

Thermoelectric properties and crystallographic shear structures in titanium oxides of the Magnéli phases

Shunta Harada,^{a)} Katsushi Tanaka, and Haruyuki Inui

Department of Materials Science and Engineering, Kyoto University, Sakyo-ku, Kyoto 606-8501, Japan

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The thermoelectric properties of Magnéli phase titanium oxides $\text{Ti}_n\text{O}_{2n-1}$ ($n=2,3,\dots$) have been investigated, paying special attention to how the thermoelectric performance can be altered by changing the microstructure. Dense polycrystalline specimens with nominal composition of TiO_{2-x} ($x=0.05, 0.10, 0.15$, and 0.20) prepared by conventional hot-pressing are all identified to be one of the Magnéli phases, in which crystallographic shear planes are regularly introduced according to the oxygen deficiency. Electrical conduction is n-type for all specimens and the carrier concentration increases with the increase in the oxygen deficiency. The values of lattice thermal conductivity, on the other hand, decrease with the increase in the oxygen deficiency, which can be attributed to phonon scattering at the crystallographic shear plane. The largest value of thermoelectric figure of merit Z , $1.6 \times 10^{-4} \text{ K}^{-1}$ was obtained at 773 K for the hot-pressed specimen of $\text{TiO}_{1.90}$. © 2010 American Institute of Physics. [doi:10.1063/1.3498801]

I. INTRODUCTION

Thermoelectric materials have been receiving great interest in recent years due to their potential applications such as in electric power generation by waste heat and in cooling system.¹ The efficiency of thermoelectric materials is evaluated by the dimensionless figure of merit $ZT = \alpha^2 T / \rho \lambda$ where Z , α , ρ , λ , and T correspond to the figure of merit, Seebeck coefficient, electrical resistivity, thermal conductivity, and absolute temperature, respectively. Thermal conductivity consists of two components; the phonon (lattice) contribution (κ_l) and the carrier contribution (κ_e). While κ_e is related to electrical resistivity through Wiedemann–Franz law, κ_l is independent of carrier concentration. Therefore, low lattice thermal conductivity is beneficial to thermoelectric performance. There may be many different ways to reduce lattice thermal conductivity. One way to achieve this is to introduce crystal lattice defects such as point defect and grain boundary that act as sources for phonon scattering.^{2–4} However, many of them sometimes act as sources for carrier scattering as well, which leads to the degradation of thermoelectric performance. This indicates that some special crystal lattice defects that act as sources for phonon scattering but not as sources for carrier scattering have to be introduced for thermoelectric materials to achieve the high performance.

In the present study, we pay special attention to crystallographic shear structures introduced in some reduced TiO_2 (rutile) of homologous series of the Magnéli phase. Homologous series of Magnéli phase titanium oxides are expressed with $\text{Ti}_n\text{O}_{2n-1}$ ($n=2,3,\dots$) (Ref. 5) and they form so-called crystallographic shear structures, in which dense planar defects are regularly introduced in the mother rutile structure with their spacing depending on the oxygen deficiency,⁶ as will be described in detail in the next section. According to Bartholomew and Fankl⁷ who investigated systematically the

electrical properties of single crystals of Magnéli phase titanium oxides, electrical conduction of Magnéli phase titanium oxides is metallic and the value of electrical resistivity decreases with the increase in the oxygen deficiency. This may clearly indicate that the crystallographic shear plane in Magnéli phase titanium oxides does not act significantly as sources for carrier scattering. If the crystallographic shear plane acts as sources for phonon scattering, we may expect the high thermoelectric performance for Magnéli phase titanium oxides. Although there are some recent reports on thermoelectric properties for some reduced TiO_2 ,^{8,9} the thermoelectric properties of Magnéli phase titanium oxides have not been thoroughly understood yet in terms of structure-property relations.

In the present study, we investigate the thermoelectric properties of Magnéli phase titanium oxides $\text{Ti}_n\text{O}_{2n-1}$, paying special attention to how the thermoelectric performances are affected by the presence of crystallographic shear planes.

