

Susceptibility cancellation of a microcoil wound with a paramagnetic-liquid-filled copper capillary

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Abstract

Even though microcoils improve the sensitivity of NMR measurement of tiny samples, magnetic-field inhomogeneity due to the bulk susceptibility effect of the coil material can cause serious resonance-line broadening. Here, we propose to fabricate the microcoil using a thin, hollow copper capillary instead of a wire and fill paramagnetic liquid inside the capillary, so as to cancel the diamagnetic contribution of the copper. Susceptibility cancellation is demonstrated using aqueous solution of NiSO₄. In addition, the paramagnetic liquid serves as coolant when it is circulated through the copper capillary, effectively transferring the heat generated by radiofrequency pulses.

Key words: microcoil; bulk magnetic susceptibility; copper capillary;
paramagnetic liquid; susceptibility cancellation

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For NMR measurements of mass-limited samples, a microcoil is advantageous in terms of the sensitivity[1,2], while the price to pay is the reduced spectral resolution due to magnetic-field inhomogeneity caused by the bulk susceptibility effect (BMS) of the coil wire[2]. In general, a body with non-zero magnetic susceptibility is magnetized in the presence of an external magnetic field. As a consequence, an additional perturbative field arises in the vicinity of the body. Since the strength of the induced field decreases rapidly with the distance, the BMS effect is relatively small for NMR measurements using sample coils with the conventional size. However, in the case of the microcoils, the sample is inevitably close to the coil wire. Thus, the BMS effect can cause significant line broadening.

Copper, which is used for the coil material in many cases, is diamagnetic, so that a magnetization antiparallel to the external field develops. The profile of the induced magnetic field is determined by the geometry of the coil. In the case of a solenoid coil, the resultant field distribution contains high-order terms that are difficult to remove by the standard shimming technique.

So far, several schemes to suppress the BMS-induced field inhomogeneity have been proposed[3]. They include susceptibility matching[2,4,5], zero-susceptibility wire[6–8], and magic-angle coil spinning (MACS)[9–11]. It is also worth noting that the effect of susceptibility broadening is small in stripline probes[12,13]. Here, we report an alternative approach. Our idea is to make a microcoil with a thin capillary made of copper and to fill paramagnetic liquid solution inside the capillary. We aim at cancelling the diamagnetic contribution of the copper.

Our scheme, which is similar to that of zero-susceptibility wire, has a noteworthy feature that the net susceptibility can be modified simply by changing

the concentration of the paramagnetic solute. This contrasts with the case of the zero-susceptibility wire, where such fine adjustment is formidable. Indeed, when Hoult and Ginsberg used a commercial zero-susceptibility wire in their studies on nuclear spin noise, they had to do an elaborate job of electroplating an additional copper layer, as they found that the diameter of their copper-clad aluminum-core wire differed significantly from the nominal value[14]. In addition, the paramagnetic liquid can flow through the capillary, serving as effective coolant, as demonstrated below.

Thin copper capillaries are used for the electrodes of discharge machining devices and are commercially available. In this work, we used one with an outer diameter of 0.2 mm and an inner diameter of 0.1 mm, which was purchased from Nippon Tokushukan MFG. CO., LTD. Since the copper capillary was fragile, we wound it gently into microcoils so as not to clog the passage. An example of copper-capillary-wound microcoils is shown in Fig. 1(a). Its inner diameter is 0.4 mm, and the number of turns is 8. Using a chip ceramic capacitor for balancing and a pair of surface mount trimmer capacitors (TZC3, Murata Electronics) for impedance matching, we fabricated a tank circuit resonating at ca. 300 MHz on a printed circuit board (Fig. 1(b)). The Q factor of the circuit was measured to be 23. Each end of the coil penetrates the board through a conducting via, at which the electrical connection is established by soldering. To supply liquid, poly ether ether ketone (PEEK) tubes were connected at both ends of the copper capillary (Fig. 1(c)).

For paramagnetic liquid, we used aqueous solution of NiSO_4 . For molar concentration α , the susceptibility at room temperature is given by $50.3\alpha \times 10^{-6}$ in SI unit, while the susceptibility of our microcoil was measured to be -10.6×10^{-6} (*vide infra*). Since the volume fraction of the hollow region of the capillary is

25 percent, we naively estimated the concentration α that annuls the net susceptibility to be 0.63 M.

