

1 Short title: **Vascular bundles shape and relaxation properties of bamboo**

2

3

4 **Vascular bundle shape in cross-section and relaxation properties of Moso bamboo (*Phyllostachys***
5 ***pubescens*)**

6

7

8 **Eisuke Kanzawa¹, Shoko Aoyagi², Takato Nakano^{1,*}**

9

10

11 **Keywords: Bamboo, Vascular bundle, Image analysis, creep**

12

13

14 ¹ Laboratory of Biomaterials Design, Division of Forest and Biomaterials Science, Graduate School of
15 Agriculture, Kyoto University.

16 ² ASAHI WOODTECH COMPANY, Cyuuou-ku, Osaka, 541-0054, Japan

17 * Corresponding author; Laboratory of Biomaterials Design, Division of Forest and Biomaterials
18 Science, Graduate School of Agriculture, Kyoto University, Kita-Shirakawa, Kyoto, 606-8502 Japan.

19

20

21

22 **Abstract**

23 The variation in the longitudinal and radial direction of the R/T ratio and area ratio of vascular
24 bundles, which are cross-sectional image features of bamboo, and the relationships between the R/T
25 ratio or area ratio and relaxation behavior were investigated. These image features varied
26 characteristically in the longitudinal and radial direction. Relationships between these image features
27 and relaxation behavior was evaluated using the instantaneous creep compliance $\ln[J(0)]$ and the
28 creep intensity $\ln [J(3 \times 10^4) - J(0)]$. Although both instantaneous compliance and creep intensity
29 decreased as density increased, their dependence properties were remarkably different.
30 Instantaneous compliance was strongly correlated with R/T ratio and density, which was related to
31 the area ratio, whereas creep intensity was weakly correlated with density in a given range. The
32 results indicate a difference between the two relaxation properties, because creep intensity depends
33 more on microstructures, such as the conformation of molecular chains in the substance, or
34 interactions among cells than on R/T ratio and area ratio image features.

35

36

37 **Key words:** Bamboo; Vascular bundle; Shape factor; Cross-section; Creep

38

39 **1. Introduction**

40

41 Bamboo is an important forest biomass resource. However, the use of bamboo is limited to
42 handiwork in most cases, although it is sometimes used as a fill material in various composites.
43 Bamboo has characteristic structures and properties, which have been investigated in various
44 respects [1–7]. In recent years, bamboo has been studied for a variety of applications, including its use
45 as a biomimetic model.

46 The properties of bamboo originate from the composition and distribution of the vascular
47 bundles and parenchyma tissues, which are the main constituents of the central cylinder of the
48 internodes. The organizational structure of bamboo was reported in a review by Liese et al. [8–10].
49 Bundle sheaths, consisting of thick-walled fibrous cells with multilayered wall structures, surround
50 the vessels and sieve tubes of the vascular bundles. The bundle sheaths provide the vascular bundles
51 with rigidity by stretching continuously in the longitudinal direction of each internode. In contrast,
52 parenchyma tissues, which consist of thin-walled parenchyma cells, contribute little to the rigidity of
53 bamboo. Thus, the mechanical properties of bamboo depend on variation in the distribution and shape
54 of the cross-sections of the vascular bundles protected by bundle sheaths.

55 Nakato [11] divided the culm wall into four equal layers and examined one vascular bundle
56 cross-section in each layer. He found no clear relationship between the height from the ground of the
57 internodes and the ratio derived by dividing the maximum radius of a vascular bundle in the radial
58 direction by the maximum radius in the tangential direction and that the ratio decreased from the
59 outer to inner layers. However, to our knowledge, no reports have focused on the relationship between
60 the shape of vascular bundles and relaxation properties.

61 The mechanical properties of bamboo have been discussed in terms of tissue structures,
62 particularly the cross-sectional distribution of vascular bundles [12–23]. Although Low et al. [24]
63 mentioned the relaxation property, which is time dependent, they did not discuss its relationship to
64 organizational structure. Aoyagi and Nakano [23] investigated position dependence, which affects the
65 relationship between relaxation property and higher-order structures. They reported that Nutting's
66 equation could be applied to the creep property of Moso bamboo. However, the relaxation property has
67 not been discussed in relation to the shape of vascular bundles.

68 In this study, we analyzed variation in the distribution and shape of vascular bundles as well
69 as radial and longitudinal density of Moso bamboo. In addition, the effects of higher-order structures
70 on the creep property are discussed.