II. CRYSTALLOGRAPHIC SHEAR STRUCTURES IN MAGNÉLI PHASE TITANIUM OXIDES

Magnéli *et al.*⁵ and co-workers started a systematic investigation of some oxides of transition metal such as titanium, vanadium, molybdenum, and tungsten by x-ray diffraction (XRD). As a result, they confirmed the existence of homologous compounds expressed by $\text{Ti}_n\text{O}_{2n-1}$ ($n=2,3,\dots$) and predicted that these structures could be all derived from the rutile structure as the mother structure. Later, Wadsley proposed the structure principle of these structures (called crystallographic shear structure¹⁰), describing how these structures are derived from the mother structure, as follows:⁶

- (1) The mother structure is divided into blocks periodically parallel to a crystallographic plane called shear plane [Fig. 1(a)].
- (2) Blocks are translated relatively each other by a certain vector called shear vector [Fig. 1(b)].

^{a)}Electronic mail: harada.shunta@t02.mbox.media.kyoto-u.ac.jp.

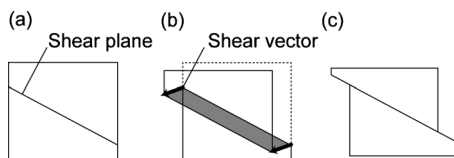


FIG. 1. Schematic illustration of crystallographic shear operation.

- (3) The overlapping parts, if generated by (2), are removed [Fig. 1(c)].

They identified that the crystallographic shear plane and vector for titanium oxides $\text{Ti}_n\text{O}_{2n-1}$ ($n=2,3,\dots,10$) are $(121)_{\text{rutile}}$ and $1/2[0\bar{1}1]_{\text{rutile}}$, respectively.^{6,11,12} Later, Bursill *et al.*¹³ have reported that the crystallographic shear plane changes to $(132)_{\text{rutile}}$ when n in $\text{Ti}_n\text{O}_{2n-1}$ is greater than 10. The crystallographic shear structures formed with the shear operations described above are schematically illustrated in Fig. 2. The shear vector corresponds to a vector connecting a position of oxygen ion with another in the bc -plane, thus resulting in no disturbance in the oxygen arrangement. However, the titanium arrangement is disturbed since the shear vector moves titanium ions in the octahedron formed by six oxygen ions to the interstitial octahedral positions (Fig. 2). As a result, the oxygen deficiency occurs on the shear plane (Fig. 2) and homologous series of Magnéli phase titanium oxides with various Ti/O ratios are formed by changing the spacing of the crystallographic shear plane.

In the rutile type structure, the stacking sequence of $\{121\}$ and $\{132\}$ planes, both of which can be the shear plane, is described as **BAB BAB**-, where **A** is a plane consisting of titanium ions only (**A**=Ti) and **B** is a plane consisting of oxygen ions only (**B**=O). The shear operation corresponds to the removal of pure oxygen planes of the **B**-type in a periodic manner. If the shear plane is introduced every n **A** planes, the stacking sequence changes to **BAB BA*** **BAB**- (* denotes the position of the shear plane) and the overall composition is described as the sum of n **A** planes and $(2n-1)$ **B** planes so as to be $\text{Ti}_n\text{O}_{2n-1}$. The atomic arrangement in Ti_6O_{11} , one of the Magnéli phase formed with $n=6$ is schematically illustrated in Fig. 3, where the oxygen deficiency and the disturbance of the titanium ion arrangement is evident to occur at the crystallographic shear plane.

When the crystallographic shear planes are introduced in

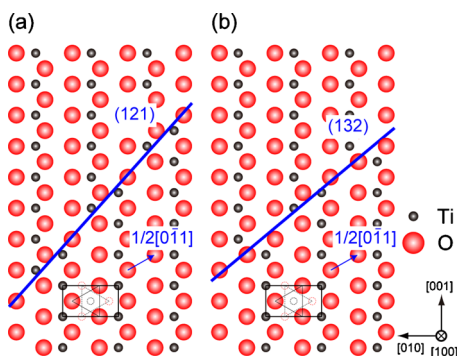


FIG. 2. (Color online) Schematic illustration of crystallographic shear structure of Magnéli phase titanium oxide. (a) Crystallographic shear operation $(121)_{\text{rutile}}$ $1/2[0\bar{1}1]_{\text{rutile}}$ and (b) $(132)_{\text{rutile}}$ $1/2[0\bar{1}1]_{\text{rutile}}$.

