit}$ (V/cm)	$2.5{ imes}10^5$	$2.2{\times}10^6$
Thermal conductivity (W/cm-K)	1.5	3.7

devices have been proposed, but they are currently under development [19–21]. The main research now focuses on the unipolar devices of such as Junction Field-Effect Transistor (JFET) and Metal Oxide Semiconductor Field-Effect Transistor (MOS-FET). SiC JFETs are expected to be the first commercial transistor available in this technology, and SiC MOSFETs are nearing commercial viability. The characteristics of the switching devices must be analyzed and modeled, so that SiC power devices based applications can be designed and built.

## **1.2** Characterization of SiC power transistors

Power electronics require high efficiency and versatile power conversion. High voltage capability is preferable, especially in high-power conversion circuits, to reduce the conduction loss by large currents. High-frequency switching enables minimization of bulky passive components and provides control functionality. Power switching devices are the key components to realize them; therefore, the developments focus on a power device with a high breakdown voltage, low forward voltage drop, and fast switching capability [3,7,22,23]. However, the limitations to the above requirements are not sufficient for the silicon (Si) power devices. To overcome the difficulty, SiC power devices have been researched and developed to realize lower loss, higher voltage breakdown, and faster switching with a thin voltage blocking layer. And also, the largest efforts have concentrated on unipolar (SiC power switching devices). These include Field-Effect Transistors (FETs) such as JFET, MOSFET, and so on. Therefore, power MOSFETs and JFETs are the most possible power switches in present for high switching frequency power converters due to fast turn-off capability. Power MOSFETs have a high input impedance that makes the gate drive circuitry very simple [4,5,20]. JFETs, which have the possibility of lateral-type and vertical-type structure, are preferred because of the low resistance and ruggedness in harsh environments [21,24–26].

The switching behavior of actual power devices cannot be ideal. The non-ideal characteristics of SiC power devices affect on the performance of power conversion circuits, especially at high switching frequency. Then, the characteristics of devices must be clarified and evaluated in advance of the design of power conversion circuits. Here, the switching characteristics of SiC power MOSFET and SiC JFET are discussed with relation to their ac characteristics and dc characteristics [27–30]. The ac characteristics are involved with their internal parasitic capacitances. The internal parasitic capacitances residing in the SiC power MOSFET are composed of the gate oxide and the depletion region formed in the semiconductor [7,8,31]. The internal parasitic capacitances residing in the SiC JFET are the depletion region formed at pn junction [29,32]. The capacitances of the SiC power MOSFET and the SiC JFET are integrated into the terminal capacitances, which are charged and discharged during turn-on and turn-off operations [33, 34]. The terminal capacitances of the power devices increase as the thickness of the voltage blocking layer is reduced to minimize conduction resistance. The capacitances vary widely with the applied bias voltage because of depletion region in the voltage blocking layer. Therefore, it is necessary to quantify these capacitances of the power devices as well as the voltage dependence of capacitances. There is no commercial apparatus that is able to measure the terminal capacitances of a highvoltage power device with applying the bias voltage up to its rated value. JEDEC [35] and IEC [36] standardized the capacitance measurement methods between the terminals of a power device with a capacitance bridge, but no actual configuration or circuit topology for the measurements are provided. Elferich *et al.* [37] measured the C-V characteristics of a power MOSFET and validated the finite-element (FE) device simulation; however, the measurement setup is not clearly described and the applied voltage was low (0 V  $\leq V_{\rm DS} \leq 20$  V, -10 V  $\leq V_{\rm GS} \leq 0$  V). Therefore, we developed a C-V measurement system for high-voltage power devices. Funaki *et al.* [38,39] presented the C-V measurement system for high-voltage power diodes with evolving [40] and clarified the punch-through structure of SiC SBDs from the measured results. This study develops a C-V measurement system for gate-controlled, high-voltage power devices, e.g., power MOSFET, JFET, and so on. There exist three terminals (Gate, drain, and source terminals) in a single device, and five specifications of the capacitance measurement circuit for  $C_{\rm GS}$ ,  $C_{\rm GD}(= C_{\rm RSS})$ ,  $C_{\rm DS}$ ,  $C_{\rm ISS}$ , and  $C_{\rm OSS}$  are presented to measure the terminal capacitances. On the contrary, the dc characteristics of the power devices are easily measured by a curve tracer.

A model of semiconductor device is indispensable for evaluating the voltage and current responses at switching in circuit simulation and estimating the system performance in their applications. The dynamics at the transient state are obviously governed by these characteristics of power devices.

This dissertation characterizes the voltage dependency of terminal capacitances of the SiC power MOSFET, lateral-type SiC JFET, and vertical-type SiC JFET, models the I-V characteristics with discussing the C-V characteristics of the power devices, and extracts the model parameters from the measured C-V characteristics. Then, the switching behavior of the power devices is experimentally evaluated. Next, we discuss and compare the difference in voltage dependence of the terminal capacitances between the SiC power MOSFET and the Si power MOSFET, and also between the lateraltype SiC JFET and the vertical-type SiC JFET to estimate the difference in their switching behaviors based on their device structures and the semiconductor physics. In the end, the simulated switching behavior of the power devices is validated with the experimental results. The SiC power MOSFET is also experimentally evaluated its performances in a high frequency switching converter circuit.

## 1.3 Purpose and overview

This dissertation aims to characterize the C-V characteristics of the SiC power MOSFET, lateral-type SiC JFET, and vertical-type SiC JFET with capacitance measurement system at first. Then the static I-V and switching characteristics of the devices are experimentally evaluated with a curve tracer and in power conversion circuits. Also, this study discuses and clarifies the difference of these characteristics between SiC and Si power MOSFETs. The difference in device structures is also focused on between lateral-type and vertical-type SiC JFETs. Finally, the models of the devices are validated by comparing the experimental results on the switching response.

Chapter 2 begins with the introduction of physics and device structures of the SiC power MOSFET and SiC JFET. At first, the simplified cross section of single cell structure in a SiC Double-implanted MOSFET (DiMOSFET) is explained with considering the physical capacitances, which are composed of the gate oxide and the depletion layer formed in the semiconductor. They are integrated into the equivalent capacitances between terminals. Secondly, the cross sections of the lateral-type and vertical-type SiC JFET cells are also explained with considering that the depletion region formed at pn junction behaves as parasitic capacitances, which are lumped into terminal capacitances. The thickness of depletion region changes with the applied reverse bias voltage. Therefore, the dependence of the depletion capacitance on the reverse bias voltage can be represented by the uniformly doped and linearly graded doped capacitances.

In Chapter 3, we describe the developed C-V characterization system for highvoltage power transistors (e.g., MOSFET, IGBT, and JFET). The system realizes the selective measurement of a specified capacitance among several capacitances integrated in one device. Three capacitances between terminals are evaluated to specify device characteristics. They are the capacitances for gate-source, gate-drain, and drain-source. The input, output, and reverse transfer capacitance are also evaluated to assess the switching behavior of the power transistor in a circuit. Thus, this chapter discusses the five specifications of a C-V characterization system and its measurement results. Moreover, the developed C-V characterization system enables measurement of the transistor capacitances from its blocking condition to the conducting condition with varying gate bias voltage. The measured C-V characteristics show intricate changes in the low-bias-voltage region, which reflect the device structure. The monotonic capacitance change in the high-voltage region is attributable to the expansion of the depletion region in the drift region. These results help us to understand the dynamic behavior of high-power devices during switching operation.

In Chapter 4, the characteristics of the SiC power MOSFET are characterized and modeled. The charge/discharge phenomenon of terminal capacitances and static I-V characteristics affect on its switching behavior of the device. Models for Si power MOSFET have already been obtained through the previous studies. Based on the model, a model for SiC power MOSFET is proposed with including the semiconductor physics, the structures of the device, and extracted parameters from the measured C-V characteristics. The static I-V characteristics are also discussed with the C-Vcharacteristics. And also, this chapter characterizes the relationship between the input capacitance of the SiC power MOSFET and the gate voltage with considering the internal device structure. It compares the difference in gate-source voltage dependency between the SiC power MOSFET with Si power MOSFET in order to estimate the switching behavior. The results give us a clue to understand the switching characteristics of the power MOSFET. It is clearly shown that the simulated results in switching behavior of the proposed model coincide with experimental results suitably in some conditions.

In Chapter 5, the characteristics of the lateral-type and vertical-type SiC JFETs are characterized and modeled. The both types of SiC JFET studied here are normally-on type devices. The transient behavior in switching operation of the SiC JFETs is discussed with their intrinsic parasitic capacitances. Therefore, this chapter characterizes both C-V characteristics at first, and then the switching behavior is experimentally evaluated. The terminal capacitances of both types of SiC JFET are substantial for understanding the switching characteristics. Finally, the difference of these characteristics is discussed between lateral-type and vertical-type structures with the parasitic capacitances of the devices. The voltage dependency of the capacitance characteristics remarkably shows their device structure. Their switching phenomenon is clearly grasped.

In Chapter 6, the SiC power MOSFET is experimentally evaluated its performances in a high frequency switching converter circuit. We demonstrate the operation of the SiC power MOSFET in the resonant-switch dc-dc step-up voltage converter as switch to control the output current and voltage. Additionally, the results of the resonant converter by using the SiC power MOSFET are compared with the results by using Si power MOSFET.

In Chapter 7, the conclusions of this study are summarized. Some proposals for the future works are also presented.

# Chapter 2

# Device structure and internal parasitic capacitances of SiC power MOSFET and SiC JFET

## 2.1 Introduction

Power semiconductor devices play a crucial role in the regulation and distribution of power and energy for many applications. Recently, power conversion circuits require the power switching devices to operate at high voltage, high-temperature, and fast switching. Power MOSFETs and JFETs are the most possible power switches for high frequency switching power converter circuits due to fast turn-off capability. The capacitances are inherently presented as internal parasitic devices in the structure of power MOSFETs and JFETs. These internal parasitic capacitances typically determine the high frequency behavior of the switching circuit. Also, the principle of operation of power MOSFETs and JFETs is essentially based on the capacitance effect.

Therefore, this chapter describes the device structure of a SiC power MOSFET, a lateral-type SiC JFET, and a vertical-type SiC JFET with considering the internal parasitic capacitances in their devices.

# 2.2 Device structure and internal parasitic capacitances of SiC power MOSFET

#### 2.2.1 Device structure of SiC power MOSFET

Figure 2.1 illustrates the simplified cross section of one cell structure in a SiC Double-implanted MOSFET (DiMOSFET) studied in this study [7,8]. SiC DiMOS-FET is fabricated to have the structure similar to that of a Si Double-diffused MOSFET (DMOSFET) [27]. The main differences between these two devices are the fabrication process and dimensions of p well and  $n^+$  source regions. They are formed by ion implantation for SiC DiMOSFET and shallower than a Si DMOSFET formed by diffusion. The various internal parasitic components of the device are superimposed on its cross section in Fig. 2.1.

The physical capacitances residing in the SiC DiMOSFET are composed of the gate oxide and the depletion layer formed in the semiconductor. They are integrated into the equivalent terminals capacitances of MOSFET, which are composed of gate-source capacitance  $C_{\rm GS}$ , gate-drain capacitance  $C_{\rm GD}$ , and drain-source capacitance  $C_{\rm DS}$ . The  $C_{\rm DS}$  corresponds to the junction capacitance stemmed by depletion at the junction



Figure 2.1 Cross section of a SiC DiMOSFET cell.

between the p well and the n<sup>-</sup>-epitaxial layer  $C_{\rm dsj}$ . It largely depends on drain-source voltage  $V_{\rm DS}$ . The two other  $C_{\rm GS}$  and  $C_{\rm GD}$  have MOS structures provided with inversion charge injectors. The  $C_{\rm GS}$  is comprised of the gate oxide capacitance between the gatesource electrode  $C_{\rm m}$ , the capacitance between the gate electrode and source n<sup>+</sup> region  $C_{\rm oxs}$ , the capacitance between the gate electrode and the top surface of the p well region  $C_{\rm oxc}$ , and the capacitance between the depletion region of the p well region under the gate  $C_{\rm c}$ . The  $C_{\rm c}$  varies depending on gate-source voltage  $V_{\rm GS}$ . Though the polysilicon is utilized as gate electrode, it also depletes the applied gate voltage. It is heavily doped, so that its effect on the synthesized capacitance can be neglected [41]. As for  $C_{\rm GD}$ , it is the series connection of the gate-drain oxide capacitance  $C_{\rm oxd}$  and the drain depletion layer beneath the gate oxide capacitance  $C_{\rm gdj}$ . It varies with gate-drain voltage  $V_{\rm GD}(=V_{\rm GS}-V_{\rm DS})$ .

#### 2.2.2 Internal parasitic capacitances of SiC power MOSFET

#### Gate-Source capacitance $C_{\text{GS}}$ [29, 42]

The dominant components of the gate-source capacitance  $C_{\rm GS}$  of SiC DiMOSFET are shown in Fig. 2.1.  $C_{\rm oxs}$ ,  $C_{\rm m}$ , and  $C_{\rm oxc}$ , related to the gate oxide, do not change with the applied voltage.  $C_{\rm c}$ , originated from the depletion layer in the top of p well, are associated with the depletion region formed in the semiconductor beneath the gate oxide. It can be derived from the depleted space charge  $Q_{\rm s}$ , which varies as a function of the surface potential of semiconductor  $\psi_{\rm s}$ . Here, the surface potential  $\psi_{\rm s}$  is governed by gate voltage. The total gate-source capacitance  $C_{\rm GS}$  can be given by Eq. (2.1):

$$C_{\rm GS} = C_{\rm oxs} + C_{\rm m} + C_{\rm gb}, \qquad (2.1)$$

where

$$C_{\rm gb} = \frac{1}{1/C_{\rm oxc} + 1/C_{\rm c}}.$$

The surface potential  $\psi_s$  of p-type semiconductor (p well) obtained from the Pois-

son's equation:

$$\frac{d^2\psi}{dx^2} = -\frac{\rho(x)}{\epsilon_{\rm s}} = -\frac{q}{\epsilon_{\rm s}} [p(x) - n(x) - N_{\rm A}] 
= -\frac{qN_{\rm A}}{\epsilon_{\rm s}} \Big[ e^{-\psi(x)/\phi_{\rm t}} - 1 - e^{-2\phi_{\rm F}/\phi_{\rm t}} (e^{\psi(x)/\phi_{\rm t}} - 1) \Big],$$
(2.2)

where  $\rho$  denotes the charge density,  $N_{\rm A}$  the accepter impurity concentration,  $\phi_{\rm t}$  the thermal voltage, and  $\phi_{\rm F}$  the Fermi potential. Multiplied both sides of Eq. (2.2) by  $2d\psi/dx$ ;

$$d\left(\frac{d\psi}{dx}\right)^{2} = -\frac{2qN_{A}}{\epsilon_{s}} \left[ e^{-\psi(x)/\phi_{t}} - 1 - e^{-2\phi_{F}/\phi_{t}} (e^{\psi(x)/\phi_{t}} - 1) \right] d\psi.$$
(2.3)

Integration both sides of Eq. (2.3) leads

$$\left(\frac{\mathrm{d}\psi}{\mathrm{d}x}\right)^{2} = \frac{2qN_{\mathrm{A}}}{\epsilon_{\mathrm{s}}} \Big[\phi_{\mathrm{t}}e^{-\psi(x)/\phi_{\mathrm{t}}} + \psi - \phi_{\mathrm{t}} + e^{-2\phi_{\mathrm{F}}/\phi_{\mathrm{t}}}(\phi_{\mathrm{t}}e^{\psi(x)/\phi_{\mathrm{t}}} - \psi - \phi_{\mathrm{t}})\Big].$$
(2.4)

When electric field potential  $E(x) = -d\psi/dx$ , therefore, the following is then obtained:

$$E(x) = -\frac{\mathrm{d}\psi}{\mathrm{d}x} = \pm \frac{\sqrt{2q\epsilon_{\mathrm{s}}N_{\mathrm{A}}}}{\epsilon_{\mathrm{s}}} \sqrt{\phi_{\mathrm{t}}e^{-\psi/\phi_{\mathrm{t}}} + \psi - \phi_{\mathrm{t}} + e^{-2\phi_{\mathrm{F}}/\phi_{\mathrm{t}}}(\phi_{\mathrm{t}}e^{\psi/\phi_{\mathrm{t}}} - \psi - \phi_{\mathrm{t}})}.$$
 (2.5)

This gives  $-E_s = Q'_s/\epsilon_s$ . Evaluating  $E_s$  with  $\psi = \psi_s$ , the depleted space charge per unit area  $Q'_s$  is obtained as Eq. (2.6):

$$Q'_{\rm s} = \mp \sqrt{2q\epsilon_{\rm s}N_{\rm A}} \sqrt{\phi_{\rm t} e^{-\psi_{\rm s}/\phi_{\rm t}} + \psi_{\rm s} - \phi_{\rm t} + e^{-2\phi_{\rm F}/\phi_{\rm t}}(\phi_{\rm t} e^{\psi_{\rm s}/\phi_{\rm t}} - \psi_{\rm s} - \phi_{\rm t})}.$$
 (2.6)

The electric field at the surface of the p-type semiconductor and the space-charge density in the p-type semiconductor are shown in Figs. 2.2 and 2.3, respectively. They vary with the surface potential  $\psi_s$  across the p-type semiconductor.

Therefore, the  $C_c$  is derived from the space charge  $Q_s$ . It can be discussed as a differential capacitance per unit area of the space-charge region in p-type semiconductor, which is given by Eq. (2.7):

$$C'_{\rm s} = -\frac{\mathrm{d}Q'_{\rm s}}{\mathrm{d}\psi_{\rm s}} = \pm \sqrt{2q\epsilon_{\rm s}N_{\rm A}} \Big[ \frac{1 - e^{-\psi_{\rm s}/\phi_{\rm t}} + e^{-2\phi_{\rm F}/\phi_{\rm t}}(e^{\psi_{\rm s}/\phi_{\rm t}} - 1)}{2\sqrt{\phi_{\rm t}e^{-\psi_{\rm s}/\phi_{\rm t}} + \psi_{\rm s} - \phi_{\rm t} + e^{-2\phi_{\rm F}/\phi_{\rm t}}(\phi_{\rm t}e^{\psi_{\rm s}/\phi_{\rm t}} - \psi_{\rm s} - \phi_{\rm t})}}\Big].$$
(2.7)

Eqs. (2.6) and (2.7) are validated in all conditions as accumulation, depletion, and inversion.



Figure 2.2 Electric field at the surface of the p-type semiconductor as a function of the surface potential.



Figure 2.3 Variation of the space-charge density in the p-type semiconductor of a MOS junction as a function of the surface potential.

#### - Accumulation condition $(V_{\rm GS} < V_{\rm FB})$

Figure 2.4(a) shows the structure of p-type semiconductor of power MOSFET, spacecharge distribution  $\rho(x)$ , electric field strength E(x), and internal potential  $\psi$  in accumulation condition. The condition in which  $V_{\rm GS} < V_{\rm FB}$  is considered here. The surface potential  $\psi_{\rm s}$  being less than zero ( $\psi_s < 0$ ),  $Q'_s$  is positive and corresponds to the accumulation condition, which varies exponentially with the surface potential  $\psi_{\rm s}$ . Because the first term on the right-hand side of Eq. (2.6) becomes dominant. The surface charge in p-type semiconductor for accumulation condition is given by



$$Q_{\rm s}' = \sqrt{2q\epsilon_{\rm s}N_{\rm A}}\sqrt{\phi_{\rm t}e^{|\psi_{\rm s}|/\phi_{\rm t}}},\tag{2.8}$$

Figure 2.4 Formation of accumulation layer in p-type semiconductor. (a) Structure of p-type semiconductor of power MOSFET, space-charge distribution, electric field strength, and internal potential; (b) Equivalent capacitance  $C_{\rm GS}$  in accumulation condition.

and the accumulation capacitance per unit area  $C'_{\rm A}$ , which is shown in Fig. 2.4(b) as a part of the  $C'_{\rm GS}$  capacitance, is equal to

$$C'_{\rm A} = -\frac{\mathrm{d}Q'_{\rm s}}{\mathrm{d}\psi_{\rm s}} = \sqrt{2q\epsilon_{\rm s}N_{\rm A}}\frac{e^{|\psi_{\rm s}|/\phi_{\rm t}}}{2\sqrt{\phi_{\rm t}e^{|\psi_{\rm s}|/\phi_{\rm t}}}}.$$
(2.9)

Therefore,

$$\frac{1}{C'_{\rm gb}} = \frac{1}{C'_{\rm oxc}} + \frac{1}{C'_{\rm A}}.$$
(2.10)

where  $C'_{\rm gb}$  is the gate-body capacitance per unit area and  $C'_{\rm oxc}$  the gate-channel oxide capacitance per unit area.

