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Research Article

Subcritical Multiplication Parameters of the Accelerator-Driven System with 100 MeV Protons at the Kyoto University Critical Assembly

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Basic experiments on the accelerator-driven system (ADS) at the Kyoto University Critical Assembly are carried out by combining a solid-moderated and -reflected core with the fixed-field alternating gradient accelerator. The reaction rates are measured by the foil activation method to obtain the subcritical multiplication parameters. The numerical calculations are conducted with the use of MCNPX and JENDL/HE-2007 to evaluate the reaction rates of activation foils set in the core region and at the location of the target. Here, a comparison between the measured and calculated eigenvalues reveals a relative difference of around 10% in C/E values. A special mention is made of the fact that the reaction rate analyses in the subcritical systems demonstrate apparently the actual effect of moving the tungsten target into the core on neutron multiplication. A series of further ADS experiments with 100 MeV protons needs to be carried out to evaluate the accuracy of subcritical multiplication parameters.

1. Introduction

The accelerator-driven system (ADS) is a hybrid technique combining a reactor core and an accelerator, which has been used worldwide in research and development of nuclear transmutation of minor actinides (MAs), long-lived fission products (LLFPs), and next-generation neutron sources. In ADS, a large number of high-energy neutrons are generated directly at a heavy metal target when high-energy protons produced by the accelerator are injected onto the target. The high-energy neutrons can be utilized for maintaining nuclear fission reactions in the reactor core and achieving the purposes of the introduction of ADS. The current research on ADS involved mainly an experimental feasibility study with the use of critical assemblies and test facilities: MASURCA [1–3], YALINA-booster and -thermal [4–6], VENUS-1 [7], and the Kyoto University Critical Assembly (KUCA) [8–14]. Moreover, numerical simulations [15–20] were executed by the deterministic and stochastic approaches for the evaluation of MAs and LLFPs in ADS. The new ADS test facility of GUINEVERE [21] is being commissioned to start actual operation in subcritical states after the first critical experiments.

The Kyoto University Research Reactor Institute is pursuing an innovative research program (Kart & Lab.: Kumatori Accelerator-Driven Reactor Test Facility & Innovation Research Laboratory) to develop the fixed-field alternating gradient (FFAG) [22–24] accelerator and to establish a new neutron source by ADS in combination with KUCA and the FFAG accelerator. With the coupling of the KUCA core and the FFAG accelerator, the spallation neutrons generated by 100 MeV proton beams have been successfully injected into the uranium-loaded [25] KUCA core. In the first injection of spallation neutrons, the proton beam intensity and shape were low and poor, respectively, resulting in large statistical errors in the experiments, such as the reaction rate analyses. On the other hand, the spallation neutrons generated at the location of the tungsten target position were expected to make a reasonable contribution to neutron multiplication in the core region; however, the disadvantage of setting the target outside the core was low neutron generation in the core region by high-energy proton beams.
To resolve this drawback and enhance neutron multiplication, additional ADS experiments on the reaction rates were carried out by moving the tungsten target to another location in the subcritical core. Here, special note was taken of the effect of moving the target from the original location on subcritical multiplication parameters, including the neutron multiplication and the subcritical multiplication factor. The numerical analyses of the subcritical experiments were executed with the use of the Monte Carlo calculation code MCNPX [26] together with the nuclear data library JENDL/HE-2007 [27, 28]. The main objective of this study was to examine the accuracy of the subcritical multiplication parameters in the subcritical configurations of ADS by comparing the measured and calculated reaction rates. The preliminary (previous) experiments with high-energy neutrons generated by 100 MeV protons from the FFAG accelerator are shown in Section 2 and include descriptions of the core configuration; experimental and numerical results. The results of basic (additional) experiments on moving the target are presented in Section 3, and the conclusions are summarized in Section 4.

