

## Metamagnetic Behavior and Kondo Breakdown in Heavy-Fermion CeFePO

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We report that nonmagnetic heavy-fermion (HF) iron oxypnictide CeFePO with two-dimensional XY-type anisotropy shows a metamagnetic behavior at the metamagnetic field  $H_M \simeq 4$  T perpendicular to the  $c$  axis and that a critical behavior is observed around  $H_M$ . Although the magnetic character is entirely different from that in other Ce-based HF metamagnets,  $H_M$  in these metamagnets is linearly proportional to the inverse of the effective mass, or to the temperature where the susceptibility shows a peak. This finding suggests that  $H_M$  is a magnetic field breaking the local Kondo singlet, and the critical behavior around  $H_M$  is driven by the Kondo breakdown accompanied by the Fermi-surface instability.

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Metamagnetism is represented by a sudden increase in magnetization with increasing an applied field. In heavy-fermion (HF) systems, CeRu<sub>2</sub>Si<sub>2</sub> with the tetragonal ThCr<sub>2</sub>Si<sub>2</sub> structure shows the metamagnetic behavior at about 7.7 T when a magnetic field ( $H$ ) is applied parallel to the  $c$  axis. Although various experiments as well as theoretical studies have been carried out [1,2], the mechanism is still controversial. In order to understand the metamagnetic behavior in HF systems, it might be desired to investigate new metamagnetic compounds.

The iron oxypnictide CeFePO is a related material of the iron-based superconductor LaFePO [3,4]. They possess the same two-dimensional layered structure, stacking Ce(La)O and FeP layers alternately. Brüning *et al.* reported that CeFePO is a magnetically nonordered HF metal with a Sommerfeld coefficient  $\gamma = 700$  mJ/(mol K<sup>2</sup>) [5]. At present, it is difficult to synthesize large single crystals of CeFePO for NMR measurements, but <sup>31</sup>P-NMR can probe in-plane and out-of-plane magnetic response separately using  $c$ -axis aligned polycrystalline samples. Here we report novel metamagnetic behavior observed in  $H \perp c$ , and suggest that metamagnetism of Ce-based HF compounds is driven by Kondo breakdown (drastic reduction of  $c$ - $f$  hybridization) as clarified experimentally.

The polycrystalline CeFePO was synthesized by solid-state reaction [4]. Basic properties are consistent with the previous report [5]. To measure anisotropic magnetic properties of CeFePO, the samples were uniaxially aligned using a magnetic field [6]. The polycrystalline CeFePO was ground into powder, mixed with stycast 1266, and was rotated in the external field of 1.4 T while the stycast cures. The  $c$  axis of the sample is nicely aligned, which is shown from the angle dependence of <sup>31</sup>P-NMR spectra (see in the inset of Fig. 1), and <sup>31</sup>P-NMR measurement was performed on the sample.

Figure 1 shows  $H$ -swept NMR spectra in  $H \parallel c$  and  $H \perp c$  obtained at 31.4 MHz and various temperatures ( $T$ ). The resonance peak for  $H \parallel c$  is almost  $T$  independent, but the peak for  $H \perp c$  shows the characteristic  $T$  dependence originating from  $\chi(T)$ . The Knight shift  $K_{\perp(\parallel)}$  was determined from the peak field of the <sup>31</sup>P NMR spectrum obtained in  $H$  perpendicular (parallel) to the  $c$  axis.  $K = 0$  was determined by reference material H<sub>3</sub>PO<sub>4</sub>.  $K_i(T, H)$  ( $i = \perp$  and  $\parallel$ ), which is the measure of the local susceptibility at the nuclear site, is defined as

$$K_i(T, H_{\text{res}}) = \left( \frac{H_0 - H_{\text{res}}}{H_{\text{res}}} \right)_{\omega=\omega_0} \propto \frac{M_i(T, H_{\text{res}})}{H_{\text{res}}}, \quad (1)$$