#### - Depletion condition $(V_{\rm T} > V_{\rm GS} > V_{\rm FB})$

Figure 2.5(a) shows the structure of p-type semiconductor of power MOSFET, spacecharge distribution  $\rho(x)$ , electric field strength E(x), and internal potential  $\psi$  in depletion condition. The condition in which  $V_{\rm T} > V_{\rm GS} > V_{\rm FB}$  is considered here. The surface potential  $\psi_{\rm s}$  being more than zero ( $\phi_{\rm F} > \psi_{\rm s} > 0$ ),  $Q'_{\rm s}$  is negative and corresponds to the depletion condition. The negative charge in the depletion region can also be calculated from Eq. (2.6). In this condition, the second term on the right-hand side of Eq. (2.6) becomes dominant. The surface charge in p-type semiconductor for depletion condition is given by

$$Q_{\rm s}' = -\sqrt{2q\epsilon_{\rm s}N_{\rm A}\psi_{\rm s}},\tag{2.11}$$

and the depletion capacitance per unit area  $C'_{\rm D}$ , which is shown in Fig. 2.5(b) as a part of the  $C'_{\rm GS}$  capacitance, is equal to

$$C'_{\rm D} = -\frac{\mathrm{d}Q'_{\rm s}}{d\psi_{\rm s}} = \sqrt{2q\epsilon_{\rm s}N_{\rm A}}\frac{1}{2\sqrt{\psi_{\rm s}}}.$$
(2.12)

Therefore,

$$\frac{1}{C'_{\rm gb}} = \frac{1}{C'_{\rm oxc}} + \frac{1}{C'_{\rm D}}.$$
(2.13)

#### - Inversion condition $(V_{\rm GS} > V_{\rm T})$

Figure 2.6(a) shows the structure of p-type semiconductor of power MOSFET, spacecharge distribution  $\rho(x)$ , electric field strength E(x), and internal potential  $\psi$  in inversion condition. The condition in which  $V_{\rm GS} > V_{\rm T}$  is considered here. The surface



Figure 2.5 Formation of depletion layer at surface semiconductor of p-type. (a) Structure of p well of power MOSFET, space-charge distribution, electric field strength, and internal potential; (b) Equivalent capacitance  $C_{\rm GS}$  in depletion condition.

potential  $\psi_{\rm s}$  being more than fermi potential ( $\psi_{\rm s} > \phi_{\rm F}$ ),  $Q'_{\rm s}$  is negative and corresponds to the inversion condition. The negative charge in the inversion region can also be calculated from Eq. (2.6). In this condition, the fourth term on the right-hand side of Eq. (2.6) becomes dominant. The total charge per unit area in the space-charge region  $Q'_{\rm s}$  is then the sum of the charge of electron in the inversion layer  $Q'_{\rm I}$  and the charge of the ionized acceptor atoms in the depletion region  $Q'_{\rm D}$ . Therefore, the surface charge in p-type semiconductor for inversion condition is given by

$$Q'_{\rm s} = Q'_{\rm D} + Q'_{\rm I} = -\sqrt{2q\epsilon_{\rm s}N_{\rm A}}\sqrt{\psi_{\rm s} + \phi_{\rm t}e^{(\psi_{\rm s} - 2\phi_{\rm F})/\phi_{\rm t}}},$$
(2.14)

and the inversion and depletion capacitance per unit area  $C'_{\rm D} + C'_{\rm I}$ , which is shown in Fig. 2.6(b) as a part of the  $C'_{\rm GS}$  capacitance, is equal to

$$C'_{\rm D} + C'_{\rm I} = -\frac{\mathrm{d}Q'_{\rm s}}{d\psi_{\rm s}} = \sqrt{2q\epsilon_{\rm s}N_{\rm A}} \frac{1 + e^{(\psi_{\rm s} - 2\phi_{\rm F})/\phi_{\rm t}}}{2\sqrt{\psi_{\rm s} + \phi_{\rm t}e^{(\psi_{\rm s} - 2\phi_{\rm F})/\phi_{\rm t}}}}.$$
(2.15)



Figure 2.6 Formation of inversion layer in p-type semiconductor. (a) Structure of p well of power MOSFET, space-charge distribution, electric field strength, and internal potential distribution; (b) Equivalent capacitance  $C_{\rm GS}$  in inversion condition.

Therefore,

$$\frac{1}{C'_{\rm gb}} = \frac{1}{C'_{\rm oxc}} + \frac{1}{C'_{\rm D} + C'_{\rm I}},\tag{2.16}$$



Figure 2.7 Variation of  $C'_{\rm GS}/C'_{\rm ox}$  as a function of  $V_{\rm GS}$  for a p-type semiconductor.



Figure 2.8 Variation of  $C'_{\rm GS}/C'_{\rm ox}$  as a function of  $V_{\rm GS}$  for a p-type semiconductor with considering the potential in the polygate.

#### Real C-V curves: Polysilicon depletion effects

Polysilicon gates have been used in MOS technologies since the seventies in order to obtain source and drain regions self-aligned to the gate [41]. When the p-semiconductor substrate is in depletion and/or inversion, the positive charge in the polygate is stored in a thin depletion layer. Thus, the capacitance of this depletion layer must be included in the MOS equivalent circuit.

Considering the potential drop in the polygate  $\psi_{poly}$ , the potential balance equation must be rewritten as

$$V_{\rm GS} = V_{\rm FB} + \psi_{\rm s} + \psi_{\rm poly} - \frac{Q'_{\rm s}}{C'_{\rm oxc}}.$$
 (2.17)

$$C'_{\rm gb} = \frac{1}{\frac{1}{C'_{\rm oxc}} + \frac{1}{C'_c} + \frac{1}{C'_{\rm poly}}}.$$
(2.18)

A very simple charge-control model of the capacitances is available when the semiconductor bulk is in inversion. The poly depletion capacitance per unit area  $C'_{\text{poly}}$  can be calculated as Eq. (2.19):

$$C'_{\rm poly} = \frac{\sqrt{2q\epsilon_{\rm s}N_{\rm poly}}}{2\sqrt{\psi_{\rm poly}}},\tag{2.19}$$

and

$$\frac{\psi_{\text{poly}}}{\psi_{\text{s}}} = \frac{N_{\text{A}}}{N_{\text{poly}}}.$$
(2.20)

The variation of  $C'_{\rm GS}/C'_{\rm ox}$  as a function of  $V_{\rm GS}$  for a p-type semiconductor with considering the potential in the polygate are shown in Fig. 2.8.

#### Gate-Drain capacitance $C_{\text{GD}}$ [29, 42]

The gate-drain voltage  $V_{\rm GD}$  sweeps from a highly positive to a very low voltage, the n-drain interface starts in accumulation. Once  $V_{\rm GD}$  drops below the drain flat-band voltage  $V_{\rm FB_D}$ , the n-drain surface charges to depletion. Finally, when  $V_{\rm GS}$  goes below the threshold drain voltage  $V_{\rm TD}$ , the inversion layer starts to build up.

The surface potential  $\psi_s$  of n-type semiconductor obtained from the Poisson's equa-

tion:

$$\frac{d^{2}\psi}{dx^{2}} = -\frac{\rho(x)}{\epsilon_{s}} = -\frac{q}{\epsilon_{s}}[p(x) - n(x) + N_{D}] \\
= -\frac{qN_{D}}{\epsilon_{s}} \Big[ e^{2\phi_{F}/\phi_{t}} (e^{-\psi(x)/\phi_{t}} - 1) - e^{\psi(x)/\phi_{t}} + 1 \Big],$$
(2.21)

where  $N_{\rm D}$  denotes the donor impurity concentration. Multiplied both sides of Eq. (2.21) by  $2d\psi/dx$ ;

$$d\left(\frac{d\psi}{dx}\right)^{2} = -\frac{2qN_{\rm D}}{\epsilon_{\rm s}} \left[ e^{2\phi_{\rm F}/\phi_{\rm t}} (e^{-\psi(x)/\phi_{\rm t}} - 1) - e^{\psi(x)/\phi_{\rm t}} + 1 \right] d\psi.$$
(2.22)

Integrate both sides of Eq. (2.22), the following relation is obtained:

$$\left(\frac{\mathrm{d}\psi}{\mathrm{d}x}\right)^{2} = \frac{2qN_{\mathrm{D}}}{\epsilon_{\mathrm{s}}} \Big[\phi_{\mathrm{t}}e^{\psi/\phi_{\mathrm{t}}} - \psi - \phi_{\mathrm{t}} + e^{2\phi_{\mathrm{F}}/\phi_{\mathrm{t}}}(\phi_{\mathrm{t}}e^{-\psi/\phi_{\mathrm{t}}} + \psi - \phi_{\mathrm{t}})\Big].$$
(2.23)

When  $E(x) = -\mathrm{d}\psi/\mathrm{d}x$ ,

$$E(x) = -\frac{\mathrm{d}\psi}{\mathrm{d}x} = \pm \frac{\sqrt{2q\epsilon_{\mathrm{s}}N_{\mathrm{D}}}}{\epsilon_{\mathrm{s}}} \sqrt{\phi_{\mathrm{t}}e^{\psi/\phi_{\mathrm{t}}} - \psi - \phi_{\mathrm{t}} + e^{2\phi_{\mathrm{F}}/\phi_{\mathrm{t}}}(\phi_{\mathrm{t}}e^{-\psi/\phi_{\mathrm{t}}} + \psi - \phi_{\mathrm{t}})}.$$
 (2.24)

This gives  $-E_{\rm s} = Q_{\rm s}'/\epsilon_{\rm s}$ . Evaluating  $E_{\rm s}$  with  $\psi = \psi_{\rm s}$ , we obtain:

$$Q'_{\rm s} = \mp \sqrt{2q\epsilon_{\rm s}N_{\rm D}} \sqrt{\phi_{\rm t} e^{\psi_{\rm s}/\phi_{\rm t}} - \psi_{\rm s} - \phi_{\rm t} + e^{2\phi_{\rm F}/\phi_{\rm t}}(\phi_{\rm t} e^{-\psi_{\rm s}/\phi_{\rm t}} + \psi_{\rm s} - \phi_{\rm t})}.$$
 (2.25)



Figure 2.9 Electric field at the surface of the n-type semiconductor as a function of the surface potential across the n-type semiconductor.



Figure 2.10 Variation of the space-charge density in n-type semiconductor of a MOS junction as a function of the surface potential.

Therefore, the  $C_{\text{gdj}}$  is derived from the space charge  $Q_{\text{s}}$ . It can be discussed as a differential capacitance per unit area of the space-charge region in n-type semiconductor, which is given by

$$C'_{\rm s} = -\frac{\mathrm{d}Q'_{\rm s}}{\mathrm{d}\psi_{\rm s}} = \pm \sqrt{2q\epsilon_{\rm s}N_{\rm D}} \Big[ \frac{-1 + e^{\psi_{\rm s}/\phi_{\rm t}} - e^{2\phi_{\rm F}/\phi_{\rm t}}(e^{-\psi_{\rm s}/\phi_{\rm t}} - 1)}{2\sqrt{\phi_{\rm t}e^{\psi_{\rm s}/\phi_{\rm t}} - \psi_{\rm s} - \phi_{\rm t} + e^{2\phi_{\rm F}/\phi_{\rm t}}(\phi_{\rm t}e^{-\psi_{\rm s}/\phi_{\rm t}} + \psi_{\rm s} - \phi_{\rm t})} \Big].$$
(2.26)

Eqs. (2.25) and (2.26) are validated in all conditions (accumulation, depletion, and inversion).

#### - Accumulation condition $(V_{\rm GD} > V_{\rm FB_D})$

Figure 2.11(a) shows the structure of n<sup>-</sup> drift region of power MOSFET, space-charge distribution  $\rho(x)$ , electric field strength E(x), and internal potential  $\psi$  in accumulation condition. The condition in which  $V_{\rm GD} > V_{\rm FB_D}$  is considered in this section. The surface potential  $\psi_{\rm s}$  being more than zero ( $\psi_{\rm s} > 0$ ),  $Q'_{\rm s}$  is negative and corresponds to the accumulation condition that varies exponentially with the surface potential because the first term on the right-hand side of Eq. (2.25) becomes dominant. The surface charge in n-type semiconductor for accumulation condition is given by



Figure 2.11 Formation of accumulation layer in n-type semiconductor. (a) Structure of  $n^-$  drift region of power MOSFET, space-charge distribution, electric field strength, and internal potential; (b) Equivalent capacitance  $C_{\rm GD}$  in accumulation condition.

$$Q_{\rm s}' = -\sqrt{2q\epsilon_{\rm s}N_{\rm D}}\sqrt{\phi_{\rm t}e^{\psi_{\rm s}/\phi_{\rm t}}},\qquad(2.27)$$

and the accumulation capacitance per unit area  $C_{\rm A}^\prime$  is equal to

$$C'_{\rm A} = -\frac{\mathrm{d}Q'_{\rm s}}{\mathrm{d}\psi_{\rm s}} = \sqrt{2q\epsilon_{\rm s}N_{\rm D}}\frac{e^{\psi_{\rm s}/\phi_{\rm t}}}{2\sqrt{\phi_{\rm t}e^{\psi_{\rm s}/\phi_{\rm t}}}}.$$
(2.28)

Therefore,

$$\frac{1}{C'_{\rm GD}} = \frac{1}{C'_{\rm oxd}} + \frac{1}{C'_{\rm A}},\tag{2.29}$$

where  $C'_{\rm GD}$  is the gate-drain capacitance per unit area and  $C'_{\rm oxd}$  the gate-drain oxide capacitance per unit area. The gate voltage dependency of  $C'_{\rm GD}$  capacitance in the accumulation condition is shown in Fig. 2.11(b).

- Depletion condition ( $V_{\rm FB_D} > V_{\rm GD} > V_{\rm TD}$ )

Figure 2.12(a) shows the structure of n<sup>-</sup> drift region of power MOSFET, space-charge distribution  $\rho(x)$ , electric field strength E(x), and internal potential  $\psi$ . The condition



Figure 2.12 Formation of depletion layer at surface semiconductor of n-type. (a) Structure of  $n^-$  drift region of power MOSFET, space-charge distribution, electric field strength, and internal potential; (b) Equivalent capacitance  $C_{\rm GD}$  in depletion condition.

in which  $V_{\rm FB_D} > V_{\rm GD} > V_{\rm TD}$  is considered here. When the surface potential  $\psi_{\rm s}$  is less than zero ( $0 > \psi_{\rm s} > \phi_{\rm F}$ ),  $Q'_{\rm s}$  is positive and corresponds to the depletion condition. The positive charge in the depletion region can also be calculated from Eq. (2.25). In this condition, the second term on the right-hand side of Eq. (2.25) becomes dominant. The surface charge in n-type semiconductor for depletion condition is given by

$$Q_{\rm s}' = \sqrt{2q\epsilon_{\rm s}N_{\rm D}|\psi_{\rm s}|},\tag{2.30}$$

and the depletion capacitance per unit area  $C'_{\rm D}$  is equal to

$$C_{\rm D}' = -\frac{\mathrm{d}Q_{\rm s}'}{\mathrm{d}\psi_{\rm s}} = \sqrt{2q\epsilon_{\rm s}N_{\rm D}}\frac{1}{2\sqrt{|\psi_{\rm s}|}}.$$
(2.31)

Therefore,

$$\frac{1}{C'_{\rm GD}} = \frac{1}{C'_{\rm oxd}} + \frac{1}{C'_{\rm D}}.$$
(2.32)

The gate voltage dependency of  $C'_{\text{GD}}$  capacitance in the depletion condition is shown in Fig. 2.12(b).

### - Inversion condition ( $V_{ m GD} < V_{ m TD}$ )

Figure 2.13(a) shows the structure of n<sup>-</sup> drift region of power MOSFET, space-charge distribution  $\rho(x)$ , electric field strength E(x), and internal potential  $\psi$  in inversion condition. The condition in which  $V_{\rm GD} < V_{\rm TD}$  is considered here. When the surface potential  $\psi_{\rm s}$  is less than fermi potential ( $\psi_{\rm s} < \phi_{\rm F}$ ),  $Q'_{\rm s}$  is positive and corresponds to the inversion condition. The positive charge in the inversion region can also be calculated from Eq. (2.25). In this condition, the fourth term on the right-hand side of Eq. (2.25) becomes dominant. The total charge per unit area in the space-charge region  $Q'_{\rm s}$  is then the sum of the charge of electron in the inversion layer  $Q'_{\rm I}$  and the charge of the ionized acceptor atoms in the depletion region  $Q'_{\rm D}$ . Therefore, the surface charge in n-type semiconductor for inversion condition is given by

$$Q'_{\rm s} = Q'_{\rm D} + Q'_{\rm I} = \sqrt{2q\epsilon_{\rm s}N_{\rm D}}\sqrt{|\psi_{\rm s}| + \phi_{\rm t}e^{|(2\phi_{\rm F} - \psi_{\rm s})|/\phi_{\rm t}}},$$
(2.33)

and the inversion and depletion capacitance per unit area  $C'_{\rm D} + C'_{\rm I}$  is equal to

$$C'_{\rm D} + C'_{\rm I} = -\frac{\mathrm{d}Q'_{\rm s}}{\mathrm{d}\psi_{\rm s}} = \sqrt{2q\epsilon_{\rm s}N_{\rm D}}\frac{1 + e^{|(2\phi_{\rm F} - \psi_{\rm s})|/\phi_{\rm t}}}{2\sqrt{|\psi_{\rm s}| + \phi_{\rm t}e^{|(2\phi_{\rm F} - \psi_{\rm s})|/\phi_{\rm t}}}}.$$
(2.34)



Figure 2.13 Formation of inversion layer in n-type semiconductor. (a) Structure of  $n^-$  drift region of power MOSFET, space-charge distribution, electric field strength, and internal potential; (b) Equivalent capacitance  $C_{\rm GD}$  in inversion condition.

Therefore,

$$\frac{1}{C'_{\rm GD}} = \frac{1}{C'_{\rm oxd}} + \frac{1}{C'_{\rm D} + C'_{\rm I}}.$$
(2.35)

The gate voltage dependency of  $C'_{\rm GD}$  capacitance in the inversion condition is shown in Fig. 2.13(b).

The n<sup>-</sup> drift region of power MOSFET is divided into two regions: the space charge region and the ohmic region. The  $C_{\text{GD}}$  is the combination of the gate-drain



Figure 2.14 Variation of  $C'_{GD}/C'_{ox}$  as a function of  $V_{GS}$  for a n-type semiconductor.

oxide capacitance  $C_{\text{oxd}}$  and the drain depletion layer beneath the gate oxide capacitance  $C_{\text{gdj}}$ , which is shown in Fig. 2.1. For approximate calculations of switching behaviors,  $C_{\text{GD}}$  is approximated by the two discrete values  $C_{\text{oxd}}$  and  $C_{\text{gdj}}$  with the change in value occurring at  $V_{\text{DS}} = V_{\text{GS}}$  as Eq. (2.36):

$$C_{\rm GD} \cong \begin{cases} C_{\rm oxd} & \text{for } V_{\rm DS} \le V_{\rm GS} - V_{\rm TD}, \\ C_{\rm oxd} \cdot C_{\rm gdj} / (C_{\rm oxd} + C_{\rm gdj}) & \text{for } V_{\rm DS} > V_{\rm GS} - V_{\rm TD}. \end{cases}$$
(2.36)

The  $C_{\rm gdj}$  can be discussed as the  $C_{\rm DS}$  in the next section.

