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Ohmic contacts on silicon carbide: The first monolayer and its electronic effect

Zhongchang Wang,^{1,*} Susumu Tsukimoto,¹ Mitsuhiro Saito,¹ Kazuhiro Ito,² Masanori Murakami,³ and Yuichi Ikuhara^{1,4}

¹World Premier International Research Center, Advanced Institute for Materials Research, Tohoku University, 2-1-1 Katahira,

Aoba-ku, Sendai 980-8577, Japan

²Department of Materials Science and Engineering, Kyoto University, Kyoto 606-8501, Japan

³The Ritsumeikan Trust, Nakagyo-ku, Kyoto 604-8520, Japan

⁴Institute of Engineering Innovation, The University of Tokyo, 2-11-16 Yayoi, Bunkyo-ku, Tokyo 113-8656, Japan (Received 31 August 2009; revised manuscript received 3 November 2009; published 1 December 2009)

We demonstrate that origin of the long-standing contact issue in silicon carbide devices can be understood and technologically manipulated at the atomic level. Using advanced transmission electron microscopy, we attribute qualitatively the formation of ohmic contacts to silicon carbide to an epitaxial, coherent, and atomically ordered interface. Quantitatively, first-principles calculations predict that this interface can trap an atomic layer of carbon and hence enable lowered Schottky barrier and enhanced quantum electron transport. The combined experimental and theoretical studies performed provide insight into the complex electronic and electric effects of the buried contact interface, which are fundamental for improving the contact in future electronics based on wide-band-gap semiconductors such as silicon carbide and diamond.

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I. INTRODUCTION

One of the most active fields in semiconductor research is the development of electronic devices capable of function at high power and frequency levels, high temperatures, and caustic circumstances.^{1,2} This surge of activity is strongly driven by the urgent desire for replacing the current Si and GaAs-based electronics because they are unable to operate properly under harsh environmental conditions.^{3,4} As a promising substitute, the wide-band-gap semiconductor, silicon carbide (SiC),⁵ has captured considerable attention recently due to its excellent intrinsic properties,^{6,7} which involve large breakdown electric field, high electron saturation drift velocity, strong hardness, and good thermal conductivity.^{8,9} On the other hand, current significant improvements in its epitaxial and bulk crystal growth have paved the way for fabricating its electronic devices, which stimulates further interest in developing device processing techniques so as to take full advantage of its superior inherent properties.

One of the most critical issues currently limiting the device processing is the manufacturing of reliable and lowresistance ohmic contacts especially contacts to *p*-type 4H-SiC.^{10,11} The ohmic contacts are primarily important in SiC devices because a Schottky barrier of high energy is inclined to form at an interface between metal and wideband-gap semiconductor, which consequently results in lowcurrent driving, slow switching speed, and increased power dissipation. Much of effort expended to date to realize the ohmic contact has mainly focused on two techniques. One is the high-dose ion-implantation approach.^{12,13} which can increase the carrier density of SiC noticeably and reduce its depletion width significantly so that increasing tunneling current is able to flow across barrier region. The key problem of this method is the easy formation of lattice defects or amorphization during the ion implantation. These defects are unfortunately very stable and need to be recovered via annealing at an extremely high temperature (~ 2000 K), thereby complicating the mass production of SiC devices.

The other alternative is to generate an intermediate semiconductor layer with narrower band gap or higher carrier density at the contacts/SiC interface via depositing and annealing technique.^{14,15} To form such layers, many materials have been examined in a trial-and-error designing fashion, including metals,¹⁶ silicides,¹⁷ carbides,¹⁸ nitrides,¹⁹ and graphite.²⁰ Of all these materials, the metallic alloys have been investigated extensively,^{21,22} largely because their fabrication process is simple, standard, and requires no exotic materials. In particular, most of research activities have been focused on TiAl-based alloys, the only currently available materials that yield significantly low contact resistance (ohmic contact) to p SiC.^{23,24} Moreover, they demonstrate high thermal stability.¹ Although a lot of intriguing results have been obtained regarding the TiAl-based contact systems,^{25,26} the mechanism whereby the Schottky becomes ohmic after annealing has not been well clarified yet. In other words, the key factor to understanding the formation origin of ohmic contact remains controversial. Mohney et al.²⁷ proposed that a high density of surface pits and spikes underneath the contacts contributes to the formation of ohmic behavior based on their observations using scanning electron microscopy and atomic force microscopy. Nakatsuka et al.,²⁸ however, concluded that the Al concentration in the TiAl alloy is important for the contact formation. Using the liquid etch and ion-milling techniques, John and Capano²⁹ ruled out these possibilities and claimed that what matters in realizing the ohmic character is the generation of carbides, Ti₃SiC₂ and Al₄C₃, between the metals and semiconductor. This, however, differs, to some extent, from the x-ray diffraction (XRD) findings of Chang et al.³⁰ showing that the compounds formed at the metal/SiC interface are silicides, TiSi₂, TiSi, and Ti₃SiC₂. In addition, Ohyanagi *et al.*³¹ argued that carbon exists at the contacts/SiC interface and might play a crucial role in lowering Schottky barrier. These are just a few representative examples illustrating the obvious discrepancies in clarifying the formation mechanism of ohmic contact. Taking the amount of speculations on the mechanism and the

increasing needs for better device design and performance control, understanding the underlying formation origin is timely and relevant.

To develop an understanding of the origin in such a complex system, it is important to focus first on microstructure characterization. Transmission electron microscopy (TEM) studies by Tsukimoto et al.^{32,33} have provided useful information in this aspect. They have found that the majority of compounds generated on the surface of 4H-SiC substrate after annealing consist of Ti₃SiC₂ and hence proposed that the SiC/Ti₃SiC₂ interface is responsible for the lowering of Schottky barrier in the TiAl-based contact system. However, the role of this interface in realizing the ohmic nature is still unclear. It is not even clear how the two materials atomically bond together from their experiments, which is very important because it may strongly affect physical properties of the system. Theoretically, we have calculated the atomic structures, adhesive energies, and bonding nature of the SiC/Ti₃SiC₂ interface.³⁴ However, this calculation does not actually reveal the formation mechanism of ohmic contact because it only addresses interface structure. Furthermore, lacking essential experimental information about the interfacial atomic-scale structure, such calculations have been incomplete.