The standard electrode potentials for nickel and copper are -0.23 V and $+0.35$ V, respectively. Since the ionization tendency increases with the negative potential, $\text{Ni} + \text{Cu}^{2+} \rightarrow \text{Ni}^{2+} + \text{Cu}$, rather than $\text{Ni}^{2+} + \text{Cu} \rightarrow \text{Ni} + \text{Cu}^{2+}$, is favoured thermodynamically. Thus, dissolution of copper into the NiSO_4 solution is thermodynamically unfavourable.

^1H NMR measurements were performed using a 7 T superconducting magnet at room temperature. The carrier frequency was 299.52 MHz. First, we carried out experiments with the microcoil without filling liquid inside the capillary. Fig. 2(a) shows a ^1H spectrum of 0.1 M aqueous solution of CuSO_4 in a quartz tube with an inner/outer diameter of 0.2/0.4 mm. We found considerable broadening and distortion in the spectrum acquired with the microcoil, which were caused by the BMS effect of the microcoil. The full width at half maximum was 93 Hz. For comparison, we also acquired a ^1H NMR spectrum of the same sample using a microcoil of the same geometry but wound with a solid copper wire with a diameter of 0.2 mm (Fig. 2(b)). We found that the sensitivity was comparable for both coils, while the broadening and distortion of the resonance line were less appreciable for the capillary-wound microcoil. In addition, we measured ^1H NMR of the same sample using a larger coil with a diameter of 5 mm (Fig. 2(c)). Here, the origin of the line width (38 Hz) was ascribed to the field inhomogeneity of our 7 T magnet used in the present study.

Next, we performed experiments by supplying aqueous solution of NiSO_4 inside the copper capillary. No background ^1H signal due to the paramagnetic

liquid was observed. As demonstrated in Fig. 3(a), the line width of the ^1H spectrum decreased with the concentration of NiSO_4 , reached the minimum (52 Hz) at 0.54 M. With increasing the NiSO_4 concentration further, the spectral resolution degraded, because the paramagnetic contribution became too strong. As shown in Fig. 3(b), with the optimal concentration, the peak height was enhanced by 58% compared to that in the case of pure water (i.e., no NiSO_4 dissolved). In addition, with increasing the overall paramagnetic contribution, the resonance line shifted to higher frequencies (Fig. 3(c)).

The optimal NiSO_4 concentration of 0.54 M was ca. 14% smaller than the estimated value of 0.63 M. In order to discuss the difference, we performed numerical analysis as follows. The longitudinal component $b_z(\mathbf{r}; \mathbf{r}')$ of the magnetic field produced at point $\mathbf{r} = (x, y, z)$ by an infinitesimal magnetization $\mathbf{m}(\mathbf{r}')d\mathbf{r}'$ at point $\mathbf{r}' = (x', y', z')$ is given by

$$b_z(\mathbf{r}; \mathbf{r}') = -\frac{\mu_0}{4\pi} \frac{\mathbf{m}(\mathbf{r}')d\mathbf{r}'}{|\mathbf{r} - \mathbf{r}'|^3} \left[1 - \frac{3(z - z')^2}{|\mathbf{r} - \mathbf{r}'|^2} \right]. \quad (1)$$

In our case, the magnetization density $\mathbf{m}(\mathbf{r}')$ is represented using the material-dependent magnetic susceptibility $\chi(\mathbf{r}')$ and the external-field strength B_0 as

$$\mathbf{m}(\mathbf{r}') = \chi(\mathbf{r}')B_0. \quad (2)$$

The overall BMS-induced field $B_m(\mathbf{r})$ at position \mathbf{r} is obtained by performing integration

$$B_z(\mathbf{r}) = \int d\mathbf{r}' b_z(\mathbf{r}; \mathbf{r}') \quad (3)$$

over the volume of the coil material and the paramagnetic liquid inside the copper capillary.

To estimate BMS-induced broadening, we carried out numerical calculations according to Eq. (3) for the geometry of the setup used in the experiments

presented above. The actual susceptibility of the microcoil was determined with a SQUID fluxmeter (MPMS-XL7ACMKO, Quantum Design, Inc.) at 300 K to be -10.6×10^{-6} .