71

72

73 **2. Materials and methods**

74

75 *2.1 Materials*

76 We used samples from a 6-year-old Moso bamboo (*Phyllostachys pubescens*) collected in
77 Shimane, Japan. The bottommost internode was labeled internode 1, and the uppermost internode at
78 the top of the culm was labeled internode 27. Twenty-four internodes were used for the image analysis.
79 The epidermis and endodermis of specimens were removed. In the central cylinder, which made up
80 the rest of the culm, we designated the section nearest to the epidermis the outer layer and that next
81 to the endodermis the inner layer. Photographs of the cross-sections were used for the image analysis.
82 Samples cut to a given size were used for the creep test.

83

84 *2.2 Image analysis*

85 Internode cross-sections were observed with an incident-light microscope, and cross-sectional
86 images were captured using a CCD camera. The cross-sectional area used for the image analysis was
87 determined arbitrarily for each internode. The cross-sectional images were printed, and then the
88 outline of each vascular bundle was traced by hand onto paper and scanned into a computer. The
89 cross-sectional image was converted into a binary image by painting the inside of the vascular bundle
90 outlines. Thus, the shape, including the vessel interiors and sieve tubes, was analyzed.

91 The center of gravity, area, maximum length, maximum width, and angle of direction were
92 collected for all vascular bundles within each image. Maximum length was the maximum radius of
93 the culm. Maximum width was the maximum radius perpendicular to the direction of the maximum
94 length. Angle of direction (θ) was the angle between the line including the maximum length and
95 horizontal axis of the image ($0^\circ \leq \theta \leq 180^\circ$). For this work, the direction of the horizontal line was the
96 same as the tangential direction of the culm.

97 Vascular bundle shape was evaluated using the R/T ratio, which is the ratio of the radially
98 maximum length (R) to the tangentially maximum width (T) of a vascular bundle. Parts of vascular
99 bundles located at the edges of images were not evaluated. The area ratio of vascular bundles was
100 defined as the ratio of the total area of the vascular bundles divided by the entire area of analysis in a
101 cross-sectional image.

102

103 *2.3 Creep test*

104 Specimens for the creep test were taken from the same culm as that used for the image
105 analysis. A 100-mm-long rectangular specimen was cut from the central region of each internode and
106 was shaped into the dimension: $90 \times 1.5 \times 85$ (mm) in longitudinal, radial, tangential directions of
107 bamboo, respectively. The specimen was boiled for 30 min to release internal stress, then gradually
108 dried in air at room temperature for 1 week with further drying at 60°C under vacuum for 1 day

109 before the creep test. The specimen was wrapped in polyethylene film to keep moisture content
110 constant. There was little weight change before and after the creep test for each specimen.

111 Creep tests were conducted in cantilever bending at room temperature. The load was within
112 30% of the proportional limit of the load deformation diagram.

113

114

115 **3. Results and discussion**

116

117 *3.1 Fluctuation in the R/T ratio and area ratio of vascular bundles*

118 Figure 1a shows a typical cross-section of Moso bamboo used in this work. Vascular bundles,
119 surrounded by parenchyma tissues in the region between the epidermis and endodermis, were
120 distributed characteristically. The distribution of vascular bundles became dense, and their shape was
121 elongated in the radial direction from the inner to outer layer (Fig. 1b). The characteristic change in
122 the vascular bundles depended on the position in the longitudinal direction. Although these
123 characteristics are well known, quantitative analyses of the distribution in the longitudinal and radial
124 direction have not been conducted. Here, cross-sectional image features of vascular bundles were
125 evaluated using the R/T ratio.

126 Figure 2 shows the relationship between the R/T ratio and the area ratio obtained by image
127 analysis of the cross-sectional images and the internode height. The R/T ratio depends on the
128 internode number or internode height, and the tendencies of dependence were different in the inner
129 and outer layers. The R/T ratio in the bottom section of the culm was lower than other sections in both
130 the inner and outer layers. The R/T ratio in the outer layer was almost constant for internodes 5–20
131 and tended to increase for internodes 21–27. In contrast, it was almost constant above internode 5 in
132 the inner layer. That is, the R/T ratio was constant regardless of internode height except in the bottom
133 sections. The area ratio increased continuously with internode number in both the inner and outer
134 layers. Also, the area ratio was larger in the outer layer than in the inner layer.