Recent advances in the high-angle annular-dark-field (HAADF) microscopy,^{35,36} the highest resolution, have enabled atomic-scale imaging of a buried interface.^{37,38} However, direct interpretation of the observed HAADF images is not always straightforward because there might be abrupt structural discontinuity, mixing of several species of elements on individual atomic columns, or missing contrasts of light elements. One possible way out to complement the microscopic data is through atomistic calculation, especially the first-principles calculation.^{39,40} As well known, the atomistic first-principles simulations have long been confirmed to be able to suggest plausible structures, elucidate the reason behind the observed images, and even provide a quantitative insight into how interface governs properties of materials. Consequently, a combination of the state-of-the-art microcopy and accurate atomistic modeling is an important advance for determining interface atomic-scale structure and relating it to device properties, revealing, in this way, physics origin of the contact issues in SiC electronics.41,42

In addition to determining atomic structure of the 4H-SiC/Ti₃SiC₂ interface, the goal of this work is to clarify the formation mechanism of the TiAl-based ohmic contacts so as to provide suggestions for further improvement of the contacts. 4H-SiC will hereafter be referred to as SiC. First of all, we fabricated the TiAl-based contacts and measured their electric properties in order to confirm the formation of ohmic contact. Next, the metals/SiC interface was analyzed using the XRD to identify reaction products and TEM, highresolution TEM (HRTEM), and scanning TEM (STEM) to observe microstructures. Based on these observations, we finally performed systematic first-principles calculations aimed to assist understanding of the ohmic contact formation at a quantum-mechanical level. Interestingly, we find that the SiC is totally covered by a well-defined layer-by-layer compound⁴³ and that a carbon monolayer emerges at the interface. The presence of the atomic layer of C is found to enable stronger adhesion, lowered Schottky barrier, and enhanced electron transport. This C layer, together with the abruptness and coherency of the contact interface, is critical for understanding the origin of ohmic nature.

The rest of this paper is organized in the following way. Section II describes in detail experimental procedure and computational methodology. In Sec. III, we show experimental results on electric measurement and microstructure analysis. The calculation results of atomic structures, electronic states, bonding nature, and quantum electron transport for the experimentally observed interfaces are presented in Sec. IV, where the factors affecting the ohmic contact formation are highlighted. Finally, the formation mechanism is discussed and the results are summarized in Sec. V.

II. EXPERIMENTAL AND CALCULATIONAL DETAILS

The *p*-type 4H-SiC layers doped with Al (5 μ m thick, $N_{A} = 4.5 \times 10^{18}$ cm⁻³), which were grown on pristine 4H-SiC wafers by chemical-vapor deposition (Cree, Inc.), were used as substrates. The 4H-SiC substrates have 8°-off Siterminated (0001) surfaces inclined toward $[\overline{2}110]$ direction because the 4H is the only SiC polymorph^{44,45} that allows lateral growth of (0001)-oriented layers. After chemically cleaning the substrate surface, a 10-nm-thick sacrificial oxide (SiO_r) layer was grown on the SiC substrate by dry oxidation at 1423 K for 60 min. For the purpose of subsequent currentvoltage (I-V) measurements, a circular electrode pattern was prepared in advance on the substrates by removing the SiO_x layer using the photolithographic technique. The substrates were first cleaned by dipping in 5% diluted hydrofluoric acid solution and rinsing in deionized water. Then, high-purity Ti and Al layers were deposited sequentially onto the SiC substrates in a high-vacuum chamber with base pressure of lower than 5×10^{-6} Pa. The Ti and Al were evaporated by electron beam and resistance heater, respectively. The deposited Ti and Al layers were as thick as 100 and 380 nm, respectively, as measured by a quartz oscillator during deposition. The thicknesses were selected deliberately in order to produce an average composition of Ti (20 at. %) and Al (80 at. %) because rich Al with more than 75 at. % in concentration was found empirically to be beneficial for yielding low-contact resistance.^{46,47} After lifting off the photoresist, the binary TiAl contact layers were finally annealed at 1273 K for 2 min in an ultrahigh-vacuum chamber with pressure of less than 1×10^{-7} Pa.

Cross-section thin-foil specimens for TEM observation were prepared by first cutting several slices from the deposited contacts along the [11 $\overline{2}0$] plane. These slices were then mechanically grinded to a thickness of 0.1 mm and further dimpled down to 20 μ m. Finally, to make an electron transparency, the dimpled slices were thinned by an argon-ion sputter beam using the PIPS 691 (Gatan Co., Ltd.) with gun voltages of 2–4 kV and beam angles of 6°, which had been confirmed to prevent samples from radiation damage.

