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Ab initio study of ferroelectric closure domains in ultrathin PbTiO$_3$ films

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Ab initio density-functional theory calculations within the local density approximation were conducted to elucidate whether critical thickness for ferroelectricity intrinsically exists in free-standing polydomain PbTiO$_3$ ultrathin films, where there was no screening effect of electrodes. The ferroelectric polydomain state was found to be energetically favorable over the paraelectric state even in the thinnest film one unit-cell thick, indicating no intrinsic critical thickness existed. The ferroelectric distortions in the film were stabilized by the formation of ferromagnetic-like closure domains, because the surface charge, which caused a depolarizing field, was sufficiently screened by the in-plane aligned polarization at the surface. Further analysis of the covalent Pb-O bonding structure, which plays a central role in determining ferroelectricity in PbTiO$_3$, revealed that the closure domain structure consists of the 180° as well as 90° domain walls.

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I. INTRODUCTION

Ferroelectric ultrathin films have drawn considerable attention because of their technological applications, e.g., nonvolatile ferroelectric random access memory, transducers and electromechanical devices.1,2 Although these devices have so far employed films thicker than 100 nm under technological development, both the increasing demand for the miniaturization of devices and scientific interest in nanoscale ferroelectrics drives the investigation of fundamental ferroelectric properties in extremely thinner films of several atomic layers.

Ferroelectricity, which originates from the delicate balance between short-range covalent and long-range Coulomb interactions,3,4 is very sensitive to the size of materials (ferroelectric correlation volume).5 The existence of a critical size, where ferroelectricity vanishes, was first predicted on the basis of the classical Landau theory.6,7 In particular, the critical thickness of ferroelectric ultrathin films is of central interest in this discussion. For a ferroelectric thin film with a polar axis perpendicular to its surface, the termination of polarization at the surface or interface gives rise to surface charges. These surface charges create a depolarizing field that destabilizes the ferroelectric distortions.8,9 Two distinct ways to compensate for surface charges have traditionally been proposed: (i) screening by electrodes that accumulate surface charge at their interface8 and (ii) partitioning the system into domains.10,11

In mechanism (i), theoretical studies12–15 based on ab initio density-functional theory (DFT) (Refs. 16 and 17) calculations have already been done for various ferroelectric ultrathin capacitors, with various combinations of ferroelectrics (BaTiO$_3$ and PbTiO$_3$) and electrodes (Pt and SrRuO$_3$). These studies revealed that, in a single-domain configuration, a critical thickness for ferroelectricity still exists, ranging from two to six unit cells depending on the choice of electrodes due to their different conductive behavior, chemical nature, and constraint of atomic displacement at the interface. Below the critical thickness, the system becomes paraelectric because of the insufficiency of screening by the electrodes. In recent years, Aguado-Puente and Junquera,18 however, showed that the ferroelectric distortions in SrRuO$_3$/BaTiO$_3$/SrRuO$_3$ capacitors can be stabilized by breaking up the system into domains even below the critical thickness [mechanism (i) incorporated with (ii)].

In mechanism (ii), Fong et al.,11 experimentally showed that ferroelectricity is sustained in the PbTiO$_3$ film as thin as three unit-cell thick, which were epitaxially grown on an insulating SrTiO$_3$ substrate by forming 180° stripe domains. However, the critical thickness is expected to depend on the choice of substrate due to the different degree of constraint of displacement at the interface. To fundamentally understand the intrinsic critical thickness for ferroelectricity under mechanism (ii), it is essential to theoretically investigate a free-standing film, which is free from any substrate constraints.

In this paper, we investigated whether the critical thickness for ferroelectricity intrinsically exists in free-standing polydomain ultrathin PbTiO$_3$ films using ab initio density-functional theory calculations. In addition, the detailed ferroelectric domain structure of the ultrathin films was investigated from atomic and electronic points of view. The mechanism of stabilization of ferroelectricity in the ultrathin films is discussed, as well.

II. COMPUTATIONAL DETAILS

A. Simulation method

Ab initio (first-principles) calculations based on the density functional theory16,17 were conducted using the Vienna ab initio simulation package code.19,20 The electronic wave functions were expanded in plane-waves up to a cut-off energy of 500 eV. The electron-ion interaction was described by the projector augmented wave (PAW) potentials.21,22 which explicitly included the Pb 5$d$, 6$s$, and 6$p$, the Ti 3$s$, 3$p$, 3$d$, and 4$s$, and the O 2$s$ and 2$p$ electrons in the valence states. The use of PAW potentials is essential for the computational efficiency as well as the accuracy of the all-electron scheme that avoids the problems due to the linearization of the core-valence exchange interaction. To evaluate the exchange-correlation energy, we employed the local density

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approximation of the Ceperley-Alder form, which successfully yielded the structural and ferroelectric ground-state of PbTiO$_3$.  