Fig. 4(a) shows a contour plot of magnetic-field distribution in the plane that bisects the microcoil, which was calculated without taking paramagnetic liquid into account. That is, this calculation corresponds to the case of the hollow capillary shown in Fig. 2(a). Here, we assumed that the external magnetic field was perfectly homogeneous, so that the displayed inhomogeneity arises purely from the BMS effect. Then, we carried out calculations of the field distribution for various NiSO_4 concentrations and found that 0.66 M gave the minimum BMS-induced inhomogeneity, where far fewer contour lines appear (Fig. 2(b)).

Figs. 4(c) and 4(d) show histograms representing the field distribution for the hollow copper capillary and for the optimal NiSO_4 concentration, which were obtained by evaluating B_z over the entire sample volume (a cylindrical region with a diameter of 0.2 mm and a length of 10 mm). To incorporate the original field inhomogeneity of the 7 T magnet caused by reasons other than the BMS effect of the microcoil, we applied convolution operation to the histogram using a Gaussian function with the width of 38 Hz. The resultant spectra, shown in Figs. 4(e) and 4(f), correspond to the experimental results shown in Fig. 2(a) without paramagnetic liquid and with the concentration-optimized NiSO_4 aqueous solution; the increase in the peak height was found to be consistent with the experimental observation.

The optimal NiSO_4 concentration of 0.66 M obtained from the numerical calculation was slightly higher than that of the aforementioned estimation (0.63 M)

from the volume fraction. This is reasonable, considering that the diamagnetic part is located in the outer layer of the coil material, i.e., slightly closer to the sample region than the paramagnetic core. Since the induced field decreases with the cube of the distance from the source, the optimal paramagnetic concentration should be *higher* than the concentration that would exactly cancel the net susceptibility.

However, the experimentally obtained optimal NiSO₄ concentration of 0.54 M was lower than the estimated value. Moreover, even with the experimentally optimized condition, the ¹H resonance line width (52 Hz) was larger than that (38 Hz) expected from the field inhomogeneity of the magnet used in the present study. The discrepancies may be explained by deformation of the copper material upon winding the microcoil.

Another interesting feature of the capillary-wound coil that we found in this work is that the temperature of the coil can be regulated by circulating the liquid. Microcoil NMR allows for irradiation of such strong radiofrequency pulses that was not feasible with the conventional coil[15–17], opening many potential applications in solid-state NMR where coherent manipulation of relatively strong spin interactions is of interest. So far, strong irradiation with the microcoil has found interest in the context of ¹H decoupling[16,18,19] and multiple-quantum magic angle spinning (MQMAS)[20]. One problem regarding to the strong irradiation is coil heating. Since the radiofrequency power is eventually dissipated as heat in a small region around the microcoil, the strong irradiation can burn the microcoil, unless the coil is effectively cooled down.

To demonstrate the efficiency of cooling, we applied radiofrequency irradiation

tion every second with a duration of 100 ms and a power of 19 W, which corresponds to a nutation frequency of 500 kHz. We used an infrared camera (FLIR-i7) to monitor the temperature of the coil as well as of the probe circuit. Figs. 5(a)-(c) show heating observed without liquid flowing inside the coil capillary. The temperature indicated in the figure is that where the microcoil was located. The coil temperature increased up to 73 degrees, as we continued measurement for 500 s, when we stopped the experiment to prevent the coil from burning.

Then, we applied the same sequence with circulating water (20 degrees) at a flow rate of 0.8 mL/min. As demonstrated in Figs. 5(d)-(f), the coil temperature was found to increase only slightly. Interestingly, the thermography images revealed that the coolant carried away the heat of not only the microcoil but also of the entire resonant circuit including the capacitors and the circuit board. The water flow provides a reliable way of cooling the circuit compared to air blowing, as the former takes heat away from the whole region of the microcoil, while the latter does only on the side at which the air is blown.

