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Geometric ferroelectricity in rare-earth compounds $RGa_3$ and $RInO_3$

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We have studied the stability and ferroelectric properties of hexagonal $RGa_3$ and $RInO_3$ ($R$: rare-earth elements) by first-principles calculations. Computed spontaneous polarization in the series shows a systematic increase with the rare-earth elements, with values being larger in $RInO_3$ than in the corresponding $RGa_3$. The largest polarization found is about 10 $\mu$C/cm$^2$ for ErInO$_3$, which is about twice as large as those observed in hexagonal RMnO$_3$. The polarization can be further increased by applying in-plane compressive stress. The Born effective charges of constituent ions in the compounds are found to be similar to their formal values, implying that the ferroelectric displacements are merely driven by the ionic size effect. A transition to the high-symmetry phase at around 1500 K was confirmed in GdInO$_3$ and DyInO$_3$ in situ high-temperature powder x-ray diffractometry. The present systems should belong to the family of geometric ferroelectrics.

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I. INTRODUCTION

A group of compounds with the hexagonal LuMnO$_3$-type structure has attracted much attention because YMnO$_3$ and RMnO$_3$ ($R$: rare-earth element) families show the multiferroic property, i.e., the coexistence of magnetic ordering and ferroelectricity.1–14 Although most studies in this field have focused on the correlation of magnetism and the dielectric property, the mechanism of ferroelectricity in such compounds is also interesting. First-principles calculations of YMnO$_3$ revealed that neither Y nor Mn shows anomalous dynamical charges associated with the atomic displacements that are typically found in conventional ferroelectric compounds.2 Ferroelectricity in this compound was therefore attributed to the noncentrosymmetric atomic arrangement of the crystal caused merely by the ionic size effect, which is referred to as “geometric ferroelectricity.”2,3 Many of conventional ferroelectrics contain active cations such as Ti$^{4+}$, Nb$^{5+}$, and Ta$^{5+}$ (so-called $d^0$ ions) or Pb$^{2+}$ and Bi$^{3+}$ (so-called $s^2$ lone-pair ions). Chemical bondings between these cations and neighboring anions play important roles in these ferroelectrics.2,15 The mechanism will hereafter be called the chemical bonding effect. Since the geometric ferroelectricity does not rely on special kinds of cations, an exploration of the geometric ferroelectrics should broaden research frontiers of ferroelectric materials. At the moment, however, both a systematic understanding of the nature of geometric ferroelectricity and a clear strategy for enhancing their properties are lacking. Values of the spontaneous polarization of the rare-earth manganites have been reported to be around 5–6 $\mu$C/cm$^2$.10 However, one cannot find a clear trend in the variation of the ferroelectric properties of the compounds—spontaneous polarizations and ferroelectric Curie temperatures—in relation to the rare-earth elements. Furthermore, the idea of the geometric ferroelectricity in the compound has recently been still controversial.14

In the present study, we focus on a series of $RGa_3$ and $RInO_3$ compounds having the hexagonal structure. The synthesis of some $RGa_3$ was reported in the mid-1970s.17 The compounds were found to be isostructural to LuMnO$_3$ with the space group of $P6_3/mcm$. The synthesis of hexagonal $RInO_3$ compounds was reported in the early 1960s.18 Later, they were confirmed to show the LuMnO$_3$-type structure.19 The replacement of Mn by Ga, being almost the same in their ionic sizes, should provide an ideal material for the examination of the geometric effect on the structure of these systems, as magnetic or other electronic effects on crystal chemistry are eliminated. In fact, studies on the $Y(Mn,Ga)O_3$ system showed that Ga substitution causes only small changes in the crystal structure or the ferroelectric Curie temperature of the compound.12,13 Studies of the $RInO_3$ system should reveal the effects of oversized ions at the Mn site of the structure. Although possible ferroelectricity in $RGa_3$ and $RInO_3$ has been suggested in earlier reports,20,21 there have been no quantitative predictions or experimental confirmations made on their ferroelectric properties. In the present study, the structural and ferroelectric properties of these compounds are investigated by first-principles calculations, followed by experimental confirmation of the phase-transition behavior in GdInO$_3$ and DyInO$_3$.