2. Preliminary ADS Experiments with 100 MeV Protons

2.1. Core Configuration. Among three cores designated A, B, and C at KUCA, A and B are polyethylene solid-moderated and solid-reflected cores, and C is a light water-moderated and light water-reflected one. The three cores are operated at a low mW power in the normal operating state, whereas the maximum power is 100 W. The preliminary ADS experiments were carried out in the A-core (Figure 1), which contains polyethylene reflector rods and three different fuel assemblies: normal, SV, and partial fuel assemblies (Figures 2(a), 2(b), and 2(c), resp.). The normal fuel assembly is composed of 36-unit cells and upper and lower polyethylene blocks about 591 and 537 mm long, respectively, in an aluminum sheath 54 × 54 × 1520 mm3. For the normal and partial fuel assemblies, a unit cell in the fuel region is composed of a highly enriched uranium-aluminum fuel plate 1.59 mm (1/16″), and polyethylene plates 3.18 mm (1/8″) and 6.35 mm (1/4″). The numeral 14 corresponds to the number of fuel plates in the partial fuel assembly used to reach the criticality mass. The horizontal dimensions of all fuel and polyethylene plates are 5.08 × 5.08 mm2 (2′′ × 2′′).

The tungsten target located outside the core is not easily moved to the center of the core because control and safety rods are fixed in the core and function as the control driving system. The neutron guide composed of several shielding materials, including iron (Fe), boron (B), polyethylene, the beam duct, and a special fuel assembly with a void (SV, Figure 2(b)), are installed. In the neutron guide, the role of the SV assemblies is to direct the highest number possible of the high-energy neutrons generated in the target to the center of the fuel region, in order to improve neutron multiplication. Moreover, to collimate the high-energy neutrons, it was necessary to reduce the thermal component moderated in the reflector region before their reaching the fuel region. This reduction was achieved by shielding unnecessary fast neutrons and by capturing parasite thermal neutrons. For deflecting unnecessary fast neutrons, the close vicinity in front of the target included the Fe block around the guide void to shield the fast neutrons from inelastic scattering. For capturing parasite thermal neutrons, polyethylene blocks containing 10 wt% B around the guide void were set around the Fe shielding near the target and in the two rows next to the assemblies. The rest of the neutron guide consisted of polyethylene assemblies and one void space. Details of the neutron guide were as described in [8, 9].

2.2. Experimental Analyses. In the subcritical experiments, gold (197Au) and indium (115In) foils were selected as normalization factors for monitoring reactor power in the core and neutron source generation at the target, respectively. The difference between the normalization factors in the core and at the target was attributable to the sensitivity of the thermal neutrons and the high-energy neutrons, respectively. The reaction rates of the 115In wire (1.5 mm diameter and 750 mm long) in the core and the 115In foil (10 × 10 × 1 mm3) at the target were normalized by those of the 197Au foil (8 mm diameter and 0.05 mm thick) emitted by 197Au(n, γ)198Au reactions attached in the core center (O, 15; Figure 1), and of the 115In foil emitted by 115In(n, n′)115mIn reactions attached at the original location of the target, respectively. The experimental error in each activation foil was estimated to be about 5%, including the statistical error of γ-ray counts and the full width at half maximum (FWHM) of the γ-ray spectrum peak. The experiments were carried out within subcriticality level 770 pcm (0.77%Δk/k). Here, the subcritical state was attained by the full insertion of C1, C2, and C3 control rods and the full withdrawal of S4, S5, and S6 safety rods (Figure 1). The measured subcriticality was obtained from the combination of both the control and safety rod worth by the rod drop method and its calibration curve by the positive period method. In the KUCA core, the subcriticality was attained by the full insertion of all control and safety rods within 2,000 pcm (0.20%Δk/k; keff = 0.98), and the representative subcriticality level around 3,000 pcm is achieved by the removal of fuel rods in the ADS experiments. When the representative subcriticality level is obtained, as a result, the change in the core characteristics, including the control rod worth, the neutron flux shape and the neutron spectrum, is apparently observed in comparison with before and after the removal of fuel rods. Therefore, the ADS experiments were carried out within the subcritical level attained by inserting the control and safety rods to maintain the core characteristics from the viewpoint of reactor physics.