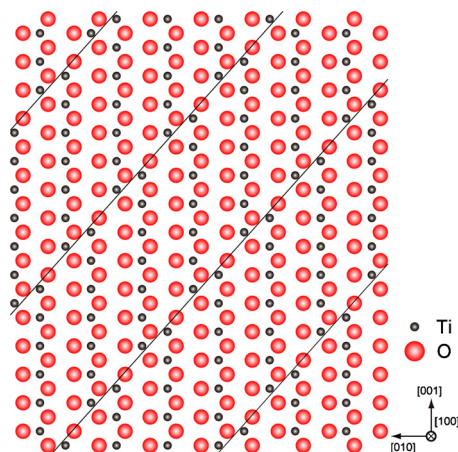


FIG. 3. (Color online) (a) Schematic illustration of ideal structure of Ti_6O_{11} ($n=6$) crystallographic shear structure in Magnéli phase titanium oxide.

the mother rutile structure, one can anticipate the occurrence of a series of superlattice reflection spots along the reciprocal lattice vector corresponding to the shear plane [either along $g(121)_{\text{rutile}}$ or along $g(132)_{\text{rutile}}$] at positions corresponding to n (the periodicity to introduce the crystallographic shear planes). The electron diffraction pattern expected for Ti_6O_{11} formed by introducing the crystallographic shear planes parallel to $(121)_{\text{rutile}}$ with $n=6$ is depicted in Fig. 4. The incident beam direction is chosen to be so as to include the reciprocal lattice vector corresponding to the shear plane in the diffraction pattern. Six equally spaced superlattice reflection spots are observed between the transmitted beam spot and that corresponding to the shear plane $(121)_{\text{rutile}}$. Thus, once the incident beam direction is chosen so that the reciprocal lattice vector corresponding to the shear plane is included in the diffraction pattern, the identification of the Magnéli phases ($\text{Ti}_n\text{O}_{2n-1}$) can be readily made by noting the positions (number) of a series of superlattice reflection spots along the reciprocal lattice vector corresponding to the shear plane. We utilize this method for the identification of the Magnéli phases in the present study.

III. EXPERIMENTAL PROCEDURE

Commercial TiO_2 and TiO powders weighted in proper ratios were mixed in ethanol solvent by planetary-type ball-milling for 12 h. After drying, the mixtures were sealed in a

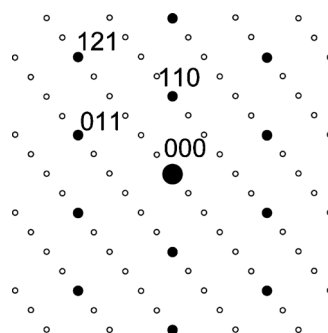


FIG. 4. Schematic illustration of electron diffraction pattern taken from Ti_6O_{11} . The zone axis is $[1\bar{1}1]$. A series of super spots are aligned along $g(121)$.

TABLE I. Condition of hot-pressing, identified phases from XRD, and average grain size of prepared specimens.

Nominal composition	HP conditions			Phase assemblage	Average grain size (μm)
	Temperature (K)	Time (min)	Pressure (MPa)		
TiO _{2.00}	1123	30	50	TiO ₂	0.51
TiO _{1.95}	1373	20	50	...	0.93
TiO _{1.90}	1473	10	50	Ti ₈ O ₁₅	0.90
TiO _{1.85}	1473	10	50	Ti ₅ O ₉ +Ti ₆ O ₁₁	1.12
TiO _{1.80}	1473	10	50	Ti ₄ O ₇	1.26

silica tube partially backfilled with Ar gas and were annealed at 1473 K for 12 h to produce TiO_{2-x} powders with $x = 0.05, 0.10, 0.15$, and 0.20 through solid-state reaction. Then, TiO_{2-x} powders were sintered by conventional hot-pressing in a carbon die under the conditions described in Table I. Since significant reduction is noted as the change in color to black for TiO₂ after sintering even the sintering temperature was considerably decreased, the TiO₂ sintered body was annealed again at 1073 K for 4 h in air to oxidize.