#### Drain-Source capacitance $C_{\rm DS}$ [29, 32]

Figure 2.15(a) shows the structure of  $p^+-n^--n^+$  of power MOSFET, space-charge distribution  $\rho(x)$ , and electric field distribution E(x). The drain-source capacitance  $C_{\rm DS}$  corresponds to the junction capacitance stemmed by depletion at the junction between the p well and the n<sup>-</sup>-epitaxial layer  $C_{\rm dsj}$ . It largely depends on  $V_{\rm DS}$ . Here,  $C_{\rm DS}$  can be considered as  $p^+-n^--n^+$  structure shown in Fig. 2.15. It is supported the punch-through structure at high breakdown voltage. When  $V_{\rm DS}$  increases, the depletion region expands from the  $p^+$  to the uniformly doped drift region  $n^-$  and  $n^+$  substrate. Therefore, the depletion region will appreciably simplify the solution


Figure 2.15  $p^+-n^--n^+$  junction under reverse bias voltage. (a) Structure of  $p^+-n^--n^+$  of power MOSFET, space-charge distribution, and electric field strength; (b) Equivalent capacitance  $C_{DS}$ .

of Poisson's equation. Since the carrier concentrations are assumed to be much less than the net ionized dopant density in the depletion region. Poisson's equation can be written as

$$\frac{\mathrm{d}^2 V(x)}{\mathrm{d}x^2} \cong \begin{cases} -\frac{qN_{\mathrm{D}}}{\epsilon_{\mathrm{s}}} & \text{for } 0 \le x \le W_{\mathrm{D}}, \\ -\frac{qN_{\mathrm{Sub}}}{\epsilon_{\mathrm{s}}} & \text{for } W_{\mathrm{D}} < x, \end{cases}$$
(2.37)

where  $N_{\rm D}$  denotes the donor impurity concentration in n<sup>-</sup>-drift region,  $N_{\rm Sub}$  the donor impurity concentration in n<sup>+</sup>-substrate layer, and  $W_{\rm D}$  the drift region width. When both sides of Eq. (2.37) are integrated in the depletion region from x = 0 to x = W, the following is obtained in the differential equation by

$$\frac{\mathrm{d}V(W)}{\mathrm{d}W} = \begin{cases} -\frac{qN_{\mathrm{D}}}{\epsilon_{\mathrm{s}}}W & \text{for } 0 \le W \le W_{\mathrm{D}}, \\ -\frac{qN_{\mathrm{Sub}}}{\epsilon_{\mathrm{s}}}W & \text{for } W > W_{\mathrm{D}}. \end{cases}$$
(2.38)

From Eq. (2.38), depletion region width W can be expressed with voltage V and  $V_{\text{bi}}$  in Eq. (2.39):

$$W = \begin{cases} \sqrt{\frac{2\epsilon_{\rm s}}{qN_{\rm D}}}(-V+V_{\rm bi}) & \text{for } 0 \le W \le W_{\rm D}, \\ \sqrt{\frac{2\epsilon_{\rm s}}{qN_{\rm D}}}(-V+V_{\rm bi}) + \left(1-\frac{N_{\rm D}}{N_{\rm Sub}}\right)W_{\rm D}^2 & \text{for } W > W_{\rm D}. \end{cases}$$
(2.39)

The depletion region capacitance can be related to the applied reverse-bias voltage  $V_{\rm R}$  through depletion region width W:

$$C = A \frac{\epsilon_{\rm s}}{W} \tag{2.40}$$

Therefore, the drain-source capacitance  $C_{\rm DS}$  can be expressed with applying  $V_{\rm DS}$  by Eq. (2.41):

$$C_{\rm DS} = \begin{cases} A_{\rm DS} \frac{\epsilon_{\rm s}}{\sqrt{\frac{2\epsilon_{\rm s}}{qN_{\rm D}}(V_{\rm DS} + V_{\rm bi})}} & \text{for } 0 \le W \le W_{\rm D}, \\ A_{\rm DS} \frac{\epsilon_{\rm s}}{\sqrt{\frac{2\epsilon_{\rm s}}{qN_{\rm D}}(V_{\rm DS} + V_{\rm bi}) + \left(1 - \frac{N_{\rm D}}{N_{\rm Sub}}\right)W_{\rm D}^2}} & \text{for } W > W_{\rm D}, \end{cases}$$

$$(2.41)$$

where  $A_{\rm DS}$  denotes the drain-source overlap area. And also, the drain depletion layer beneath the gate oxide capacitance  $C_{\rm gdj}$  can be expressed with applying  $V_{\rm DG} (= V_{\rm DS} - V_{\rm GS})$  and  $V_{\rm bi} = V_{\rm TD}$  by Eq. (2.42):

$$C_{\rm gdj} = \begin{cases} A_{\rm GD} \frac{\epsilon_{\rm s}}{\sqrt{\frac{2\epsilon_{\rm s}}{qN_{\rm D}}(V_{\rm DS} - V_{\rm GS} + V_{\rm TD})}} & \text{for } 0 \le W \le W_{\rm D}, \\ A_{\rm GD} \frac{\epsilon_{\rm s}}{\sqrt{\frac{2\epsilon_{\rm s}}{qN_{\rm D}}(V_{\rm DS} - V_{\rm GS} + V_{\rm TD}) + \left(1 - \frac{N_{\rm D}}{N_{\rm Sub}}\right) W_{\rm D}^2}} & \text{for } W > W_{\rm D}, \end{cases}$$

$$(2.42)$$

where  $A_{\rm GD}$  denotes the gate-drain overlap area.

# 2.3 Device structure and internal parasitic capacitances of SiC JFET

#### 2.3.1 Device structure of SiC JFET

Figure 2.16(a) shows the cross section of the lateral-type SiC JFET cell. The n-channel is formed between buried  $p^+$  gate and  $p^-$  substrate. Their separation determines the n-channel thickness. The n-region between drain and source areas is designed to have a double reduced surface field (RESURF) effect to prevent electric field concentration [21]. Figure 2.16(b) shows the cross section of the vertical-type SiC JFET cell [60, 66]. It has lateral and vertical channels. The lateral channel is sandwiched between p gate at the center top of the device and buried  $p^+$  gate sections connected to the source terminal at the top of the drift region. The vertical channel is located between the two buried  $p^+$  gate regions.



Figure 2.16 Cross section of a SiC JFET cell.

#### 2.3.2 Internal parasitic capacitances of SiC JFET

The depletion region formed at pn junction behaves as internal parasitic capacitances, which are lumped into terminal capacitances  $C_{\rm GS}$ ,  $C_{\rm GD}$ , and  $C_{\rm DS}$ , as depicted in Fig. 2.16. The capacitances of pn junction depend on the doping profile, device structure, and reverse-bias voltage  $V_{\rm R}$ . In practice, most impurity concentration profiles can be approximated by the following two limiting cases: the uniformly doped junction and the linearly graded doped junction [29, 32, 65]. The uniformly doped approximation provides an adequate description for alloyed junctions, shallowly diffused junctions, and ion-implanted junctions. The linearly graded doped approximation is reasonable for deeply diffused junctions. Therefore, the Poisson's equation is valid for the both approximation.

#### Uniformly doped junction capacitance

A pn junction is considered uniformly doped or abrupt if there dominates donor impurity concentration  $N_{\rm D}$  on one side of the junction and acceptor impurity concentration  $N_{\rm A}$  on the other side. Here, the impurity concentration in a semiconductor changes abruptly from  $N_{\rm A}$  to  $N_{\rm D}$ , as shown in Fig. 2.17. The charge density  $\rho$  around the pn junction is graphically shown in Fig. 2.17, which can be separated into four parts. Therefore, the relationship between the electric field E and the charge density  $\rho$  is given by the Poisson's equation as Eq. (2.43):

$$\frac{\mathrm{d}^2 V(x)}{\mathrm{d}x^2} \cong \begin{cases} 0 & \text{for } x \leq -x_{\mathrm{p}}, \\ \frac{qN_{\mathrm{A}}}{\epsilon_{\mathrm{s}}} & \text{for } -x_{\mathrm{p}} \leq x < 0, \\ -\frac{qN_{\mathrm{D}}}{\epsilon_{\mathrm{s}}} & \text{for } 0 < x \leq x_{\mathrm{n}}, \\ 0 & \text{for } x \geq x_{\mathrm{n}}. \end{cases}$$
(2.43)



Figure 2.17 Uniformly doped pn junction in thermal equilibrium.

The electric field E is then obtained by integrating Eq. (2.43) on x:

$$-\frac{\mathrm{d}V(x)}{\mathrm{d}x} = E(x) = \begin{cases} 0 & \text{for } x \le -x_{\mathrm{p}}, \\ -\frac{qN_{\mathrm{A}}}{\epsilon_{\mathrm{s}}}(x+x_{\mathrm{p}}) & \text{for } -x_{\mathrm{p}} \le x < 0, \\ \frac{qN_{\mathrm{D}}}{\epsilon_{\mathrm{s}}}(x-x_{\mathrm{n}}) & \text{for } 0 < x \le x_{\mathrm{n}}, \\ 0 & \text{for } x \ge x_{\mathrm{n}}. \end{cases}$$
(2.44)

The integration of Eq. (2.44) gives the potential distribution V(x) as:

$$V(x) = \begin{cases} 0 & \text{for } x \leq -x_{\rm p}, \\ \frac{qN_{\rm A}}{2\epsilon_{\rm s}} (x+x_{\rm p})^2 & \text{for } -x_{\rm p} \leq x < 0, \\ V_{\rm bi} - \frac{qN_{\rm D}}{2\epsilon_{\rm s}} (x-x_{\rm n})^2 & \text{for } 0 < x \leq x_{\rm n}, \\ V_{\rm bi} & \text{for } x \geq x_{\rm n}. \end{cases}$$
(2.45)

At the condition  $E(0) = N_{\rm D} x_{\rm n} = N_{\rm A} x_{\rm p}$ ,  $x_{\rm p}$  and  $x_{\rm n}$  are obtained as

$$x_{\rm p} = \sqrt{\frac{2\epsilon_{\rm s} V_{\rm bi}}{q N_{\rm A} [1 + (N_{\rm A}/N_{\rm D})]}},$$
 (2.46)

$$x_{\rm n} = \sqrt{\frac{2\epsilon_{\rm s} V_{\rm bi}}{q N_{\rm D} [1 + (N_{\rm D}/N_{\rm A})]}}.$$
 (2.47)

The total depletion region width W is obviously given by

$$W = x_{\rm p} + x_{\rm n} = \sqrt{\frac{2\epsilon_{\rm s}}{q} \left(\frac{N_{\rm A} + N_{\rm D}}{N_{\rm A}N_{\rm D}}\right) V_{\rm bi}}.$$
(2.48)

In Eq. (2.48),  $V_{\rm bi} + V_{\rm R}$  will appear instead of  $V_{\rm bi}$ :

$$W = \sqrt{\frac{2\epsilon_{\rm s}}{q} \left(\frac{N_{\rm A} + N_{\rm D}}{N_{\rm A}N_{\rm D}}\right) (V_{\rm bi} + V_{\rm R})}.$$
(2.49)

The depletion region capacitance is related to the applied reverse-bias voltage  $V_{\rm R}$  through depletion region width W as Eq. (2.40), so that the depletion region capacitance can be expressed in the following compact form:

$$C = C_0 \left( 1 + \frac{V_{\rm R}}{V_{\rm bi}} \right)^{-1/2}, \tag{2.50}$$

where  $C_0$  is

$$C_{0} = \begin{cases} \frac{A}{2} \sqrt{\frac{2\epsilon_{\rm s} N_{\rm A}}{V_{\rm bi}}} & \text{for } N_{\rm D} >> N_{\rm A}, \\ \frac{A}{2} \sqrt{\frac{2\epsilon_{\rm s} N_{\rm D}}{V_{\rm bi}}} & \text{for } N_{\rm A} >> N_{\rm D}. \end{cases}$$

$$(2.51)$$



Figure 2.18 Linearly graded doped pn junction in thermal equilibrium.

#### Linearly graded doped junction capacitance

A pn junction is considered linearly graded doped, where the charge density  $\rho$  changes from the most negative value to the most positive value in the smoothest possible way, which is shown in Fig. 2.18. Therefore, the relationship between the electric field E and the charge density  $\rho$  is governed by the Poisson's equation as Eq. (2.52):

$$\frac{\mathrm{d}^2 V(x)}{\mathrm{d}x^2} = -\frac{\rho}{\epsilon_{\mathrm{s}}} = \frac{qax}{\epsilon_{\mathrm{s}}}, \qquad \text{for } -W/2 \le x \le W/2, \tag{2.52}$$

where a denotes the slope of the linear dependence, which depends on the doping concentration. The electric field E is then obtained by integrating Eq. (2.52):

$$-\frac{\mathrm{d}V(x)}{\mathrm{d}x} = E(x) = -\frac{qa}{\epsilon_{\rm s}} \frac{(W/2)^2 - x^2}{2}, \qquad \text{for } -W/2 \le x \le W/2. \tag{2.53}$$

The potential distribution V(x) is obtained by integrating the Eq. (2.53):

$$V(x) = \frac{qa}{2\epsilon_{\rm s}} \left[ \frac{x^3}{3} - \left(\frac{W}{2}\right)^2 x + \frac{W^3}{12} \right].$$
 (2.54)

The built-in potential  $V_{\rm bi}$  is given by

$$V_{\rm bi} = \frac{qaW^3}{12\epsilon_{\rm s}}.\tag{2.55}$$

The depletion region width W is obtained from Eq. (2.55) as

$$W = \left(\frac{12\epsilon_{\rm s}V_{\rm bi}}{qa}\right)^{1/3}.$$
(2.56)

The depletion region capacitance can be related to the applied reverse-bias voltage  $V_{\rm R}$  through depletion region width W as Eq. (2.40). Therefore, the depletion region capacitance can be expressed in the following compact form:

$$C = C_0 \left( 1 + \frac{V_{\rm R}}{V_{\rm bi}} \right)^{-1/3},\tag{2.57}$$

where  $C_0$  is

$$C_0 = A \left(\frac{qa\epsilon_{\rm s}^2}{12V_{\rm bi}}\right)^{1/3}.$$
 (2.58)

Eventually, the depletion capacitance depending on the applied reverse-bias voltage  $V_{\rm R}$  can be expressed in the following compact form:

$$C = C_0 \left( 1 + \frac{V_{\rm R}}{V_{\rm bi}} \right)^{-m}, \tag{2.59}$$

where  $C_0$  denotes the zero-bias capacitance,  $V_{\rm bi}$  the built-in potential barrier, and m the junction grading coefficient. In addition, m = 1/2 is for the uniformly doped and m = 1/3 for the linearly graded doped.

## 2.4 Summary

This chapter illustrated the cross section of a SiC power MOSFET cell, a lateraltype SiC JFET cell, and a vertical-type SiC JFET cell. This chapter also described the two most commonly used types of capacitances, which are the MOS capacitance and pn junction capacitance. Their device structures decide the voltage dependence of the capacitance characteristics. The voltage dependence of the MOS capacitance is distinguished as accumulation, depletion, and inversion conditions. The voltage dependence of the pn junction capacitance is expressed as the uniformly doped and the linearly graded doped junctions. The capacitances of the SiC power MOSFET and SiC JFETs including the internal parasitic capacitances will be measured by the capacitance measurement system, which is explained in Chapter 3. The measured capacitances of the SiC power MOSFET and SiC JFETs will be also shown and discussed in Chapter 4 and Chapter 5, respectively.

# Chapter 3

# Measurement of terminal capacitances and its voltage dependency for high-voltage power transistors

## 3.1 Introduction

Power electronics require high efficiency and versatile power conversion. High-voltage capability is preferable, especially in high-power circuits, to reduce the conduction loss of large currents. High-frequency switching enables minimization of bulky passive components and provides control functionality. Power switching devices are the key components to realize for power electronics. Therefore, it is strongly focused on a developing power device with a high breakdown voltage, low forward voltage drop, and fast switching capability [3,7,22,23].

It is well known that an Si-insulated gate bipolar transistor (IGBT) has been developed and improved to meet these requirements [45,46]. Recently, a superjunction structure of Si power MOSFET was proposed to realize a high breakdown voltage using a pn junction and fast switching capability by majority carriers [47–49]. In addition to the Si-based power device, wide band gap semiconductor power devices

have been researched and developed to achieve lower loss, higher voltage breakdown, and faster switching with a thin voltage blocking layer. SiC and GaN devices are good examples [1,3,9,11,16,31,48,50–57].

The terminal capacitances of a power device affect its switching behavior, because it must be charged and discharged during turn-off and turn-on operations [33,34]. The capacitances of a power device increase as the thickness of the voltage blocking layer is decreased to minimize conduction resistance. The capacitances vary widely with the applied bias voltage because of depletion in the voltage blocking layer. Therefore, it is necessary to quantify the terminal capacitances of the power device as well as the voltage dependency of capacitance. One method is to estimate the capacitance value with finite-element (FE) device simulation and validate it with circuit simulation or experiments [37,58]. However, this approach requires physical parameters a detailed device structure, dimensions, and process parameters. Another method is to characterize the capacitances experimentally. However, there is no commercial product that is able to measure the terminal capacitances of a high-voltage power device by applying the bias voltage up to its rated value. JEDEC [35] and IEC [36] standardized the capacitance measurement between the terminals of a power device with a capacitance bridge, but no actual configuration or circuit topology for the measurements are provided. Elferich et al. [37] measured the C-V characteristics of a power MOSFET and validated the FE device simulation; however, the measurement setup is not clearly described and the applied voltage was low (0 V  $\leq V_{\rm DS} \leq 20$  V, -10 V  $\leq V_{\rm GS} \leq 0$  V). Therefore, we developed a C-V measurement system for high-voltage power devices. Funaki et[38, 39] presented the C-V measurement system for high-voltage power diodes al.with evolving [40] and clarified the punch-through structure of SiC Schottky barrier diodes (SBDs) from the measured results. This study develops a C-V measurement system for gate-controlled, high-voltage power devices, e.g., power MOSFET, JFET, and IGBT. There are three terminals in a single device, and five specifications of the measurement circuit are presented to measure the capacitance between gate-source  $(C_{\rm GS})$ , gate-drain  $(C_{\rm GD})$ , and drain-source  $(C_{\rm DS})$ , and to measure input  $(C_{\rm ISS})$ , output  $(C_{\text{OSS}})$ , and reverse transfer  $(C_{\text{RSS}} = C_{\text{GD}})$  capacitances. The capacitances  $C_{\text{GS}}$ ,  $C_{\text{GD}}$ , and  $C_{\rm DS}$  are measured to clarify the device structure and physical behavior, and  $C_{\rm ISS}$ ,  $C_{\text{OSS}}$ , and  $C_{\text{RSS}}$  are used to estimate their influence on circuit operation.

The developed measurement circuit can apply a bias voltage between drain and source, and simultaneously to the gate with reference to the source potential. Thus, the circuit can measure the C-V characteristics for both normally-off and normally-on devices [60]. Also, it enables measurement of the capacitances from the blocking condition to the conducting condition with varying gate bias voltage. For instance, a power MOSFET is a high-voltage power device, and its measurements illustrate the physical phenomenon occurring in the device, which depends on the applied drain and gate bias voltages.

# 3.2 Capacitance of a power device and measurement circuit

This section examines the makeup of the capacitive component in a power transistor when assuming a planar gate device structure and a vertical drift region-type doublediffused MOSFET (VDMOSFET) [7]. Further, this chapter discusses a circuit for measuring the capacitance between the power device terminals. The circuit can apply bias voltages between drain and source  $V_{\rm DS}$ , and gate and source  $V_{\rm GS}$ , up to the rated voltage of the device.

#### 3.2.1 Terminal capacitances of VDMOSFET

Figure 3.1(a) shows the cross section of one cell in a VDMOSFET chip. The main dielectrics for inducing capacitance in the cell are the depletion layer formed in the semiconductor and the gate oxide. The capacitances arising from the gate oxide have a constant value, irrespective of the voltage applied across it. However, the capacitance arising from the depletion layer, which is formed in the semiconductor, changes with the applied voltage across it, where the capacitance is treated as a differential capacitance dQ/dV. Here, dQ denotes the charge depleted to the incremental bias voltage dV. The capacitance components residing in the VDMOSFET are integrated into three terminal capacitances  $C_{GS}$ ,  $C_{GD}$ , and  $C_{DS}$ , when they are estimated from the terminal of the



Figure 3.1 Example of a gate-controlled transistor to illustrate device capacitance.(a) Cross section of a VDMOSFET cell.(b) Equivalent capacitances between terminals of VDMOSFET.

electrode in a discrete device, as shown in Fig. 3.1(b). These terminal capacitances are configured by the capacitive components shown in Fig. 3.1(a) as

$$\begin{cases} C_{\rm GS} = C_{\rm m} + C_{\rm oxs} + \frac{1}{1/C_{\rm oxc} + 1/C_{\rm c}}, \\ C_{\rm GD} = \frac{1}{1/C_{\rm oxd} + 1/C_{\rm gdj}}, \\ C_{\rm DS} = C_{\rm dsj}. \end{cases}$$
(3.1)

Here,  $C_{\rm m}$  denotes the capacitance between the gate electrode and the source electrode across the gate oxide,  $C_{\rm oxs}$  the capacitance of the gate electrode and source n<sup>+</sup> region,  $C_{\rm oxc}$  the capacitance of the gate electrode and the top surface of the p<sup>+</sup> region,  $C_{\rm c}$ the capacitance of the depletion region for the p<sup>+</sup> region under the gate,  $C_{\rm oxd}$  the capacitance of the gate electrode and top surface of the drain region across the gate oxide,  $C_{\rm gdj}$  the capacitance of the depletion region for the drain under the gate, and  $C_{\rm dsj}$  the capacitance of the depletion region for the drain under the source.

