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<tr>
<td>Citation</td>
<td>Physical Review B (2011), 83(18)</td>
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<tr>
<td>Issue Date</td>
<td>2011-05</td>
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<td>URL</td>
<td><a href="http://hdl.handle.net/2433/145975">http://hdl.handle.net/2433/145975</a></td>
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<tr>
<td>Type</td>
<td>Journal Article</td>
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Homogeneous coexistence of superconducting and spin-density-wave states in CaFe\textsubscript{1-x}Co\textsubscript{x}AsF as seen via nuclear magnetic resonance

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(Received 18 April 2011; published 26 May 2011)

We investigated the homogeneous coexistence of spin-density-wave (SDW) and superconducting (SC) states in \textsuperscript{75}As-nuclear magnetic resonance (NMR) in CaFe\textsubscript{1-x}Co\textsubscript{x}AsF and found that the electronic and magnetic properties of this compound are intermediate between those of LaFeAsO\textsubscript{1-x}F\textsubscript{x} and Ba(Fe\textsubscript{1-x}Co\textsubscript{x})\textsubscript{2}As\textsubscript{2}. For 6% Co-doped samples, the paramagnetic spectral weight completely disappears in the crossover regime between the SDW and SC phases followed by anomalous behavior of relaxation rate (1/T\textsubscript{relax}), implying that the two phases are not segregated. \textsuperscript{59}Co-NMR spectra show that spin moments are not commensurate but spatially modulated. These experimental results suggest that incommensurate SDW (IC-SDW) and SC states are compatible in this compound.

DOI: 10.1103/PhysRevB.83.180508

To date, a number of iron-based high-critical-temperature (T\textsubscript{c}) superconductors have been discovered since the first discovery of superconductivity in LaFeAsO\textsubscript{1-x}F\textsubscript{x}. Among these, 1111 series (RFeAsO\textsubscript{1-x}F\textsubscript{x}, [R=Nd, Sm, Ce, and La, etc.])\textsuperscript{1-6} and 122 series such as Ba(Fe\textsubscript{1-x}Co\textsubscript{x})\textsubscript{2}As\textsubscript{2}\textsuperscript{7-9} have been studied intensively because the former has a relatively high T\textsubscript{c} compared with the others, and the latter is available in a single-crystal form. A clear difference between the two series is apparent from the electronic phase diagrams shown in Fig. 1. The structural and magnetic phase transitions occur at almost the same temperature (T\textsubscript{c}) for the 1111 series, whereas the optimal T\textsubscript{c} for the 122 series is realized near the AF phase, although the optimal T\textsubscript{c} values are almost the same at ambient pressure. In other words, the overlap between the AF and SC phases is large for the 1111 series. This necessarily leads to the problem of coexistence in the crossover regime. Several theoretical investigations have focused on charge and spin states in the vicinity of the crossover regime.\textsuperscript{10-12} The coexistence of the order parameters of the incommensurate spin-density-wave and superconducting (IC-SDW + SC) states has been investigated in the crossover regime for s\textsuperscript{+-} or s\textsuperscript{++}-wave symmetry.\textsuperscript{10-12} The homogeneous coexistence of the AF and SC states has been suggested for Ba(Fe\textsubscript{1-x}Co\textsubscript{x})\textsubscript{2}As\textsubscript{2} on a microscopic level,\textsuperscript{13-15} whereas microscopic or mesoscopic segregation of the AF and SC phases has been suggested for K-doped Ba(Fe\textsubscript{1-x}Co\textsubscript{x})\textsubscript{2}As\textsubscript{2}.\textsuperscript{16-18} The topics have been investigated mainly for the Ba 122 series\textsuperscript{19} and it is presently unclear whether the observed phenomena are inherent to all iron-based superconductors with a crossover regime.

In this study, we focus on CaFe\textsubscript{1-x}Co\textsubscript{x}AsF\textsuperscript{20} to investigate whether the AF and SC phases coexist homogeneously or are segregated. The compound is a member of the 1111 series, but exhibits an intermediate phase diagram, as shown in Fig. 1.\textsuperscript{20-23} The degree of overlap of the SC and AF phases is intermediate between the La1111 and Ba122 series. The doping dependence of the structural (T\textsubscript{c}) and magnetic (T\textsubscript{N}) transition temperatures is also intermediate between the two series.