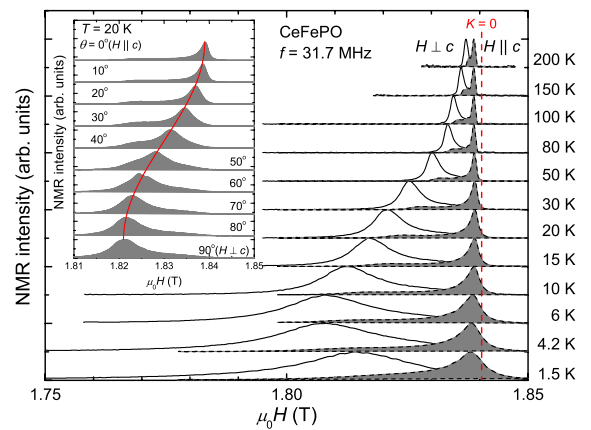


FIG. 1 (color online). (Main panel)  $T$  dependence of  $H$ -swept NMR spectra at 31.7 MHz for  $H \perp c$  (solid line) and  $H \parallel c$  (broken line).  $K = 0$  was determined by reference material H<sub>3</sub>PO<sub>4</sub>. (Inset) Angle dependence of  $H$ -swept NMR spectra at 31.7 MHz measured at 20 K.  $\theta$  is the angle between magnetic field and  $c$  axis. Solid line is corresponding to fitting line.

where  $H_{\text{res}}$  are magnetic fields at resonance peaks,  $H_0$  and  $\omega_0$  are the resonance field and frequency of bare  $^{31}\text{P}$  nucleus and have the relation of  $\omega_0 = \gamma_n H_0$  with gyromagnetic ratio  $\gamma_n$ , and  $M_i(T, H_{\text{res}})$  is the magnetization under  $H_{i,\text{res}}$  ( $i = \perp$  and  $\parallel$ ) at  $T$ .  $K_{\parallel}$  is almost independent of  $T$  and  $H$ , whereas  $K_{\perp}$  shows strong  $T$  dependence originating from the Curie-Weiss behavior of  $\chi(T)$  above 10 K as shown in Fig. 2(a). The anisotropic Knight shift suggests that static spin properties possess  $XY$ -type spin anisotropy. It should be noted that  $K_{\perp}$  exhibits  $H$  dependence below 4 K and above 2 T, indicative of a nonlinear relation between  $M_{\perp}$  and  $H$ . Using the hyperfine coupling constant  $^{31}\text{A}_{\text{hf}} = 0.2 \text{ T}/\mu_B$ , which is estimated from the plot between isotropic component of  $K$  and  $\chi(T)$  above 10 K (not shown), we can plot  $M_i(H)$  against  $H$  in Fig. 2(b).  $M_{\perp}(H)$  becomes superlinear against  $H$  at 0.1 K, which is the hallmarks of metamagnetism, whereas  $M_{\parallel}(H)$  is linear up to 6.2 T, which is again highly anisotropic.

Next, we focus on  $T$  and  $H$  dependence of low-energy spin dynamics probed with the nuclear spin-lattice relaxation rate  $(1/T_1)$ .  $1/T_1$  of  $^{31}\text{P}$  was measured at each resonance peak by the saturation-recovery method, and was uniquely determined by a single component in whole measured range. The inset of Fig. 3 shows  $T$  dependence of  $1/T_1 T$  at low field  $\mu_0 H \approx 0.6 \text{ T}$  parallel and perpendicular to the  $c$  axis. Below 1.5 K,  $1/T_1 T$  as well as  $K$  along both directions becomes constant, indicative of the formation of a Fermi-liquid (FL) state of heavy electrons. In general,  $1/T_1$  probes spin fluctuations perpendicular to applied  $H$ , and thus  $1/T_1$  in  $H \parallel c$  and  $H \perp c$  are described as

$$\begin{aligned} (1/T_1)_{H\parallel c} &= 2(\mu_0 \gamma_n)^2 \sum_q |H_{\perp}(q, \omega_{\text{res}})|^2 \\ &\propto 2A^2 \sum_q |S_{\perp}(q, \omega \sim 0)|^2, \quad \text{and} \\ (1/T_1)_{H\perp c} &= (\mu_0 \gamma_n)^2 \sum_q [|H_{\parallel}(q, \omega_{\text{res}})|^2 + |H_{\perp}(q, \omega_{\text{res}})|^2] \\ &\propto A^2 \sum_q [|S_{\parallel}(q, \omega \sim 0)|^2 + |S_{\perp}(q, \omega \sim 0)|^2]. \end{aligned} \quad (2)$$

Here  $|X(\omega)|$  denotes the power spectral density of a time-dependent random variable  $X(t)$ , and  $A$  is assumed to be  $q$  independent due to the metallic state. From these equations, we can decompose spin fluctuations along each direction as shown in the main panel of Fig. 3.  $\sum_q |S_{\perp}(q, \omega \sim 0)|^2$  is dominant at low  $T$ , since  $(1/T_1 T)_{H\parallel c}$  is almost twice larger than  $(1/T_1 T)_{H\perp c}$ . This indicates that the spin dynamics also possess  $XY$ -type anisotropy. The  $XY$ -type spin fluctuations have the predominance of ferromagnetic (FM) correlations as inferred from the Korringa relation between  $(1/T_1 T)_{H\parallel c}$  and  $K_{\perp}$  in low- $T$  FL state, which is consistent with the previous  $^{31}\text{P}$ -NMR result [5] and with the experimental facts that CeFePO is close to FM instability [7,8].