The combination of terminal capacitances in the power device determines circuit operation. The input capacitance is the equivalent capacitance when the transistor is grasped from the gate terminal to drive the gate; it can be expressed as  $C_{\rm ISS} = C_{\rm GS} + C_{\rm GD}$ . The reverse transfer capacitance  $C_{\rm RSS}$  is the same as  $C_{\rm GD}$ . It induces the wellknown Miller effect and deteriorates the gate driving response because of the effectively increased capacitance by the multiplier factor of device transconductance [22]. The output capacitance corresponds to the capacitance from the drain terminal, and its charge/discharge operation by the drain current affects the main circuit response. It can be expressed as  $C_{\rm OSS} = C_{\rm DS} + C_{\rm GD}$ . Thus, five capacitance specifications are needed to characterize the device.

#### **3.2.2** $C_{\rm GS}$ measurement circuit

Figure 3.2 shows the circuit for measuring  $C_{\rm GS}$ . This circuit can perform fourterminal (Kelvin sense) measurements— $H_{pot}$  and  $L_{pot}$  (for detecting the small ac voltage of the measurement signal) and  $H_{cur}$  and  $L_{cur}$  (for detecting the current of the measurement signal). The four measurement terminals are connected to an LCR meter or impedance analyzer. C1 and C2 block the bias gate voltage, transferring only the ac measurement signal from terminals  $H_{\rm pot}$  and  $H_{\rm cur}$ . These blocking capacitors enable application of the  $V_{GS}$ , and the circuit measures the capacitance characteristics related to channel condition, such as accumulation, depletion, and inversion. Moreover, the blocking capacitance enables the measurement of  $C_{GS}$  for a normally-on device by applying a gate voltage and making the device channel operate in the blocking condition. The  $V_{\rm GS}$  and  $V_{\rm DS}$  impose the dc bias voltage, and the C-V characteristics are measured by sweeping one of them. The ac measurement signal at the source terminal is blocked by L1 (because of its high impedance at the operating frequency); therefore, it is transferred to terminals  $L_{cur}$  and  $L_{pot}$ . L1 shorts the source terminal to dc ground and establishes the dc bias voltages  $V_{\rm GS}$  and  $V_{\rm DS}$  at the device terminals with reference to ground potential. Diodes D1-D12 and ZD1-ZD4 provide protection. The RC circuit at the  $V_{\rm GS}$  and  $V_{\rm DS}$  input and the monitor output constitute a low-pass filter to block the measurement signal, and apply and measure the dc bias voltage. C7 shorts the drain terminal when measuring an ac frequency and blocks dc from the measurement.



Figure 3.2  $C_{\rm GS}$  measurement circuit.



Figure 3.3  $C_{\text{GD}}(C_{\text{RSS}})$  measurement circuit.

#### **3.2.3** $C_{\text{GD}}(C_{\text{RSS}})$ measurement circuit

Figure 3.3 shows the circuit diagram for measuring  $C_{\rm GD}(C_{\rm RSS})$ . This circuit has two groups of blocking capacitors for the drain and source terminals to ensure ground potential at the source terminal. C1 and C2 block the dc bias voltage of  $V_{\rm DS}$ , and C7 and C8 block the dc bias voltage of  $V_{\rm GS}$ . The capacitances transfer the ac measurement signal from  $H_{\rm cur}$  and  $H_{\rm pot}$  to  $L_{\rm cur}$  and  $L_{\rm pot}$ , respectively. The source terminal is directly grounded, and the capacitance component in the device related to the source terminal is excluded from the measurement. The dc bias voltages  $V_{\rm DS}$  and  $V_{\rm GS}$  are applied and monitored through the RC filter.

### **3.2.4** $C_{\rm DS}$ measurement circuit

Figure 3.4 shows the circuit diagram for measuring  $C_{\rm DS}$ . C1 and C2 block the dc bias voltage  $V_{\rm DS}$  and transfer the ac measurement signal from  $H_{\rm cur}$  and  $H_{\rm pot}$  terminals. The dc bias voltages  $V_{\rm DS}$  and  $V_{\rm GS}$  are applied and monitored through the RC filter



Figure 3.4  $C_{\rm DS}$  measurement circuit.

circuit. L1 connected to the source terminal, blocks the measurement ac signal and transfers it to  $L_{\rm cur}$  and  $L_{\rm pot}$ . However, it shorts the source terminal to dc ground and helps to establish the dc bias voltage with reference to the source terminal. C6 connected to the gate terminal, blocks the dc voltage, and establishes the dc potential of the gate terminal, but shorts ac signals to ground. Therefore, the capacitive component connected to the gate terminal is excluded from the measurement since it is shunted to the ground.

#### **3.2.5** $C_{\rm ISS}$ measurement circuit

Figure 3.5 shows the circuit diagram for measuring the input capacitance  $C_{\text{ISS}}$ . This circuit differs from the former measurement circuits in that it measures the combined capacitance of  $C_{\text{GS}}$  and  $C_{\text{GD}}$ , which have different dc potentials for the drain and source. C1, C2, C7, and C8 block the dc bias voltages of  $V_{\text{DS}}$  and  $V_{\text{GS}}$ , and transfer the ac measurement signal from  $H_{\text{cur}}$  and  $H_{\text{pot}}$  to  $L_{\text{cur}}$  and  $L_{\text{pot}}$ , respectively. The dc bias voltages  $V_{\text{DS}}$  and  $V_{\text{GS}}$  are applied and monitored through the RC filter. L1 shorts dc signals at the source terminal to ground, establishes the reference potential for the



Figure 3.5  $C_{\rm ISS}$  measurement circuit.

dc bias voltage, and blocks the ac measurement signal from shorting to ground. The blocked ac measurement signal is transferred to  $H_{\rm cur}$  and  $H_{\rm pot}$  terminals through the bypass capacitors C9 and C10. Consequentially, the capacitance between the drain and source terminals are eliminated by bypass capacitors C1, C2, C9, and C10.

#### **3.2.6** C<sub>OSS</sub> measurement circuit

Figure 3.6 shows the circuit diagram for measuring the output capacitance  $C_{\text{OSS}}$ , which is the combined capacitance of  $C_{\text{DS}}$  and  $C_{\text{GD}}$ —the capacitances have different dc potentials at the gate and source terminals. Capacitors C1 and C2 block the dc bias voltage of  $V_{\text{DS}}$  and transfer the ac measurement signal from terminals  $H_{\text{cur}}$ and  $H_{\text{pot}}$ . The dc bias voltages  $V_{\text{DS}}$  and  $V_{\text{GS}}$  are applied and monitored through the RC filter. L1 shorts dc signals to ground at the source terminal and establishes the reference potential for the dc bias voltage. It also blocks the ac measurement signal from shorting to ground and helps transfer it to terminals  $L_{\text{cur}}$  and  $L_{\text{pot}}$ . C6 blocks the



Figure 3.6  $C_{OSS}$  measurement circuit.

dc bias voltage of  $V_{\rm GS}$  from the source and passes the ac measurement signal, which is then transferred to  $L_{\rm cur}$  and  $L_{\rm pot}$  terminals. L1 provides a high ac resistance to ground. C6 bypasses and eliminates the  $C_{\rm GS}$ .

The values of the blocking and bypass capacitances are selected to have sufficiently small impedance with relation to the capacitance measurement or elimination ability in the device. Film-type capacitors are adopted because of their superior high frequency performance, but high-voltage-blocking large capacitors tend to be bulky and



Figure 3.7 Frequency characteristics of blocking element. (a) Blocking capacitor (1  $\mu$ F, 850 V) ( $C_{\rm S} + R_{\rm S}$  measurement), (b) Blocking capacitor (5  $\mu$ F, 700 V) ( $C_{\rm S} + R_{\rm S}$  measurement), and (c) Blocking inductor (1 mH) ( $L_{\rm S} + R_{\rm S}$ measurement)

have relatively large effective series inductance (ESL). Figure 3.7 shows the frequency characteristics of blocking element used for blocking high voltages and measurement ac signal as measured by an impedance analyzer (Agilent 4294A). The largest capacitance used in the measurement circuit has a self-resonant frequency around 300 kHz because of the capacitance and ESL, as shown in Fig. 3.7. JEDEC [60] suggests that the measurement frequency be low enough to prevent the introduction of the error stemming from parasitic components, and frequencies below 2 MHz are preferred. Therefore, 100 kHz was selected as the measurement frequency.

## **3.3** Measurement of *C*-*V* characteristics

This section certifies the measured capacitance using the developed capacitance measurement circuit, based on a reference capacitance set whose values are known a *priori*. The measured C-V characteristics of an example device are presented and their features discussed as associated with the device structure and composition.



Figure 3.8 Configuration of C-V characterization system.

$\mathbf{GS}$	GD	DS	$C_{\rm GS}$	$C_{\rm GD}$	$C_{\rm ISS}$	$C_{\rm GS} + C_{\rm GD}$	$C_{\rm DS}$	$C_{\rm OSS}$	$C_{\rm DS} + C_{\rm GD}$
			(err%)	(err%)	(err%)	$(\mathrm{err}\%)$	(err%)	(err%)	$(\mathrm{err}\%)$
$C_{\rm a}$	$C_{\rm b}$	$C_{\rm c}$	11.47	21.44	32.64	32.90	33.35	54.50	54.79
			(4.10)	(0.60)	(0.18)	(0.99)	(0.04)	(0.79)	(0.26)
$C_{\rm a}$	$C_{\rm c}$	$C_{\rm b}$	11.33	33.25	44.46	44.59	22.11	53.89	55.37
			(2.90)	(0.31)	(0.21)	(0.49)	(2.52)	(1.89)	(0.80)
$C_{\rm b}$	$C_{\rm a}$	$C_{\rm c}$	22.02	11.02	32.72	33.04	34.05	44.30	45.07
			(2.10)	(0.05)	(0.41)	(1.41)	(2.08)	(0.15)	(1.58)
$C_{\rm b}$	$C_{\rm c}$	$C_{\rm a}$	21.74	33.42	55.18	55.16	11.46	43.35	44.87
			(0.80)	(0.17)	(0.45)	(0.42)	(4.02)	(2.29)	(1.13)
$C_{\rm c}$	$C_{\rm a}$	$C_{\rm b}$	33.83	11.05	44.65	44.88	22.40	32.47	33.45
			(1.40)	(0.33)	(0.62)	(1.14)	(3.85)	(0.36)	(2.66)
$C_{\rm c}$	$C_{\rm b}$	$C_{\rm a}$	33.59	21.38	55.25	54.97	11.51	32.16	32.88
			(0.70)	(0.90)	(0.58)	(0.08)	(4.47)	(1.31)	(0.92)

Table 3.1 Test results for reference capacitance (nF)  $[C_a = 11.01 \text{ nF}, C_b = 21.57 \text{ nF}, C_c = 33.36 \text{ nF}].$ 

#### 3.3.1 Certification of the measurement circuit

The developed capacitance measurement circuit is connected to a HIOKI 3522 LCR meter to quantify the capacitance through measurement terminals  $H_{cur}$ ,  $H_{pot}$ ,  $L_{cur}$ , and  $L_{pot}$  as shown in Fig. 3.8. At the beginning of setting up the experiment, open- and short-circuit calibration of the measurement circuit is performed for LCRmeter operation. Although the developed circuit applies a bias voltage between terminals, a dc short-circuit current flows through the bias voltage source. Therefore, a 0-V dc bias voltage is applied during circuit calibration. Three capacitances  $C_a$ ,  $C_b$ , and  $C_c$ , whose values are given in the margin of Tab. 3.1 and are similar to those of an actual semiconductor device, are used to validate the measurement circuit. The test capacitors are constant capacitances connected in delta to imitate the terminal capacitance of a power device, and six possible combinations of the terminal connection are tested for the five capacitance measurements. The measured values for the respective combinations of reference capacitance connections are given in Tab. 3.1. The relative percentage error of the actual value is also given in parentheses. The compound capacitances  $C_{\rm GS} + C_{\rm GD}$  and  $C_{\rm DS} + C_{\rm GD}$ , which are, respectively, equivalent to  $C_{\rm ISS}$  and  $C_{\rm OSS}$ , are also shown in the table for comparison.

The measurement errors for  $C_{\rm GD}$  and  $C_{\rm ISS}$  were confirmed as less than 1% that is a low error. The error in measuring  $C_{\rm GS}$  tends to become large when  $C_{\rm DS}$  is larger than  $C_{\rm GS}$ . This can be attributed to measurement signal leakage in the blocking inductor L1 and bypass capacitor C7 (see Fig. 3.2). The opposite effects are found in the measurement of  $C_{\text{DS}}$ . The error in  $C_{\text{DS}}$  becomes large when  $C_{\text{GS}}$  is larger than  $C_{\text{DS}}$ . This is attributed to measurement signal leakage in blocking inductor L1 and bypass capacitor C6 (see Fig. 3.4). Thus, the errors of compound capacitance  $C_{\rm GS} + C_{\rm GD}$ tend to become larger than directly measured  $C_{\rm ISS}$ , except when  $C_{\rm DS}$  is small. The error in the measured  $C_{\text{OSS}}$  becomes large when  $C_{\text{GD}}$  is larger than  $C_{\text{DS}}$ . The leakage of the measurement signal through L1 in Fig. 3.6 cannot explain this phenomenon. Hence, this can be attributed to the residue of the measurement signal for the bypass capacitor C6 (see Fig. 3.6), i.e., the detection terminal for  $C_{\rm DS}$  is directly connected to the LCR meter through  $L_{cur}$  and  $L_{pot}$  terminals, but the detection terminal for  $C_{\rm GD}$  is connected to the *LCR* meter through C6. Therefore, the  $C_{\rm OSS}$  measurement circuit is amenable to  $C_{\rm GD}$  value. The errors of directly measured  $C_{\rm OSS}$  tend to become larger than the compound capacitance  $C_{\rm DS} + C_{\rm GD}$  when  $C_{\rm GD}$  is small. The extracted error falls within 5% using the measurement circuit parameters, as shown in Figs. 3.2-3.7. This error can be reduced by increasing the value of the blocking and bypassing elements. The accuracy given in Tab. 3.1 is sufficient to characterize the device because of the dispersion of the characteristics among devices.

#### 3.3.2 Measured Results

The measured C-V characteristics are exemplified here by considering a planar gate VDMOSFET with a 600-V-rated voltage (2SK3767) as an example, and the relationship of the capacitance characteristics to the device structure is discussed.

Figure 3.9(a) illustrates the relationship of the measured  $C_{\text{GS}}$ ,  $C_{\text{GD}}$ , and  $C_{\text{DS}}$  to  $V_{\text{DS}}$  with  $V_{\text{GS}} = 0$  V.  $C_{\text{GS}}$  is larger than  $C_{\text{DS}}$  and  $C_{\text{GD}}$  when  $V_{\text{DS}} > 1$  V because of the



Figure 3.9 Measured C-V characteristics of VDMOSFET for  $V_{\text{DS}}$ . (a)  $C_{\text{GS}}$ ,  $C_{\text{GD}}$ , and  $C_{\text{DS}}$  ( $V_{\text{GS}} = 0$  V). (b)  $C_{\text{ISS}}$  and  $C_{\text{OSS}}$  ( $V_{\text{GS}} = 0$  V). (c)  $C_{\text{GS}}$  for different  $V_{\text{GS}}$ . (d)  $C_{\text{GD}}$  for different  $V_{\text{GS}}$ .

closely spaced gate and source electrodes at the surface of the device. It barely changes with the applied  $V_{\rm DS}$ , because  $V_{\rm DS}$  does not affect the expansion of the depletion region across the gate and source. Also, depletion in the drift layer depends on  $V_{\rm DS}$ . Therefore,  $C_{\rm DS}$  and  $C_{\rm GD}$  decrease with increasing  $V_{\rm DS}$  in accordance with the expansion of the depletion region. There are irregular capacitance changes around  $V_{\rm DS} = 13$  V, which can be attributed to the transition of the expanding depletion region from the JFET region of the planar gate VDMOSFET to the entire drift region.

Figure 3.9(b) illustrates the directly measured  $C_{\rm ISS}$  and  $C_{\rm OSS}$  and the calculated  $C_{\rm ISS}(=C_{\rm GS}+C_{\rm GD})$  and  $C_{\rm OSS}(=C_{\rm DS}+C_{\rm GD})$  from the measured  $C_{\rm DS}$ ,  $C_{\rm GS}$ , and  $C_{\rm GD}$ .



Figure 3.10 (a) Measured C-V characteristics of VDMOSFET for  $V_{\text{GS}}$ . (b) Measured  $I_{\text{DS}_{\text{sat}}}$ - $V_{\text{G}}$  characteristics of VDMOSFET.

The respective results coincide, validating the adequacy of the measured results. Figure 3.9(c) shows measured  $C_{\rm GS}$  to  $V_{\rm DS}$  for different  $V_{\rm GS}$ . The accumulation of charge (holes) occurs at the device channel and results in a decrease in  $C_{\rm c}$ , as shown in Fig. 3.1(a), when a gate voltage of  $V_{\rm GS} = -20$  V is applied.  $C_{\rm GS}$  becomes larger than the depleted condition of the channel by the time  $V_{\rm GS} = 0$  V. This phenomenon is shown clearly in Fig. 3.10(a), where  $C_{\rm GS}$  is measured to  $V_{\rm GS}$  and  $V_{\rm DS} = 0$  V.  $C_{\rm GS}$ begins to decrease when  $V_{\rm GS}$  becomes higher than  $-3~{\rm V}$  and it reaches a minimum around  $V_{\rm GS} = 3$  V. This indicates the depletion of the accumulated charge (holes) at the channel with increase in  $V_{GS}$ . The inversion at the channel begins to occur with increasing gate voltages when  $V_{\rm GS}$  exceeds 3 V, and  $C_{\rm GS}$  increases to the threshold voltage. The threshold voltage of this device is 3.5 V, as shown in Fig. 3.10(b), and the channel conducts for a higher gate voltage. Figure 3.9(d) shows  $C_{\text{GD}}(C_{\text{RSS}})$  to  $V_{\text{DS}}$ for different  $V_{\rm GS}$ . The accumulation phenomenon is also seen at the top of the JFET region in a planar device around  $C_{gdj}$ , as shown in Fig. 3.1(a), and  $C_{GD}$  varies with  $V_{GS}$ . It also shows that negative  $V_{\rm GS}$  reduces  $C_{\rm GD}$ . This phenomenon is clearly confirmed in Fig. 3.10(a), where  $C_{\rm GD}$  is measured at  $V_{\rm GS}$  and  $V_{\rm DS} = 0$  V. The accumulation at the top of the JFET region tends to occur when voltages with different polarities are applied across that part, resulting in an increase in  $C_{\rm gdj}$  as shown in Fig. 3.1(a). Then,

 $C_{\rm GD}$  becomes large for low  $V_{\rm DS}$  within the -3 V  $< V_{\rm GS} < 3$  V region. The capacitance measurement is by no means restricted to merely determining the capacitance between terminals, but it can also clarify a wide variety of physical phenomenon occurring in the device.

### 3.4 Summary

The capacitances between the terminals of a power device are important for understanding the dynamic behavior of the device, such as its switching operation. The device capacitances are not constant and change with the voltage applied between the terminals. Therefore, a C-V characterization system for gate-controlled power devices was developed in this study. Five measurement circuits were proposed to measure the three combinations of capacitances between the device terminals, and three combinations of device capacitance for circuit operation. The adequacy of the proposed measurement system was verified using a reference capacitance and the factor of error was discussed. The developed capacitance characterization system can measure capacitance from the blocking condition to the conducting condition while changing the gate bias voltage. The variation of the accumulation, depletion, and inversion conditions in the device was reflected to the device capacitance. The measured capacitance explained the device structure and the physical phenomenon occurring in the device.

# Chapter 4

# Characterization of SiC power MOSFET

# 4.1 Introduction

Power MOSFETs are practically used in high frequency switching power converter circuits due to the fast turn-off capability [27,28]. Recently, power converters have been requested to operate at high voltage, high-temperature, and fast switching to realize their high performances. However, the limitation to the above requirements is low for the silicon (Si) power devices. To overcome the difficulty, silicon carbide (SiC) power devices have been researched and developed because of its several superior physical characteristics than Si [1,3,7]. The device modeling is inevitable in circuit simulation to evaluate the voltage and current response in power converter circuit and to achieve system performance in their applications. This chapter focuses on the modeling based on detailed measurements.