To summarize, we proposed to use a thin copper capillary for the microcoil and fill the capillary with paramagnetic liquid. By adjusting the concentration of the paramagnetic solute, the overall bulk susceptibility effect can be suppressed significantly, leading to the improved spectral resolution. The paramagnetic liquid also serves for coolant. By circulating the liquid through the capillary-wound microcoil, significant suppression of coil heating is realized. We plan to assemble this into the microcoil MAS system.

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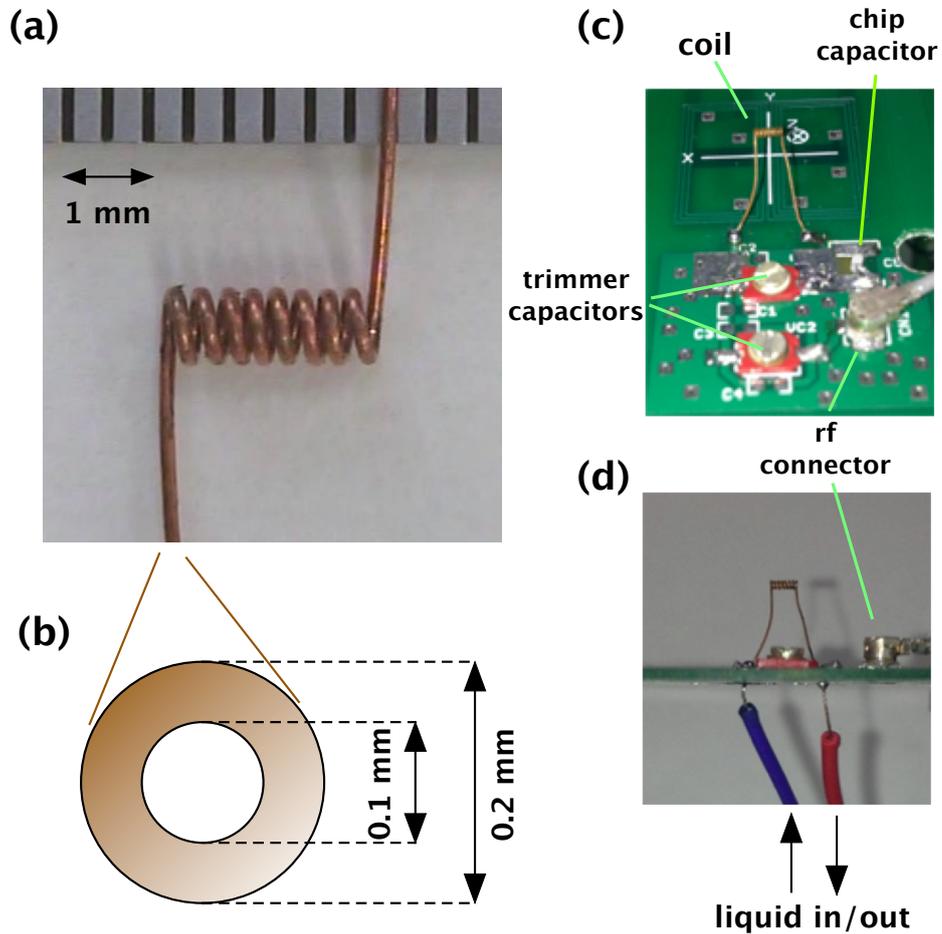


Fig. 1. (a) A photo of a microcoil wound with a copper capillary with an inner diameter of 0.1 mm and an outer diameter of 0.2 mm. (b) Schematic drawing of the cross section of the capillary. (c) A probehead composed of the microcoil, a chip capacitor, and trimmer capacitors. (d) A side view of the probe. Tubes are connected to both end of the copper capillary to supply liquid.