The electric properties of the TiAl contacts were measured by a two-point probe method using the circular patterns with an interspacing of 8 μ m. Microstructure analyses were performed using the XRD and TEM. For the XRD, a Rigaku RINT-2500 diffractometry with Cu $K\alpha$ radiation operated at 30 kV and 100 mA was used. The interfacial microstructures and orientation relationships were characterized by the TEM, HRTEM, and selected-area diffraction pattern (SADP), using a JEOL JEM-4000EX electron microscope operated at an accelerating voltage of 400 kV. The point-topoint resolution of this microscope was approximately 0.17 nm. The interface atomic-scale structures were observed using the HAADF-STEM (JEM-2100F, JEOL Ltd.). The STEM used in this study was equipped with an aberration corrector (CEOS Gmbh, Heidelberg, Germany), which offers an unprecedented opportunity to probe details of interface atomic structure with a sub-angstrom electron probe. A HAADF detector with an inner semiangle of more than 60 mrad was used. Under this collection condition, the contrast of an atomic column in the incoherent HAADF image is approximately proportional to the square of atomic number $(Z).^{48}$

The calculations of total energies and electronic structures were performed using the Vienna ab initio simulation package (VASP) within the framework of density-functional theory (DFT).^{49,50} The projector augmented wave method⁵¹ was used for electron-ion interactions and the generalized gradient approximation (GGA) of Perdew et al.⁵² (PW91) was employed to describe the exchange-correlation functional. The single-particle Kohn-Sham wave function was expanded using the plane waves with a cutoff energy of 400 eV and sampling of irreducible Brillion zone was carried out with a regular Monkhorst-Pack grid of $8 \times 8 \times 1$ k points.⁵³ For interface calculations, a vacuum region of 10 Å was embedded into the supercell to avoid the unwanted interaction between the slab and its period images.⁵⁴ We conducted a series of convergence tests for the interface systems and confirmed that the above parameters were sufficient to ensure totalenergy convergence to less than 1 meV/atom. All atoms in the calculated slabs were fully relaxed using the conjugate gradient algorithm⁵⁵ until the magnitude of Hellmann-Feynman force⁵⁶ on each atom converged to less than 0.05 eV/Å.

As for transport calculations, we applied the state-of-theart quantum transport technique, that is, the fully selfconsistent nonequilibrium Green's-function method combined with the DFT, which was implemented in Atomistix ToolKit (ATK) code.^{57,58} The reliability of this method was tested^{59,60} and applicability of this code was examined on many systems.^{61,62} The core electrons were modeled with the Troullier-Matrins nonlocal pseudopotential⁶³ while the valence electrons were expanded in a numerical atomic-orbital basis set of single zeta plus polarization. The total energy was well converged to within 1–2 meV/atom upon using 4 ×4 k points to sample the irreducible Brillouin zone and a cutoff of 100 Ry for the grid integration to present charge density. A 10×10 k-point mesh was then used to obtain sufficiently converged transmission spectra.

III. EXPERIMENTAL RESULTS

A. Formation of ohmic contacts

To verify the formation of ohmic contact, we measured the electric properties (I-V characteristics) for the TiAl con-



FIG. 1. (Color online) Current-voltage properties of the TiAl contact systems before and after thermal annealing at 1273 K for 2 min.

tact systems before and after annealing, as shown in Fig. 1. For the system before annealing, its current almost maintains zero despite that the applied bias ranges from -3.0 to 3.0 V, which clearly reflects Schottky character of this system.^{64,65} This can be understood by considering that the potential induced by applied bias drops largely at an contact interface between metals and semiconductors, thus hindering the current flow. The annealed system, however, exhibits a typical ohmic nature, as its *I-V* curve is nearly linear and the current increases sharply with the rise of applied bias.^{66,67} This drastic change in electric properties agrees well with previous experimental reports^{68–70} and suggests that there might be substantial changes in microstructure during the annealing.

B. Identification of reaction products

To determine chemical composition of the TiAl contact systems, we performed XRD analyses, as shown in Fig. 2, where textural orientations of the detected matters are shown as well for easy reference. As expected from the preparation process, one can see in Fig. 2(a) peaks of deposited metals, Ti and Al, and the (0001)-oriented SiC in the system before annealing. It is worthy of mentioning that the detected Ti has a much weaker intensity of diffraction peak than the Al, which can be attributed to its lower concentration and smaller grains. On the other hand, the XRD spectrum alters significantly after annealing [Fig. 2(b)], as the original Ti and Al peaks disappear and new peaks emerge, which suggests that chemical reactions occur at interface.



FIG. 2. (Color online) XRD spectra of (a) as-deposited and (b) annealed TiAl contact systems. Note that the TSC represents Ti_3SiC_2 .



FIG. 3. (Color online) (a) Cross-sectional bright-field TEM image of the annealed TiAl contact system showing exclusive reaction product of Ti_3SiC_2 and (b) EDS data obtained at the SiC and Ti_3SiC_2 region near to interface. The vertical axis in (b) denotes the counts (i.e., intensity).

From Fig. 2(b), the reaction products are found to be dominated by ternary Ti₃SiC₂ with strongly (0001)-oriented textures, as only the (000l) diffraction peaks are observed. In addition to the Ti₃SiC₂, binary Al₄C₃ is also present in the annealed specimen. However, its amount is very small because the intensities of its diffraction peaks are comparatively much weaker. The formation of these compounds at elevated temperature is also supported by the Ti-Al-SiC equilibrium phase diagram,⁷¹ which predicts that four phases, SiC, Al₄C₃, Ti₃SiC₂, and liquid, can coexist in an equilibrium state when the aforementioned composition of TiAl alloy is adopted. Furthermore, the XRD results agree well with the experimental reports of Jennings et al.⁷² and Johnson and Capano,²⁹ but deviate somewhat from those of Nakatsuka *et al.*,²⁸ which show that binary Al₃Ti is present as well. This slight difference is mainly because the intensity of Al₃Ti peak is so low that might be overlapped by the strong peaks of SiC and Ti₃SiC₂. Finally, we note that the SiC retains the (0001)-oriented texture after annealing, thereby facilitating the development of heteroepitaxy between the reaction products and substrates.