II. METHODS

A. Computational method

First-principles total-energy calculations on the compounds were performed by a plane-wave basis projector augmented wave (PAW) method22 using the VASP code.23,24 The exchange and correlation effects were treated by the generalized gradient approximation (GGA).25 In the potentials for lanthanide elements $f$ electrons are kept frozen in the core. The $k$ mesh was sampled according to the Monkhorst-Pack scheme26 with a spacing of 0.3 Å$^{-1}$. The cutoff energy in the plane-wave expansion was 500 eV. The convergence of relative energies with respect to the mesh size and energy cutoff was found to be better than 1 meV/atom. Structure optimi-
zations were performed allowing the relaxation of the unit-cell volume, cell dimensions, and fractional positions. The effect of in-plane compression in the hexagonal phase was calculated by imposing the constraint of a fixed lattice constant \( a \). \( c \)-axis length at the condition was determined by calculating cells with several values of \( c \) length to draw energy versus \( c \)-length curve, obtaining the equilibrium value from the energy minima. The optimization of fractional positions was then performed with the fixed cell dimensions.

B. Sample preparation and x-ray diffraction measurements

Polycrystalline samples of GdInO\(_3\) and DyInO\(_3\) were synthesized by reacting an equimolar mixture of \( \text{In}_2\text{O}_3 \) (Kojundo Chemical Laboratory, 99.99%) and \( \text{Gd}_2\text{O}_3 \) or \( \text{Dy}_2\text{O}_3 \) (Rare Metallic, 99.9%) powders in air, respectively. Powders of these starting materials were mixed and ground in ethanol using a planetary ball mill (Fritsch P-7). Then the mixture was dried up, isostatically pressed into a pellet at 100 MPa, and sintered in air at 1623 K for 6 h. The compound thus prepared was examined by powder x-ray diffractometry and found to have a single phase of the desired hexagonal structure. Diffraction lines at room temperature were indexed by the hexagonal structure with the space group \( \text{P}6_{3}/\text{mmc} \). Lattice constants of GdInO\(_3\) and DyInO\(_3\) at room temperature were determined to be \( a=6.3462(1) \text{ Å}, \ c=12.3305(2) \text{ Å} \) and \( a=6.2915(1) \text{ Å}, \ c=12.2885(2) \text{ Å} \), respectively. High-temperature in situ measurements of powder x-ray diffraction were carried out up to 1573 K in air using Rigaku RINT-Ultima III with SHT1500 high-temperature attachment.

III. RESULTS AND DISCUSSION

A. Theoretical results for phase stability and spontaneous polarization

First we examine the relative stability of the hexagonal phase in these compounds against its competing phase of the perovskite structure. The existence of the hexagonal phase with the \( \text{P}6_{3}/\text{cm} \) space group has been reported for some \( \text{RGaO}_3 \) and \( \text{RInO}_3 \).\(^{17,19}\) In these compounds, the hexagonal phase has been considered to compete with the perovskite phase.\(^{27}\) Indeed, the occurrence of both phases has been reported in \( \text{RGaO}_3 \) and \( \text{RInO}_3 \).\(^{17,19,28-31}\) In gallates, the orthorhombic perovskite phase (space group \( \text{Pnma} \), \( \text{GdFeO}_3\)-type structure) was obtained with rare-earth elements from La to Er,\(^{28-31}\) whereas the hexagonal phase was also reported with some late rare earths (\( \text{R} = \text{Ho}, \text{Er}, \text{and Y} \)).\(^{17}\) For indates, the perovskite phase was obtained with early rare earths of La, Nd, and Sm.\(^{31,32}\) The hexagonal phase was observed in middle to late rare-earth indates of \( \text{R} = \text{Gd}, \text{Tb}, \text{Dy}, \text{and Ho} \).\(^{19}\) In ErInO\(_3\), a cubic solid solution with the bixbyite structure was obtained.\(^{19}\) On the whole, the hexagonal phase tends to be more stable than the perovskite phase in compounds with late rare earths, with a larger structural window in the indates series.