135 Figure 3 compares the change in R/T ratio and area ratio in the radial direction for the bottom,
136 middle, and top sections of the culm. Radial and longitudinal fluctuations were observed for both the
137 R/T ratio and the area ratio. Notably, the R/T ratio in the inner layer hardly depended on internode
138 height.

139 The mechanical properties of bamboo depend on density [12]. Because bamboo consists of
140 parenchyma tissues and vascular bundles, we investigated the density dependency of the R/T ratio
141 and area ratio, which are cross-sectional image features of vascular bundles. Figure 4 shows the
142 density dependency of the R/T ratio and area ratio.

143 A correlation was observed between area ratio and density, though it became weaker as the

144 area of the cavity varied within the vascular bundles, because the area ratio was calculated based on
145 the area including the vessel cavities and sieve tubes. The correlation coefficient was higher in the
146 low-density region but somewhat lower in the high-density region. In contrast, the R/T ratio tended to
147 depend on density differently than did the area ratio. Little scatter in the R/T ratio was observed, and
148 the correlation was weak in the inner layer, although R/T ratio was strongly correlated with density in
149 the outer layer.

150
151

152 *3.2 Change in vascular bundle area ratio*

153 As shown in Figure 1, there was variation in the average size of the vascular bundles across
154 the culm wall in the radial direction. The average size of the vascular bundles in the inner and outer
155 layers was evaluated from the relationship between the density of vascular bundles Nr and the area
156 ratio Ar (Fig. 5). Nr and Ar are given as $Nr = n/A$ and $Ar = \sum_{i=1}^n a_i / A$, respectively, where n is the
157 number of vascular bundles in the cross-sectional region of which area is A , and a_i is the area of a
158 vascular bundle. From the two equations given above, the following equation is obtained:

159 $Ar = (\sum_{i=1}^n a_i / n)Nr$. Thus, when the relationship between Ar and Nr is linear, the slope $\sum_{i=1}^n a_i / n$ gives

160 the average area of a vascular bundle in the region. The slopes obtained from Figure 5 were 0.0642
161 and 0.1585 in the outer and inner layer, respectively. The average area of a vascular bundle in the
162 inner layer was 2.5 times larger than that in the outer layer, indicating that small vascular bundles
163 are distributed densely in the outer layer, whereas large vascular bundles are scattered throughout
164 the inner layer.

165 The image analysis of 24 cross-sectional images revealed that R/T ratio and area ratio varied
166 longitudinally and radially, and that the size of the vascular bundle itself varied from the inner to the
167 outer layer in the radial direction.

168
169

170 *3.3 Effects of vascular bundle shape and area ratio on relaxation properties*

171 Creep tests were conducted on the specimens cut from the inner and outer layers of some
172 internodes. Although there are many reports on the mechanical properties of bamboo, there are few
173 reports on its relaxation properties [12, 23], especially in relation to area ratio. Chuma et al. [12]
174 showed that the results of mechanical testing can be described by the mixture rule of vascular bundles
175 and parenchymal tissues. Aoyagi and Nakano [23] investigated the effects of position in the
176 longitudinal and radial direction on creep behavior and reported that there is a characteristic

177 dependency on density and the application of Nutting's equation.

178 We evaluated the relationship between relaxation properties and the R/T ratio or area ratio,
179 which are the instantaneous compliance $J(0)$ and the creep intensity $J(3 \times 10^4) - J(0)$. The former is
180 the creep compliance when the measuring time t is zero and the latter is the difference between the
181 values of creep compliance at $t = 3 \times 10^4$ and $t = 0$.

182 Figure 6 shows the density dependences of the instantaneous compliance and creep intensity.
183 Both instantaneous compliance and creep intensity were negatively correlated with density and
184 tended to decrease with increasing density. However, their density dependences largely differed.

185 No difference was observed between $\ln [J(0)]$ versus density in the inner layer and that in the
186 outer layer, although $\ln [J(0)]$ decreased continuously as density increased. Both relations were
187 represented by the same curve. Logarithmic $J(0)$ in the outer layer of internode No.26 was ten times
188 larger than that in the inner layer of internode No.2, indicating that instantaneous compliance
189 depended on the volume fraction or the ratio of vascular bundles, considering that density dependence
190 is equal to the volume fraction dependence. Therefore, the relationship between the R/T ratio or area
191 ratio and the instantaneous compliance was examined, and the results are shown in Figure 7. Clear
192 correlation was observed between the cross-sectional image features and $\ln [J(0)]$, except for the R/T
193 ratio in the inner layer.