We performed nuclear magnetic resonance (NMR) measurements using 6% and 12% Co-doped powder samples. Figures 2(a) and 2(b) show the T dependence of the resistivity. The SC phase was confirmed for both samples; the T\textsubscript{c} onset is 7 and 20 K for the 6% and 12% Co-doped samples, respectively. The detuning of an NMR tank circuit is shown in Fig. 2(c). The bending point at 7 K is closer to the zero-resistivity temperature than the T\textsubscript{c} onset.

For the 6% Co-doped samples, the field-swept\textsuperscript{75}As-NMR spectra were measured at a frequency v\textsubscript{0} = 45.1 MHz, as shown in Fig. 3. The low-field peak around 50 kOe corresponds to the transition I = −3/2 ⇐⇒ −1/2, and the central peak with two bumps corresponds to the transition I = −1/2 ⇐⇒ 1/2. The two bumps of the central peak originate from the second-order quadrupole effect. The frequency shift (ν) arising from this effect is expressed using two polar coordinates, θ and φ, of the applied field (H) in the coordinate system of the electric field gradient (EFG). The coordinate θ represents the angle between H and the maximal principal axis (Z axis) of EFG. In this case, the Z axis is equivalent to the crystal c axis. The coordinate φ represents the angle between the second principal axis (X axis) and the H component projected onto the XY plane. The XY plane coincides with the crystal ab plane. The θ and φ dependence of ν is given as

\[ ν(θ, φ) = -\frac{3μ_0^2}{16v_0} \sin^2 θ[(9\cos^2 θ - 1) + η f(θ, φ) + η^2 g(θ, φ)], \]

where \( v_0 \) and η (0 < η < 1) are the pure quadrupole frequency and the EFG anisotropy, respectively. From the analysis of the NMR spectra, \( v_0 \) and η are estimated to be 22.6 MHz and 0.3, respectively. The value of \( v_0 \) is almost twice as large as that for the La1111 series.\textsuperscript{24} The terms \( η f(θ, φ) \) and \( η^2 g(θ, φ) \) in Eq. (1) are correction terms arising from axial asymmetry. The θ and φ dependence of \( f \) and \( g \) is explained in detail in Ref. 25.

\[ ν(θ, φ) = -\frac{3μ_0^2}{16v_0} \sin^2 θ[(9\cos^2 θ - 1) + η f(θ, φ) + η^2 g(θ, φ)], \]

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FIG. 1. (Color online) Phase diagrams of Ba(Fe_{1−x}Co_{x})_2As_2, CaFe_{1−x}Co_{x}AsF, and LaFeAsO_{1−x}F_{x}. Red up triangles, green down triangles, and blue circles represent the structural (TS), AF (TN), and SC (Tc) transition temperatures, respectively.

At the field \( h = H - H_0 \), where \( H_0 \) represents the resonance field expected for \( \nu_Q = 0 \), the spectral intensity \( I_{\text{As}}(h) \) is

\[
I_{\text{As}}(h) \propto \int \delta(h - (2\pi/\gamma_N)\nu) d(\cos \theta) d\phi,
\]

where the gyromagnetic ratio (\( \gamma_N \)) of \(^{75}\text{As} \) is 7.292 MHz/10 kOe. For \( \eta = 0 \),

\[
I_{\text{As}}(h) \propto \int \delta(h - 2\pi/\gamma_N)\sin \theta \left| \frac{\partial \nu}{\partial \theta} \right| d\nu.
\]

The bumps originate from the powders with \( \theta = 90^\circ \) or \( 42^\circ \) that satisfy \( \frac{\partial \nu}{\partial \theta} / \sin \theta = 0 \). Even for \( \eta \neq 0 \), the bumps appear at the same angle (\( \theta = 90^\circ \) or \( 42^\circ \)). The low-field bump originates from the powders with \( \theta = 90^\circ \) in which the Fe basal planes are aligned with \( \mathbf{H} \), whereas the high-field bump originates from the powders with \( \theta = 42^\circ \). The spectral weight weakens below \( T_N \) and completely disappears in the SC state. An analogous disappearance is not observed for the 12% Co-doped samples in which the AF phase is absent. The disappearance of the bump is characteristic of the AF phase.

Unlike the high-field bump, the low-field bump is maintained even at low temperatures. The resonance position of the low-field bump is almost unchanged, even when the Co nuclei experience the internal field that appears in the AF phase. For the commensurate SDW state, stripe-type antiferromagnetic spin moments aligned in an Fe plane (the ab plane) induce the internal field normal to the Fe plane on \(^{75}\text{As} \) sites; therefore, As nuclei experience no internal field when the Fe plane is parallel to \( \mathbf{H}(\theta = 90^\circ) \). Consequently, the low-field bump is maintained even in the spin-ordered state. For crystals with other \( \theta \) angles, As nuclei experience nonzero internal fields, and the corresponding signals are swept over a wider field range. This explanation is possible for the IC-SDW state accompanied by long-wave spin modulation.