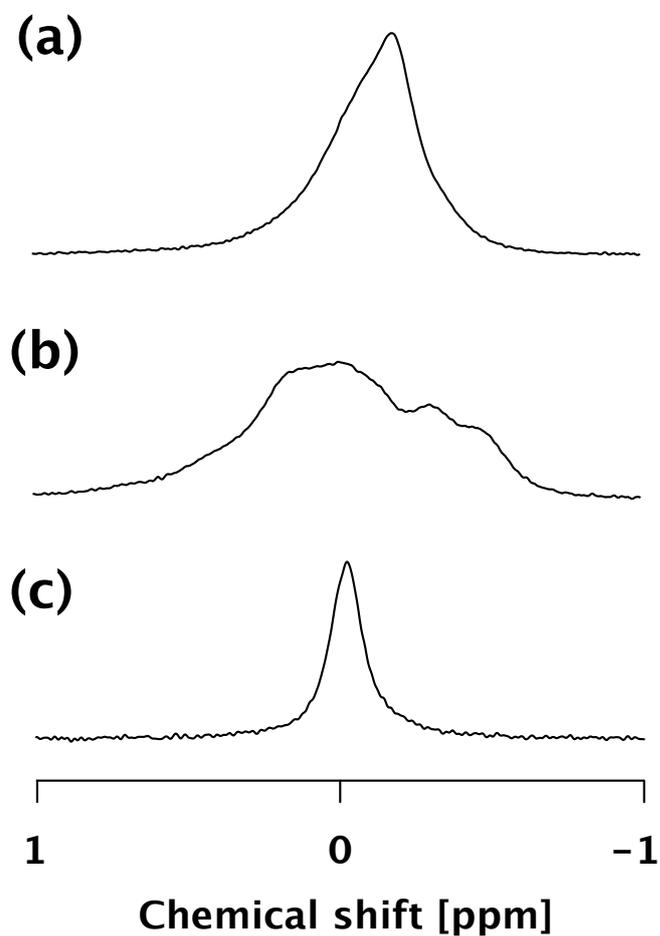


Fig. 2. ^1H spectra of aqueous solution of 0.1 M CuSO_4 in a quartz tube with an inner diameter of 0.2 mm and a length of 10 mm. The resonance frequency was 299.52 MHz. (a) was acquired using the microcoil probe shown in Fig. 1 without filling paramagnetic liquid, while (b) was obtained with a microcoil of the same geometry but wound with a 0.2 mm solid copper wire. (c) shows a ^1H spectrum of the same sample measured with a larger coil with a diameter of 5 mm.