In the references [28, 61, 62], the dynamic behavior of the device is discussed with relation to their internal parasitic capacitances, drain-source current  $I_{\rm DS}$ , drain current  $I_{\rm T}(=I_{\rm D})$ , gate current  $I_{\rm G}$ , gate-source voltage  $V_{\rm GS}$ , and drain-source voltage  $V_{\rm DS}$ . The equivalent capacitance between terminals of the device affects on its switching behavior. The capacitance in a power device changes nonlinearly with applied voltage between terminals ( $V_{\rm GS}$  and  $V_{\rm DS}$ ), because it comprises the depletion capacitance in



Figure 4.1 (a) Equivalent terminal capacitances. (b) Cross section of SiC DiMOS-FET cell.

the device [29]. Then, it is important to characterize the C-V characteristics of the SiC MOSFET to estimate its switching performance. Figures 4.1(a) and (b) show the equivalent capacitance between terminals and the cross section of the SiC DiMOSFET cell, respectively [7, 8]. The equivalent terminal capacitances are composed of the capacitances  $C_{\rm GS}$ ,  $C_{\rm GD}$ , and  $C_{\rm DS}$ . Here, the  $C_{\rm GS}$  and  $C_{\rm GD}$ , which combine the gate oxide and depletion capacitance, constitute the input capacitance  $C_{\rm ISS}(=C_{\rm GS}+C_{\rm GD})$ . It is charged and discharged by the gate drive circuit for switching operation.  $C_{\rm GD}$  is also equivalent to the reverse transfer capacitance  $C_{\rm RSS}$ . The effective capacitance is multiplied the voltage gain of the MOSFET in switching operation by Miller effect. Also,  $C_{\rm GD}(=C_{\rm RSS})$  and  $C_{\rm DS}$  constitute the output capacitance  $C_{\rm OSS}(=C_{\rm GD} + C_{\rm DS})$ , which is charged and discharged by the load current, and governs the switching speed. The  $C_{\rm GS}$  mainly depends on the applied  $V_{\rm GS}$ , the  $C_{\rm GD}$  varies with both the  $V_{\rm GS}$  and  $V_{\rm DS}$ , and the  $C_{\rm DS}$  largely varies with the  $V_{\rm DS}$ .

This chapter characterizes the voltage dependency of terminal capacitances of the power MOSFETs, models the I-V characteristics with discussing the C-V characteristics of the devices, and extracts the model parameters from the measured C-V

characteristics. Next, this chapter discusses and compares the difference in  $V_{\rm GS}$  dependency of terminal capacitances between the SiC MOSFET and the Si MOSFET to estimate the difference in their switching behavior. The constitution of internal parasitic components in the devices are also addressed. Finally, the obtained model is validated by comparing the experimental results of the switching response.

### 4.2 Characterization

The details of the studied SiC power MOSFET are mentioned in Chapter 2. This section describes the characterization of the SiC power MOSFET, which has been carried out under room temperature. The static I-V characteristics for the forward conduction condition were measured as the dc characteristics using IWATSU IE-1198 curve tracer. The C-V characteristics for the reverse non-conducting condition were measured as the ac characteristics by the capacitance measurement system in Chapter 3.

#### 4.2.1 Forward dc characteristics of power MOSFET

Figures 4.2 and 4.3 show the measured and modeled forward conduction characteristics of the 900-V, 1-A SiC DiMOSFET and 600-V, 2-A Si DMOSFET, respectively. The  $V_{\rm GS}$  is set at a governing parameter. The charged/discharged currents for parasitic capacitance are neglected at steady-state condition. The steady-state forward *I-V* characteristics of a power MOSFET is drawn by a pentode like curve to a parameter of  $V_{\rm GS}$ . The relationship between  $I_{\rm DS}$  and  $V_{\rm DS}$  is modeled as [27,64] a function of  $V_{\rm GS}$ and  $V_{\rm DS}$  at the steady-state by Eq. (4.1) :

$$I_{\rm DS} \cong \begin{cases} \frac{\beta}{2(1+\theta(V_{\rm GS}-V_{\rm T}))} [2(V_{\rm GS}-V_{\rm T})V_{\rm DS}-V_{\rm DS}^2](1+\lambda V_{\rm DS}) \\ \text{for } V_{\rm DS} \le V_{\rm GS}-V_{\rm T}, \\ \frac{\beta}{2(1+\theta(V_{\rm GS}-V_{\rm T}))} (V_{\rm GS}-V_{\rm T})^2(1+\lambda V_{\rm DS}) \\ \text{for } V_{\rm DS} > V_{\rm GS}-V_{\rm T}, \end{cases}$$
(4.1)

where  $\beta$  denotes the MOSFET channel transconductance,  $V_{\rm T}$  the threshold voltage,  $\lambda$  the channel length modulation factor, and  $\theta$  the mobility modulation coefficient. Here, the effect of drain resistance  $R_{\rm D}$  and source resistance  $R_{\rm S}$  in this model is neglected.



Figure 4.2 Static *I-V* characteristics of SiC DiMOSFET.



Figure 4.3 Static *I-V* characteristics of Si DMOSFET.



Figure 4.4 Transfer characteristics of power MOSFET.

#### Determination of $\beta$ and $V_{\rm T}$

The drain-source current of MOSFET  $I_{\rm DS}$  is given irrespectively to the drain voltage by Eq. (4.1) for saturation region of  $V_{\rm DS} > V_{\rm GS} - V_{\rm T}$ . Thus, the MOSFET channel transconductance  $\beta$  and the threshold voltage  $V_{\rm T}$  can be estimated from Eq. (4.1) with the MOSFET transfer characteristics, which is shown in Fig. 4.4, when the  $\lambda$  is approximately equal to zero.

#### Determination of $\lambda$

The channel length modulation factor  $\lambda$  is determined from the rating current on a set of static *I-V* characteristics in the saturation region. The detailed definition on  $\lambda$  is given in Ref. [63].

#### Determination of $\theta$

The deviation of the measured  $I_{\rm DS}$  current from the linear dependence in due to the mobility reduction effect, and is taken into account by the mobility modulation coefficient  $\theta$ . Therefore,  $\theta$  is determined from the linear region by Eq. (4.1) [65].

The model extracted parameters of static I-V characteristics of power MOSFET are summarized to Tab. 4.1.

# 4.2.2 Reverse conduction dc characteristics of power MOS-FET

Due to the device structure, the power MOSFET has a body diode, which is connected anti-parallel to drain-source of the power MOSFET as depicted in Fig. 4.1(b). In the body diode *I-V* curve measurement, the device channel needs to be pinched off during the measurement. This implies shorting the gate-source terminals ( $V_{\rm GS} = 0$ 



Figure 4.5 Reverse conduction characteristics of power MOSFET.

V) of the power MOSFET. Figure 4.5 shows the reverse conduction characteristics of power MOSFET. The dc characteristics of body diode of power MOSFET can be expressed as

$$I_{\rm AK} = I_{\rm S} \left( e^{\frac{V_{\rm D}}{nV_{\rm t}}} - 1 \right), \tag{4.2}$$

where  $V_t$  denotes the thermal voltage, *n* the diode emission coefficient, and  $I_s$  the saturation current. Then,  $I_s$  and *n* are extracted by the LMS method by applying the measured data to Eq. (4.2).

#### 4.2.3 C-V characteristics of power MOSFET

The various internal parasitic components of the device are superimposed on its cross section in Fig. 4.1(b). The physical capacitances residing in the SiC DiMOSFET are composed of the gate oxide and the depletion layer formed in the semiconductor. They are integrated into the equivalent terminal capacitances of power MOSFET  $C_{\rm GS}$ ,  $C_{\rm GD}$ , and  $C_{\rm DS}$ .  $C_{\rm GS}$  and  $C_{\rm GD}$  constitute the input capacitance  $C_{\rm ISS}(=C_{\rm GS}+C_{\rm GD})$ , which is charged and discharged by the gate drive circuit for switching operation.  $C_{\rm GD}$ is also equivalent to the reverse transfer capacitance (or Miller capacitance)  $C_{\rm RSS}$ . Also,  $C_{\rm GD}(=C_{\rm RSS})$  and  $C_{\rm DS}$  constitute the output capacitance  $C_{\rm OSS}(=C_{\rm GD}+C_{\rm DS})$ , which is charged and discharged by the load current, and governs the switching speed.

In the experimental setup for C-V characterization, the voltage dependence of the terminal capacitances is evaluated by the clarification of the device structure and fabrication. The C-V characteristics of power MOSFET are precisely measured by a LCR meter with applying the dc bias voltage  $V_{\rm GS}$  and  $V_{\rm DS}$  to the device, through C-Vmeasurement fixture in Chapter 3.

#### Characterization of the drain-voltage dependency of terminal capacitances

This section characterizes the drain-voltage dependency of terminal capacitances  $C_{\text{GS}}$ ,  $C_{\text{GD}}$ , and  $C_{\text{DS}}$ . The  $C_{\text{GS}}$ ,  $C_{\text{GD}}$ , and  $C_{\text{DS}}$  are individually measured with applying dc bias voltage  $V_{\text{DS}}$ .

Figures 4.6 and 4.7 show the C- $V_{\rm DS}$  characteristics of power MOSFET, which illustrate the relationships between the measured  $C_{\rm GS}$ ,  $C_{\rm GD}$ ,  $C_{\rm DS}$ , and the  $V_{\rm DS}$ , for a 600-V,



Figure 4.6  $C-V_{\rm DS}$  characteristics of Si DMOSFET.

2-A Si DMOSFET and a 900-V, 1-A SiC DiMOSFET, respectively. The measured C- $V_{\rm DS}$  characteristics of the Si DMOSFET and SiC DiMOSFET are shown in Figs. 4.6(a) and 4.7(a) at logarithmic scale. The measured and modeled C- $V_{\rm DS}$  characteristics of the Si DMOSFET and SiC DiMOSFET are shown in Figs. 4.6(b) and 4.7(b) at linear



Figure 4.7  $C-V_{DS}$  characteristics of SiC DiMOSFET.

scale. Setting  $V_{\rm GS} = 0$  V to block the device channel for  $V_{\rm DS}$  dependency,  $V_{\rm DS}$  is swept from 0 V to 600 V. The relationship between the capacitance characteristics can be obtained.  $C_{\rm GS}$  hardly changes with the variation of  $V_{\rm DS}$ . The values are around 304 pF for Si DMOSFET and 88 pF for SiC DiMOSFET. Because  $V_{\rm DS}$  does not govern the expansion of the depletion region across the gate and source. Also, depletion region in drift layer depends on  $V_{\rm DS}$ . On the other hand,  $C_{\rm GD}$  and  $C_{\rm DS}$  decrease with increase of  $V_{\rm DS}$  in accordance with the expansion of the depletion region. For the Si DMOSFET, there are irregular capacitance changes around  $V_{\rm DS} = 12$  V, which can be attributed to the transition of the expanding depletion region from JFET region of the planar gate MOSFET to the entire drift layer. For the SiC DiMOSFET, there are no irregular capacitance, and the decrease of the capacitance in  $C_{\rm GD}$  and  $C_{\rm DS}$  stops around  $V_{\rm DS}$ = 200 V. It indicates that the expansion of the depletion region is terminated in the drift layer because of the punch-through structure of the device.

The  $C-V_{\text{DS}}$  characteristics of power MOSFETs are modeled by using Eqs. (2.36), (2.41), and (2.42). It can be expressed in the following compact form:

$$C_{\rm GS} = C_{\rm GS}(0),$$
 (4.3)

$$C_{\rm gdj} = C_{\rm GD}(0) \left(1 + \frac{V_{\rm DS} - V_{\rm GS}}{V_{\rm TD}}\right)^{-1/2},$$
 (4.4)

$$C_{\rm DS} = C_{\rm DS}(0) \left(1 + \frac{V_{\rm DS}}{V_{\rm bi}}\right)^{-1/2},\tag{4.5}$$

where  $C_{\rm GS}(0)$  denotes the gate-source zero-bias capacitance,  $C_{\rm GD}(0)$  the gate-drain zero-bias capacitance, and  $C_{\rm DS}(0)$  the drain-source zero-bias capacitance.

#### Characterization of the gate-voltage dependency of terminal capacitances

This section characterizes the gate-voltage dependency of input capacitance  $C_{\rm ISS}(=C_{\rm GS}+C_{\rm GD})$ . The  $C_{\rm GS}$ ,  $C_{\rm GD}$ , and  $C_{\rm ISS}$  are individually measured with applying dc bias voltage  $V_{\rm GS}$ .

Figures 4.8(a) and (b) show the measured C-V characteristics, which illustrate the relationships between the measured  $C_{\rm GS}$ ,  $C_{\rm GD}$ ,  $C_{\rm ISS}$ , and the  $V_{\rm GS}$ , for a 600-V, 2-A Si DMOSFET and a 900-V, 1-A SiC DiMOSFET, respectively. The measurements are performed with keeping  $V_{\rm DS} = 0$  V to minimize the depletion region at the top of the n<sup>-</sup>-epitaxial layer ( $C_{\rm gdj}$ ) and to neglect its influence in the equivalent capacitance. When  $V_{\rm GS}$  is swept from -25 V to +25 V, the relationship between the capacitance characteristics and the device structure can be estimated.


Figure 4.8 Measured  $C-V_{GS}$  characteristics of power MOSFET.

When the applied voltage  $V_{\rm GS}$  is lower than -5 V for a Si DMOSFET and -7 V for a SiC DiMOSFET, the capacitance holds a constant value. This is because the carrier accumulation occurs at the device channel in the top of the p well region. The  $C_{\rm c}$  results in very large capacitance or disappears with conducting condition. Then,

the  $C_{\rm GS}$  achieves their highest values. On the other hand, the inversion occurs at the top of the n<sup>-</sup>-epitaxial layer under the gate oxide as the negative  $V_{\rm GS}$  attracts holes to the interface and constitutes depletion layer underneath. Then the  $C_{\rm gdj}$  becomes very small. Thus, the  $C_{\rm GD}$  achieves its lowest value.

When the applied voltage  $V_{\rm GS}$  becomes higher than -5 V for the Si DMOSFET and -7 V for the SiC DiMOSFET, the  $C_{\rm GS}$  begins to decrease and reaches to a minimum value. The minimum value occurs around  $V_{\rm GS} = 3$  V for the Si DMOSFET and = 1 V for the SiC DiMOSFET, because the holes in the p well are repelled from the surface. Thus, the depletion layer appears at the surface of the channel. The inversion at the channel begins to occur with increasing  $V_{\rm GS}$  when  $V_{\rm GS}$  exceeds 3 V for the Si DMOSFET and 1 V for the SiC DiMOSFET. The  $C_{GS}$  increases up to the threshold gate voltage  $V_{\rm T}$  where the  $C_{\rm c}$  disappears by channel conduction. At the same region of  $V_{\rm GS}$ , the electrons are attracted to the top of the JFET region or the n<sup>-</sup>-epitaxial layer under the gate oxide. Thus, it induces the accumulation layer there, and increase of  $C_{\rm gdj}$ . Then, the  $C_{\rm GD}$  becomes large within  $-3 \text{ V} < V_{\rm GS} < 3 \text{ V}$  region for the Si DMOSFET and -5 V  $< V_{\rm GS} < 5$  V for the SiC DiMOSFET. The  $V_{\rm T}$  of the Si DMOSFET is 3.5 V and the  $V_{\rm T}$  of the SiC DiMOSFET is 5.0 V, as shown in Fig. 4.3. The  $V_{\rm T}$  from measured C-V characteristics corresponds to the  $V_{\rm T}$  from the measured  $\sqrt{I_{\rm DS_{sat}}}$ -V<sub>GS</sub> characteristics. In Fig. 4.4, when  $V_{\rm GS} < V_{\rm T}$ , the measured  $\sqrt{I_{\rm DS_{sat}}}$  is kept around 0.1  $A^{1/2}$ . This does not imply the leakage current, but the residual error due to quantization of A/D converter in the curve tracer.

The channel conducts when the applied voltage  $V_{\rm GS}$  becomes higher than the  $V_{\rm T}$ . Then, the strong inversion of electrons occurs at the top of the p well region. The  $C_{\rm GS}$  of the Si DMOSFET becomes abruptly large and saturates with increasing  $V_{\rm GS}$ , but the  $C_{\rm GS}$  of the SiC DiMOSFET becomes gradually large and hardly saturates due to  $V_{\rm GS}$ . This non-saturable characteristics stem from the short channel effects [43]. The channel length of the SiC DiMOSFET is approximately equal to 0.75  $\mu$ m. Thus, the channel resistance  $R_{\rm ch}$  of the Si DMOSFET in Fig. 4.1(a) is much lower than that of the SiC DiMOSFET. At the same region of  $V_{\rm GS}$ , the electrons are attracted to the surface of the JFET region and forms the accumulation layer when  $V_{\rm DS}$  is lower than  $V_{\rm GS}$ . The  $C_{\rm GD}$  of the Si DMOSFET becomes abruptly small and saturates with increasing  $V_{\rm GS}$ , but the  $C_{\rm GD}$  of the SiC DiMOSFET becomes gradually small and hardly saturates with increasing  $V_{\rm GS}$ . The variation of the  $C_{\rm GD}$  associates with the total of the parasitic resistance  $R_{\rm JFET}$  and epitaxial resistance  $R_{\rm epi}$ , which depend on the impurity concentration in n<sup>-</sup>-epitaxial layer [27] [44]. These resistances of the Si DMOSFET are higher than that of the SiC DiMOSFET, because the doped impurity concentration of Si DMOSFET is lower than that of SiC DiMOSFET [7,44]. The  $C_{\rm GD}$ characteristics in Fig. 4.8 is validated for this facts.

As the results in Figs. 4.8(a) and (b), the  $C_{\rm ISS}$  are obtained as the sum of  $C_{\rm GS}$ and  $C_{\rm GD}$ . In Fig. 4.8(b), the measured  $C_{\rm ISS}$  is smaller than the sum of  $C_{\rm GS}$  and  $C_{\rm GD}$ . This can be attributed to the overlap area, between p well and n<sup>-</sup>-epitaxial layer, which appears through the strong inversion and the accumulation of electrons at the top of them individually. The difference of the *C-V* characteristics between the Si DMOSFET and the SiC DiMOSFET is explained by the short channel effects in SiC DiMOSFET and the doping density difference in the n<sup>-</sup>-epitaxial layer.

The model extracted parameters of C-V characteristics of power MOSFET are detailed in Tab. 4.1.

Parameter	Si power MOSFET	SiC power MOSFET
eta	$1.1 \mathrm{A/V^2}$	$0.055 \text{ A/V}^2$
$V_{\mathrm{T}}$	$3.5 \mathrm{V}$	$5.0 \mathrm{~V}$
$\lambda$	$0.002~1/\mathrm{V}$	$0.035~1/\mathrm{V}$
heta	$0.046 \ 1/V$	$0.025 \ 1/V$
$C_{\mathrm{oxd}}$	$293~\mathrm{pF}$	$176 \mathrm{\ pF}$
$C_{\rm GS}(0)$	304  pF	88 pF
$C_{ m GD}(0)$	$98 \mathrm{\ pF}$	$95 \mathrm{ pF}$
$C_{\rm DS}(0)$	$228 \mathrm{\ pF}$	$144 \mathrm{\ pF}$

Table 4.1 Model extracted parameters for Si and SiC power MOSFETs.