194 The density dependence of the creep intensity was different from that of the instantaneous
195 compliance as shown in Figure 6. That in the outer layer, where density was greater than 0.51, was
196 obviously different from that in the inner layer, where density was lower. The creep intensity was
197 almost constant in internodes 4–22, which are the middle regions of the bamboo culm. The relaxation
198 behavior in the outer layer of the middle region of the culm was constant regardless of density. The
199 relationship between instantaneous compliance and creep intensity is shown in Figure 8. The clear
200 difference shown in Figure 8 indicates that the density dependence of short-term behavior differs from
201 that of long-term behavior.

202 Figures 6–8 show that creep intensity, a time-dependent mechanical property, was
203 independent of the density in a particular range, although a strong correlation existed between
204 instantaneous compliance and density. This implies that relaxation behavior was independent of the
205 vascular bundle image features in this range, considering the correlation in Figure 4. Therefore, other
206 factors should be involved. The finding that the ratio and shape have no relationship with relaxation
207 behavior indicates that this relaxation behavior is not directly related to formation of vascular bundles
208 or its changes in cross-section. This is probably because relaxation behavior is attributed to the
209 conformation change and interaction of the molecular chains in the substance. This difference appears
210 in the flat region in Figure 6, where the density is 0.5–0.7, that is, in the outer layer of internodes 4–22.
211 That may be related to the fact that bamboo grows into a large culm despite its small diameter [23].

212
213
214
215
216
217
218
219
220
221
222
223
224
225
226
227
228
229
230
231
232
233

4. Conclusions

The R/T ratio and area ratio of vascular bundles, which are cross-sectional image features of bamboo, had a characteristic distribution in both the longitudinal and radial directions. The R/T ratio was larger in the outer layer than the inner layer in the radial direction, and smaller in the bottom section than other sections of the longitudinal direction. In the outer layer, the R/T ratio was almost constant for internodes 5–20, whereas it increased as the internode number became larger for internodes greater than internode 20. It was almost constant in the inner layer of internodes greater than internode 5. The area ratio was larger in the outer layer than the inner layer. It increased continuously with internode number, and the degree of increase was larger in the outer layer. The average vascular bundle area in the inner layer was 2.5 times as large as that in the outer layer.

Although both instantaneous compliance, $\ln [J(0)]$, and creep intensity, $\ln [J (3 \times 10^4) - J (0)]$, decreased as density increased, the density dependence of $\ln [J(0)]$ was largely different from that of $\ln [J (3 \times 10^4) - J (0)]$. Instantaneous compliance was strongly correlated with density, which was related to the R/T ratio and area ratio, whereas creep intensity had a poor correlation with density. This result suggests that the difference between instantaneous compliance and creep intensity is attributable to the dependence of creep intensity on microstructure, such as the conformation of molecular chains in the substance, more strongly than the R/T ratio and area ratio, which are cross-sectional image features.