We have performed a series of total-energy calculations to investigate the relative stabilities of the perovskite and hexagonal phases. For the hexagonal phases, we considered a hypothetical high-symmetry phase with the space group of \( \text{P}6_{3}/\text{mmc} \) in addition to the low-symmetry ferroelectric phase. The symmetry can be lower from the \( \text{P}6_{3}/\text{mmc} \) to the \( \text{P}6_{3}/\text{cm} \) phase in the hexagonal structure by tilting the \( \text{BO}_5 \) bipyramids and buckling the \( \text{R} \) layers, as depicted in Fig. 1. The calculation results of relative energies of different phases are presented in Fig. 2. The energy of the cubic perovskite phase [space group \( \text{Pm}3\text{\(\text{m} \)}} \) is taken to be 0 eV as a reference. We can see that in \( \text{RGaO}_3 \) with early rare earths (\( \text{R} = \text{Nd} \) and Sm), the perovskite phase has a lower energy than the hexagonal phase. In \( \text{GdGaO}_3 \), the energies of the perovskite and hexagonal phases become almost the same, implying competing stability. As for gallates with later rare earths (Dy, Er), the hexagonal phase has a lower energy than the perovskite phase. On the other hand, in \( \text{RInO}_3 \), the hexagonal phase has a lower energy than the perovskite throughout the rare-earth series. The energy difference between the perovskite and the hexagonal phase becomes larger with the atomic number of rare-earth elements, indicating an increasing preference of the hexagonal phase over the perovskite counterpart. These calculated results are consistent with the experimentally observed tendencies of the phase stabilities in \( \text{RGaO}_3 \) and \( \text{RInO}_3 \).

**FIG. 1.** (Color online) Schematic view of crystal structures of \( \text{RGaO}_3 \) and \( \text{RInO}_3 \) in the hexagonal structure. (a) High-symmetry (\( \text{P}6_{3}/\text{mmc} \)) phase. (b) Low-symmetry (\( \text{P}6_{3}/\text{cm} \)) phase.

**FIG. 2.** (Color online) Relative energies of the different structures in the rare-earth compounds (a) \( \text{RGaO}_3 \) and (b) \( \text{RInO}_3 \). The energy of the cubic perovskite phase is taken to be 0 eV as a reference. The energies of orthorhombic perovskite (\( \text{Pnma} \)) and high-symmetry (\( \text{P}6_{3}/\text{mmc} \)) and low-symmetry (\( \text{P}6_{3}/\text{cm} \)) hexagonal phases are indicated by circles, diamonds, and squares, respectively.
Within the hexagonal structures, the low-symmetry $P6_3/cm$ phase always has lower energy than the high-symmetry $P6_3/mmc$ phase. The difference in the energy between $P6_3/mmc$ and $P6_3/cm$ phases becomes larger with an increase in the atomic number of the rare-earth elements, as shown in Fig. 3. A larger energy difference is found in the indates than in the corresponding gallates. The energy difference between the high- and low-symmetry phases in ErInO$_3$ is about 1650 K. The value is much higher than the corresponding energy difference of 150 K in BaTiO$_3$ (between the cubic and the tetragonal structure).\(^2\) Although the energy difference at the ground states does not correspond to the transition temperature (because of neglecting the entropy contribution), the results may suggest that the ferroelectric Curie temperature or coercive field in the present system is much higher than those of BaTiO$_3$.

From the theoretically obtained crystal structures, one can evaluate the spontaneous polarization using displacements between the centrosymmetric and the noncentrosymmetric structures and ionic charges of constituents. Constituent ions are assumed to have either formal charges or Born effective charges. Calculated values of spontaneous polarizations for the series of compounds are shown in Fig. 4. The formal charges are taken as +3 for $R$, Ga, and In, and −2 for O, respectively. Born effective charges were calculated in the present study by Berry’s phase approach.\(^3,4\) We found that the Born effective charges are close to the formal values and they bring about no significant enhancement in the spontaneous polarization, as in the previously reported case of YMnO$_3$.\(^2,35\) This contrasts with the behavior of conventional ferroelectrics, such as BaTiO$_3$, where the Born effective charges are much larger than the formal charges.\(^36,37\) The ferroelectricity in RGaO$_3$ and RInO$_3$ can therefore be attributed to the noncentrosymmetric atomic arrangement driven by the geometric effect (or the ionic size effect) rather than the chemical bonding effect. The present system should be included in the family of geometric ferroelectrics.