#### 4.2.4 Dynamic behavior of power MOSFET

The internal parasitic capacitances of the power MOSFET, which are shown in Fig. 4.1(a), mainly depend on the variable depletion capacitances and constant MOS layer capacitances in Fig. 4.1(b). The dynamic behavior of Si and SiC power MOSFET is governed by these capacitances that are the functions of the relative terminal voltages  $(V_{\rm GS} \text{ and } V_{\rm DS})$ . The gate current  $I_{\rm G}$  flowing through the input of power MOSFET is given by Eq. (4.6):

$$I_{\rm G} = \left(C_{\rm GS} + C_{\rm GD}\right) \frac{\mathrm{d}V_{\rm GS}}{\mathrm{d}t} - C_{\rm GD} \frac{\mathrm{d}V_{\rm DS}}{\mathrm{d}t},\tag{4.6}$$

and the difference between drain current  $I_{\rm T}(=I_{\rm D})$  and drain-source current  $I_{\rm DS}$  is expressed by Eq. (4.7):

$$I_{\rm T} - I_{\rm DS} = \left(C_{\rm DS} + \frac{C_{\rm GS}C_{\rm GD}}{C_{\rm GS} + C_{\rm GD}}\right) \frac{{\rm d}V_{\rm DS}}{{\rm d}t} - \frac{C_{\rm GD}}{C_{\rm GS} + C_{\rm GD}}I_{\rm G}.$$
(4.7)

Eventually, the dynamic behavior of Si and SiC power MOSFET is given by Eqs. (4.8) and (4.9) at charging/discharging these capacitances:

$$\frac{\mathrm{d}V_{\mathrm{GS}}}{\mathrm{d}t} = \frac{I_{\mathrm{G}}}{C_{\mathrm{GS}} + C_{\mathrm{GD}}} + \frac{C_{\mathrm{GD}}}{C_{\mathrm{GS}} + C_{\mathrm{GD}}} \cdot \frac{\mathrm{d}V_{\mathrm{DS}}}{\mathrm{d}t},\tag{4.8}$$

$$\frac{\mathrm{d}V_{\mathrm{DS}}}{\mathrm{d}t} = \frac{I_{\mathrm{T}} - I_{\mathrm{DS}} + \frac{C_{\mathrm{GD}}}{C_{\mathrm{GS}} + C_{\mathrm{GD}}} \cdot I_{\mathrm{G}}}{C_{\mathrm{DS}} + \frac{C_{\mathrm{GS}}C_{\mathrm{GD}}}{C_{\mathrm{GS}} + C_{\mathrm{GD}}}}.$$
(4.9)

The depletion capacitance in gate-drain capacitance  $C_{\text{GD}}$  and drain-source capacitance  $C_{\text{DS}}$  is modeled by using the differential capacitance in Chapter 2.

## 4.3 Evaluation of switching response

The transient switching response of the Si and SiC power MOSFET is evaluated by the test circuit with a power supply, a load, and a gate drive circuit. The inductive load circuit is shown in Fig. 4.9. The state equations of the load circuit and gate drive circuit are given as Eqs. (4.10) and (4.11), respectively:

$$\frac{\mathrm{d}I_{\mathrm{D}}}{\mathrm{d}t} = \frac{1}{L_{\mathrm{L}}} \Big( V_{\mathrm{AA}} - R_{\mathrm{L}}I_{\mathrm{D}} - V_{\mathrm{DS}} \Big),\tag{4.10}$$

$$I_{\rm G} = \frac{V_{\rm GG} - V_{\rm GS}}{R_{\rm G}},\tag{4.11}$$



Figure 4.9 Inductive load circuit for measured switching characteristics of power MOSFET.

where  $I_{\rm D}$  denotes the total current  $I_{\rm T}$ ,  $L_{\rm L}$  the drain series inductance including parasitic,  $R_{\rm L}$  the drain series resistance,  $V_{\rm AA}$  the drain supply voltage, and  $V_{\rm GG}$  the gate pulse generator voltage.

The state equations in Eqs. (4.8) and (4.9) of the power MOSFET can be solved simultaneously with state equations in Eqs. (4.10) and (4.11) of the load circuit.

Figures 4.10-4.13 show both simulated and measured waveforms of the Si power MOSFET at turn-on and turn-off. Figures 4.14-4.17 also show both simulated and measured waveforms of the SiC power MOSFET at turn-on and turn-off. The drain supply voltage  $V_{AA}$  is set at 100 V. The drain series inductance including parasitic  $L_{L}$  is 200 nH, and the drain series resistance  $R_{L}$  is 103  $\Omega$ . The gate pulse generator voltage  $V_{GG}$  is set at 20 V. The gate series resistance  $R_{G}$  is varied to provide different turn-on and turn-off speed for the Si and SiC power MOSFET by 10  $\Omega$ , 51  $\Omega$ , 100  $\Omega$ , and 200  $\Omega$ .

The turn-on process begins with the gate drive circuit when the gate drive voltage rises up to 20 V. Gate current  $I_{\rm G}$  immediately begins to flow as the gate-source capacitance  $C_{\rm GS}$  and gate-drain capacitance  $C_{\rm GD}$  are charged passing through the gate series resistance  $R_{\rm G}$ . When gate-source voltage  $V_{\rm GS}$  increases to the threshold voltage  $V_{\rm T}$ , the drain current  $I_{\rm D}$  begins to increase and the drain-source voltage  $V_{\rm DS}$  also begins to decrease to  $I_{\rm D}R_{\rm DSon}$ . The simulated and measured turn-on responses of  $I_{\rm G}$  and  $V_{\rm GS}$  are shown in Fig. 4.10 for Si power MOSFET and Fig. 4.14 for SiC power MOSFET. The SiC power MOSFET shows faster turn-on speed of measured  $V_{\rm GS}$  than the Si power MOSFET. Because the SiC power MOSFET has smaller the gate-source capacitance  $C_{\rm GS}$  and gate-drain capacitance  $C_{\rm GD}$  than the Si power MOSFET, as shown in Fig. 4.8. On the other hand, The simulated and measured turn-on responses of  $I_{\rm D}$  and  $V_{\rm DS}$ are shown in Fig. 4.11 for Si power MOSFET and Fig. 4.15 for SiC power MOSFET. The turn-on speed of  $V_{\rm DS}$  between the SiC power MOSFET and the Si power MOS-FET is slightly different, because the gate-drain capacitance  $C_{\rm GD}$  and drain-source capacitance  $C_{\rm DS}$  of the Si and SiC power MOSFETs respectively shown in Figs. 4.6 and 4.7 are rather same values.

Additionally, the turn-off process begins when the gate drive voltage falls to 0 V. The gate-source capacitance  $C_{\text{GS}}$  and gate-drain capacitance  $C_{\text{GD}}$  are discharged with the gate current  $I_{\rm G}$  passing through the gate series resistance  $R_{\rm G}$ . Once gate-source voltage  $V_{\rm GS}$  decreases to the threshold voltage  $V_{\rm T}$ , the drain current  $I_{\rm D}$  begins to decrease and the drain-source voltage  $V_{\rm DS}$  also begins to increase to the drain voltage supply  $V_{AA}$ . The simulated and measured turn-off responses of  $I_G$  and  $V_{GS}$  are shown in Fig. 4.12 for Si power MOSFET and Fig. 4.16 for SiC power MOSFET. And also, the SiC power MOSFET shows faster turn-off speed of measured  $V_{GS}$  than the Si power MOSFET. Because the SiC power MOSFET has smaller the gate-source capacitance  $C_{\rm GS}$  and gate-drain capacitance  $C_{\rm GD}$  than the Si power MOSFET, as shown in Fig. 4.8. On the other hand, The simulated and measured turn-off responses of  $I_{\rm D}$  and  $V_{\rm DS}$  are shown in Fig. 4.13 for Si power MOSFET and Fig. 4.17 for SiC power MOSFET. The turn-off speed of  $V_{\rm DS}$  between the SiC power MOSFET and the Si power MOSFET is slightly different, because the gate-drain capacitance  $C_{\text{GD}}$  and drain-source capacitance  $C_{\rm DS}$  of the Si and SiC power MOSFETs respectively shown in Figs. 4.6 and 4.7 are rather same values. But the SiC power MOSFET has smaller delay time of  $I_{\rm D}$  and  $V_{\rm DS}$  than the Si power MOSFET during turn-off, when the gate series resistance  $R_{\rm G}$ increases. Because the gate-source capacitance  $C_{\rm GS}$  and gate-drain capacitance  $C_{\rm GD}$ of the SiC power MOSFET in Fig. 4.8(b) are less than that of the Si power MOSFET in Fig. 4.8(a).

At small gate series resistance  $R_{\rm G}$  about 10  $\Omega$ , the measured current and voltage oscillate due to the resonance between parasitic inductances of wiring and internal parasitic capacitances. There are differences between the simulated results through the model and the measured results for the gate current  $I_{\rm G}$  and gate-source voltage  $V_{\rm GS}$ , especially at turn-off of Si and SiC power MOSFET with high gate series resistance  $R_{\rm G}$ . When gate series resistance  $R_{\rm G}$  increases, the measured  $I_{\rm G}$ ,  $V_{\rm GS}$ , and  $I_{\rm D}$  become smooth waveforms. Because time constant increasingly associated with the gate series resistance  $R_{\rm G}$  increase. Thereby, the responses of all of the current and voltage are not affected by parasitic components. Therefore, the current and voltage show the well correspondence with measured results. In this case, the simulated results cannot show the oscillation of the current and voltage at small gate series resistance  $R_{\rm G}$  because its parasitic gate inductance  $L_{\rm G}$  in the gate drive circuit are neglected.

The SiC power MOSFET shows faster turn-off speed than the Si power MOSFET. Because the SiC power MOSFET has smaller  $C_{\text{GS}}$ ,  $C_{\text{GD}}$ , and  $C_{\text{DS}}$  than the Si power MOSFET as shown in Fig. 4.6 and 4.7 for Si power MOSFET and SiC power MOSFET, respectively. And also, the rise time and fall time of current and voltage for Si and SiC power MOSFET increase when  $R_{\text{G}}$  increases.

### 4.4 Summary

In order to predict the device characteristics of Si and SiC power MOSFET accurately over their wide range of operation, a physics-based model was studied and proposed based on terminal capacitances. This chapter also discussed the parameter extraction for the model and the I-V characteristics for model with precisely measured C-V characteristics of Si and SiC power MOSFETs. It was shown that the simulated results of the switching behavior well agree with the experimental results for some conditions of the model and extracted parameters.

In addition, this chapter characterized and discussed the switching characteristics of power MOSFETs through the voltage dependency of terminal capacitances. The difference between the switching characteristics of the Si and SiC power MOSFETs depends on their internal parasitic capacitances, which can be classified by the MOS capacitance and pn junction capacitance.



Figure 4.10 Measured and simulated turn-on response of  $I_{\rm G}$  and  $V_{\rm GS}$  for Si power MOSFET as a function of gate series resistance.



Figure 4.11 Measured and simulated turn-on response of  $I_{\rm D}$  and  $V_{\rm DS}$  for Si power MOSFET as a function of gate series resistance.



Figure 4.12 Measured and simulated turn-off response of  $I_{\rm G}$  and  $V_{\rm GS}$  for Si power MOSFET as a function of gate series resistance.



Figure 4.13 Measured and simulated turn-off response of  $I_{\rm D}$  and  $V_{\rm DS}$  for Si power MOSFET as a function of gate series resistance.



Figure 4.14 Measured and simulated turn-on response of  $I_{\rm G}$  and  $V_{\rm GS}$  for SiC power MOSFET as a function of gate series resistance.



Figure 4.15 Measured and simulated turn-on response of  $I_{\rm D}$  and  $V_{\rm DS}$  for SiC power MOSFET as a function of gate series resistance.



Figure 4.16 Measured and simulated turn-off response of  $I_{\rm G}$  and  $V_{\rm GS}$  for SiC power MOSFET as a function of gate series resistance.



Figure 4.17 Measured and simulated turn-off response of  $I_{\rm D}$  and  $V_{\rm DS}$  for SiC power MOSFET as a function of gate series resistance.

## Chapter 5

## **Characterization of SiC JFET**

## 5.1 Introduction

Recently, SiC-based semiconductor power devices are strongly expected to replace Si power devices at high-temperature, high switching frequency, and high voltage application [1]. Among the devices, transistors are the most possible power switches for power conversions. Several types of SiC-based transistors have been proposed and developed. Junction field-effect transistor (JFET) is preferred for its low onresistance  $R_{\rm DSon}$  and ruggedness in harsh environments. Lateral-type and verticaltype SiC JFETs [21, 60, 66] have been developed. Their structures have shown the normally-on characteristics for a long time, but recently the normally-off type devices were developed. In this dissertation, both types are under test experimentally. However, low on-resistance  $R_{\rm DSon}$  characteristics of JFET are violated by achieving normally-off characteristics. Then, the SiC JFETs discussed in this study are limited in normally-on type devices.

The switching behavior of actual power devices is far from ideal. The non-ideal characteristics of SiC device affect on the performance of power conversion circuits, especially at high switching frequency. Then, the characteristics of the devices must be clarified and evaluated in advance of the design of power conversion circuits. Here, the switching characteristics of two different types SiC JFETs are discussed with relation to their internal parasitic capacitances, drain-source current  $I_{\rm DS}$ , drain current



Figure 5.1 (a) Equivalent parasitic terminal capacitances of JFET, (b) Cross section of lateral-type SiC JFET cell, and (c) Cross section of vertical-type SiC JFET cell.

 $I_{\rm D}$ , gate current  $I_{\rm G}$ , gate-source voltage  $V_{\rm GS}$ , and drain-source voltage  $V_{\rm DS}$ . Their definitions are shown in Fig. 5.1(a). The parasitic capacitances in FET, which are shown in Figs. 5.1(b) and (c), are composed of gate-source capacitance  $C_{\rm GS}$ , gate-drain capacitance  $C_{\rm GD}$ , and drain-source capacitance  $C_{\rm DS}$ .  $C_{\rm GS}$  and  $C_{\rm GD}$  constitute the input capacitance  $C_{\rm ISS}(=C_{\rm GS}+C_{\rm GD})$ , which is charged and discharged by the gate drive circuit for switching operation.  $C_{\rm GD}$  is also equivalent to the reverse transfer capacitance  $C_{\rm RSS}$ . The effective capacitance is multiplied by the voltage gain of the FET in switching operation by Miller effect. Also,  $C_{\rm GD}(=C_{\rm RSS})$  and  $C_{\rm DS}$  constitute the output capacitance  $C_{\rm OSS}(=C_{\rm GD}+C_{\rm DS})$ , which is charged and discharged by the load current and governs the switching speed. Major part of these effective capacitance is originated from the junction capacitances in the semiconductor, which vary in accordance with the applied voltage. Therefore, the characteristics of terminal capacitances are substantial for understanding the switching behavior.

A model of semiconductor device is indispensable for evaluating the voltage and current response at switching in circuit simulation and estimating the system performance in their applications. The dynamics at the transient state are obviously governed by these characteristics of devices.

This chapter characterizes the static I-V characteristics and the voltage dependency of terminal capacitances of SiC JFETs at first, then the switching behaviors are experimentally evaluated. Next, we discuss the C-V and switching characteristics based on their device structures and the semiconductor physics. In the end, the simulated switching behaviors of both SiC JFETs are validated with the experimental results.

## 5.2 Characterization of SiC JFET devices

The details of the studied lateral-type and vertical-type SiC JFETs were explained in Chapter 2. In this section, the characterizations of both SiC JFETs are figured out under room temperature. The static I-V characteristics for the forward conduction condition were measured as the dc characteristics using IWATSU IE-1198 curve tracer. The C-V characteristics for the reverse non-conducting condition were measured as the ac characteristics by the capacitance measurement system in Chapter 3.



Figure 5.2 Static *I-V* characteristics of SiC JFET.

### 5.2.1 Static *I-V* characteristics

Figures 5.2(a) and (b) show the measured and modeled static I-V characteristics of lateral-type SiC JFET and vertical-type SiC JFET, respectively, for different values of gate-source voltage  $V_{\rm GS}$ . The steady-state forward I-V characteristics of both SiC JFETs are drawn by pentode like curves to the gate-source voltage  $V_{\rm GS}$ . The relationship between the drain-source current  $I_{\rm DS}$  and the drain-source voltage  $V_{\rm DS}$  is modeled at the steady-state as a function of  $V_{\rm GS}$  and  $V_{\rm DS}$ . The both of SiC JFETs studied in this chapter are the normally-on type devices, so that  $I_{\rm DS}$  flows at  $V_{\rm GS} = 0$  V. The static *I-V* characteristics of both SiC JFETs in unipolar operation can be expressed by Eq. (5.1) [32,65,67]:

$$I_{\rm DS} \cong \begin{cases} \frac{\beta}{2(1+\theta(V_{\rm GS}-V_{\rm T}))} [2(V_{\rm GS}-V_{\rm T})V_{\rm DS}-V_{\rm DS}^2](1+\lambda V_{\rm DS}) \\ \text{for } V_{\rm DS} \le V_{\rm GS}-V_{\rm T}, \\ \frac{\beta}{2(1+\theta(V_{\rm GS}-V_{\rm T}))} (V_{\rm GS}-V_{\rm T})^2(1+\lambda V_{\rm DS}) \\ \text{for } V_{\rm DS} > V_{\rm GS}-V_{\rm T}. \end{cases}$$
(5.1)

Here,  $\beta$  denotes the JFET channel transconductance,  $V_{\rm T}$  the threshold voltage,  $\lambda$  the channel length modulation factor, and  $\theta$  the mobility modulation coefficient. In this model, the effect of drain resistance  $R_{\rm D}$  and source resistance  $R_{\rm S}$  is neglected.

These four parameters used in Eq. (5.1) can be extracted from the measurement results. The threshold voltage  $V_{\rm T}$  and JFET channel transconductance  $\beta$  are determined in advance to extracting the channel length modulation factor  $\lambda$  from the measured data as shown in Figs. 5.3 and 5.4 for lateral-type SiC JFET and vertical-type SiC



Figure 5.3 Measured  $\sqrt{I_{\text{DS}_{\text{sat}}}}$ - $V_{\text{GS}}$  characteristics of lateral-type SiC JFET.



Measured  $\sqrt{I_{\text{DS}_{\text{sat}}}}$ - $V_{\text{GS}}$  characteristics of vertical-type SiC JFET. Figure 5.4

Table 5.1 Model extracted parameters for static I-V characteristics of both SiC JFETs.

Parameter	Lateral-type SiC JFET	Vertical-type SiC JFET
β	$0.184 \text{ A/V}^2$	$0.428 \text{ A/V}^2$
$V_{\mathrm{T}}$	-6.9 V	-18.3 V
$\lambda$	$0.013 \ 1/V$	$0.0015 \ 1/V$
heta	$0.048 \ 1/V$	$0.077 \ 1/V$
-		

JFET, respectively. The model extracted parameters for static I-V characteristics of both SiC JFETs are shown in Tab. 5.1.

#### C-V characteristics 5.2.2

-

The depletion region formed at pn junction behaves as parasitic capacitances, which are lumped into terminal capacitances  $C_{\text{GS}}$ ,  $C_{\text{GD}}$ , and  $C_{\text{DS}}$ , as depicted in Fig. 5.1(a). The thickness of depletion region changes with the applied reverse bias voltage  $V_{\rm R}$  ( $V_{\rm GS}$ and  $V_{\rm DS}$ ). The dependence of the depletion capacitance on the  $V_{\rm R}$  can be expressed in the following compact form by Eq. (2.59) [29, 60, 65] in Chapter 2.

Both SiC JFETs are limited to the normally-on type as mentioned above. The lateral-type SiC JFET has  $0.006 \times 60$ -mm in RESURF and  $0.36 \text{ mm}^2$  active area with 200 V blocking voltage and the rated 5 A drain current. The vertical-type SiC JFET has  $2.32 \times 2.32$ -mm in die size and 4 mm<sup>2</sup> active area with 900 V blocking voltage and the rated 2.5 A drain current.

In the experimental setup for characterization, the C-V characteristics of both devices are precisely measured by a LCR meter with applying dc bias voltages  $V_{\rm GS}$  and  $V_{\rm DS}$  to the devices, through C-V measurement fixture in Chapter 3. The measurements are performed with applying  $V_{\rm DS} = 0$  V to avoid short circuit current for  $V_{\rm GS}$  dependency, and  $V_{\rm GS} = -20$  V to block the channel of devices for  $V_{\rm DS}$  dependency. For characterizing the  $V_{\rm GS}$  dependency,  $V_{\rm GS}$  is swept from 0 V to -20 V for both SiC JFETs. For the measurement of  $V_{\rm DS}$  dependency,  $V_{\rm DS}$  is swept from 0 V to 200 V for lateral-type and from 0 V to 600 V for vertical-type.