Phase identification was made by powder XRD and electron diffraction, and microstructures were examined by transmission electron microscopy (TEM). Measurements of electrical resistivity and Seebeck coefficient were made with our ULVAC ZEM-2 apparatus in the temperature range from 323 to 773 K. Measurements of thermal conductivity were carried out at room temperature by the static method. Values of thermal conductivity above room temperature were evaluated with the thermal diffusivity measured by the laser flash method and the reported values of specific heat for rutile.^{14,15}

IV. RESULTS

A. Phase identification and microstructures

Figure 5 shows XRD patterns from hot-pressed specimens of TiO_{2-x} with $x = 0, 0.05, 0.10, 0.15$, and 0.20 . Diffraction peaks from all these specimens, except for that with $x = 0.05$, are almost all consistently indexed as those from

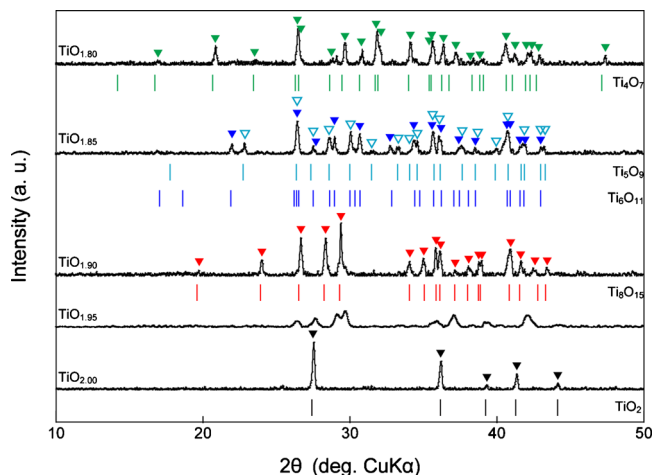


FIG. 5. (Color online) XRD patterns from hot-pressed specimens of TiO_{2-x} ($x = 0, 0.05, 0.10, 0.15$, and 0.20) together with the reported XRD patterns from Magnéli phase Ti_nO_{2n-1} (Ref. 6).

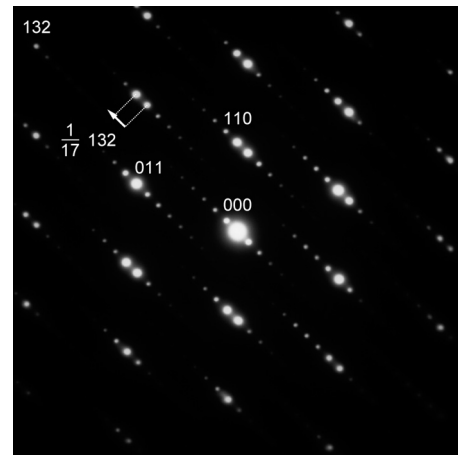


FIG. 6. Selected area electron diffraction pattern from hot-pressed specimen of TiO_{1.95} along the $[1\bar{1}1]$ zone axis.

one of titanium oxides of the Magnéli phase previously identified by Andersson *et al.*⁵ Phases identified for each of hot-pressed specimens of TiO_{2-x} by XRD are summarized in Table I. While essentially only a single phase is identified for hot-pressed specimens of TiO_{2.00}, TiO_{1.90}, and TiO_{1.80}, the hot-pressed specimen of TiO_{1.85} is observed to consist of two phases, Ti₅O₉ and Ti₆O₁₁. When judged from the chemical formulae of these identified Magnéli phases, the actual oxygen contents of these hot-pressed specimens of TiO_{1.90}, TiO_{1.85} and TiO_{1.80} are all lower than their nominal compositions, indicating the occurrence of reduction during hot-pressing. XRD peaks from the hot-pressed specimen of TiO_{1.95} do not coincide with those of any of titanium oxides of the Magnéli phase ever reported. This is because of the fact that phase identification by XRD has been so far made only for titanium oxides, Ti_nO_{2n-1} of the Magnéli phase with $n = 2$ to 10 .⁵ We thus utilized electron diffraction for phase identification of the hot-pressed specimen of TiO_{1.95}. A selected area electron diffraction pattern taken from the hot-pressed specimen of TiO_{1.95} along $[1\bar{1}1]_{\text{rutile}}$ is shown in Fig. 6. The line of superlattice reflection spots are directed approximately $(132)_{\text{rutile}}$ and the interval of the superlattice reflection spots correspond to about 17 times as long as the $(132)_{\text{rutile}}$ interplanar spacing. This fact indicates that the composition of the hot-pressed specimen of TiO_{1.95} is approximately Ti₁₇O₃₃ (TiO_{1.941}).