The evolution of the spin dynamics against  $H$  was investigated for both directions. Figure 4 shows  $T$  dependence of  $(1/T_1 T)_{H\perp c}$  below 4 T (approximately the metamagnetic field,  $H_M$ ) (a) and above 4 T (b). Although  $(1/T_1 T)_{H\parallel c}$  does not depend on  $H$  up to 6.2 T as shown in the inset of Fig. 3,  $(1/T_1 T)_{H\perp c}$  changes significantly by  $H$  as shown in Figs. 4(a) and 4(b).  $H$  dependence of

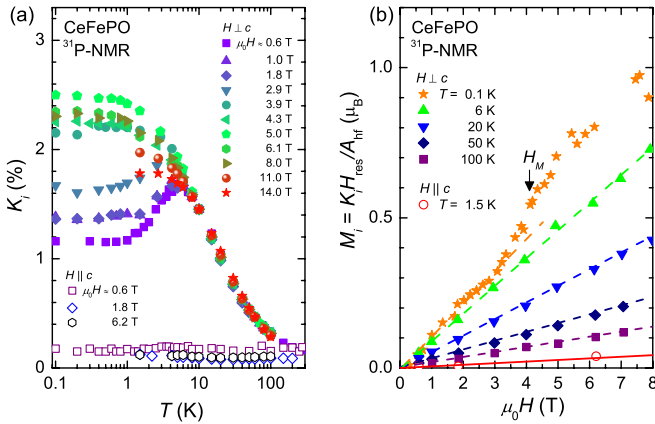


FIG. 2 (color online). (a)  $T$  dependence of the Knight shift determined at the peaks of  $H \perp c$  and  $H \parallel c$  spectra obtained at various  $H$ . Strong anisotropy of Knight shift suggests that static spin properties possess  $XY$ -type spin anisotropy. (b)  $H$  dependence of magnetization  $M_i(H)$  ( $i = \perp$  and  $\parallel$ ) using the relation of  $M_i(H) = K_i(H)H_{\text{res}}/A_{\text{hf}}$ . Solid and broken lines are guide to eyes.  $M_{\perp}(H)$  suddenly increases with increasing  $H$  and deviates from linear relation in the field range of 3–5 T, which is a definition of a metamagnetic behavior, while such a behavior was not observed in  $M_{\parallel}(H)$  up to 6.2 T and down to 1.5 K.

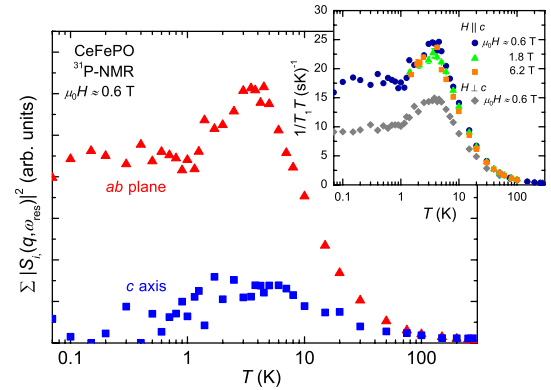


FIG. 3 (color online). (Main panel)  $T$  dependence of low-energy spin fluctuations parallel and perpendicular to the  $c$  axis at  $\approx 0.6 \text{ T}$  evaluated with  $1/T_1 T$  measured in  $H \perp c$  and  $H \parallel c$  [see Eq. (2)]. The in-plane spin fluctuations are dominant at low  $T$ , suggesting that the spin dynamics also possess  $XY$ -type anisotropy. (Inset)  $T$  dependence of  $1/T_1 T$  at 10.3 MHz ( $\approx 0.6 \text{ T}$ ) for  $H \perp c$  and at 10.3 MHz ( $\approx 0.6 \text{ T}$ ), 31.7 MHz ( $\approx 1.8 \text{ T}$ ), and 107.2 MHz ( $\approx 6.2 \text{ T}$ ) for  $H \parallel c$ .  $(1/T_1 T)_{H\parallel c}$  is independent of  $H$  up to 6.2 T.