The effect of the subcritical multiplication parameters was evaluated by thermal neutron flux distribution estimated through the horizontal measurement of 115In(n, γ)116mIn reaction rates by activation analysis of the In wire. The wire was set in an aluminum guide tube within the 3 mm
The subcriticality calculations were executed with the use of the Monte Carlo multiparticle transport code, MCNPX, in combination with nuclear data library JENDL/HE-2007. The irradiation foils and the In wire were included in the simulated geometry and transport calculation because the effects of their reactivity are not negligible; reaction rates were deduced from tallies taken in the reaction rate experiments. Although better in the core region, an overall statistical error of 5% remained in the reaction rate in the present results. The results of eigenvalue calculations were obtained after 1,000 active cycles of 50,000 histories each. The deduced subcriticalities had statistical errors of 10 pcm ($0.01\%\Delta k/k$). The fixed-source calculations were executed by a total of $1.0 \times 10^8$ histories, which led to a statistical error of less than 5% in the reaction rates.

The results of measured and calculated subcriticalities are presented in Table I. A comparison between the experiments and the calculations demonstrated the ability of MCNPX calculations to reproduce the subcriticality level to within 2% of the C/E (calculation/experiment) value. A comparison made of the measured and the calculated reaction rate distributions to validate the calculation method demonstrated that the calculated reaction rate distribution
(Figure 3) agreed approximately with the experimental one within the statistical errors in the experiments; however, the experimental errors were considerably larger than those of the calculations. These larger errors were attributable to the status of the proton beams, including the weak beam intensity and the poor beam shape at the target.

### Table 1: Comparison between the measured and calculated subcriticalities obtained from the experiments (Figure 1) and calculations (MCNPX with JENDL/HE-2007).

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<th>Calculation (pcm)</th>
<th>Experiment (pcm)</th>
<th>C/E</th>
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<tr>
<td>773</td>
<td>760</td>
<td>1.02</td>
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#### 3. Basic ADS Experiments with 100 MeV Protons

The neutron spectrum analyses were conducted numerically for investigating anticipated high-energy neutrons at each location for the injection of the high-energy protons before the basic experiments, as shown in Figure 4. The high-energy neutrons were attained in front of target location (A, 15) and were dominant over the region of a few MeV neutrons of energy. The further the distance was from the tungsten target, including locations (E, 15), (J, 15), and (O, 15), the more thermalized the neutron spectrum is: this fact demonstrated that the high-energy neutrons generated at the location of the original target should be little affected upon neutron multiplication in the core, and the thermal neutrons
moderated in the reflector region were compared to be less than other locations.

For optimizing the effect of moving the target from its original location, additional experiments were carried out in the same core (Figure 5) as in a previous study described in Section 2: the composition of the neutron guide was made partly of lead (Pb) instead of Fe, thereby attaining neutron multiplication around the target region by the injection of high-energy neutrons into the shielding material, Pb. Also, the effect of moving the target was investigated through analyses of neutron multiplication, as in the previous study [29] at KUCA. In the experiments, the $^{115}$In($n$, $\gamma$)$^{116m}$In reaction rates were measured in the core region, and neutron multiplication was deduced by the reaction rate distribution, when the tungsten target was moved from the original location to another one close to the core center. Finally the actual effect of moving the target was examined by comparing the experimental and numerical analyses. As in Section 3, the experiments were carried out around subcriticality level 750 pcm (0.75$\%\Delta k/k$), and subcriticality was attained and then measured. Notably, the 100 MeV protons generated from the accelerator were injected into a subcritical system under the following parameters: 30 pA beam intensity; 30 Hz repetition rate; 200 ns pulsed width; $1.0 \times 10^7$ 1/s neutron yield.

3.1. Subcriticality. The numerical calculations were executed with the use of MCNPX together with the JENDL/HE-2007 library. The numerical evaluation of subcriticality by JENDL/HE-2007 was in agreement with experimental data and within a relative difference of 10$\%$ (Table 2), whereas the accuracy of eigenvalue calculations was not good compared with the previous analyses presented in Section 2. By MCNPX, the eigenvalue calculations were executed for 5,000 active cycles of 10,000 histories. The subcriticalities in the eigenvalue calculations had statistical errors within 10 pcm (0.01$\%\Delta k/k$). Since the reactivity effects of activation foils and wire in the core are not negligible, they were included in the simulated geometry and transport calculations.