TEM microstructures of hot-pressed specimens of TiO_{2-x} with $x = 0, 0.05, 0.10, 0.15$, and 0.20 are depicted in Fig. 7. Electron diffraction analyses confirm the results of phase identification by XRD tabulated in Table I. Although some planar faults are observed in some grains, many of them are identified to be twin boundaries. The grain size is evaluated for each of specimens and the results obtained are also tabulated in Table I. The grain size does not differ significantly from each other for all the specimens of the Magnéli phases. Figure 8 shows a high-resolution TEM image of the Ti₆O₁₁ Magnéli phase observed in a hot-pressed specimen of TiO_{1.85}. Being consistent with the attached electron diffraction pattern, the crystallographic shear structure is formed by introducing the shear planes parallel to $(121)_{\text{rutile}}$ every six pure titanium planes. Of importance to note in Fig.

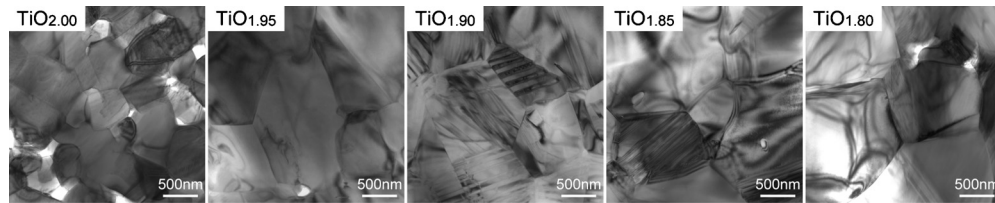


FIG. 7. TEM bright field images of hot-pressed specimens of TiO_{2-x} with $x=0, 0.05, 0.10, 0.15$, and 0.20 .

8 is that the disturbance of the periodicity to introduce the shear planes is hardly observed, which is consistent with the sharpness of superlattice reflection spots in the diffraction pattern. The disturbance of the shear plane periodicity is hardly observed also for other specimens of the Magnéli phases.

B. Thermoelectric properties

Values of electrical resistivity for hot-pressed specimens of TiO_{2-x} with $x=0.05, 0.10, 0.15$, and 0.20 are plotted in Fig. 8(a) as a function of temperature. The temperature dependence of electrical resistivity varies with the ratio of O/Ti of specimens, i.e., with the value of x in TiO_{2-x} . The value of electrical resistivity decreases with the increase in temperature for $\text{TiO}_{1.95}$ and $\text{TiO}_{1.90}$, while it increases with the increase in temperature for $\text{TiO}_{1.80}$. In contrast, the value of electrical resistivity for $\text{TiO}_{1.85}$ is virtually independent of temperature. Over the whole temperature range investigated, the values of electrical resistivity decreases as the value of x in TiO_{2-x} increases, i.e., as the oxygen content decreases. This indicates that electrical conduction of TiO_{2-x} of the Magnéli phase is metallic when the carrier concentration is high (i.e., when the x value is large, which is consistent with the results obtained by Bartholomew and Fankl,⁷ whereas it is semiconducting when the carrier concentration is low.

Values of Seebeck coefficient for hot-pressed specimens of TiO_{2-x} with $x=0.05, 0.10, 0.15$, and 0.20 are plotted in Fig. 8(b) as a function of temperature. The values of Seebeck coefficient for all specimens are negative in sign (n-type conduction). The absolute value of Seebeck coefficient increases as the oxygen content decreases over the whole temperature range investigated. While the value of Seebeck coefficient for $\text{TiO}_{1.95}$ is virtually temperature independent, it increases with the increase in temperature for other specimens.

The values of thermal conductivity for hot-pressed specimens of TiO_{2-x} with $x=0, 0.05, 0.10, 0.15$, and 0.20

measured by the static method at room temperature are tabulated in Table II together with the estimated values of the lattice contribution (λ_{lattice}) to thermal conductivity. The values of λ_{lattice} were estimated according to the Wiedemann–Franz approximation with the use of following equation:¹⁶

$$\lambda_{\text{lattice}} = \lambda_{\text{total}} - \lambda_{\text{electron}} = \lambda_{\text{total}} - \frac{L_0 T}{\rho} \left(\frac{k_B}{e} \right)^2,$$

where λ_{total} and $\lambda_{\text{electron}}$ stand, respectively, for total and lattice contribution (λ_{lattice}) to thermal conductivity, and k_B , e , L_0 stand, respectively, for Boltzmann's constant, electron charge, and a constant usually take a value of $\pi^2/3$ for metallic conductors. The value of λ_{lattice} decreases as the oxygen content decreases. Values of λ_{total} and λ_{lattice} are plotted, respectively, in Figs. 9(a) and 9(b) as a function of temperature. As seen in Fig. 9(b), the value of λ_{lattice} systematically decreases as the oxygen content decreases over the whole temperature range investigated.