In Fig. 4, a trend similar to that observed in the energy difference (Fig. 3) can be found in the change in the spontaneous polarization across the rare-earth gallates and indates. For the early RGaO$_3$ ($R$=Nd and Sm), the obtained values range from 5 to 6 $\mu$C/cm$^2$, which are close to the experimental values of hexagonal YMnO$_3$ and RMnO$_3$ reported previously.\(^16\) Although experimentally reported values of the spontaneous polarization of RMnO$_3$ show no clear trend relative to the rare-earth elements,\(^16\) the present calculated values of polarization show a systematic increase with the atomic number of rare-earth elements. The present results are reasonable if one recalls that the ferroelectricity in these compounds is brought about by a purely geometric effect. Rare-earth indates show larger polarization than the corresponding gallates. The maximum polarization of 10.0 $\mu$C/cm$^2$ is found in ErInO$_3$. This value for ErInO$_3$ is about twice as large as the experimentally observed value of YMnO$_3$. Previous analysis on YMnO$_3$ suggested that the dominant components of the structural distortion come from the out-of-plane (c-axis direction) displacements of the equatorial oxygen ions of MnO$_5$ bipyramid.\(^2\) The decrease in $R$ ion radius or increase in Ga/In site size makes the relatively small separation between Ga/In ions and equatorial oxygen ions more closer. This makes the equatorial oxygen ions feel more compressed by Ga/In ions within the c plane. The oxygen ions are therefore pushed away from the plane more strongly, resulting in larger displacements along c direction. Larger structural distortions should lead to larger polarizations or higher transition temperatures in the compounds.

Since the spontaneous polarization in these compounds occurs along the c axis of the crystal, one can expect that the application of the compressive stress within the ab plane or the elongation of the cell along the c axis will enhance their electric-dipole moment and therefore the spontaneous polarization. We investigate the effect of in-plane stress on the spontaneous polarization of these compounds. Compression was introduced to ErInO$_3$ by reducing the cell dimension $a$ by −4%, 2%, 4%, 6%, or 8% from its equilibrium value. Such in-plane compression causes cell elongation along the c-axis direction. The dependence of the spontaneous polarization of ErInO$_3$ on the in-plane compression is depicted in Fig. 5. We can see that the in-plane compression enhances spontaneous polarization in the compound. An increase of about 80% in the polarization is achieved with an 8% reduc-

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**FIG. 3.** Energy difference between the high-symmetry and low-symmetry hexagonal phases in (a) RGaO$_3$ and (b) RInO$_3$. The difference is obtained by subtracting the energy of the low-symmetry ($P6_3/cm$) phase from that of the high-symmetry ($P6_3/mmc$) phase.

**FIG. 4.** (Color online) Calculated spontaneous polarizations of hexagonal (a) RGaO$_3$ and (b) RInO$_3$. Squares and circles show values calculated using formal charges and Born effective charges, respectively.

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1. The Born effective charges are much larger than the formal charges.\(^36,37\) The ferroelectricity in RGaO$_3$ and RInO$_3$ can therefore be attributed to the noncentrosymmetric atomic arrangement driven by the geometric effect (or the ionic size effect) rather than the chemical bonding effect. The present system should be included in the family of geometric ferroelectrics.

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3. Since the spontaneous polarization in these compounds occurs along the c axis of the crystal, one can expect that the application of the compressive stress within the ab plane or the elongation of the cell along the c axis will enhance their electric-dipole moment and therefore the spontaneous polarization. We investigate the effect of in-plane stress on the spontaneous polarization of these compounds. Compression was introduced to ErInO$_3$ by reducing the cell dimension $a$ by −4%, 2%, 4%, 6%, or 8% from its equilibrium value. Such in-plane compression causes cell elongation along the c-axis direction. The dependence of the spontaneous polarization of ErInO$_3$ on the in-plane compression is depicted in Fig. 5. We can see that the in-plane compression enhances spontaneous polarization in the compound. An increase of about 80% in the polarization is achieved with an 8% reduc-
tion of the cell dimension $a$. The polarization under this condition reaches about 18 $\mu$C/cm$^2$, which is 3 times as large as those of uncompressed YMnO$_3$ and RMnO$_3$ families. This is the largest among the geometric ferroelectrics reported so far. These enhancements of the polarization may be attained by the physical pressure effect caused by the constraint from the substrate in epitaxially grown thin films or by the chemical pressure effect caused by doping or alloying with other materials of different ionic sizes of the constituents. The strategy applied to increase the polarization of ErInO$_3$ should be relevant to the control of the structural and ferroelectric properties of the other rare-earth gallates, indates, and manganites with the hexagonal LuMnO$_3$-type structure.

B. Experimental phase transition

In order to confirm the occurrence of the low-symmetry (ferroelectric) to high-symmetry (paraelectric) phase transition experimentally, we have synthesized polycrystalline samples of compounds with the hexagonal structure and performed in situ measurements of powder x-ray diffraction at elevated temperatures. Among these $R$GaO$_3$ and $R$InO$_3$, the desired hexagonal phase was successfully obtained for GdInO$_3$ and DyInO$_3$. Attempts to synthesize late rare-earth gallates and early rare-earth indates under the same process conditions result in different phases other than the hexagonal structure. From our calculations, large polarization and high transition temperature close to the maximum value among these gallates and indates are expected in GdInO$_3$ and DyInO$_3$.