B. Simulation models and procedure

In this study, we investigate the free-standing polydomain PbTiO$_3$ ultrathin films with upward and downward spontaneous polarizations normal to the (001) surfaces. Figure 1 shows the simulation model of a three unit-cell thick (m = 3) film with a domain period of six unit cells ($N_z = 6$), where $m$ and $N_z$ denote the number of perovskite unit cells in the film thickness and the domain period, respectively. The models with a thickness of less than or equal to three unit cells ($m \leq 3$) were simulated in this study because the existence of a polydomain ferroelectric phase has already been observed experimentally in thicker films. To study the ferroelectric stability with respect to the domain period, the models with different $N_z$ were considered, as well. The TiO$_2$ termination was selected for the (001) surfaces of films because the termination is energetically favorable compared to another choice of the PbO termination. Twinning on both the TiO$_2$ (Ti centered) and PbO (Pb centered) (010) planes was considered for the 180° domain wall (see Figs. 1(a) and 1(b), respectively). Since the three-dimensional periodic boundary condition was applied in the plane-wave pseudopotential calculations, a vacuum region of $l_z = 20$ Å was introduced in the $z$ direction so that undesirable interactions from the neighboring films were sufficiently avoided. Thus, the simulation supercells.

FIG. 1. (Color online) Simulation models of the free-standing PbTiO$_3$ ultrathin film with the TiO$_2$-terminated (001) surfaces for the (a) Ti-centered and (b) Pb-centered 180° domain wall (DW) configurations. Spontaneous polarization, $P_s$, is initially set along the +$z$ and −$z$ directions on the right and left sides of the film, respectively. $N_z$ and $m$ denote the number of perovskite unit cells for the domain period and the thickness of film, respectively. The model shown here is $N_z = 6$ and $m = 3$. The solid boxes represent the simulation supercells.

FIG. 2. (Color online) Total energy difference between the ferroelectric polydomain and paraelectric phases as a function of the domain period, $N_z$, for the (a) $m = 3$, (b) $m = 2$, and (c) $m = 1$ unit-cell thick films with the TiO$_2$-terminated (001) surfaces. Full symbols indicate the minimum for each film thickness.
agrees with experimentally observed 180° stripe domain patterns of $N_z=6$ in a PbTiO$_3$ thin film of the same thickness ($m=3$) grown on SrTiO$_3$, which supports the reliability of our DFT calculations.

For thinner films of $m=2$ and 1, the Pb-centered domain with a period of $N_z=4$ and the Ti-centered domain with an $N_z=2$ configuration, respectively, are energetically favored over the paraelectric state. It should be noted that the ferroelectric single-domain free-standing film was energetically unstable because of the existence of nontrivial depolarizing field, which brings the system back to a paraelectric configuration. This suggests that the depolarizing field in the films can be sufficiently cancelled out only by the formation of domains, even in the thinnest, one unit-cell thick ($m=1$) film, without any screening effect of electrodes. Therefore, no intrinsic critical thickness for ferroelectricity exists in free-standing ultrathin films.

We briefly mention that as the film thickness decreased ($m=3$, 2, and 1, respectively), the stable domain period became shorter ($N_z=6$, 4, and 2, respectively). This trend corresponds well with the experimentally observed relationship between film thickness and domain period in thicker films.

B. Polarization distribution in polydomain PbTiO$_3$ films

The detailed ferroelectric domain structure in the ultrathin PbTiO$_3$ film is now investigated by introducing a site-by-site local polarization, $\mathbf{P}$, which can be evaluated by

$$
\mathbf{P} = \frac{e}{\Omega_z} \sum_j w_j \mathbf{Z}_j^* \mathbf{u}_j,
$$

where $\Omega_z$, $e$, and $\mathbf{u}_j$ denote the volume of the unit cell, the electron charge and the atomic displacement vector from the ideal lattice site of atom $j$, respectively. Index $j$ covers all atoms in the unit cell. $\mathbf{Z}_j^*$ is the Born effective charge tensor of cubic bulk PbTiO$_3$. In this study, we employed the theoretical values of the Born effective charge tensors calculated by Zhong et al. The local polarization was evaluated for each Ti-edged unit cell in the film shown as dashed lines in Fig. 1. Weights were set to $w_{\text{pb}}=1$, $w_{\text{ti}}=1/8$, and $w_{\text{o}}=1/4$, which correspond to the number of unit cells sharing the atom. Note that this evaluation was previously validated and has been applied to the nanostructures such as 90° domain walls and nanowires.