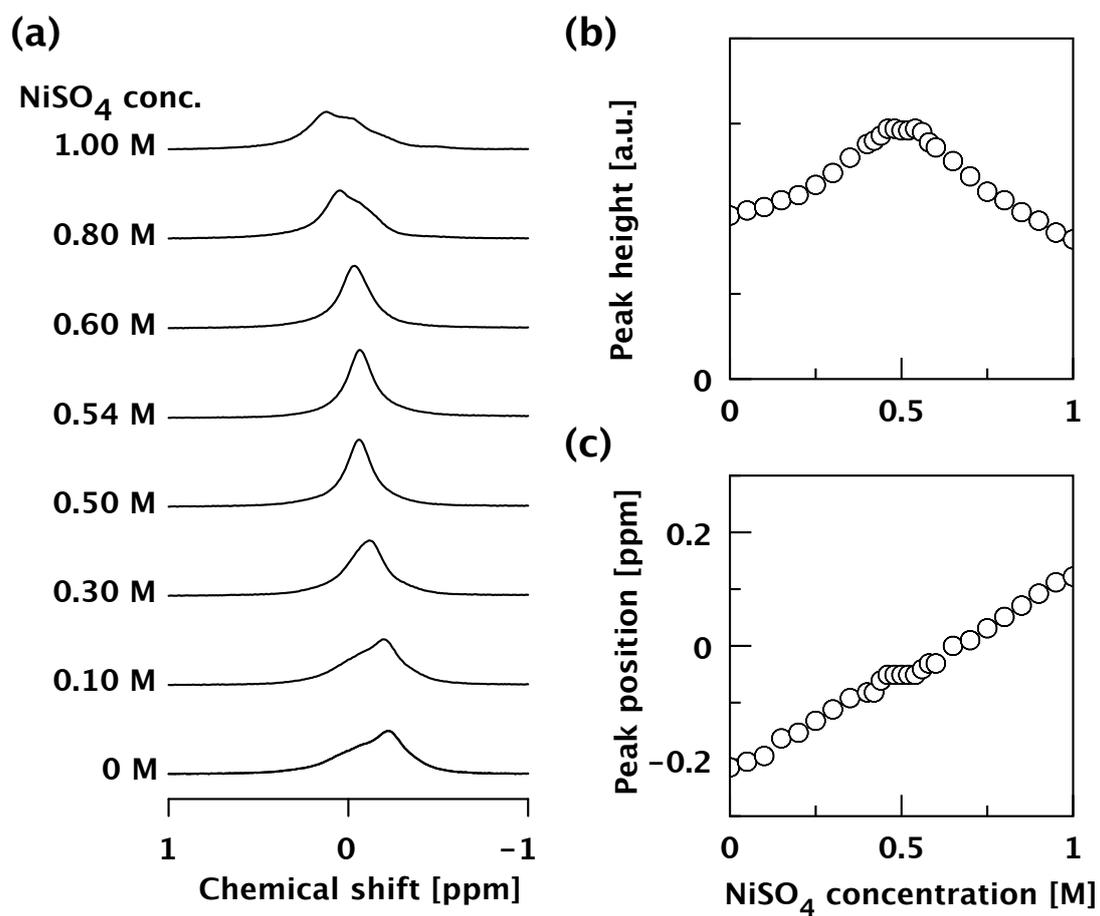


Fig. 3. ^1H spectra of aqueous solution of 0.1 M CuSO_4 obtained using a copper-capillary-wound microcoil filled with NiSO_4 aqueous solution with varying concentration. (b)(c) NiSO_4 concentration dependences of the peak height and the peak position.