The relaxation time \( T_1 \) was measured using the conventional saturation-recovery method. The \( T \) dependence of \( 1/T_1T \) was measured at the low-field bump. The bump position is almost unchanged for the observed temperatures. Therefore, \( 1/T_1T \) is successively measured, even in the AF phase, with the same conditions as the paramagnetic phase. The recovery

FIG. 2. (Color online) (a, b) Superconducting transition temperature determined by resistivity and (c) detuning of an NMR tank circuit. Figure 2(b) is an expanded view of Fig. 2(a). These measurements were operated at zero field.

FIG. 3. Field-swept \(^{75}\text{As}-\)NMR spectra at several temperatures for the 6% Co-doped samples. The sharp signals at 37.3 and 40.0 kOe originate from \(^{65}\text{Cu} \) and \(^{63}\text{Cu} \), respectively, which are present in the copper NMR coil. The cusp-shaped signal observed at 45 kOe originates from \(^{59}\text{Co} \) in the Fe basal planes. The other signals originate from \(^{75}\text{As} \). The peak around 50 kOe corresponds to the transition \( I = -3/2 \leftrightarrow -1/2 \), and the double-bump peak corresponds to \( I = -1/2 \leftrightarrow 1/2 \).
curves $1 - M(t)/M(\infty)$, where $M(t)$ represents the nuclear magnetization after the saturation pulse, exhibit a fast-recovery component throughout the entire temperature range. The data were analyzed using three-component fitting: that is, fast-recovery component $1/T_1$, is introduced tentatively into the recovery curve as follows:

$$1 - \frac{M(t)}{M(\infty)} = c(0.9e^{-t/T_1} + 0.1e^{-t/T_2} + (1 - c)e^{-t/T_\infty}).$$  

A recovery curve measured at 4.2 K for the 6% Co-doped samples is shown in Fig. 4(a). The magnitude of $1/T_1$, which allows us to separate the two terms without ambiguity, the $T$ dependence of $1/T_1$, $T$ and $1/T_2$, $T$ is shown in Figs. (b, c), respectively. Below 50 K, the value of $c$ is approximately 0.4 to 0.5. The results of $1/T_1$, $T$ are almost unchanged even if the experimental data are analyzed using $0.9e^{-t/T_1} + 0.1e^{-t/T_2}$ instead of $e^{-t/T_\infty}$ in Eq. (4). The $T$ dependence of $1/T_1$, $T$ reflects the AF and SC transitions both, whereas that of $1/T_2$, $T$ reflects neither of them. In Fig. 4(d), $T_s = 75 \pm 5$ K and $T_p = 26$ K are derived from the bending point and peak, respectively. From neutron scattering measurements, the magnitude of the ordered moments is estimated to be 0.15 $\mu_B$, which is considerably small compared with that in the undoped case (0.49 $\mu_B$). The bending point at 7 K observed in Fig. 4(d) corresponds to $T_c$, which is consistent with the temperature observed from the detuning of the tank circuit and the resistivity measurements. Although $1/T_1$ was measured under an applied magnetic field, $T_c$ is almost the same, implying that the decrease in $T_c$ due to the applied field is negligible. As a result, the effect of the vortex is neglected when the Fe basal planes are parallel to $\mathbf{H}$.

Actually, we could not observe the field dependence of $1/T_1$ which is expected to appear for the vortex motion. The temperature dependence at low temperatures follows the power law, $1/T_1 \sim T^{-1.5}$. We tentatively attribute this dependence to an intrinsic electronic state in the Fe basal planes. The fast-recovery component $1/T_2$, $T$ is also observed for the 12% Co-doped samples. Therefore, this component may be extrinsic to the low-frequency fluctuation arising from the Fe basal planes. A possible origin of the fast-recovery component is nuclear spin diffusion.