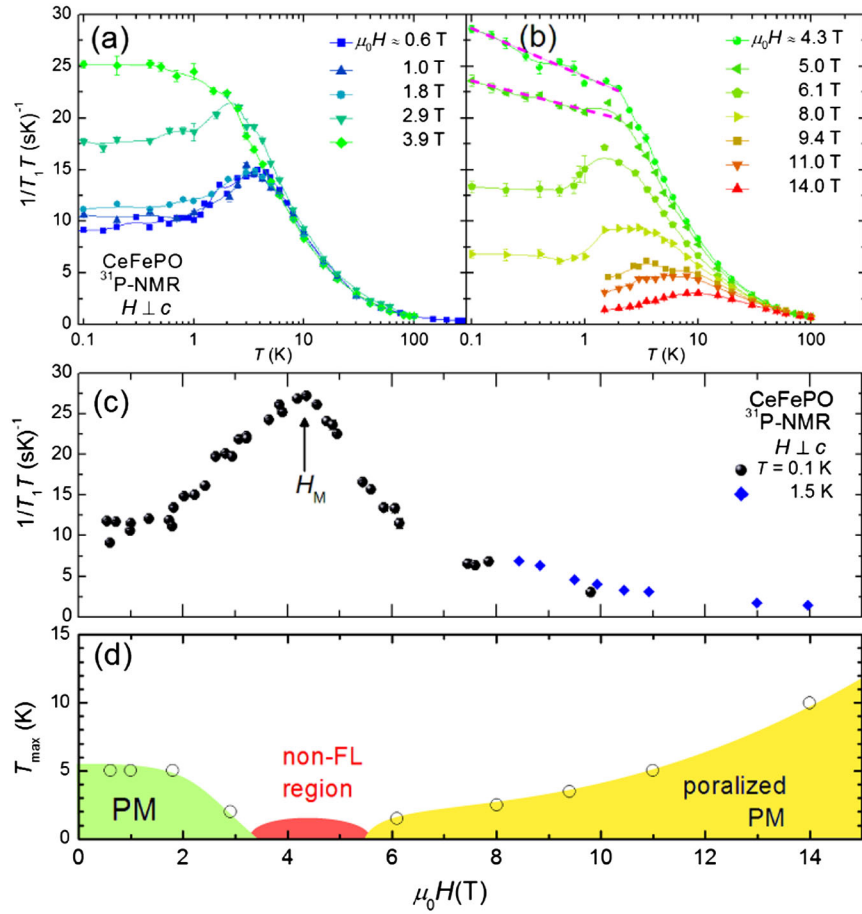


FIG. 4 (color online).  $T$  dependence of  $(1/T_1T)_{H\perp c}$  below 4 T (a), and above 4 T (b). (c)  $H$  dependence of  $(1/T_1T)_{H\perp c}$  at low  $T$ .  $(1/T_1T)_{H\perp c}$  shows a distinct maximum at around  $H_M$ , indicating the enhancement of  $N(E_F)$  related to metamagnetic anomaly. (d)  $H$ - $T$  phase diagram defined by  $T_{\max}$  where  $(1/T_1T)_{H\perp c}$  shows a maximum. Non-FL behavior characterized by continuous increase in  $(1/T_1T)_{H\perp c}$  with decreasing  $T$  [broken lines are shown in (b)] was observed in a narrow field region intervening between low-field paramagnetic (PM) state and high-field polarized PM state above 6 T.

$(1/T_1T)_{H\perp c}$  at 0.1 and 1.5 K is shown in Fig. 4(c).  $(1/T_1T)_{H\perp c}$  shows a distinct maximum at  $H_M$ , suggesting that the enhancement of the density of states (DOS) is related to metamagnetic behavior. If we assume that  $1/T_1T \propto N(E_F)^2$ ,  $N(E_F)$  at  $H_M$  is almost 1.5 times larger than  $N(E_F)$  at 0 T. However, it is noteworthy that non-FL behavior characterized by a continuous increase in  $(1/T_1T)_{H\perp c}$  with decreasing  $T$  was observed down to 100 mK [ $(1/T_1T)_{H\perp c} \sim -\log T$ ] in 4.3 T  $< \mu_0H < 5$  T intervening between low-field paramagnetic (PM) state and high-field polarized PM state above 6 T. In the high-field polarized state,  $(1/T_1T)_{H\perp c}$  decreases with increasing  $H$  and  $(1/T_1T)_{H\perp c}$  at 14 T shows almost the same value as (LaCa)FePO [ $\approx 1.5$  (sK)<sup>-1</sup>] without 4*f* electrons [9]. The  $H$  variation of  $(1/T_1T)_{H\perp c}$ , reflecting the evolution of DOS at the Fermi level with  $H$ , strongly suggests the evolution of the Fermi surfaces (FSs) by  $H$ . It is noted that such a significant  $H$  dependence was not reported in the previous specific-heat measurement [5]. This would be because the magnetic field is applied in the various angles against the  $c$  axis, and suggests that the metamagnetic behavior