#### 5.2.3 Switching characteristics

The switching behaviors of both SiC JFETs are governed by the parasitic terminal capacitances (Fig. 5.1(a)) [28–30], which are the functions of the applied voltages between terminals. Eventually, the transient behavior of terminal voltages for both SiC JFETs can be represented by Eqs. (5.2) and (5.3) at charging/discharging states of the capacitances. When  $V_{\rm GS} > V_{\rm T}$ , JFET is conducting, then,  $\frac{dV_{\rm DS}}{dt} \approx 0$ .  $V_{\rm GS}$  changes as follows

$$\frac{\mathrm{d}V_{\mathrm{GS}}}{\mathrm{d}t} \cong -\frac{V_{\mathrm{GS}} - V_{\mathrm{GG}}}{R_{\mathrm{G}} \left( C_{\mathrm{GS}}(V_{\mathrm{GS}}) + C_{\mathrm{GD}}(V_{\mathrm{GS}}) \right)}.$$
(5.2)

When  $V_{\rm GS} < V_{\rm T}$ , JFET is blocked,  $V_{\rm DS}$  is built up as follows

$$\frac{\mathrm{d}V_{\mathrm{DS}}}{\mathrm{d}t} \cong -\frac{V_{\mathrm{DS}} - V_{\mathrm{AA}}}{R_{\mathrm{L}} \left( C_{\mathrm{GD}}(V_{\mathrm{DS}}) + C_{\mathrm{DS}}(V_{\mathrm{DS}}) \right)}.$$
(5.3)

The switching behaviors of both devices are evaluated with the inductive load circuit, which is shown in Fig. 5.5. Then  $V_{\rm DS}$ ,  $V_{\rm GS}$ , and  $I_{\rm D}$  are measured in the experiments.  $V_{\rm AA}$  is varied with setting three different  $V_{\rm DS}$  at 25 V, 50 V, and 75 V.



Figure 5.5 Inductive load circuit for measured switching characteristics of SiC JFET.

Here,  $L_{\rm L}$  is set at 200 nH and  $R_{\rm L}$  at 103  $\Omega$ .  $V_{\rm GG}$  applied to the gate of JFET through  $R_{\rm G}$  5  $\Omega$  is switched between 0 V and -20 V.

## 5.3 Results of *C*-*V* and switching characteristics of SiC JFETs

#### **5.3.1** *C-V* characteristics

The measured and modeled C- $V_{\rm GS}$  characteristics are shown for both SiC JFETs in Figs. 5.6(a) and (b).  $C_{\rm GS}$  and  $C_{\rm GD}$  decrease with negative  $V_{\rm GS}$ , because the depletion region expands in the n-region facing at p<sup>+</sup> gate in Fig. 5.1(b) and the n<sup>-</sup>-drift region facing at p gate in Fig. 5.1(c). Then,  $C_{\rm GS}$  and  $C_{\rm GD}$  become constant around 66 pF and 33 pF for lateral-type, respectively. They become 400 pF and 200 pF for verticaltype, respectively. Because the channel area is fully depleted for  $V_{\rm GS} < V_{\rm T}$  (cut-off condition). The  $V_{\rm T}$  is approximately equal to -6.9 V for lateral-type and -18.3 V for vertical-type.  $C_{\rm GS}$  and  $C_{\rm GD}$  of lateral-type increase for  $V_{\rm GS} < -11.3$  V as shown in Fig. 5.6(a). They stem from the leakage current at pn junction between gate and source. The capacitance model parameters of  $C_{\rm GS}$  and  $C_{\rm GD}$  are extracted for  $V_{\rm GS}$  higher than cut-off voltage to neglect the influence of leakage current. They are  $C_0 = 119$  pF, m = 0.48 (uniformly doped) and  $C_0 = 106$  pF, m = 0.24 (linearly graded doped) for



Figure 5.6 C- $V_{GS}$  characteristics of SiC JFETs.

lateral-type, respectively. They are  $C_0 = 1045$  pF, m = 0.33 (linearly graded doped) and  $C_0 = 500$  pF, m = 0.33 (linearly graded doped) for vertical-type, respectively.

The measured and modeled  $C-V_{\rm DS}$  characteristics for both SiC JFETs are shown in Figs. 5.7(a) and (b).  $C_{\rm GS}$  hardly changes with the variation of  $V_{\rm DS}$ . The values are around 415 pF for lateral-type and 368 pF for vertical-type. Because the electric



Figure 5.7  $C-V_{\rm DS}$  characteristics of SiC JFETs.

fields induced by  $V_{\rm DS}$  does not affect on the electric field across gate and source due to the fixed  $V_{\rm GS}$ . On the other hand,  $C_{\rm GD}$  and  $C_{\rm DS}$  decrease smoothly according to the increase of  $V_{\rm DS}$ . The extracted capacitance model parameters of  $C_{\rm GD}$  and  $C_{\rm DS}$ are  $C_0 = 77$  pF, m = 0.34 (linearly graded doped) and  $C_0 = 148$  pF, m = 0.38(linearly graded doped) for lateral-type, respectively. They are  $C_0 = 278$  pF, m = 0.55 (uniformly doped) and  $C_0 = 481$  pF, m = 0.52 (uniformly doped) for vertical-type, respectively. For the lateral-type in Fig. 5.1(b),  $C_{\rm GD}$  and  $C_{\rm DS}$  change slightly with the variation of  $V_{\rm DS}$ , because the depletion region expands from the linearly graded doped n-region to p<sup>+</sup> gate and n-region to p<sup>-</sup> region, respectively. For the vertical-type in Fig. 5.1(c), the n-channel is aligned in horizontal-axis, but the n-type semiconductor (n<sup>-</sup> drift region) is aligned in vertical-axis. Therefore,  $C_{\rm GD}$  has almost constant around 132 pF at  $V_{\rm DS} \leq 13$  V, because the depletion region expands around channel opened between buried p<sup>+</sup> region for low  $V_{\rm DS}$ . Then,  $C_{\rm GD}$  changes substantially with the variation of  $V_{\rm DS}$  when  $V_{\rm DS} > 13$  V, because the depletion region expands from the p gate to the uniformly doped drift region.  $C_{\rm DS}$  also changes substantially with the variation of  $V_{\rm DS}$  in the low and high voltage ranges. It is because the depletion region expands from under the buried p<sup>+</sup> region to the uniformly doped drift region.

#### 5.3.2 Switching characteristics

Figures 5.8(a) and (b) demonstrate the switching behaviors of both SiC JFETs for turn-off operation. Derivative of the  $V_{\rm GS}$ ,  $\frac{dV_{\rm GS}}{dt}$ , in Eq. (5.2) obviously depends on  $C_{\rm ISS}(=C_{\rm GS}+C_{\rm GD})$  with variation of  $V_{\rm GS}$ . The derivative of the  $V_{\rm GS}$ ,  $\frac{dV_{\rm GS}}{dt}$ , is equal to  $-2.83 \times 10^8$  V/s (modeled) and  $-2.50 \times 10^8$  V/s (measured) for lateral-type in Fig. 5.8(a). It is also  $-3.14 \times 10^8$  V/s (modeled) and  $-3.59 \times 10^8$  V/s (measured) for vertical-type in Fig. 5.8(b). The simulated results by the model well coincide with experimental results. The lateral-type has smaller the derivative of the  $V_{\rm GS}$ ,  $\frac{dV_{\rm GS}}{dt}$ , than the vertical-type. Because  $C_{\rm GS}$  and  $C_{\rm GD}$  of lateral-type SiC JFET increase substantially for  $V_{\rm GS} < -11.3$  V as mentioned above. The accumulated charge Qcalculated from gate voltage dependency of capacitance is equal to 6.79 nC for lateraltype in Fig. 5.6(a) and 19.15 nC for vertical-type in Fig. 5.6(b). The lateral-type has smaller Q than the vertical-type. Because the lateral-type device has smaller  $C_{\rm GS}$  and  $C_{\rm GD}$  than the vertical-type while  $V_{\rm GS} \geq -11.3$  V.

Derivative of the  $V_{\rm DS}$ ,  $\frac{dV_{\rm DS}}{dt}$ , in Eq. (5.3) depends on  $C_{\rm OSS}(=C_{\rm GD}+C_{\rm DS})$  with variation of  $V_{\rm DS}$ . It affects on the switching behaviors when  $V_{\rm GS} < V_{\rm T}$  (cut-off condition). It is obvious that Eqs. (5.2) and (5.3) cannot take the Miller effect into account. The



Figure 5.8 Switching characteristics of SiC JFET during turn-off.

derivatives of the  $V_{\rm DS}$ ,  $\frac{dV_{\rm DS}}{dt}$  for lateral-type in Fig. 5.8(a) at  $V_{\rm DS} = 25$  V, 50 V, and 75 V correspond to  $7.89 \times 10^8$  V/s,  $20.42 \times 10^8$  V/s, and  $33.67 \times 10^8$  V/s by the model. They are  $8.00 \times 10^8$  V/s,  $17.06 \times 10^8$  V/s, and  $23.88 \times 10^8$  V/s in the measurement. The derivatives of the  $V_{\rm DS}$ ,  $\frac{dV_{\rm DS}}{dt}$ , for vertical-type in Fig. 5.8(b) at  $V_{\rm DS} = 25$  V, 50 V, and 75 V correspond to  $3.07 \times 10^8$  V/s,  $8.05 \times 10^8$  V/s, and  $14.03 \times 10^8$  V/s by the model. They are  $2.60 \times 10^8$  V/s,  $5.71 \times 10^8$  V/s, and  $10.47 \times 10^8$  V/s in the measurement. The model accurately explains the experimental results. The accumulated charges Q, calculated from drain voltage dependency of capacitance at  $V_{\rm DS} = 25$  V, 50 V, and 75 V, are equal to 3.27 nC, 5.35 nC, and 7.09 nC for lateral-type in Fig. 5.7(a). Those are 8.42 nC, 13.33 nC, and 17.12 nC for vertical-type in Fig. 5.7(b). The ratios of the derivative of the  $V_{\rm DS}$ ,  $\frac{dV_{\rm DS}}{dt}$ , between lateral-type and vertical-type are equal to 2.57, 2.53, and 2.40. The ratios of Q between both types are equal to 1/2.57, 1/2.50, and 1/2.41. Therefore, the ratio of turn-off speed of  $V_{\rm DS}$  between SiC JFETs depends on the inverse ratio of Q. The lateral-type shows about 2.5 times faster turn-off speed than the vertical-type. Because the lateral-type has smaller  $C_{\rm DS}$  and  $C_{\rm GD}$  than the vertical-type as mentioned above.

### 5.4 Summary

This chapter characterized and discussed the switching characteristics of SiC JFETs through the voltage dependency of terminal capacitances. The difference between the switching characteristics of the lateral-type and the vertical-type SiC JFETs depends on their internal parasitic capacitances, which can be classified by the dependence of depletion capacitance. Therefore, the device structure and switching phenomenon can be characterized and explained for these SiC JFETs by the measurement of C-V characteristics of devices. The simulated results of the switching behavior well agree with the experimental results for some conditions of the model and extracted parameter from the C-V and I-V characteristics of these devices.

## Chapter 6

# An application of SiC power transistors

## 6.1 Introduction

Silicon carbide (SiC) power devices have been researched and developed because of its several superior physical characteristics than Si. SiC power MOSFETs are currently under development almost closed to commercial use. The theoretical analysis predicts that the SiC power MOSFETs have potentials at high frequency, high temperature, and high voltage. Therefore, it is important to confirm these performances of SiC power MOSFET at high voltage and fast switching operation.

This chapter estimates the use of SiC power MOSFETs for the control of the voltages and currents in a high frequency switching converter circuit [28, 68]. To evaluate the performances of the power devices, the SiC power MOSFETs are here used in a resonant-switch converter to shape the switch voltage and current at zero-voltage switching (ZVS) and/or zero-current switching (ZCS) with comparison to the performances of the Si power MOSFETs.



Figure 6.1 Functional block diagram of resonant-switch dc-dc step-up voltage converter

### 6.2 Resonant-switch dc-dc step-up voltage converter

The functional block diagram of the resonant-switch dc-dc step-up voltage converter is shown in Fig. 6.1. It consists of the rectifier and filter, power circuit, and control circuit. Figure 6.2 shows the power circuit of the resonant-switch dc-dc step-up voltage converter. Its main application is in regulated dc power supplies. The converter transforms a dc voltage input to a dc voltage output that is greater in magnitude but has the same polarity as the input. It operates at a 25  $\mu$ s (40 kHz) with involving a H-bridge circuit, which generates an ac square-wave voltage. The operation of circuit is originally similar to a boost converter [28, 68], but the circuit is performed by four switches  $Q_1$ ,  $Q_2$ ,  $Q_3$ , and  $Q_4$  to shape the switch voltage and current to provide ZVS and/or ZCS. It can be utilized primarily by an LC resonance.

#### 6.2.1 Power circuit

The power circuit of the resonant-switch dc-dc step-up voltage converter is shown in Fig. 6.2. The components of this converter are given in Tab. 6.1. The switches  $Q_1$ ,



(a) Schematic power circuit



(b) Experimental power circuit

Figure 6.2 Resonant-switch dc-dc step-up voltage converter.

 $Q_2$ ,  $Q_3$ , and  $Q_4$  are operated by control signal to transform the dc voltage input to the dc voltage output. The inductances  $L_1$  and  $L_2$  are a transformer that performs a primary boosting function and provides nearly constant current to the output circuit through body diode  $D_1$  of switch  $Q_1$ . The inductance  $L_r$  and capacitance  $C_r(=C_2)$ provide a simple LC resonant circuit, thereby shaping the switch voltage and current in order to yield ZVS and ZCS in this converter. The capacitance  $C_1$  is a snubber capacitor for switch  $Q_1$ . The diodes  $D_5$  and  $D_6$  are used to kill the effect of body

Component	Value
Inductance $L_1$	$3 \mathrm{mH}$
Inductance $L_2$	760 $\mu H$
Inductance $L_{\rm r}$	$10 \ \mu { m H}$
Input capacitance $C_{\rm in}$	100 $\mu \mathrm{F},900~\mathrm{V}$
Capacitance $C_1$	$10 \mathrm{nF}$
Capacitance $C_2$	$10 \mathrm{nF}$
Output capacitance $C_{\rm out}$	$2.5~\mu\mathrm{F},850~\mathrm{V}$
Diode $D_5, D_6$	30 A, 600 V (RHRP3060)
Gate resistance $R_{\rm G}$	$10 \ \Omega$
Output resistance $R_{\rm out}$	$660 \ \Omega$

Table 6.1 Components of resonant-switch dc-dc step-up voltage converter.

diodes  $D_3$  and  $D_4$  inside the switches  $Q_3$  and  $Q_4$ , respectively. The capacitances  $C_{\rm in}$ and  $C_{\rm out}$  are the filter capacitor for input and output of the converter to keep a nearly constant instantaneous value. The  $L_{\rm r}C_{\rm r}$  resonance around the switches  $Q_2$  and  $Q_4$  do not affect the primary boosting function of inductances  $L_1$  and  $L_2$ . The  $L_1$  and  $L_2$  act as a step-up transformer to increase the input voltage  $V_{\rm in}$  with setting a duty-cycle Dand a turn ratio  $n_{\rm T}$  of transformer between  $L_1$  and  $L_2$ . Therefore, the ratio between the input voltage  $V_{\rm in}$  and the output voltage  $V_{\rm out}$  is expressed by Eq. (6.1):

$$\frac{V_{\text{out}}}{V_{\text{in}}} = \frac{1}{1-D} \cdot n_{\text{T}},\tag{6.1}$$

where  $n_{\rm T} = \sqrt{L_1/L_2}$ .

#### 6.2.2 Control circuit

The control circuit is composed of the signal generator and gate drive circuit, which are shown in Fig. 6.1. Here, the signal generator is timing generator Time98-50MHz [69], which is utilized to generate the signal for gate drive circuit. The signal generator can be programmed by PC-computer. Figure 6.3 shows the gate drive circuit



(a) Schematic gate drive circuit



(b) Experimental gate drive circuit

Figure 6.3 Gate drive circuit for resonant-switch dc-dc step-up voltage converter.

of the resonant-switch dc-dc step-up voltage converter. PC929 photocoupler is used for gate drive circuit to drive the switches  $Q_1$ ,  $Q_2$ ,  $Q_3$ , and  $Q_4$ . The schematic gate drive circuit and experimental gate drive circuit are shown in Fig. 6.3. To stabilize the operation of the photocoupler, it is recommended to connect a bypass capacitor Cb about 0.01  $\mu$ F or more between Vcc and GND. For the detecting voltage of pin-C from drain terminal of power MOSFET, it is recommended to connect a capacitor Cp (approximately 1000 pF) between pin-C and GND, and a resistor Rc (approximately 1.0 k $\Omega$ ) between Vcc and pin-C. For the blocking diode D, which is connected between pin-C and drain of power MOSFET, it is recommended to use a diode that has the withstand voltage characteristic equivalent to power MOSFET and also has little leak current. Then, for preventing the failure mode or breakdown of pin-C from variation voltage of power MOSFET, it is recommended to connect a resistor R1 (approximately 10 k $\Omega$ ) and a diode D7 at near pin-C, and a resistor R2 (approximately 50 k $\Omega$ ) and a diode D8 at between pin-C and GND.

## 6.2.3 Modes of operation—resonant-switch dc-dc step-up voltage converter

The sequence operation of the resonant-switch dc-dc step-up voltage converter depends on the gate drive signal, which is given by a signal generator. It is separated to 7 modes depending on the operation of switches  $Q_2$  and  $Q_4$ . Here each mode is explained as follows:

#### Mode 1

The converter is operated in Mode 1 as shown in Fig. 6.4, when the switch  $Q_2$  is turned on. The inductance  $L_1$  provides nearly constant current to the output circuit. The input current  $i_{L_1}$  flows through inductance  $L_1$  and switch  $Q_2$ . Therefore, the voltage dropping on inductance  $L_1$  is given as Eq. (6.2):

$$L_1 \frac{\mathrm{d}i_{\mathrm{L}_1}}{\mathrm{d}t} = V_{\mathrm{in}}.\tag{6.2}$$

#### Mode 2

Figure 6.5 shows the operation of the converter in Mode 2, when the switch  $Q_2$  is turned off. In this case, the output voltage  $V_{\text{out}}$  is higher than the input voltage


Figure 6.4 Operation of the converter in Mode 1.



Figure 6.5 Operation of the converter in Mode 2.

 $V_{\text{in}}$ . The input current  $i_{L_1}$  and output current  $i_{\text{out}}(=i_{C_1})$  flow through capacitance  $C_2$ . The input current  $i_{L_1}$  is equal to  $-i_{C_1} + i_{C_2}$ . Therefore, the input current  $i_{L_1}$  can be represented by Eq. (6.3):

$$i_{\rm L_1} = -C_1 \frac{\mathrm{d}v_{\rm C_1}}{\mathrm{d}t} + C_2 \frac{\mathrm{d}v_{\rm C_2}}{\mathrm{d}t}.$$
(6.3)

#### Mode 3

Figure 6.6 shows the operation of the converter in Mode 3. The output voltage  $V_{\text{out}}$  is lower than the input voltage  $V_{\text{in}}$ . The input current  $i_{L_1}$  continuously flows through diode  $D_1$  inside switch  $Q_1$  to the output circuit. The voltage dropping inductance  $L_1$ 



Figure 6.6 Operation of the converter in Mode 3.

can be represented by Eq. (6.4):

$$L_1 \frac{\mathrm{d}i_{\mathrm{L}_1}}{\mathrm{d}t} = -(V_{\mathrm{out}} - V_{\mathrm{in}}).$$
(6.4)

#### Mode 4

Figure 6.7 shows the operation of the converter in Mode 4, when the switch  $Q_4$  is turned on and the switch  $Q_2$  is still turned off. In this case, the output voltage  $V_{\text{out}}$  is lower than the input voltage  $V_{\text{in}}$ . Then, the input current  $i_{L_1}$  continuously flows through diode  $D_1$ , inductance  $L_2$ , and inductance  $L_r$ . The voltage dropping on inductance  $L_1$  and  $L_2$  in transformer is given by Eqs. (6.5) and (6.6):

$$v_{\rm L_1} = L_1 \frac{{\rm d}i_{\rm L_1}}{{\rm d}t} + M \frac{{\rm d}i_{\rm L_2}}{{\rm d}t},\tag{6.5}$$

$$v_{\rm L_2} = L_2 \frac{{\rm d}i_{\rm L_2}}{{\rm d}t} + M \frac{{\rm d}i_{\rm L_1}}{{\rm d}t},\tag{6.6}$$

where  $M = k\sqrt{L_1L_2}$  is the mutual inductance between  $L_1$  and  $L_2$ , and k the coupling coefficient. Then, the input voltage  $V_{\rm in}$  can be expressed by Eq. (6.7):

$$V_{\rm in} = L_1 \frac{{\rm d}i_{\rm L_1}}{{\rm d}t} + M \frac{{\rm d}i_{\rm L_2}}{{\rm d}t} + V_{\rm out}.$$
 (6.7)



Figure 6.7 Operation of the converter in Mode 4.



Figure 6.8 Operation of the converter in Mode 5.