C. Interfacial orientation relationships and microstructures

Although the XRD can reveal detailed information on chemical composition of reaction products, it provides limited insight into matters concerning how the products distribute and contact the substrate. To observe the microstructure directly, we present in Fig. 3(a) a cross-sectional bright-field TEM image of a representative region in the annealed TiAl contact system. The incident electron beam is along [0110] direction of the SiC, which is parallel to the tilting axis of the 8°-off SiC(0001) surface. As seen in this figure, the SiC surface is covered entirely by the plate-shaped Ti₃SiC₂ with thickness ranging approximately from 30 to 300 nm. This universal cover means that no any other compounds contact directly the SiC surface, thereby ensuring an exclusive contact of Ti₃SiC₂ to SiC. Consequently, the SiC/Ti₃SiC₂ inter-



FIG. 4. (Color online) Selected-area diffraction pattern obtained at the annealed contacts/SiC interface. The arrays of diffraction spots from the SiC and contacts are marked by dashed and dotted lines, respectively.

face might play an essential role in the formation of ohmic contact. In addition, this interface is observed to have a saw-toothlike facet structure and the Ti_3SiC_2 surface inclines by nearly 8° toward the substrate surface, suggesting that the SiC surface affects significantly the morphology of formed Ti_3SiC_2 .

To analyze the element species around interface, we further show in Fig. 3(b) the energy-dispersive x-ray spectroscopy (EDS) spectra for the interfacial SiC and Ti₃SiC₂ regions. The substrate is mainly composed of C and Si and the reaction products C, Si, and Ti, in accordance with chemical compositions of the substrate and the main reaction products, respectively. Unexpectedly, no Al peak is observed in either the interfacial SiC or Ti₃SiC₂ area, which contravenes our previous XRD analyses showing that the Al₄C₃ compound is present in the annealed specimen. This discrepancy is mainly because the amount of Al_4C_3 is so small [Fig. 2(b)] that is hard to be detected by the EDS, or because the Al might not distribute near the interface at all but around the Ti₃SiC₂ surface instead. Whatever the reason is, the Al should not be the key to understanding the formation origin of ohmic contact. That is, a large amount of Al diffuses into the SiC and introduces a heavily *p*-doped SiC, which result in narrower depletion area and thus more tunneling. As a matter of fact, Gao et al.73 have confirmed, by analyzing interfacial chemical composition and local states, that no additional Al segregates to the interface, suggestive of a clean contact of Ti₃SiC₂ to SiC. To further corroborate this point, the characterization using the HRTEM and STEM is needed, and this will be provided later.

Figure 4 shows a SADP at the contacts/SiC interface taken along the same electron-beam direction as in Fig. 3(a). A careful indexing of this pattern confirms again the plate-shaped layers as being ternary Ti_3SiC_2 . From this figure, the formed Ti_3SiC_2 layers are observed to have epitaxial orientation relationships $(0001)_{Ti_3SiC_2} \parallel (0001)_{SiC}$ and $[0\bar{1}10]_{Ti_3SiC_2} \parallel [0\bar{1}10]_{SiC}$ with the SiC substrate, which agrees well with the XRD analyses demonstrating that both materials exhibit strongly (0001)-oriented textures. These orienta-

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FIG. 5. (Color online) A representative cross-sectional HRTEM image of the interface between the generated Ti_3SiC_2 and the SiC substrate observed from the $[11\overline{2}0]$ direction.

tion relationships are believed to be beneficial for forming a coherent and well-matched interface between the SiC and Ti₃SiC₂,³⁴ since they both belong to the hexagonal space group with lattice constants of a=3.081 Å and c=10.085 Å for the SiC (Refs. 74 and 75) and a=3.068 Å and c=17.669 Å for the Ti₃SiC₂.^{76,77}

In support of this idea, we present in Fig. 5 a crosssectional HRTEM image of the SiC/Ti₃SiC₂ interface observed from the [1120] direction. From this figure, one can clearly see well-arranged (000l)-oriented lattice fringes along the direction parallel to the interface in both the Ti_3SiC_2 layer and SiC substrate (marked in Fig. 5). The points at which the phase contrast is no longer periodic in either the Ti₃SiC₂ or SiC define the interfacial region, as indicated by arrows. Evidently, the interface is atomically abrupt and coherent without any secondary phase layers, amorphous layers, contaminants, or transition regions, which confirms a clean and direct contact of the Ti₃SiC₂ with SiC on atomic scale. In addition, no misfit dislocations are visible at interface in the present HRTEM micrograph and further examination of other interfacial regions (not shown here) demonstrates that the density of misfit dislocations is extremely low in this contact system. This can be explained from the small lattice mismatch between the two materials (less than 0.5%). Unfortunately, it remains unclear from this figure how the two materials atomically bond together at interface, which is very important because bonding nature is well known to be able to affect physical properties of interfacial systems significantly.

D. Interfacial atomic-scale structures

Figure 6 shows a typical HAADF image of the SiC/Ti_3SiC_2 interface. A simple looking at this figure confirms a clean and atomically sharp contact between the two materials, which means that we have successfully produced epitaxially grown Ti_3SiC_2 on SiC. Brighter spots in the image represent atomic columns of Ti, while the comparatively darker ones are Si, since the intensity of an atomic column in the STEM, to good approximation, is directly proportional to the square of atomic number (*Z*).^{48,78} Not surprisingly, due to small atomic number of C, its columns are not scattered strongly enough to be visualized, thereby making the image incomplete. Further complementing of this image so as to



FIG. 6. (Color online) A typical HAADF-STEM image of the SiC/Ti_3SiC_2 interface in the annealed TiAl contact system observed from the $[11\overline{2}0]$ direction. The position of interface is indicated by two arrows.

relate the atomic structure to property requires the highprecision first-principles calculations, and this will be addressed in the following section.