3.2. Reaction Rate Distribution. The calculated reaction rate was obtained by evaluating the volume tallies of activation foils. The statistical error of the reaction rates in the fixed-source calculations was within 5$\%$ after a total of $1.0 \times 10^8$ histories. The difference in the experimental results along region (13-14, A–P; Figure 5) is shown in Figure 6(a), by changing the location of the tungsten target to another one: in front of the original target (A, 15); between the target and the core (G, 15); in front of the fuel region (K, 15). From the experimental results in Figure 6(a), the reaction rate distribution was observed to be high in the SV and fuel regions, when the tungsten target was set at location (G, 15), although the core configuration of reaction rates varied in the SV and fuel regions. Comparison of the experimental and numerical results revealed the approximate reconstruction of the $^{115}$In($n$, $\gamma$)$^{116m}$In reaction rates by MCNPX with JNEDL/HE-2007 shown in Figure 6(b), whereas the discrepancy was found to be in some regions of (G, 15) by the difference in experimental results in the core configuration.

3.3. Neutron Multiplication and Subcritical Multiplication Factor. Neutron multiplication $M$ and subcritical multiplication factor $k_s$ were experimentally and numerically analyzed on the basis of the accuracy in Section 3.2, related to

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<th>Case</th>
<th>Calculation (pcm)</th>
<th>Experiment (pcm)</th>
<th>C/E</th>
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</thead>
<tbody>
<tr>
<td>(A, 15)</td>
<td>706</td>
<td>772</td>
<td>0.91</td>
</tr>
<tr>
<td>(G, 15)</td>
<td>659</td>
<td>737</td>
<td>0.89</td>
</tr>
<tr>
<td>(K, 15)</td>
<td>674</td>
<td>740</td>
<td>0.91</td>
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Table 2: Comparison between the measured and calculated subcriticalities obtained from the experiments (Figure 5) and calculations (MCNPX with JENDL/HE-2007).
the subcritical multiplication parameters. The methodology of the theoretical basis used was as briefly described [29].

In the ADS study on the subcritical system, the neutron multiplication $M$ is defined as the ratio of total fission neutrons $F$ and the external neutron source rates $S$, to the rate of external neutron source as follows:

$$M = \frac{F}{S}. \quad (1)$$

The neutron multiplication $M$ is also expressed by the subcritical multiplication factor $k_s$, which is defined as the ratio of the fission neutrons to the total neutrons in the system by the fission and source neutrons as follows:

$$M = \frac{1}{1 - k_s}. \quad (2)$$

In (1) and (2), $k_s$ can be expressed by $F$ and $S$ as follows:

$$k_s = \frac{F}{F + S}. \quad (3)$$

Assuming that the fission reaction rate $F$ is independent of one-dimensional ($x$-direction) in the thermal neutron field, the total fission neutrons can be expressed approximately by the In reaction rates $R_{1n}$ of $^{115}$In($n, \gamma$)$^{116m}$In reactions as follows:

$$F = \int_V \int_0^\infty \nu \Sigma_f(x, E) \phi_s(x, E) dE dx,$$

$$\approx \int_x R_{1n}(x, y_0, z_0) dx,$$  

where $V$ indicates the whole volume in the system, $\nu$ the average number of fission neutrons per fission reaction, $\Sigma_f$
the fission cross-section, $\phi$, the neutron flux at position $r$ with energy $E$ in the presence of an external source, and $a$ the In wire along the fuel regions (SV and fuel regions; Figure 5) in the core. The external neutron source rate $S$ can be expressed approximately by the In reaction rates $R_{fn}$ of $^{115}\text{In}(n, n')^{116}\text{mIn}$ reactions in the same manner as that of (4) as follows:

$$S = \int_{\gamma}^{115}\text{In}(n, E) dE \approx \int_{r_e} R_{fn}(r) dr,$$  \hspace{1cm} (5)

where $s(r_e, E)$ indicates the external neutron source rates at position $r_e$ with energy $E$, and $r_e$ the position of external neutron source. The validity of approximation and the applicability of the methodology mentioned above have already been demonstrated in the previous study [29].