#### Mode 5

Figure 6.8 shows the operation of the converter in Mode 5, when the switch  $Q_4$  is turned on and the switch  $Q_2$  is still turned off. In this case, the output voltage  $V_{out}$ is higher than the input voltage  $V_{in}$ . Then, the input current  $i_{L_1}$  and output current  $i_{out}(=i_{C_1})$  continuously flows through capacitance  $C_2$ , inductance  $L_2$ , and inductance  $L_r$ . The voltage dropping on inductance  $L_1$  and  $L_2$  in transformer is given by Eqs. (6.5) and (6.6) and the current flows through capacitance  $C_1$  and  $C_2$  is given by Eqs. (6.8) and (6.9):

$$i_{C_1} = C_1 \frac{\mathrm{d}v_{C_1}}{\mathrm{d}t},$$
 (6.8)

$$i_{\rm C_2} = C_2 \frac{\mathrm{d}v_{\rm C_2}}{\mathrm{d}t}.$$
 (6.9)

Then, the input voltage  $V_{in}$  can be represented by Eq. (6.10):

$$V_{\rm in} = (L_1 + M) \frac{\mathrm{d}i_{\rm L_1}}{\mathrm{d}t} + (L_2 + M + L_r) \frac{\mathrm{d}i_{\rm L_2}}{\mathrm{d}t}.$$
 (6.10)

#### Mode 6

Figure 6.9 shows the operation of the converter in Mode 6, when the switch  $Q_4$  is turned on and the switch  $Q_2$  is still turned off. In this case, the inductance current  $i_{L_2}(=i_{L_r})$  still flow through switch  $Q_4$ , diode  $D_6$ , and diode  $D_2$ . Because the voltage dropping on inductance  $L_r$  becomes higher than the voltage dropping on inductance  $L_1$  and also the polarity of inductance  $L_r$  changes oppositely. The voltage dropping on inductance  $L_1$  and  $L_2$  in transformer is given by Eqs. (6.5) and (6.6). Then, the input voltage  $V_{in}$  can be expressed by Eq. (6.11):

$$V_{\rm in} = L_1 \frac{{\rm d}i_{\rm L_1}}{{\rm d}t} + M \frac{{\rm d}i_{\rm L_2}}{{\rm d}t}.$$
 (6.11)

#### Mode 7

Figure 6.10 shows the operation of the converter in Mode 6, when the switch  $Q_4$  is turned on and the switch  $Q_2$  becomes to turn on again. In this case, the inductance



Figure 6.9 Operation of the converter in Mode 6.



Figure 6.10 Operation of the converter in Mode 7.

current  $i_{L_2}(=i_{L_r})$  still flows through switch  $Q_4$ , diode  $D_6$ , and switch  $Q_2$ . Because the voltage dropping on inductance  $L_r$  becomes higher than the voltage dropping on inductance  $L_1$  and also the polarity of inductance  $L_r$  changes oppositely. The voltage dropping on inductance  $L_1$  and  $L_2$  in transformer is given by Eqs. (6.5) and (6.6). Then, the input voltage  $V_{in}$  represented by Eq. (6.11).

### 6.3 Experimental results of resonant-switch dc-dc step-up voltage converter

The operation of the resonant-switch dc-dc step-up voltage converter is governed by the switches  $Q_2$  and  $Q_4$  as mentioned above. The switches  $Q_1$  and  $Q_3$  are entirely turned off in this operation. Here, the Si and SiC power MOSFETs are used to be the switches  $Q_1$ ,  $Q_2$ ,  $Q_3$ , and  $Q_4$ . The Si power MOSFET has 700 V blocking voltage and the rated 10 A drain current. The SiC power MOSFET has 900 V blocking voltage and the rated 10 A drain current. The static *I-V*, transfer, and *C-V* characteristics of Si and SiC power MOSFET are shown in Figs. 6.11-6.13, respectively.

In comparison between the Si and SiC power MOSFET on-state curves, the Si curves, which is shown in Fig. 6.11(a), are linear in the on-state region and have a pronounced change in curvature as the saturation or pinch-off region is approached around  $V_{\rm GS} = 6$  V. This occurs because the Si power MOSFET has a large epitaxial layer resistance in series with the MOSFET channel and the channel has a very high



Figure 6.11 Measured static *I-V* characteristics of power MOSFET.



Figure 6.12 Transfer characteristics of power MOSFET.

transconductance [7,44]. On the other hand, the SiC curves, which is shown in Fig. 6.11(b), gradually transit from the linear region to the saturation region. In SiC power MOSFET, the epitaxial layer resistance is much smaller and the channel resistance is higher, because of the non-saturable characteristics stemming from the short channel effects [43]. The  $V_{\rm T}$  of the Si power MOSFET is 3.2 V and the  $V_{\rm T}$  of the SiC power MOSFET is 4.2 V, as shown in Fig. 6.12.

The measured  $C-V_{\rm DS}$  characteristics of the Si and SiC power MOSFETs are shown in Figs. 6.13(a) and 6.13(b) at logarithmic scale. The capacitances  $C_{\rm GS}$ ,  $C_{\rm GD}$ , and  $C_{\rm DS}$ 



Figure 6.13 Measured C-V characteristics of power MOSFET.

of the SiC power MOSFET are slightly smaller that of the Si power MOSFET, when  $V_{\rm DS} < 100$  V. For the SiC power MOSFET, there are no irregular capacitance, and the decrease of the capacitance in  $C_{\rm GD}$  and  $C_{\rm DS}$  stops around  $V_{\rm DS} = 200$  V. It indicates that the expansion of the depletion region is terminated in the drift layer because of the punch-through structure of the device.

Figures 6.14 and 6.15 show the gate drive signals for Si and SiC power MOSFETs, respectively. The gate drive signals of both power MOSFETs for switches  $Q_2$  and  $Q_4$ are  $V_{GQ_2}$  and  $V_{GQ_4}$ , which are shown in Figs. 6.2 and 6.3. The switching time  $T_s$  is equal to 25  $\mu$ s, and the switch-on time  $T_{on}$  of  $V_{GQ_2}$  and  $V_{GQ_4}$  is equal to 12.3  $\mu$ s and 13.3  $\mu$ s, respectively. Here, the input voltage  $V_{in}$  is set at 50 V. The output voltage  $V_{out}$  of the converter is calculated by Eq. (6.1) as follows.

The duty cycle D of the converter, which depends on the switch-on time  $T_{\rm on}$  of  $V_{\rm GQ_2}$ , is equal to

$$D = \frac{T_{\rm on}}{T_{\rm s}} = \frac{12.3 \times 10^{-6}}{25.0 \times 10^{-6}} = 0.49,$$

and the turn ratio  $n_{\rm T}$  of transformer between  $L_1$  and  $L_2$  is equal to

$$n_{\rm T} = \sqrt{\frac{L_1}{L_2}} = \sqrt{\frac{3 \times 10^{-3}}{760 \times 10^{-6}}} = 1.99.$$

Therefore, the output voltage  $V_{\text{out}}$  of the converter is equal to

$$V_{\text{out}} = \frac{1}{1 - D} \cdot n_{\text{T}} \cdot V_{\text{in}} = \frac{1}{1 - 0.49} \times 1.99 \times 50 = 195.1 \text{ V}.$$



Figure 6.14 Gate drive signals for Si power MOSFET in the converter.



Figure 6.15 Gate drive signals for SiC power MOSFET in the converter.

Figures 6.16-6.19 show the currents and voltages of the resonant-switch dc-dc stepup voltage converter. The output voltage  $V_{out}$  is approximately equal to 194 V. It is almost similar to the calculated results. The circuit resonant frequency  $f_o$  can be



(b) Voltages dropping on switches  $Q_2, Q_4$ 

Figure 6.16 Currents flowing through  $L_1$ ,  $L_r$  and voltages dropping on switches  $Q_2$ ,  $Q_4$  in the converter by using Si power MOSFET as switch.



(b) Voltages dropping on inductances  $L_1$ ,  $L_2$ , and  $L_r$ 

Figure 6.17 Input voltage, output voltage, and voltages dropping on inductances  $L_1$ ,  $L_2$ , and  $L_r$  in the converter by using Si power MOSFET as switch.



(b) Voltages dropping on switches  $Q_2, Q_4$ 

Figure 6.18 Currents flowing through  $L_1$ ,  $L_r$  and voltages dropping on switches  $Q_2$ ,  $Q_4$  in the converter by using SiC power MOSFET as switch.



(b) Voltages dropping on inductances  $L_1$ ,  $L_2$ , and  $L_r$ 

Figure 6.19 Input voltage, output voltage, and voltages dropping on inductances  $L_1$ ,  $L_2$ , and  $L_r$  in the converter by using SiC power MOSFET as switch.

calculated from the inductance  $L_{\rm r}$  and capacitance  $C_{\rm r}(=C_2)$ , that is

$$f_{\rm o} = \frac{1}{2\pi\sqrt{L_{\rm r}C_{\rm r}}} = \frac{1}{2\pi\sqrt{10 \times 10^{-6} \times 10 \times 10^{-9}}} = 503$$
 kHz

It is more than the switching frequency  $f_s$  tremendously. Therefore, the resonantswitch dc-dc step-up voltage converter can be operated in ZVS and ZCS resonant conditions properly.

The currents and voltages of each component in the converter, which are shown in Figs. 6.16 and 6.17 for Si power MOSFET and Figs. 6.18 and 6.19 for SiC power MOSFET, have smooth waveforms. The switch  $Q_2$  shows the operation under the zero-voltage switching (ZVS) condition, and the switch  $Q_4$  shows the operation under the zero-current switching (ZCS) condition. As the same components in the resonantswitch dc-dc step-up voltage converter, the voltage dropping on switch  $Q_4$  by using SiC power MOSFET in Fig. 6.18(b) shows smaller oscillation than that by using Si power MOSFET in Fig. 6.16(b). The maximum voltage of inductances  $L_1$ ,  $L_2$ , and  $L_r$  by using Si power MOSFET in Fig. 6.17(b) is equal to 50 V, 265 V, and 170 V, respectively. The maximum voltage of inductances  $L_1$ ,  $L_2$ , and  $L_r$  by using SiC power MOSFET in Fig. 6.19(b) is equal to 50 V, 257 V, and 143 V, respectively. Therefore, the voltage dropping on inductances  $L_2$  and  $L_r$  by using SiC power MOSFET shows smaller oscillation and magnitude than that by using Si power MOSFET. The output voltage  $V_{\text{out}}$  and currents flowing through  $L_1$ ,  $L_2$ , and  $L_r$  by using SiC power MOSFET are similar to that by using Si power MOSFET.

#### 6.4 Summary

This chapter demonstrated the operation of the SiC power MOSFET in the resonantswitch dc-dc step-up voltage converter as switch to control the output current and voltage. The experimental results show that the SiC power MOSFET achieves the resonant operation at the zero voltage and zero current switchings. The output voltage, which depends on duty cycle D and turn ratio  $n_{\rm T}$  of transformer, was constant throughout the operation. Moreover, the results of the resonant converter by using the SiC power MOSFET were compared with the results by using Si power MOSFET. The results by using SiC power MOSFET showed smoother waveforms of the current and voltage than the results by using Si power MOSFET. Therefore, the SiC power MOSFET can be used in the resonant-switch dc-dc step-up voltage converter.

## Chapter 7

# Conclusions

In this dissertation, SiC power transistors, especially power MOSFET and JFETs, were characterized for power conversion circuits. Transient behavior in switching operation of the SiC power devices is affected by their intrinsic parasitic capacitances. Therefore, it is important to characterize the C-V characteristics of the power devices to estimate their switching performance. The major conclusions obtained in the present study are summarized as follows.

Chapter 2 illustrated the simplified cross section of the SiC DiMOSFET cell, the lateral-type RESURF SiC JFET cell, the vertical-type bare die SiC JFET cell. In this chapter, we also described the two most commonly used types of capacitances in semiconductor devices. They are composed of the MOS capacitance type and the pn junction capacitance type. Their device structures decide the voltage dependence of the capacitance characteristics. The voltage dependence of the MOS capacitance in the SiC DiMOSFET can be distinguished as accumulation, depletion, and inversion conditions, which is similar to the Si power MOSFET. The voltage dependence of the pn junction capacitance in both SiC JFETs is expressed at the uniformly doped and the linearly graded doped junctions.

In Chapter 3, we described the developed C-V characterization system for highvoltage power transistors. Because the terminal capacitances of a power device are important to understand the dynamic behavior of the device, such as its switching operation. The device capacitances are not constant, but change with terminal applied voltage. Therefore, a C-V characterization system for gate-controlled power devices was developed in this study. It consists of five measurement circuits, which were proposed to measure the three combinations of terminal capacitances and three combinations of device capacitance for circuit operation. The developed capacitance characterization system can measure capacitance from the blocking condition to the conducting condition while changing the gate bias voltage. The variation of the depletion and accumulation condition in the device was reflected in the device capacitance. The measured capacitance explained the device structure and the physical phenomenon occurring in the device clearly.

In order to predict the device characteristics of the Si and SiC power MOSFETs accurately over their wide range of operation, a physics-based model was studied and proposed based on terminal capacitances in Chapter 4. In this chapter, we characterized the voltage dependence of terminal capacitances of the power devices, modeled the I-V characteristics with discussing the C-V characteristics of the power devices, and extracted the model parameters from their characteristics. And also, this chapter characterized and discussed the switching characteristics of power MOSFETs through the voltage dependence of terminal capacitances. The difference between the switching characteristics of the Si and SiC power MOSFETs depends on their internal parasitic capacitances, which can be classified by the MOS capacitance and pn junction capacitance. Finally, it was shown that the simulated results of the switching behavior well agree with the experimental results for some conditions of the model and extracted parameters. The SiC power MOSFET has faster turn-on and turn-off speed than the Si power MOSFET. Because the SiC power MOSFET has smaller terminal capacitances than the Si power MOSFET.

In Chapter 5, we characterized and discussed the switching characteristics of the lateral-type and vertical-type SiC JFETs through the gate and drain voltage dependency of terminal capacitances, and also the static *I-V* characteristics of both SiC JFETs. The difference between the switching characteristics of the lateral-type and the vertical-type SiC JFETs depends on their internal parasitic capacitances, which can be classified by the dependence of depletion capacitance. The lateral-type SiC JFET has faster turn-off speed than the vertical-type SiC JFET. Therefore, the de-

vice structure and switching phenomenon can be characterized and explained for these SiC JFETs by the measurement of C-V characteristics of devices. In the end of this chapter, it was shown that the simulated results of the switching behavior well agree with the experimental results.

Finally, the SiC power MOSFET was experimentally evaluated its performances in a high frequency switching converter circuit. The characterization of the SiC power MOSFET was examined via measured and simulated results in Chapter 4. In Chapter 6, we demonstrated the operation of the SiC power MOSFET in the resonant-switch dcdc step-up voltage converter as switch to control the output current and voltage. As the experimental results, the SiC power MOSFET in the resonant converter was switched at the zero-voltage and zero-current switching conditions. The output voltage, which depends on duty cycle D and turn ratio  $n_{\rm T}$  of transformer, was constant throughout the operation. And also, the results of the resonant converter using the SiC power MOSFET were compared with the results using Si power MOSFET. The results showed smoother waveforms of the current and voltage. Therefore, the SiC power MOSFET is preferable in the resonant converter towards power conversion circuits.

Through this study, several issues in characterization of SiC power transistors for power conversion circuits have been clarified. However, there remain several issues to be solved. They have emerged several goals to be accomplished in the future:

# • An analysis of switching behavior by equivalent circuit of SiC power transistors:

We have worked on characterization of SiC power transistor to characterize the static I-V, C-V, and switching characteristics of the SiC power devices for power conversion circuits. This dissertation shows that the transient behavior in switching operation of the SiC power devices are discussed with relation to their C-V characteristics and static I-V characteristics. The simulated results in switching behavior of the SiC power devices coincided with experimental results suitably in some conditions. Therefore, we now are analyzing on the dynamics model of SiC power devices with equivalent circuit based on C-V measurement for suitably all conditions.

• Evaluation of SiC power transistors in a high frequency switching power conversion circuit:

SiC semiconductor is the most promising material for power switching devices due to their inherent material characteristics. For this reason, SiC power devices are also expected to have fast switching capability. Under development, SiC power MOSFETs and SiC JFETs now are the most possible power switches for high switching frequency power converters. To realize the fast switching with a thin voltage blocking layer, the switching characteristics of the SiC power MOS-FETs and SiC JFETs have to be evaluated in a high frequency switching power conversion circuit.

• Performance evaluation of a SiC power MOSFET in a resonant circuit application:

In Chapter 6, we demonstrated the operation of the SiC power MOSFET in a resonant converter to regulate the output voltage. The obtained experimental results of the resonant converter by using the SiC power MOSFET showed the smooth waveforms of the current and voltage of the converter. Therefore, the SiC power MOSFET can be used as a switch to control the output current and voltage appropriately. Next, we are evaluating and discussing the performance of the SiC power MOSFET in the resonant converter with comparing the Si power MOSFET.

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# List of Publications

The published papers, which contain most parts of this dissertation, by the author are listed below.

### Archival journal articles

- T. Funaki, <u>N. Phankong</u>, T. Kimoto, and T. Hikihara, "Measuring terminal capacitance and its voltage dependency for high-voltage power devices," *IEEE Trans. on Power Electron.*, vol. 24, no. 6, pp. 1486-1493, Jun. 2009.
- <u>N. Phankong</u>, T. Funaki, and T. Hikihara, "Characterization of the gate-voltage dependency of input capacitance in a SiC MOSFET," *IEICE Electron. Express*, vol. 7, no. 7, pp. 480-486, Apr. 2010.
- <u>N. Phankong</u>, T. Funaki, and T. Hikihara, "Switching characteristics of lateraltype and vertical-type SiC JFETs depending on their internal parasitic capacitances," *IEICE Electron. Express*, vol. 7, no. 14, pp. 1051-1057, July. 2010.
- <u>N. Phankong</u>, T. Funaki, and T. Hikihara, "Characterization of switching behavior of SiC FETs based on measuring terminal capacitances," *IEEE Trans.* on Power Electron. (in preparation).
- <u>N. Phankong</u>, T. Yanagi, and T. Hikihara, "An analysis of switching behavior by equivalent circuit of SiC power MOSFET based on C-V measurement," *IEEE Trans. on Power Electron.* (in preparation).

### International conference proceedings

• <u>N. Phankong</u>, T. Funaki, and T. Hikihara, "A static and dynamic model for a silicon carbide power MOSFET," *The 13th European Conference on Power Electronics and Applications (EPE2009)*, Barcelona, Spain, September 8-10, 2009.

# Domestic conference proceedings and technical reports

- <u>N. Phankong</u>, T. Funaki, and T. Hikihara, "A Discussion on the High Level Carrier Lifetime Effect of IGBT Model," *The Papers of Joint Technical Meeting* on Electron Devices and Semiconductor Power Converter, IEE Japan, EDD-07-73/SPC-07-99, Mie University, Japan, October 25-26, 2007.
- <u>N. Phankong</u>, T. Funaki, and T. Hikihara, "Evaluation of base region parameters in IGBT based on capacitance-voltage characteristics," *Proceeding of the 2008 IEICE General Conference*, Kitakyushu Science and Research Park, Japan, March 18-21, 2008.
- <u>N. Phankong</u>, T. Funaki, and T. Hikihara, "Modeling of power MOSFET based on capacitance-voltage characteristics," *The 22nd Annual Conference of the Industry Applications Society of the Institute of Electrical Engineers of Japan (JI-ASC2008)*, Kochi City Culture-Plaza (CUL-PORT), Japan, August 27-29, 2008.
- <u>N. Phankong</u>, T. Funaki, and T. Hikihara, "Experimental study on dynamic behavior of power MOSFET based on capacitance-voltage characteristics," *The Papers of Joint Technical Meeting on Electron Devices and Semiconductor Power Converter, IEE Japan*, EDD-08-65/SPC-08-152, Kyushu Institute of Technology Tobata Campus, Japan, October 23-24, 2008.
- <u>N. Phankong</u>, T. Funaki, and T. Hikihara, "A study on C-V characterization of lateral-type silicon carbide JFET," *The 2009 Annual Meeting Record IEE Japan*, Hokkaido University, Japan, March 17-19,2009.

- T. Funaki, <u>N. Phankong</u>, and T. Hikihara, "Measurement of terminal capacitance of high voltage MOS power transistors," *The Papers of Joint Technical Meeting on Electron Devices and Semiconductor Power Converter, IEE Japan*, EFM-09-38/EDD-09-72/SPC-09-139, Tokyo Institute of Technology, Japan, October 29, 2009.
- <u>N. Phankong</u>, T. Yanagi, and T. Hikihara, "An analysis of switching behavior by equivalent circuit of power MOSFET," *The 2010 Annual Meeting Record IEE Japan*, Meiji University, Japan, March 17-19, 2010.