To see the interface atomic structure clearer, we magnify the cross-sectional HAADF image of the SiC/Ti₃SiC₂ interface in Fig. 7(a) and further filter it to reduce noise, as shown in Fig. 7(b). The interface location is indicated by a horizontal line, which is determined based on the arrangement of atomic columns in bulk SiC and Ti₃SiC₂. The Si-terminated Ti₃SiC₂ is observed intuitively to make a direct contact with the Si-terminated SiC substrate with the interfacial Si atoms of Ti₃SiC₂ sitting above hollow sites of the interfacial Si plane of SiC. However, as we will see in the upcoming simulations, this interpretation is premature in that it neglects a possibility, namely, the unseen C might be trapped at interface. Another interesting feature in this figure is that no Al columns are detected surrounding interface, which eliminates the possibility of additional p doping via Al diffusion into the top few SiC layers. Since there are also no pits, spikes, or dislocations which might act as pathways for current transport, we conclude that the clean and coherent SiC/Ti_3SiC_2 interface should be critical for the ohmic contact formation.



FIG. 7. (Color online) (a) Magnified HAADF image of the SiC/Ti_3SiC_2 interface. An overlay is shown as well for easy reference. The bigger balls denote Si and the smaller ones Ti. (b) The same image as in (a) but has been low-pass filtered to reduce the noise.

FIG. 8. (Color online) Relaxed SiC(0001)/Ti₃SiC₂(0001) interface models (a) without interfacial C atoms (SiSi) and (b) with interfacial C atoms (SiCSi). (c) Optimized SiC(0001)/Ti(0001) interface model. The distance between interfacial Si-Si layers [Si-Ti layers for (c)] is represented by *d*1 and that between interfacial Si-Si atoms [Si-Ti atoms for (c)] projected onto the paper plane by *d*2. The interfaces are represented by dotted lines.

The ensuing question is how this interface lowers the Schottky barrier, which is rather difficult to investigate by experiment alone but can be suggested by calculations.

IV. ATOMISTIC CALCULATION RESULTS

A. Determination of interface atomic structure

To clarify the mechanism theoretically, we first determined atomic structure of the SiC/Ti₃SiC₂ interface via complementing the acquired HAADF image (Fig. 7). From the consideration of bulk structures of 4H-SiC and Ti₃SiC₂, the aforementioned orientation relationships, and the relative stacking order of Ti and Si, the observed image in Fig. 7 can be intuitively fitted by a SiSi model shown in Fig. 8(a). In this model, the interfacial Si atoms of Ti₃SiC₂ sit above the hollow sites of interfacial Si plane of SiC, where the optimal distance between interfacial Si-Si planes [denoted as d1 in Fig. 8(a)] and that between interfacial Si-Si atoms projected onto paper plane [denoted as d2 in Fig. 8(a)] are calculated to be 2.13 and 2.53 Å (Table I), respectively. These distances, however, deviate severely from their average experimental values, 2.5 and 2.8 Å, which are obtained by characterizing quantitatively the HAADF image (Fig. 7). In addition, an examination of interface stability by calculating adhesion energy W_{ad} , a key quantity to predict mechanical property of an interface,^{79,80} indicates that the SiSi model is

TABLE I. Relaxed $W_{ad}(J/m^2)$, optimal interfacial distances $d1(\text{\AA})$ and $d2(\text{\AA})$, and calculated *p*-type Schottky barrier heights (SBH) (eV) for the SiC/Ti₃SiC₂ interfaces without (SiSi) and with interfacial C (SiCSi), and for the SiC/Ti interface (SiTi). Refer to Fig. 8 for their schematic configurations.

	SiSi	SiCSi	SiTi
$W_{\rm ad}~({\rm J}/{\rm m}^2)$	1.62	6.81	2.06
d1 (Å)	2.13	2.31	2.36
d2 (Å)	2.53	2.81	2.97
SBH (eV)	1.05	0.60	1.10

not favored (1.62 J/m²). It is even less stable than the model with interfacial Si of Ti_3SiC_2 resting straight atop the interfacial Si of SiC (2.58 J/m²), which contravenes again the observed image. Why does the less preferred interface predicted by our simulations emerge in our experimental observation? It is worth mentioning that we have examined many other regions using the STEM but failed to see other possibilities.

Could these pronounced discrepancies between results of experiment and calculation be ascribed to computational inaccuracies? Since the calculation parameters described above are verified to be sufficient to ensure a total-energy precision of better than 1 meV/atom, one might be concerned that another numerical inaccuracy arises from size effect of the used slabs. However, we found this inaccuracy to be within 0.1 J/m^2 via enlarging the slabs along the interface so that it does not affect our simulated W_{ad} . In addition, convergence tests show that the used slab thickness yields surface-energy convergence to smaller than 0.02 J/m^2 . Furthermore, the used GGA was tested to evaluate bulk lattice constants and distances between atoms within an error of less than 0.5%.^{81,82} Finally, there is a small lattice mismatch of 0.63% at interface,³⁴ which can be damped out by structural optimization. Moreover, Wang et al.⁸³ have reported that a lattice mismatch as large as 3.9% at an interface varies the W_{ad} only by less than 5%. Therefore, it seems that the discrepancies should not simply be attributed to the computational error.

To resolve these paradoxes, we noticed that a possibility might be ignored, that is, the unseen C might be trapped at interface, altering the local environment there. To test this hypothesis, we established a model (named as SiCSi) by introducing C into the interfacial layer from the consideration of crystal extension and stacking sequences. The calculated $W_{\rm ad}$ of this SiCSi model is listed in Table I, where one can see that the interface is strengthened substantially after the incorporation of C. Investigation into its fully optimized atomic configuration [Fig. 8(b)] reveals that the incorporation of C does not induce significant interface reconstruction. Namely, the two Si layers proximal to the interface maintain the stacking seen in Fig. 8(a), thus matching the HAADF image geometrically. Quantitatively, the d1 and d2 distances are now 2.53 and 2.81 Å (see Table I), respectively, very close to the obtained experimental values. Therefore, the introduction of interfacial C monolayer resolves the inconsistencies between simulations and experiments. Finally, we superimpose the calculation-inferred atomic structure of SiCSi interface [Fig. 8(b)] onto the HAADF image [Fig. 7(a)] and find that they match very well.