The powder x-ray diffraction patterns of these two compounds recorded at room temperature and at elevated temperatures are shown in Fig. 6. A peak observed at around $33.0^\circ -33.5^\circ$ (marked with filled circles) corresponds to the superlattice reflection in the low-symmetry $P6_3cm$ phase, which disappeared in the high-symmetry $P6_3/mmc$ phase. It is noted that the intensity of the superlattice reflection decreases with increasing temperature. The superlattice reflection disappears in both compounds in the diffraction patterns recorded at 1573 K. This suggests that the transition from the low-symmetry to the high-symmetry phase occurs at around this temperature. The transition temperature found here is the highest among the known isostructural $RMO_3$ families.$^{16,21}$

We see new small peaks appearing in the patterns at 1573 K. The peaks marked with squares, triangle, and diamond are assigned to In$_2$O$_3$, Gd$_2$O$_3$, and Dy$_2$O$_3$, respectively. All of these have the C-type rare-earth oxide (or the bixbyite-type) structure. They are probably products of the decomposition of the samples upon heating, indicating a limited stability of these hexagonal compounds at high temperatures in air. Similar sample decomposition to the present case has also been observed in the hexagonal manganites of YMnO$_3$ (Refs. 39 and 40) and LuMnO$_3$.10

To summarize the experimental part, we have synthesized the hexagonal ferroelectric phase of GdInO$_3$ and DyInO$_3$ and confirmed the phase transition to the high-symmetry phase at around 1500 K. At the present moment, we are unable to synthesize the hexagonal phases in other $R$GaO$_3$ and $R$InO$_3$ compounds. Annealing the samples in air at above 1500 K induces the phase decomposition of GdInO$_3$ and DyInO$_3$. By optimizing the process conditions, we may be able to observe the phase transition more clearly in a wider range of $R$GaO$_3$ and $R$InO$_3$ compounds. On the basis of the present theoretical calculations, lower ferroelectric Curie temperature and, therefore, a smaller barrier for polarization reversal can be expected in early $R$GaO$_3$ and $R$InO$_3$. Ferroelectrics for practical uses should show reversible polarization upon applying external electric field near room temperature. This may be achieved in early $R$GaO$_3$ if the hexagonal structure can be synthesized. This may be accomplished in the form of thin films, as in the case of some $R$MnO$_3$.41,42 where the metastable hexagonal phases are difficult to obtain in the form of bulk materials. Then, the in-plane compressive stress can be applied by selecting an optimum substrate for increasing the spontaneous polarization.

IV. CONCLUSION

The stability and ferroelectric properties of a series of $R$GaO$_3$ and $R$InO$_3$ were investigated by first-principles calculations. The computed spontaneous polarization increased with increasing atomic number of rare-earth elements. $R$InO$_3$ showed larger polarization than the corresponding $R$GaO$_3$. The largest polarization found in this study was about
10 μC/cm² for ErInO₃, which is about twice as large as experimentally reported values of YMnO₃ and RMnO₃ families. Applying in-plane compressive stress was found to increase the polarization up to about 18 μC/cm² in ErInO₃, indicating the enhancement of the polarization by a factor of about 3 relative to that of uncompressed YMnO₃. The Born effective charges of constituent ions in RGaO₃ and RlnO₃ were found to be similar to the formal charges. This implies that the origin of ferroelectricity in these compounds is different from that of conventional ferroelectrics such as BaTiO₃ in which the anomalous dynamic charge has been pointed out. The ferroelectricity can therefore be attributed to the noncentrosymmetric atomic arrangement of the crystal that is driven by the geometric effect rather than the chemical bonding effect. The present systems should belong to the family of geometric ferroelectrics. Finally, a transition from the low-symmetry to the high-symmetry phase was confirmed in GdlnO₃ and DylnO₃ by in situ high-temperature powder x-ray diffractometry. The transition temperature was found to be at around 1500 K, which is the highest among the known isostructural RMO₃ compounds. These findings should provide a clue to the control of the structural and ferroelectric properties in this class of materials.

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[35] As a typical example, calculated values of Born effective charges in hexagonal ErInO₃ are Er: +3.35, In: +3.34, Otop: −2.46, and Oeq: −1.77, respectively.