V. DISCUSSION

A. Thermal conductivity

The lower value of thermal conductivity of hot-pressed stoichiometric TiO_2 when compared to rutile single crystal (6–8 W m/K) (Ref. 17) is due to phonon scattering by grain boundaries. This is further confirmed by the fact that the value of thermal conductivity of hot-pressed stoichiometric TiO_2 at room temperature increases from 5.18 W/K m for the average grain size of 0.51 μm to 5.88 W/K m for the grain size of 4.2 μm after further annealing at 1473 K for 72 h in air (Fig. 10). Of significance to note, however, is that although the average grain sizes for hot-pressed specimens of off-stoichiometric TiO_{2-x} , all of which are of the of Magnéli phases, are generally larger than that for the hot-pressed specimen of stoichiometric TiO_2 (Table I), the values of thermal conductivity are considerably smaller for off-stoichiometric TiO_{2-x} than for stoichiometric TiO_2 and that the value of thermal conductivity for hot-

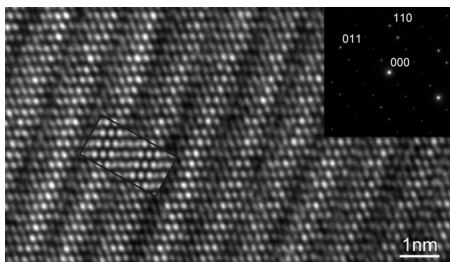


FIG. 8. A high-resolution TEM image of the Ti_6O_{11} Magnéli phase observed in the hot-pressed specimen of $\text{TiO}_{1.85}$. A inset is the simulated images of Ti_6O_{11} Magnéli phase (simulation condition: $\Delta f=-32$ nm, $t=30$ nm) using the reported atomic coordinates of Ti_6O_{11} (Ref. 11).

TABLE II. Values of thermal conductivity and lattice thermal conductivity measured by the static method at room temperature.

Nominal composition	Thermal conductivity (W/K m)	Lattice thermal conductivity (W/K m)
$\text{TiO}_{2.00}$	5.18	5.18
$\text{TiO}_{1.95}$	2.74	2.70
$\text{TiO}_{1.90}$	2.39	2.28
$\text{TiO}_{1.85}$	2.60	2.20
$\text{TiO}_{1.80}$	3.15	2.04

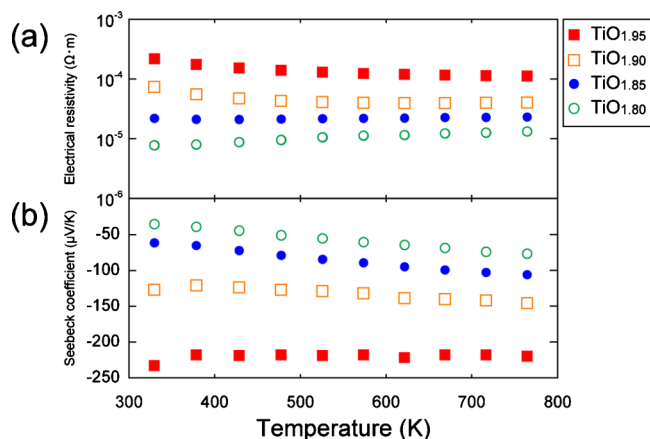


FIG. 9. (Color online) Temperature dependence of electrical resistivity (a) and Seebeck coefficient (b) for the hot-pressed specimens of TiO_{2-x} .