For the 12% Co-doped samples, $1/T_1$, $T$ is almost independent of the temperature above $T_c$, and is proportional to $T^2$ below $T_c$. There are two possible origins for this temperature-independent behavior. The first possibility is a Korringa relation $1/T_1$, $T \propto D(\varepsilon_F)^2$, where $D(\varepsilon_F)$ is the density of the states at the Fermi energy, and the second possibility is very weak Curie-Weiss behavior. Both possibilities have been observed in LaFeAsO$_{1-x}$F$_x$. The former has been observed for the underdoped regime ($x = 0.14$–0.15) just above $T_c$, whereas the latter has been observed for the underdoped regime in a wide temperature range above $T_c$. In the present case, the value of $1/T_1$, $T$ is rather close to that observed for the underdoped regime. The $T$ dependence is attributable to spin fluctuations.

The present NMR measurements confirm successive phase transitions. The complete disappearance of the high-field bump in the crossover regime indicates that no paramagnetic domains exist, which implies that no phase segregation occurs in this doping regime. The fact that the AF phase is not commensurate can be demonstrated by the $^{59}$Co($I = 7/2$)-NMR spectra shown in Figs. 5(a–c). The satellite signals expected owning to the quadrupole effect are not clearly observed in the paramagnetic state as seen in Fig. 5(a), implying that the EFG at Co nuclei is considerably small and is somewhat distributed. The broadening due to an

![FIG. 4. (Color online) (a) Recovery curve of the central transition (1/2 $\leftrightarrow$ $-1/2$) measured at 4.2 K for the 6% Co-doped samples. The data are fitted using Eq. (4). (b, c) Temperature dependence of $1/T_1$, $T$ and $1/T_2$, $T$ for the 6% and 12% Co-doped samples. (d) Logarithmic plot of Fig. 4(c). The bending point at 7 K coincides with the transition temperature ($T_c$).](180508-3)
where curve expressed by the following integral:

\[ I^{\text{Co}}(h) \propto \int \delta(h - h_{\text{AF}}) \cos \psi\, \! d(\cos \psi) \]

\[ \propto \frac{1}{h_{\text{AF}}} \left( |h/h_{\text{AF}}| \leq 1 \right), \]

where \( h = H - H_0 \) and \( \psi \) represents the angle between \( H \) and the Fe plane. The field dependence represents a well-known rectangular powder pattern, implying that the commensurate SDW state is not realized. Figure 5(b) shows simulations for the internal field modulated to the AF direction, which suggests the existence of a uniform electronic state, the IC-SDW state, where the wavelength is 2 lattice units, \( Q = \pi/n \) and \( h_{\text{AF}} = 6 \text{ kOe} \). The width of the top rectangular pattern is proportional to \( 1/n \) for a large \( n \). A pattern with a large \( n \) approaches the curve expressed by the following integral:

\[ I^{\text{Co}}(h) \propto \int \frac{1}{h_{\text{AF}} \sin \varphi} \, d\varphi \]

\[ \propto \ln \left| 1 + \sqrt{1 - (h/h_{\text{AF}})^2} \left| |h/h_{\text{AF}}| \leq 1 \right. \right. \]

The curve reproduces the experimental results well as shown in Fig. 5(c). In fact, an extremely large \( n \) is not always required owning to the small quadrupole effect: the rectangular pattern would become smooth when this effect is considered. The simulations for \( n = 50-100 \) could reproduce the experimental results. The cusp-type pattern at 4.2 K in Fig. 5(a) is almost the same as that at 12 K, suggesting that the distribution of the internal field below \( T_c \) is identical to that above \( T_c \). This result implies that the SC transition proceeds on the background of the IC-SDW state which is well developed above \( T_c \). A uniform electronic state, the IC-SDW + SC state, is a promising candidate to explain these experimental results.

In summary, we measured NMR spectra and \( 1/T_1T \) in \( \text{CaFe}_{1-x}\text{Co}_x\text{AsF} \) and found that the electronic and magnetic properties are intermediate between those of \( \text{LaFeAsO}_{1-x}\text{F}_x \) and \( \text{Ba(Fe}_{1-x}\text{Co}_x)_2\text{As}_2 \). For the 6% Co-doped samples, we confirm the coexistence of the SC and spin-ordered states from \( 1/T_1T \) at low temperatures. At \( \theta = 42^\circ \), the \(^{59}\text{As}\) spectral weight completely disappears in the crossover regime, which indicates that no phase segregation is realized in this regime. The \(^{59}\text{Co}\)-NMR spectra demonstrate that spin moments are not commensurate but spatially modulated. In addition, the SC state develops on the background of the IC-SDW state, which suggests the existence of a uniform electronic SC-SDW + SC state.

ACKNOWLEDGMENTS

The present work was partially supported by Grant-in-Aid (Grant No. KAKENHI 23340101) for the Ministry of Education, Science and Culture, Japan.