234 **References**

235

- 236 [1] Y. Suzuki, Bulletin of Tokyo University Forests. 36 (1948a) 136.
237 [2] Y. Suzuki, Bulletin of Tokyo University Forests. 36 (1948b) 206.
238 [3] Y. Suzuki, Bulletin of Tokyo University Forests. 38 (1950) 181.
239 [4] M. Ota, Bulletin of the Kyushu University 19 (1951) 25.
240 [5] M. Ota, Bulletin of the Kyushu University 22 (1953) 87.
241 [6] M. Ota, Bulletin of the Kyushu University 24 (1955a) 73.
242 [7] M. Ota, Bulletin of the Kyushu University 25 (1955b) 121.
243 [8] N. Parameswaran, W. Liese, Wood Sci. Technol. 10 (1976) 231.
244 [9] N. Parameswaran, W. Liese, Cellulose Chem. Technol. 14 (1980) 587.
245 [10] W. Liese, Wood Sci. Technol. 21 (1987) 189.
246 [11] K. Nakato, Bulletin of Kyoto Prefectural University 11 (1959)105.
247 [12] S. Chuma, M. Hirohashi, T. Ohgama, Y. Kasahara, Zairyo 39 (1990) 847.
248 [13] V.S. Godbole, S.C. Lakkad, Mater. Sci. Letters 5 (1986) 303.
249 [14] S. Amada, Y. Ichikawa, T. Munekata, Y. Nagase, H Shimizu, Compos. Part B 28 (1997) 13.
250 [15] Y. Inokuchi, M. Fushitani, S. Chuma, M. Ozawa, T. Kubo, K. Sato, Mokuzai Gakkaishi 43 (1997)
251 391.
252 [16] T.Y. Lo, H.Z. Cui, H.C. Leung, Mater. Lett. 58 (2004) 2595.
253 [17] H. Takagi, Y. Ichihara, JSME Inter. J. 47 (2004) 551.
254 [18] A.K. Ray, S. Mondal, S.K. Das, P. Ramachandrarao, J. Mater. Sci. 40 (2005) 5249.
255 [19] J.F. Ma, W.Y. Chen, L. Zhao, D.H. Zhao, J. Bio. Engi 5 (2008) 231.
256 [20] L. Zou, H. Jin, W.Y. Lu, X. Li, Mater. Sci. Engi. C29, (2009) 1375.
257 [21] T.Y. Lo, H.Z. Cui, P.W.C Tang, H.C. Leung, Construction and Building Mater. 22 (2008) 1532.
258 [22] Z.P. Sha, C.H. Fang, S.X. Huang, G.L. Tian, Wood Sci. Technol. (2009) DOI 10.
259 1007/s00226-009-0290-1.
260 [23] S. Aoyagi, T. Nakano, Zairyo 58 (2009) 57.
261 [24] L.M. Low, Z.Y. Che, B.A. Latella, J. Mater. Res. 21 (2006) 1969.

262

263 **Figure captions**

264

265 Fig. 1 Typical transverse cross-sectional features of Moso bamboo (a) and the schematic shape change
266 in the vascular bundle from the inner to outer layers (b).

267

268 Fig. 2 Change in the vascular bundle R/T ratio and area ratio with internode number.

269

270 Fig. 3 Change in the vascular bundle R/T ratio and area ratio with cross-sectional position.

271

272 Fig. 4 Relationships among area ratio, R/T ratio, and bamboo density.

273

274 Fig. 5 Relationship between area ratio and the number of vascular bundles per unit area.

275

276 Fig. 6 Dependence of instantaneous creep compliance $J(0)$ and creep intensity $J(3 \times 10^4) - J(0)$ on
277 bamboo density.

278

279 Fig. 7 Relationship between area ratio and R/T ratio and the instantaneous creep compliance $J(0)$.

280

281 Fig. 8 Relationship between instantaneous creep compliance and creep intensity $J(3 \times 10^4) - J(0)$.

282

283

284

285

286

287

288

289

290

291

292

293

294

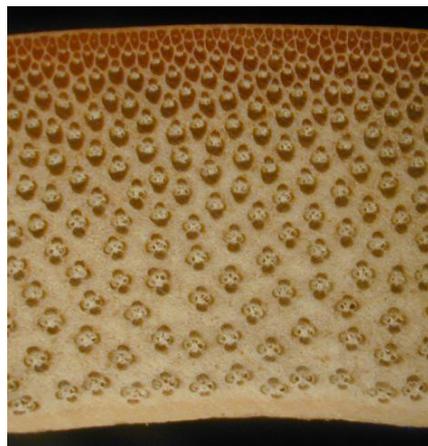
295

296

297

298
299
300
301
302
303
304
305
306
307
308
309
310
311
312
313
314
315
316
317
318
319
320
321
322
323
324
325
326
327

a. Cross-section of moso bamboo



**b. Schematic shape change
of vascular bundle**

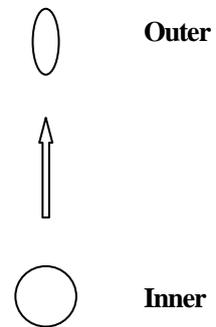


Fig. 1 Typical transverse cross-sectional features of Moso bamboo, a, and the schematic shape change in the vascular bundle from the inner to outer layers, b.