pressed specimens of off-stoichiometric TiO_{2-x} tends to decrease with the increase in the oxygen deficiency (Table II). Indeed, the value of lattice thermal conductivity of Ti_4O_7 (the hot-pressed specimen with $x=0.20$) decreases by more than 60% at room temperature and by about 40% at 773 K, when compared to stoichiometric TiO_2 . The decrease in lattice thermal conductivity with the increase in the oxygen deficiency observed for off-stoichiometric TiO_{2-x} may be concluded to be due to enhanced phonon scattering at the crystallographic shear plane, when judged from the variation in lattice thermal conductivity with the density of crystallographic shear planes (reciprocals of the spacing of crystallographic shear planes) as shown in Fig. 11. Both at room temperature and 773 K, the value of lattice thermal conductivity decreases with the increase in the density of the crystallographic shear plane. Assuming the Debye model, the mean free path for phonons can be evaluated for hot-pressed specimens of TiO_{2-x} with the use of the following equation and observed lattice thermal conductivity:

$$\lambda_{\text{lattice}} = \frac{1}{3} C_p \rho v l,$$

where C_p and v stand, respectively, for specific heat and sound velocity [$(6.91 \times 10^3 \text{ m/s})$ for TiO_2 (Ref. 18)], and l is

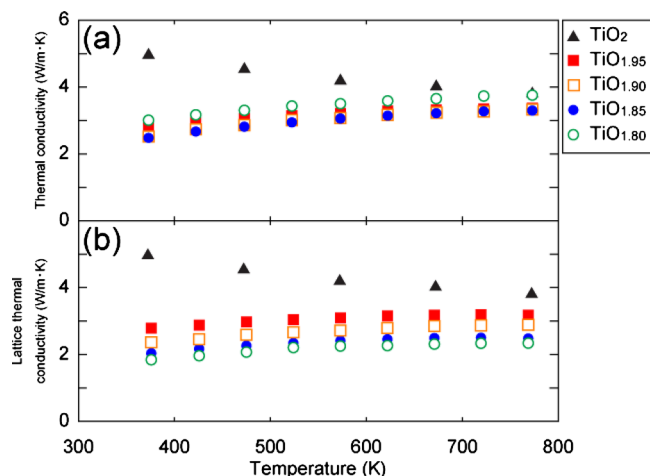


FIG. 10. (Color online) Temperature dependence of thermal conductivity (a) and lattice thermal conductivity (b) for the hot-pressed specimens of TiO_{2-x} .

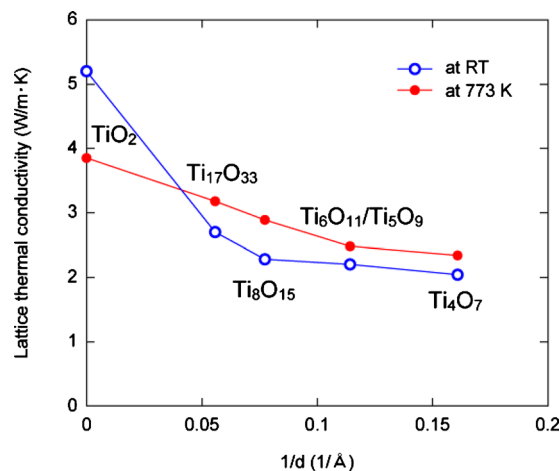


FIG. 11. (Color online) Shear plane spacing dependence of lattice thermal conductivity for Magnéli phase titanium oxides at room temperature and 773 K.

the mean free path for phonons. The value of phonon mean free path evaluated at room temperature for stoichiometric TiO_2 is 0.8 nm, which is comparable to the spacings (0.5–2 nm) for crystallographic shear planes observed for hot-pressed specimens of TiO_{2-x} . It is therefore obvious that the crystallographic shear planes in titanium oxides of the Magnéli phases can act as sources for phonon scattering. Not only the interatomic distances between titanium and neighboring oxygen ions but also their configurations (coordination) in the vicinity of the crystallographic shear plane are somewhat different from those in the mother (rutile) structure, which may lead to enhanced phonon scattering at the crystallographic shear plane, and thereby the reduced thermal conductivity in Magnéli phase titanium oxides.

B. Electrical conductivity

Assuming that the number of delocalized electrons is identical to that of conduction electrons, the electron mobility can be evaluated for hot-pressed specimens of TiO_{2-x} with the following equation:

$$\rho = \frac{1}{ne\mu},$$

where ρ , n , and μ stand, respectively, for electrical resistivity, electron charge, and electron mobility. As tabulated in Table III, the electron mobility for hot-pressed specimens of TiO_{2-x} increases with the increase in the oxygen deficiency. It is therefore evident that the crystallographic shear plane does not act as significant sources for electron scattering,

TABLE III. Reported conduction electron density (Ref. 19) and evaluated electron mobility for some hot-pressed specimens of TiO_{2-x} .