would be observed when  $H$  is exactly perpendicular to the  $c$  axis.

To investigate such evolution of FSs by  $H$ , we performed the *ab initio* band-structure calculation in the paramagnetic state of CeFePO by using the WIEN2K package [10]. FSs in the low-field region are composed of itinerant Ce 4*f* electrons as shown in Fig. 5(a). The large FS shows the characteristic neck structures around  $X$ - $R$  at the Brillouin zone boundary, at which boundary electrons have small Fermi velocity or heavy electron mass. The orbital character is dominated by the  $j_z = \pm 1/2$  component in the  $j = 5/2$  multiplet of 4*f* orbitals, as seen in Figs. 5(a) and 5(c) [11]. These features of Fermi surface imply that the low-field HF state possesses the small  $q$  magnetic correlations and their in-plane component is much larger than the out-of-plane component, in good agreement with the experimental results. The band calculation also shows that applied field pinches off the neck FSs around  $R$  and  $X$  in order, that is, “the field-induced Lifshitz transition” appears. This is accompanied by a drastic change in DOS at the Fermi level, which can be a driving force for the

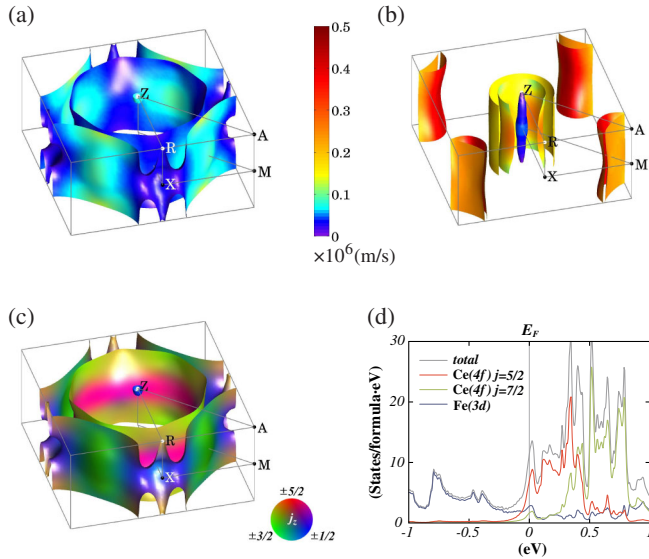


FIG. 5 (color online). Fermi surfaces (FSs) calculated with the *ab initio* band-structure calculation as Ce-4*f* electrons are itinerant (a), or localized (b), where the Fermi velocity is mapped on the FSs. (c) shows the FS colored by the  $j_z$  character in the  $j = 5/2$  multiplet of 4*f* orbitals, where  $j$  is the total angular momentum. (d) the partial density of states. The Fermi level corresponds to 0 eV.

metamagnetic transition and non-FL behavior around  $H_M$  [12,13]. With applying higher  $H$ , 4*f* electrons are localized, and thus the FSs become small. The resultant FSs are shown in Fig. 5(b), familiar in the iron-based superconductors [14]. Thus the scenario of the field-induced Lifshitz transition can link with the nature in the metamagnetic transition in CeFePO.

Here, we compare the present results with CeRu<sub>2</sub>Si<sub>2</sub>, one of the most well-known metamagnetic compounds. Although both compounds show similar  $T$  and  $H$  dependence of Knight shift and  $1/T_1T$  in  $H$  parallel to the magnetic easy axis [15], as well as the similar  $H$ - $T$  phase diagram defined by  $T_{\max}$  [16] as shown in Fig. 4(d), magnetic properties are quite different. For example, magnetic easy axis is different between CeFePO and CeRu<sub>2</sub>Si<sub>2</sub>: CeFePO possesses two-dimensional XY-type spin anisotropy, whereas CeRu<sub>2</sub>Si<sub>2</sub> possesses Ising-type spin anisotropy [17]. As a result, the ground states of the crystal-field level are different and their metamagnetic behavior is observed in different directions. In addition, dominant magnetic fluctuations in CeFePO differ from those in CeRu<sub>2</sub>Si<sub>2</sub>. It is reported that CeRu<sub>2</sub>Si<sub>2</sub> is located close to antiferromagnetic instability accompanied with FM fluctuations [18,19].