328
329
330
331
332
333
334
335
336
337
338
339
340
341
342
343
344
345
346
347
348
349
350
351
352
353

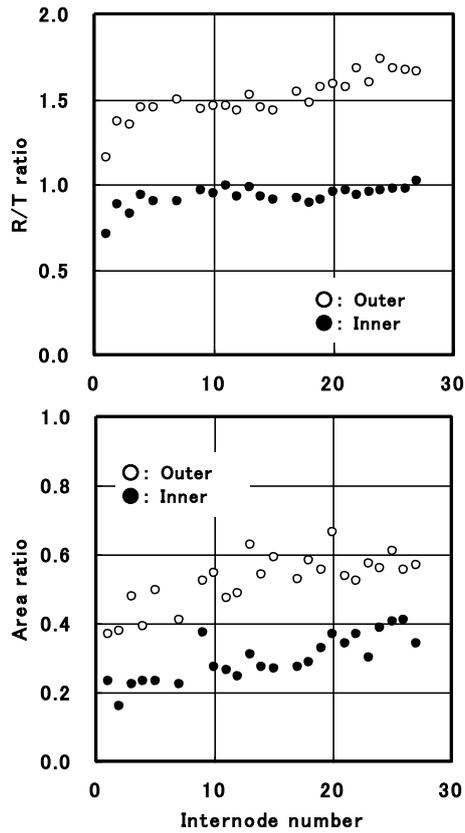


Fig. 2 Change in the vascular bundle R/T ratio and area ratio with internode number.

354
355
356
357
358
359
360
361
362
363
364
365
366
367
368
369
370
371
372
373
374
375
376
377
378

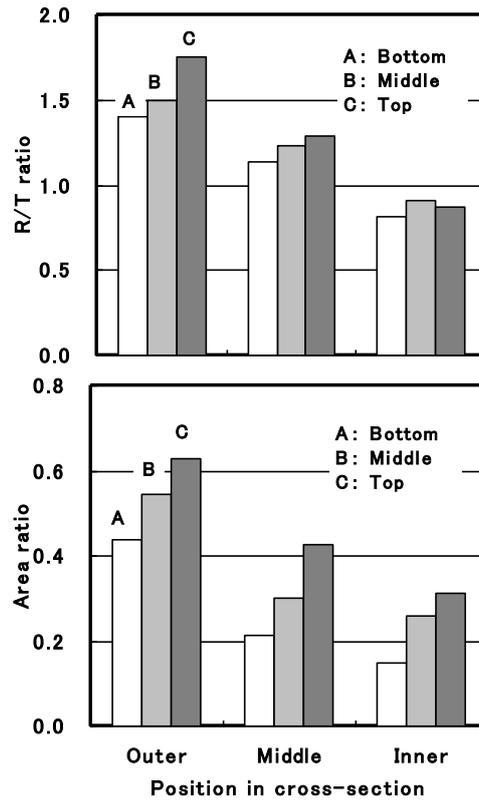


Fig. 3 Change in the vascular bundle R/T ratio and area ratio with cross-sectional position.

379
380
381
382
383
384
385
386
387
388
389
390
391
392
393
394
395
396
397
398
399
400
401
402
403

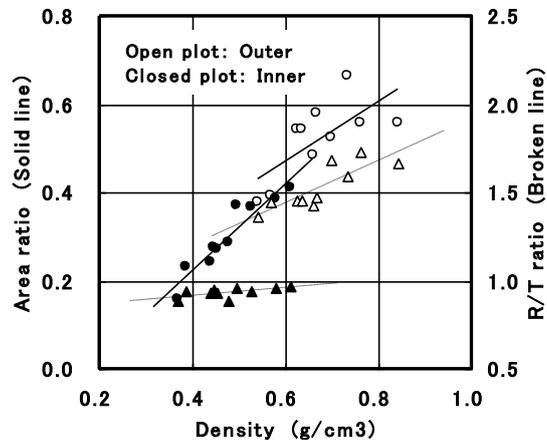


Fig. 4 Relationships among area ratio, R/T ratio, and bamboo density.