Nominal composition	Conduction electron density (g/cm^2)	Electron mobility ($\text{cm}^2/\text{V s}$)
$\text{TiO}_{1.90}$	4.60×10^{27}	0.184
$\text{TiO}_{1.85}$	9.90×10^{27}	0.289
$\text{TiO}_{1.80}$	1.54×10^{28}	0.526

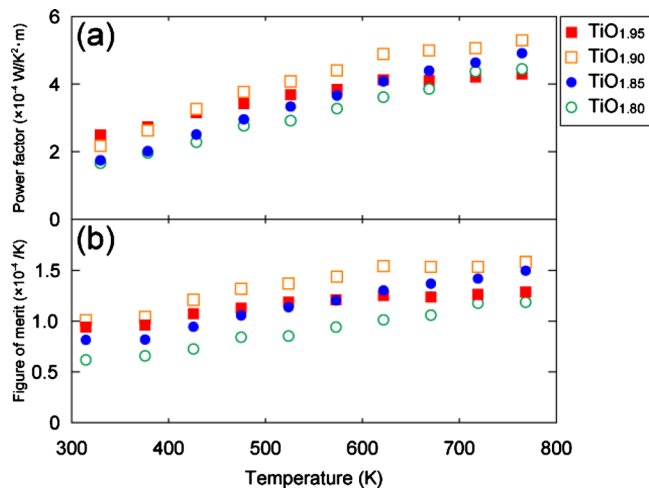


FIG. 12. (Color online) Values of power factor (α^2/ρ) and figure of merit ($\alpha^2/\rho\lambda$) obtained for hot-pressed specimens of TiO_{2-x} .

unlikely for phonon scattering. This is a favorable characteristic for thermoelectric materials.

C. Thermoelectric performance

Values of power factor (α^2/ρ) and figure of merit ($\alpha^2/\rho\lambda$) obtained for hot-pressed specimens of TiO_{2-x} are plotted, respectively, in Figs. 12(a) and 12(b) as a function of temperature. The maximum value ($5.3 \times 10^{-4} \text{ W/K}^2 \text{ m}$) of thermoelectric power factor is obtained at 773 K for the specimen with $x=0.10$. The maximum Z value (thermoelectric figure of merit) of $1.6 \times 10^{-4} \text{ K}^{-1}$ is obtained also at 773 K ($ZT=0.13$) for the specimen with $x=0.10$. Although the maximum Z value obtained in the present study for Magnéli phase titanium oxides are not surprisingly high when compared to nonoxide thermoelectric materials such as Bi_2Te_3 , SiGe , and so on, it is comparable to those obtained for other nonoriented polycrystalline oxides so far reported such as Y doped SrTiO_3 ,²⁰ $\text{ZnO-In}_2\text{O}_3$ (Ref. 21), and so on. Similar crystallographic shear structures have also been observed in TiO_2 doped with trivalent cations such as Cr and Fe .^{22–24} In view of the fact that the introduction of the crystallographic shear plane causes the reduction in thermal conductivity without significantly affecting electric conduction, the thermoelectric performance of Magnéli phase titanium oxides TiO_{2-x} may be further improved by introducing the crystallographic shear plane in a controlled manner with the use of trivalent cations.

VI. CONCLUSION

The thermoelectric properties of Magnéli phase titanium oxides $\text{Ti}_n\text{O}_{2n-1}$ have been investigated with the use of dense polycrystalline specimens prepared by conventional hot-pressing. The results obtained are summarized as follows:

(1) All off-stoichiometric specimens are of the Magnéli

phases, in which crystallographic shear planes are regularly introduced with the periodicity depending on the oxygen deficiency.

- (2) Electrical conduction is n-type for all specimens and the carrier concentration increases with the increase in the oxygen deficiency. The values of electrical resistivity and Seebeck coefficient therefore decrease with the increase in the oxygen deficiency. The value of lattice thermal conductivity, on the other hand, decreases the increase in the oxygen deficiency. When judged from the oxygen deficiency dependence of electrical resistivity and lattice thermal conductivity, the crystallographic shear plane is concluded to act as sources for phonon scattering but not for carrier scattering.
- (4) The largest value of thermoelectric figure of merit Z , $1.6 \times 10^{-4} \text{ K}^{-1}$ was obtained at 773 K for the hot-pressed specimen of $\text{TiO}_{1.90}$.

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