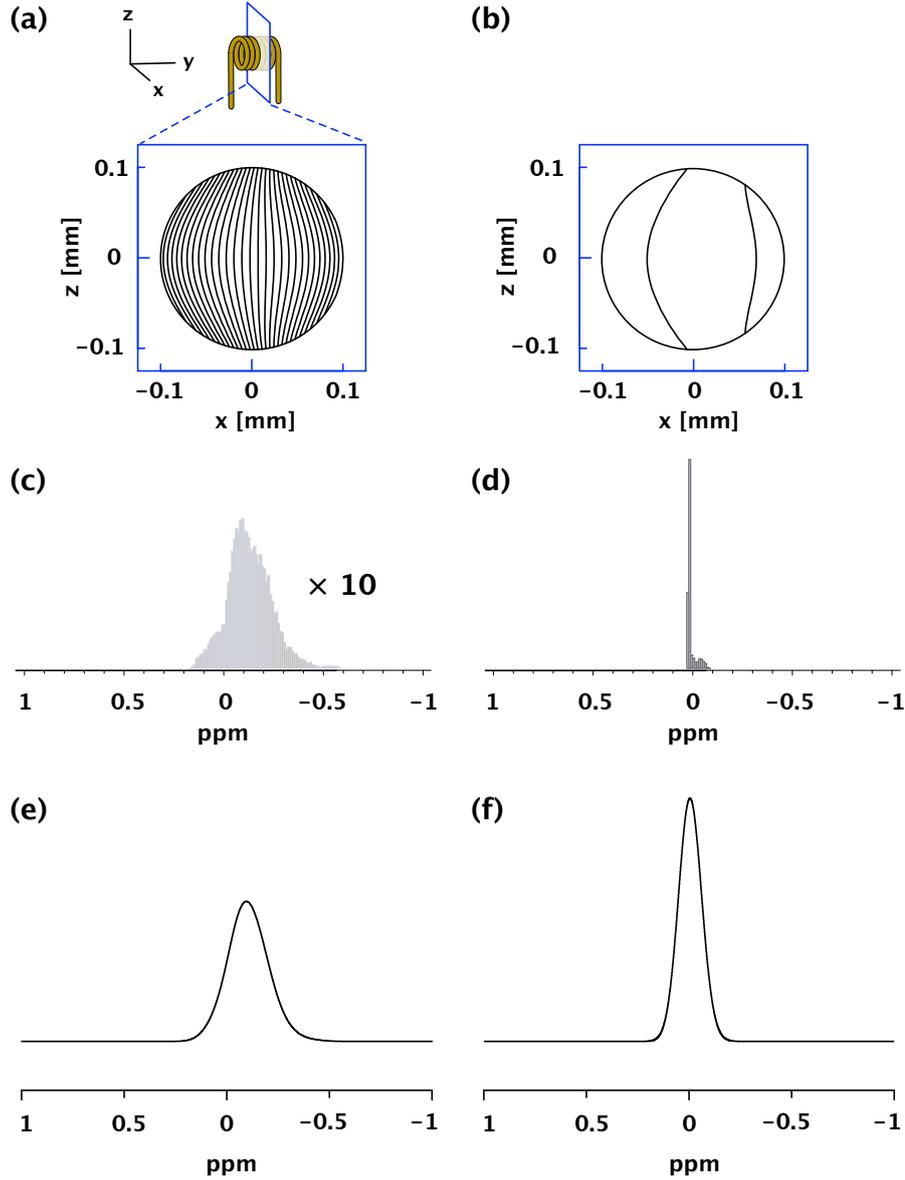


Fig. 4. (a) A contour plot of magnetic field distribution in a plane bisecting the microcoil calculated for the case where no paramagnetic liquid is supplied. (b) is a result obtained with 0.66 M aqueous solution of NiSO_4 filled inside the copper capillary. Contour lines are drawn every 0.005 ppm. (c)(d) Histograms representing the field distribution over a cylindrical region with a diameter of 0.2 mm and a length of 10 mm, which corresponds to the sample volume. (e)(f) were obtained by performing convolution operation to the histograms of (c) and (d) using a Gaussian function with a width of 38 Hz.

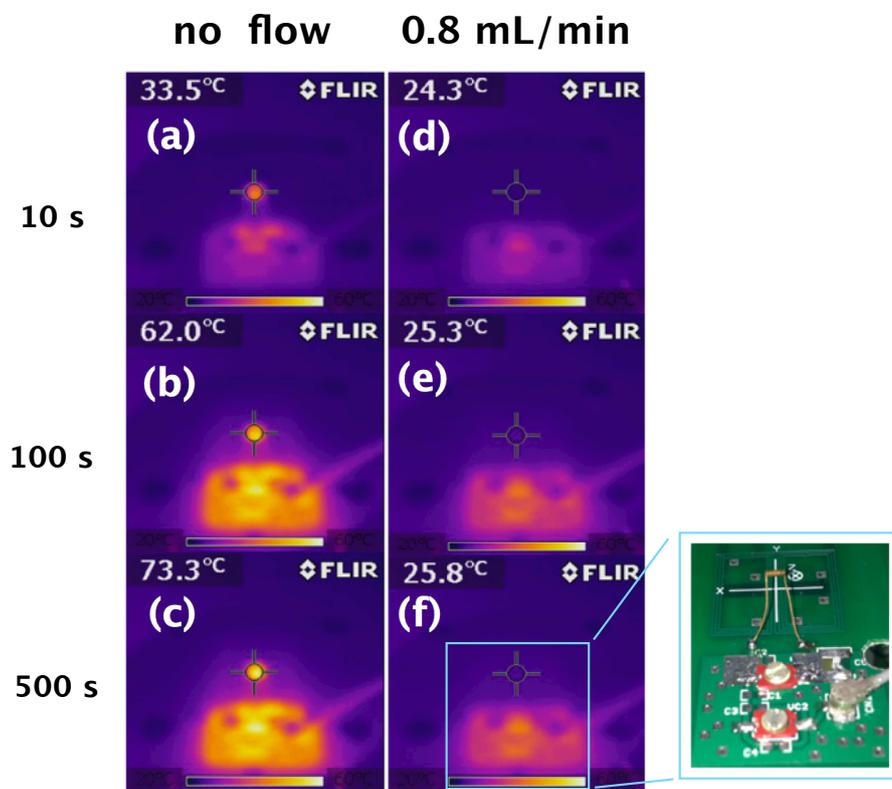


Fig. 5. Thermography images of the probe circuit under applications of radiofrequency pulses every one second at 300 MHz with a power of 19 W and a duration of 100 ms. In advance to this measurement, ^1H nutation experiments were performed and the radiofrequency power was found to correspond to a nutation frequency of 500 kHz. (a)(b)(c) show images taken after 10 s, 100 s, and 500 s after starting the experiment with no liquid flow inside the copper-capillary microcoil. (d)(e)(f) show results obtained by circulating 20 degree water at a flow rate of 0.8 mL/min.