404
405
406
407
408
409
410
411
412
413
414
415
416
417
418
419
420
421
422
423
424
425
426
427
428
429

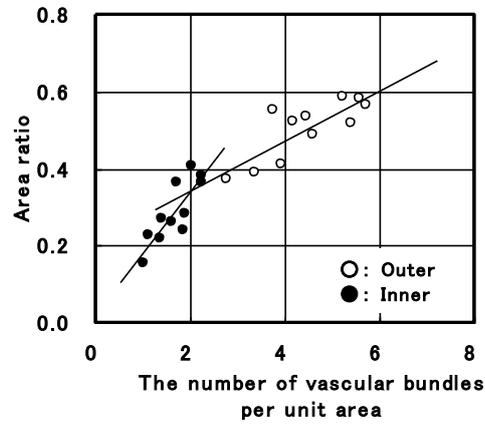


Fig. 5 Relationship between area ratio and the number of vascular bundles per unit area.

430
 431
 432
 433
 434
 435
 436
 437
 438
 439
 440
 441
 442
 443
 444
 445
 446
 447
 448
 449
 450
 451
 452
 453
 454
 455
 456
 457

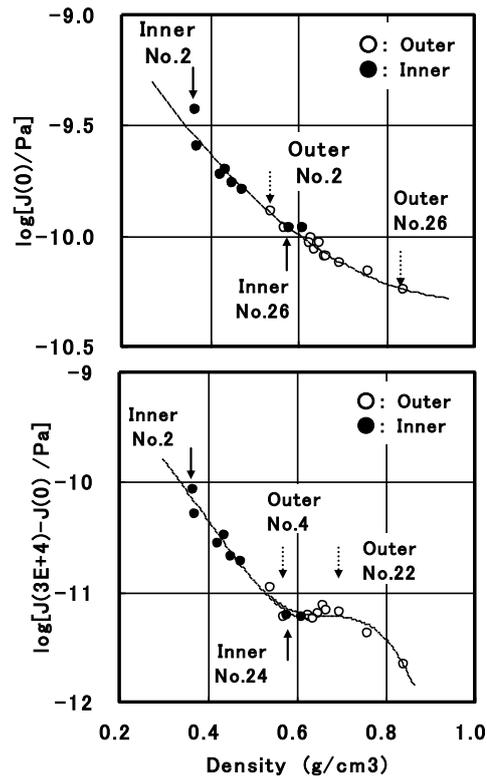


Fig. 6 Dependence of instantaneous creep compliance $J(0)$ and creep intensity $J(3 \times 10^4) - J(0)$ on bamboo density.

458
459
460
461
462
463
464
465
466
467
468
469
470
471
472
473
474
475
476
477
478

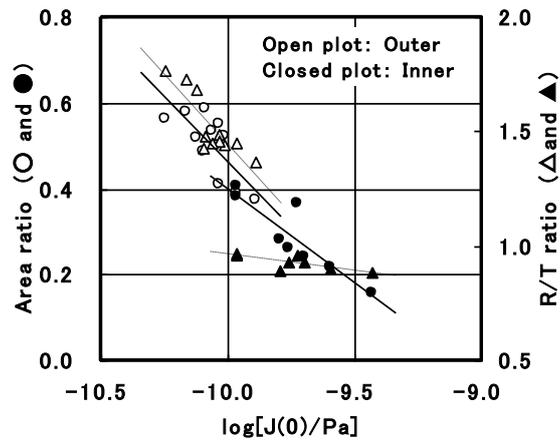


Fig. 7 Relationship between area ratio and R/T ratio and the instantaneous creep compliance $J(0)$.

479
480
481
482
483
484
485
486
487
488
489
490
491
492
493
494
495
496
497
498
499
500
501
502
503
504

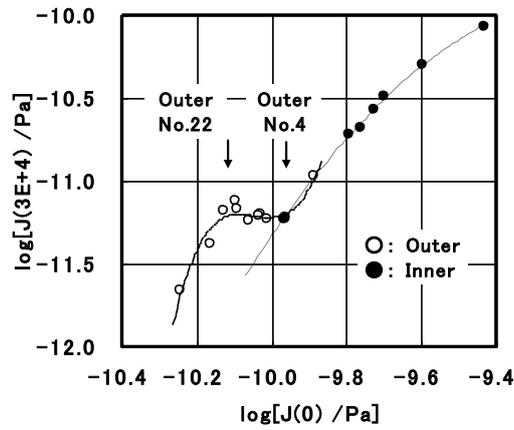


Fig.8 Relationship between the instantaneous creep compliance $J(0)$ and creep intensity $J(3 \times 10^4) - J(0)$.

Fig. 8 Relationship between instantaneous creep compliance and creep intensity $J(3 \times 10^4) - J(0)$.