B. Schottky barrier height

To further examine whether the determined interface has less Schottky character, we calculated *p*-type Schottky barrier height (SBH), an important quantity in analyzing electric properties of a metal/semiconductor contact interface.^{84,85} The *p*-type SBH is calculated from the difference between the Fermi level (E_F) of interface supercell and the valenceband top of bulk SiC region,^{86,87} which can be obtained by supercell calculations based on the DFT. It should be noted



FIG. 9. (Color online) Planar-averaged (a) total charge density and (b) charge-density difference for the relaxed SiSi, SiCSi, and SiTi interfaces along [0001] direction. The solid rectangles, circles, and triangles give the locations of C, Si, and Ti atoms, respectively. The interface position is set to zero and indicated by a vertical line.

that due to the well-known problem of discontinuity in the exchange-correlation potential across heterointerface,^{88,89} an exact quantitative estimation of SBH is unlikely. However, qualitative comparisons between the calculated SBHs for different interface configurations should be reliable.^{90,91} The p-type SBHs for the SiC/Ti₃SiC₂ interfaces with and without interfacial C are listed in Table I, where the SBH for the SiC/Ti interface [Fig. 8(c)] is listed as well for comparison (denoted as SiTi in Table I). From this table, one can see that the SiCSi interface shows the lowest SBH, meaning that it is of the least Schottky nature. Since no theoretical SBH values for the SiC/Ti₃SiC₂ interface are available and direct comparison of our calculated values with experimental data is complicated, it is hard to verify the accuracy of our results directly. However, we have noted that our simulated SBH of the SiTi case (1.10 eV) agrees well with the SBH of 1.00 eV calculated from the 6H-SiC/Ti interface.⁸⁶

C. Electronic structure and bonding

1. Planar-averaged charge density

To shed light on origin of decrease in SBH and junction strengthening in the SiCSi interface, we applied several analytic approaches to characterize in detail interfacial electronic states and bonding nature. First, we calculated planaraveraged charge density and its difference along the interface normal. The density difference is evaluated by subtracting the sum of charge density of isolated SiC and Ti₃SiC₂ slabs from the total interface charge density.⁸⁰ As seen in Fig. 9(a), after introducing the C, an interfacial Si-C pair is generated in the SiCSi case in a way similar to the pair in bulk SiC. As a result of the pair, there is a dramatic accumulation of charge within the interfacial region, in contrast to what is seen in either the SiSi or SiTi interface [Fig. 9(a)]. This indicates that the covalent bonding is strengthened for the SiCSi. Evidently, the large degree of charge accumulation at interface is at the expense of depletion of charge in the subinterfacial layers between Si and Ti, suggestive of weakened bonding between them. This is a short-range effect, however, since the charge density returns to its bulk value by the second layer. From Fig. 9(b), we note that the planar-averaged density difference for the SiCSi most prominently deviates from zero around the interface, reflecting the most significant charge transfer between SiC and Ti₃SiC₂ slabs. In addition,



FIG. 10. (Color online) DOS (states/eV atom) projected on the atomic layers close to the relaxed SiCSi interface. The left panel shows PDOSs of SiC layers and the right one those of Ti_3SiC_2 layers. The first layer is the atomic layer proximal to interface. The E_F is set to zero and marked by a dashed line.

charge is observed to be depleted noticeably in both the subinterfacial SiC and Ti_3SiC_2 region for the SiCSi, suggesting that the atoms second nearest to the interface contribute to the interfacial bonding. These missing charges, to a large extent, make their way onto the more electronegative C ions, indicative of formation of ionic bonding.

2. Partial density of states

We then presented in Fig. 10 the density of states (DOS) projected on selected atomic layers of the SiCSi interface in order to gain insight into the electronic states. As seen in this figure, the overall partial DOS (PDOS) shape of interfacial Si of Ti₃SiC₂ resembles to some extent that of a Si layer deeper in SiC but deviates remarkably from that of a Si layer deeper in Ti₃SiC₂ (seventh layer), which can be reflected from the formation of Si-C pair. Moreover, this suggests that the substrate has a fundamental effect on interface electronically. A key feature in this figure is that a strong interaction is observed between the subinterfacial Ti d and Si p states below E_F , which continues well into the SiC surface, inducing noticeable gap states in the interfacial C at E_F . This means that the interfacial C layer, the first monolayer on the substrate, is metallized, indicative of possible electric conductivity. In fact, the gap states can extend as far as they can into deeper layers of SiC, as there appear weak but visible peaks at E_F in the PDOSs of the second and third layers of SiC. Consequently, a local weak metallicity might occur in top few layers of the semiconductor surface, which could enable current flow through the SiC. Apart from the peaks in SiC, all of the Ti_3SiC_2 layers exhibit notable peaks at E_F , which can be attributed to the large degree of overlap between Ti d and C (Si) p states. Finally, we note significant hybridization between the interfacial C sp and Si sp states, suggestive of covalent bonding at interface.

3. Charge distribution

To identify the bonding type directly, we further show contour plots of charge densities (Fig. 11) and their differ-



FIG. 11. (Color online) Contour plots of charge densities for (a) SiSi, (b) SiCSi, and (c) SiTi interfaces taken along the $(11\overline{2}0)$ plane. The interface is represented by a horizontal line and the atoms that intersect the contour plane are labeled. The magnitude of charge is denoted by a scale at the bottom of (b).

ences (Fig. 12) along the (1120) plane for the optimized SiSi, SiCSi, and SiTi interfaces. From Fig. 11, we notice first that the bonding interaction between the interfacial Si and C for the SiCSi interface is remarkably similar to the Si-C interaction deeper into SiC: the majority of charge is localized on C with humps directed toward their adjacent Si. We thus conclude that the interfacial bonding for the SiCSi is of mixed covalent-ionic nature. The interfacial bonds for the SiSi interface, however, exhibit covalent character with a small amount of charge accumulated within the interfacial region [Fig. 11(a)], in consistence with our analyses on planar-averaged density difference (Fig. 9). As for the SiTi, the charge distribution of interfacial Ti is almost identical to that of Ti away from interface, having a character of weakly but broadly distributed charge density. This indicates that the interfacial bonds for the SiTi take on weakly metallic nature, yet maintain a small degree of covalency. The covalency can



FIG. 12. (Color online) Contour plots of charge-density differences for (a) SiSi, (b) SiCSi, and (c) SiTi interfaces taken along the $(11\overline{2}0)$ plane. The difference of charge density presents redistribution of charge in the interface relative to its isolated system.