Figure 6 shows the relationship between the metamagnetic field  $H_M$  and the temperature where the bulk susceptibility shows a maximum  $T_{\max}$  or inverse of Sommerfeld coefficient  $\gamma$  at  $H = 0$  for CeCu<sub>6</sub>, CeFePO, and CeRu<sub>2</sub>Si<sub>2</sub> with doped and pressurized systems [5,17,20–23]. It deserves mention that the linear relation holds between the

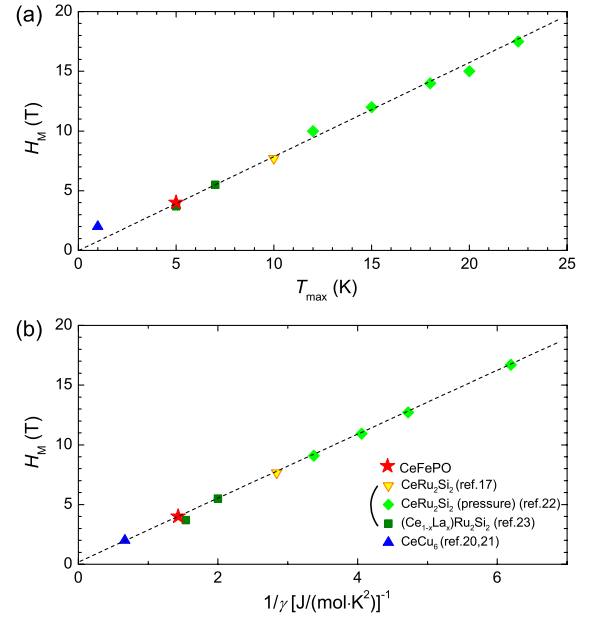


FIG. 6 (color online). (a) Values of metamagnetic fields are plotted against  $T_{\max}$  determined from a maximum in static susceptibility (a) or inverse of Sommerfeld coefficient  $\gamma$  at  $H = 0$  (b) in CeFePO, CeCu<sub>6</sub>, and CeRu<sub>2</sub>Si<sub>2</sub> with pressurized and La-doped system. Broken lines are a guide to eyes. A linear relation holds between two quantities, although three compounds possess quite different crystal structures and magnetic properties, indicating that  $H_M$  is linked with the local Kondo singlet energy  $T_{\max}$ .

two quantities, notwithstanding that the three compounds possess totally different crystal structures and magnetic properties. Since  $T_{\max}$  is regarded as a Kondo temperature  $T_K$  and roughly speaking, the relation of  $\gamma T_K = \text{const}$  holds in the HF state, these facts indicate that  $H_M$  is merely related to the local Kondo singlet energy  $T_{\max}$  and is not linked with the magnetic fluctuations originating from the intersite coupling between neighboring Ce ions and/or the nesting between the “large” FS. The experimental fact that  $H_M$  is linearly proportional to  $T_K$  in Fig. 6 strongly suggests that the metamagnetic behavior is linked with the Kondo breakdown [24]. Therefore, in the Ce-based metamagnets, the Kondo breakdown and the Fermi-surface instability accompanied by the drastic change of DOS occur almost simultaneously around  $H_M$ , which can induce novel non-FL behavior.

In summary, we performed <sup>31</sup>P-NMR in the uniaxially aligned CeFePO and found that CeFePO possesses two-dimensional XY-type FM fluctuations, and shows metamagnetic behavior when  $H$  is applied to  $H \perp c$  below 5 K, accompanied with non-FL behavior around metamagnetic field  $H_M \approx 4$  T. As far as we know, this is a first example that the metamagnetic behavior occurs in a nonmagnetic Ce-based HF compound with the XY-type spin anisotropy. From the band calculation and the comparison with other Ce-based metamagnets, we



claim that  $H_M$  is a magnetic field breaking the local Kondo singlet, which is determined with the intrasite coupling between Ce-4*f* and conduction electrons, and that the FSs change drastically due to the Kondo breakdown.

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