Figure 3 shows the local polarization distribution in a three unit-cell thick film ($m=3$) of a stable Ti-centered domain having a period of $N_z=6$. Remarkably, a nontrivial in-plane polarization (in the $x$ direction) was found near the junction between the surface and domain wall set initially [see red-colored values in Fig. 3(a)]. As a consequence, a closure domain structure, where polarization direction was aligned to form a closed flux, was formed in the film [see Fig. 3(b)]. Note that such closure domains were also formed in the thinner films of $m=2$ and 1, as well. The closure domains were first proposed in ferromagnetic systems by Landau and Lifshitz, and Kittel. In recent years, however, Aguado-Puente and Junquera have theoretically proven the existence of closure domains in ultrathin SrRuO$_3$/BaTiO$_3$/SrRuO$_3$ ferroelectric capacitors. In our model, the closure domain structure seems to consist of not only the 180° domain wall but also the 90° domain wall as Kittel proposed, which can clearly be seen in the vector field of the polarization distribution [see also Fig. 3(c) for a schematic illustration]. This will be discussed later, in terms of the covalent Pb-O bonding structure in the film. The formation of closure domains can considerably reduce the depolarizing field with respect to only the 180° domain wall configuration, because the in-plane polarization at the surface does not produce any surface charges. Thus, more effective screening of the depolarizing field was realized by the formation of closure domains, which stabilized ferroelectric distortions in the ultrathin films.

On the other hand, the spontaneous polarization was along the normal $z$ direction to the surface at the center of the domains, where there were two distinct cases of spontaneous polarization directed toward the (i) outside of the film, $P_z^\text{f}$, and (ii) inside of the film, $P_z^\text{i}$ [see also Fig. 3(b) for the location]. The magnitude of polarizations, $P_z^\text{f}$ and $P_z^\text{i}$, was reduced by about 55 % and 25 %, respectively, with respect to that of the bulk. This indicates that the presence of the surface suppressed the ferroelectricity. To be more precise,
we additionally introduced a layer-by-layer ferroelectric distortion, \( \delta_{\text{cation}} \), where \( \bar{z} \) denotes the planar-averaged atomic position. Table I lists layer-by-layer ferroelectric distortions, \( \delta \), for the (001) planes of both the cells, \( P_1 \) and \( P_1 \), shown in Fig. 3(b). Here, the topmost surface, second, and third layers are numbered 1, 2, and 3, respectively. The results of a previous DFT study\(^{34} \) of a free-standing single-domain PbTiO\(_3\) film five unit-cell thick, in which the center layers of the film were artificially fixed at the bulk state, are also shown for comparison. Overall, our result agrees reasonably well with the previous study of the single-domain film. For the case of \( P_1 \), \( \delta \) was reduced by 40\%–50\% from the bulk value on both the TiO\(_2\) and PbO layers. On the other hand, stronger suppression was found for \( P_1 \), especially, in the TiO\(_2\) layers. In addition, the topmost surface TiO\(_2\) layer exhibited a negative value of \( \delta \), suggesting that the surface relaxation led to an atomic shift in the direction opposite to the ferroelectric distortions of the bulk. Such an opposing shift of the surface TiO\(_2\) layer results in a strong suppression of ferroelectricity for \( P_1 \).

C. Atomic and electronic structure of closure domains in ultrathin PbTiO\(_3\) films

Figure 4 shows the atomic displacement from the paraelectric state in a three unit-cell thick film (\( m=3 \)) of a stable Ti-centered domain having a period of \( N_x=6 \). The displacement of atoms forms a closure-type flux across the domain wall. This displacement pattern corresponds well to the polarization orientation of closure domains described in the previous section. A similar closed-flux displacement pattern was observed in the thinner films with \( m=2 \) and 1. Remarkably, in-plane (the \( x \) direction) atomic displacement was found in the first and second surface layers of the film, which aligned the polarization parallel to the surface. In other words, the in-plane displacement played a significant role in the formation of closure domains, which stabilized the ferroelectric state in the film. In fact, the system turns back to the paraelectric state when the in-plane relaxation was neglected by constraining the \( x \) component of atomic coordinates. The displacement of closed flux was also observed in SrRuO\(_3\)/BaTiO\(_3\)/SrRuO\(_3\) ferroelectric capacitors,\(^{18} \) when a closure domain was formed. It should be noted that only the displacement of Ti atoms was dominant in the SrRuO\(_3\)/BaTiO\(_3\)/SrRuO\(_3\) capacitors, while the displacement of Pb atoms is much more active in the ultrathin PbTiO\(_3\) film. This difference originates from the bonding nature of PbTiO\(_3\) and BaTiO\(_3\): the strong covalency of the Pb-O bond through the hybridization of the Pb 6s and O 2p orbitals plays a critical role in stabilizing large ferroelectric distortions in PbTiO\(_3\),\(^{35} \) while in BaTiO\(_3\) only the Ti-O bond is responsible for ferroelectricity because of the ionic Ba-O interaction.\(^{36} \) In fact, displacement of the Ba atom was inactive in SrRuO\(_3\)/BaTiO\(_3\)/SrRuO\(_3\) capacitors. In addition, the covalent Pb-O bond often characterizes ferroelectricity in nanostructured PbTiO\(_3\).\(^{29,31,35,37} \)