FIG. 13. (Color online) Electrostatic potential as a function of distance from interface along the [0001] direction for (a) SiSi, (b) SiCSi, and (c) SiTi interfaces. Interface position is set to zero.

be further confirmed from the density-difference plot [Fig. 12(c)] displaying charge accumulation along the interfacial Si-Ti bonds. The amount of charge accumulated on the Si-Ti bonds is larger than that on the interfacial Si-Si bonds of SiSi [Fig. 12(a)] but far less significant than that on the interfacial Si-C bonds of SiCSi [Fig. 12(b)]. This heaviest charge accumulation along the interfacial Si-C bonds, together with the mixed covalent-ionic character at the SiCSi interface, explains the largest W_{ad} associated with the SiCSi interface (Table I). Finally, we note from both figures that charge variations due to interface are screened rapidly with distance from interface, suggesting that the interface effect is confined within a short range, in good agreement with our previous analyses on PDOS and planar-averaged charge.

4. Electrostatic potential

To further explain the decrease in SBH for the SiCSi, we plotted the variation in electrostatic potential along the interface normal in Fig. 13, where potential changes for the SiSi and SiTi interfaces are shown as well for comparison. As a result of the large interface dipole generated by the considerable charge transfer [Fig. 9(b)] and the partial ionicity [Fig. 11(b)], the electrostatic potential of interfacial Si in the SiCSi is lowered significantly relative to its adjacent SiC region [Fig. 13(b)], which consequently enables the reduction in SBH. This is contrary to the SiSi [Fig. 13(a)] and SiTi [Fig. 13(c)] cases, as their electrostatic potentials are high at interface. These high potentials indicate that electrons might be transferred from the SiC surface to the interface, resulting in electron depletion on substrate surface. Moreover, we note in Fig. 13 that electrostatic potential for Si atoms is always lower than that for the Ti or C atoms, which explains the lower electron density of Si shown in the charge-distribution plot (Fig. 11).

D. Electron density near Fermi level

Although the charge-distribution analysis can reveal valuable information on interfacial bonding, it provides re-



FIG. 14. (Color online) (a) Isosurface and (b) electron-density plot along the $(11\overline{2}0)$ plane in the energy window $(E_F-0.5 \text{ eV}, E_F)$ for the SiCSi interface. The interface is marked by two arrows.

strained insight into how electrons distribute around E_F , which matters because density around E_F directly determines the current transmission. Figure 14 illustrates an electrondensity isosurface and its slice along the (1120) plane for the optimized SiCSi interface around E_F . From Fig. 14(a), one can see that charges surrounding interfacial Si are connected and broadly distributed in a sheetlike fashion, which suggests possible electrical conductivity through this region. In addition, there also appear heavily accumulated electrons within the interfacial area, which are connected along the interface and extended as far as several atomic layers into the SiC. These characters can also be confirmed from the slice plot in Fig. 14(b), meaning that current might flow over top few atomic layers of semiconductor, thereby causing ohmic property. As expected, the electron density at E_F is extremely high for the Ti₃SiC₂ (i.e., sea of electrons) but becomes nil for the SiC layers away from interface [Fig. 14(b)], which can be understood from their intrinsic metallic and semiconducting nature.92,93

E. Quantum electron transport properties

To examine electrical conductivity and gain insight into how the interface influences current transport, we devised a two-probe system, $Ti/Ti_3SiC_2/SiC/Ti_3SiC_2/Ti$, and investigated nonequilibrium quantum transport properties. Figure 15 schematically shows a model of the sandwich transport system, which can be divided into a left semi-infinite electrode, a scattering region, and a right semi-infinite electrode.^{57,94} The atomic and electronic structures of the semi-infinite Ti electrodes are assumed to be the same as



transport properties SiSi, SiCSi, and Si spectra differ from c



FIG. 16. (Color online) (a) Transmission spectra under 0 V and (b) current-voltage characteristics for the sandwich systems involving the SiSi, SiCSi, and SiTi interface. Refer to Fig. 8 for their corresponding interfacial configurations.

those of bulk Ti. On the other hand, the electronic states of scattering region are calculated self-consistently. The scattering region consists of hexagonal SiC and Ti_3SiC_2 layers and the periodic boundary conditions are imposed along the directions parallel to the interface. The SiC/Ti_3SiC_2 interface could be either the SiSi or SiCSi, whereas other interfaces are maintained identical for the sandwich systems. In this sense, the difference between the two systems can be mainly attributed to their differing SiC/Ti_3SiC_2 interfaces. Furthermore, we also calculated the Ti/SiC/Ti system, wherein the SiTi model shown in Fig. 8(c) was taken as the SiC/Ti interface.

Figure 16(a) shows transmission spectra for the relaxed SiSi, SiCSi, and SiTi systems, where one can see that the spectra differ from one another suggesting variations in electronic structures with interface geometries. The most interesting feature is the presence of transmission peaks at E_F for the SiCSi, which is attributable to the electrons distributed around the interface at E_F . Further calculations on electrical properties (e.g., I-V curve) for the three systems reveal that the current in the SiCSi case increases much faster than either the SiSi or SiTi case as the applied bias voltage increases [Fig. 16(b)], which can be explained by its lowest SBH (Table I). Finally, in comparing the general trend of the calculated *I-V* with that of our experimental curve (Fig. 1), we find that they agree qualitatively: both the annealed specimen and the SiCSi model clearly show ohmic behavior, thereby validating the application of the SiCSi model to describe the ohmic contacts in the TiAl-based system.