Finally, using (4) and (5), the neutron multiplication $M$ and subcritical multiplication factor $k_s$ in (1) and (3), respectively, can be expressed approximately as follows:

$$M \approx \int_{f} R_{fn}(x, y_0, z_0) dx \int_{r_e} R_{fn}(r) dr + 1,$$  \hspace{1cm} (6)

$$k_s \approx \int_{f} R_{fn}(x, y_0, z_0) dx \int_{r_e} R_{fn}(r) dr,$$  \hspace{1cm} (7)

The measured reaction rates of the In wire (1.5 mm diameter and 750 mm long) emitted by $^{115}\text{In}(n, \gamma)^{116}\text{mIn}$ reactions in the core were normalized by those of the $^{197}\text{Au}$ foil (8 mm diameter and 0.05 mm thick) emitted by $^{197}\text{Au}(n, \gamma)^{198}\text{Au}$ reactions attached at the core center (O, 15; Figure 5), and the reaction rates of the In foil (10 $\times$ 10 $\times$ 1 mm$^3$) emitted by $^{115}\text{In}(n, n')^{115m}\text{In}$ reactions moving the target were normalized by those of the $^{115}\text{In}$ foil (10 $\times$ 10 $\times$ 1 mm$^3$) emitted by $^{115}\text{In}(n, n')^{115m}\text{In}$ reactions attached at the original location of the target. The experimental error in each activation foil was estimated to be about 5%, including the statistical error of $\gamma$-ray counts and FWHM of the $\gamma$-ray spectrum peak. The calculated reaction rates of the In wire and the Au foil in the core were included in the simulated geometry and transport calculations and deduced from tallies taken in the fixed-source calculations. Also the calculated reaction rates of the In foil at the target was obtained by the same manner of the previous fixed source calculations, modeling the proton injection on the tungsten target.

The C/E value of the experiments and calculations of fission and source terms in (4) and (5), respectively, is shown in Table 3. Comparing with absolute values, the accuracy of fission term was within a relative difference of 20%, and that of the source term was well within the allowance for experimental error. The discrepancy between the measured and the calculated fission terms was caused mainly by the uncertainties of experimental values obtained from the reaction rates of the In wire especially in locations (G, 15) and (K, 15), because locations (G, 15) and (K, 15) were far from that of original target, and the proton weak and poor beams were in intensity and shape, respectively. As a result, it was considered that the In wire was not sufficiently activated to obtain the information on the thermal neutrons. As shown in Table 4, the neutron multiplication was considered to involve a large discrepancy caused by the evaluation of the C/E values of fission and source terms; inversely, the subcritical multiplication factor was considered fairly good in the evaluation of C/E values. The constant values of the measured and the calculated $k_s$ demonstrated that the source term was not contributed largely to that of $k_s$, since the external source was located outside the core: the values of $M$ and $k_s$ in (1) and (2), respectively, were remarkably
dependent on that of F in (4), because of the location of the target outside the core. While the accuracy of the neutron multiplication was attributable to the experimental variation of reaction rates of the In wire, the actual effect of setting the tungsten target at location (G, 15) was found to be more significant than setting the target in the original location.

### 4. Conclusions

The ADS experiments with 100 MeV protons were carried out at KUCA to evaluate the subcritical multiplication parameters using the reaction rates. Comparison of the results of the experiments and the calculations by MCNPX with JENDL/HE-2007 revealed the following.

In the first injection experiments, the subcriticality C/E values of the experiments and the calculations were in fairly good agreement within a relative difference of 2%, and the calculated reaction rate distribution reconstructed the experimental one, although the proton beams were observed to be weak in intensity and poor in shape at the target. In the basic experiments, the notable effect of moving the target from the original location was clearly revealed in the analyses of the subcritical multiplication parameters for attaining further neutron multiplication in the core.

Further ADS study at KUCA needs to be conducted to investigate experimentally the effect of the subcritical multiplication parameters presented in this study, when the subcriticality and the neutron spectrum are varied. The present experimental data could be conducive to basic research of ADS, such as the verification of precision in numerical analyses by stochastic and deterministic approaches.

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