Figure 5 shows the atomic configuration and charge density distribution on the PbO (010) plane in a film three unit-cell thick (\( m=3 \)). Those of the isolated 180\(^\circ\) and 90\(^\circ\) domain walls are also shown for comparison. Here, the covalent Pb-O bonds of interest are emphasized by white lines. For the single-domain bulk with the polar axis of [001], the Pb-O bond formed a zigzag shape along the [100] direction. In the film, on the other hand, this zigzag bonding structure was terminated and switched to the inverse structure across the center of area A (see the white solid lines). This bonding sequence was characteristically similar to that of the 180\(^\circ\) domain wall, where the polarization direction changes from upward on one side to downward on the other. Meanwhile, a “\( \mathbb{0} \)”-type series of Pb-O bonds was found in the area B of

---

**TABLE I.** Layer-by-layer ferroelectric distortion, \( \delta \) (in Å), at the center of domain in a three unit-cell thick film (\( m=3 \)) with a stable period of \( N_x=6 \). In parenthesis are the ratios to the bulk value. The results of a previous study (Ref. 34) of a free-standing single-domain PbTiO\(_3\) film, in which the central layers were artificially fixed, are also shown for comparison. Cf. text.

<table>
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<tr>
<td></td>
<td>( P_1 )</td>
<td>( P_1 )</td>
</tr>
<tr>
<td>1 [TiO(_2)]</td>
<td>( -0.116 ) (−35%)</td>
<td>( -0.202 ) (61%)</td>
</tr>
<tr>
<td>2 [PbO]</td>
<td>( 0.366 ) (77%)</td>
<td>( -0.244 ) (51%)</td>
</tr>
<tr>
<td>3 [TiO(_2)]</td>
<td>( 0.133 ) (40%)</td>
<td>( -0.208 ) (63%)</td>
</tr>
<tr>
<td>Bulk [TiO(_2)]</td>
<td>( 0.333 )</td>
<td>( -0.333 )</td>
</tr>
<tr>
<td>Bulk [PbO]</td>
<td>( 0.476 )</td>
<td>( -0.476 )</td>
</tr>
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</table>

\(^a\)Reference 34.
the film, which corresponds well to the bonding sequence in the 90° domain wall (see the white solid lines). This indicates that the 180° and 90° domain walls were formed in the center of area A and in area B, respectively. Therefore, the closure domain structure in the PbTiO$_3$ film consists of both the 180° and 90° domain walls, as illustrated in Fig. 3(c).

**IV. CONCLUSION**

In this study, *ab initio* (first-principles) DFT calculations were performed to elucidate whether an intrinsic critical thickness for ferroelectricity exists in free-standing polydomain PbTiO$_3$ ultrathin films without any screening effect of electrodes. Moreover, the detailed ferroelectric domain structure of the ultrathin films was investigated from atomistic and electronic points of views to discuss the stabilization mechanism of the ferroelectric state in the films.

In a three unit-cell thick film ($m=3$), the ferroelectric polydomain state with the six unit-cell domain period ($N_x=6$) was found to be energetically favorable over the 180° stripe domain patterns. Further studies of the thinner films ($m=2$ and 1 unit-cell thick) revealed that the ferroelectric polydomain phase was also stabilized by the formation of domains with shorter periods of $N_x=4$ and 2, respectively. This suggests that no critical thickness for ferroelectricity exists in free-standing polydomain films.

Local polarization analysis determined that the polarization direction aligned as a closed flux in the film. This indicates that a ferromagnetic-like closure domain structure as first proposed by Kittel was formed. Remarkably, in-plane atomic displacement was found in the surface layer, which leads to a nontrivial in-plane polarization component. Since the in-plane polarization does not induce surface charges, which would create a depolarizing field, the formation of a closure domain plays a central role in stabilizing the ferroelectric polydomain state in ultrathin film.

The charge density distributions indicated that the closed-flux displacement of Pb atoms leads to reconstruction of the covalent Pb-O bonds in the film. The resulting bonding structures at the center of the film and at the surface were found to be characteristically similar to the 180° and 90° domain walls, respectively. This indicates that the closure domain structure consists of both the 180° and 90° domain walls.

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33 C. Kittel, Phys. Rev. 70, 965 (1946).