V. DISCUSSION AND CONCLUSIONS

FIG. 15. (Color online) Schematic illustration of a two-probe $Ti/Ti_3SiC_2/SiC/Ti_3SiC_2/Ti$ quantum transport system. The system has infinite extent in the (x, y) direction and extends to $\pm \infty$ in the *z* direction. The SiC/Ti_3SiC_ interfaces shown in Fig. 8 are adopted.

Although a number of works have been conducted on the TiAl-based ohmic contact, its mechanism remains controversial. The current understanding of its formation origin, which is based mainly on experimental studies of property measurement and structure characterization, can be summarized in three main points: (1) the deposited Al (80 at. %) might diffuse in part into the SiC and dope heavily the semiconductor because the Al is well known to act as a *p*-type dopant for SiC,^{28,67} (2) the high density of pits, spikes, or dislocations may be generated underneath the contacts after annealing so that current can transport primarily through these defects due to the possible enhancement of electric field at these features and semiconductor doping at these locations, and^{27,95} (3) the formation of intermediate semiconductor layer between the deposited metals and semiconductor, which consists of silicides or carbides, could divide the high barrier height into lower ones, thus reducing the effective barrier height.^{29,32}

The results presented in this paper first demonstrate that no Al is clearly segregated around the interfacial region, in particular, at the top few layers of SiC, which rules out the possibility of additional Al doping.^{29,73} Though a small amount of residual Al is found to be present, mostly in form of Al_4C_3 compound, it may locate on the surface of annealed contacts rather than in the layer directly contacted to the SiC, thus playing a negligible role in ohmic contact formation. The majority of deposited Al is evaporated during annealing because of its low melting point and high equilibrium vapor pressure. The dominant role played by Al in the TiAl system is to assist the formation of liquid alloy so as to facilitate chemical reaction.⁷³ Furthermore, careful characterization of the interfacial region reveals that the substrate and the generated compound are epitaxially oriented and well matched at interface with no clear evidence of high density of defects. This suggests that the morphology might not be the key to understanding the contact formation.²⁹ In support of this speculation, it has been observed previously that Ti ohmic contacts can be possibly generated without any pitting and that pit-free ohmic contacts can be fabricated.^{25,96}

One remaining theory is the alloy-assisted ohmic contact formation.^{30,33} This alloy is determined to be ternary Ti₃SiC₂ in our study, which has also been corroborated by other experiments.^{29,73} Since the bulk Ti₃SiC₂ has already been found to be of metallic nature both in experiment and theory,^{97,98} the contact between Ti₃SiC₂ and its covered metals should show ohmic character and thus the SiC/Ti₃SiC₂ interface should play a significant role in ohmic contact formation. Our calculation results support this idea by suggesting that the determined interface has a lowered SBH due to the large dipole shift at interface induced by the partial ionicity and the considerable charge transfer. In addition, the interfacial states, as indicated by the electron distribution at E_F , are also viewed as a contributing factor in reducing the SBH. These states might be further enhanced by the possible presence of point defects at interface, although these structural defects have not been detected by our TEM and addressed in this study.

Interestingly, our calculations predict that an atomic layer of carbon emerges as the first monolayer of ohmic contacts, which eventually affects interface electronic structure. Such trapped carbon was previously studied in both other interfacial systems theoretically by DFT (Ref. 83) and the TiNi ohmic contacts on 4H-SiC experimentally by Auger electron spectroscopy.³¹ It was proposed that the carbon could be segregated to the interfacial area, strengthening interface substantially and reducing the Schottky barrier dramatically.^{83,87} Further, it was reported that the ohmic contact can be realized by depositing carbon films only onto the SiC substrate, indicative of the determinative role of carbon in the ohmic contact formation.⁹⁹ The important role played by carbon in our study can be traced to the two interfacial Si layers, which provide possible sites for carbon segregation due to the strong Si-C interaction. However, direct imaging of the trapped carbon is still difficult in present study and further characterization requires the high-voltage EM and/or other advanced microscopic techniques.^{100,101}

Several experimental methods can be used to probe the ohmic character of Ti_3SiC_2 contacts on SiC discussed in this paper. For example, based on our results regarding the morphology of grown layers, epitaxial Ti_3SiC_2 layers can be deposited directly onto the SiC substrate by means of sputtering, molecular-beam epitaxy (MBE), or pulsed-laser deposition (PLD). In particular, the crucial effect of interfacial carbon can be possibly examined using the MBE and PLD techniques, which allow layer-by-layer deposition of crystalline thin films.^{102,103} If the outcome of such investigations is positive for ohmic contact formation, direct deposition of epitaxial Ti_3SiC_2 thin films rather than the metals would be a potential processing technique for easier realization of ordered structure and better control of ohmic property.

To summarize, we have determined atomic-scale structure of ohmic contacts on SiC and related it to electronic structure and electric property, aimed at understanding the formation mechanism of ohmic contact in TiAl-based system. The combined HAADF-DFT study we performed represents an important advance for relating structure to device property at atomic scale and is not limited to the contacts in SiC electronics. Our results show that the main product generated by chemical reaction can be epitaxial and have atomic bonds to the substrate. The contact interface, which could trap an atomic laver of carbon, enables lowered Schottky barrier due to the large interfacial dipole shift associated with the considerable charge transfer. These findings are relevant for technological improvement of contacts in SiC devices, and this paper presents an important step toward addressing the current contact issues in wide-band-gap electronics.

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