

数理解析研究所講究録 1747

RIMS 合宿型セミナー

Twisted topological invariants and topology  
of low-dimensional manifolds

京都大学数理解析研究所

2011年6月

*RIMS Kôkyûroku 1747*

*Twisted topological invariants and topology  
of low-dimensional manifolds*

*September 13~17, 2010*

*edited by Takayuki Morifuji*

*June, 2011*

*Research Institute for Mathematical Sciences*

*Kyoto University, Kyoto, Japan*

This is a report of research done at the Research Institute for Mathematical Sciences, Kyoto University. The papers contained herein are in final form and will not be submitted for publication elsewhere.

## Preface

The RIMS Seminar “Twisted topological invariants and topology of low-dimensional manifolds” was held at Akita Shirakami Taiken Center, Akita, Japan, during the period September 13-17, 2010.

In this seminar there were 16 talks concerning with twisted topological invariants and their applications to topology of low-dimensional manifolds. Most of the papers in this volume are based on the talks.

On behalf of the organizers, I would like to thank all the participants and speakers. Masaaki Suzuki took care of most of the practical aspects of producing this volume. His devotion is highly appreciated. I would also like to express my sincere gratitude to the RIMS for support of the seminar and publication of the proceedings.

Tokyo, March 2011

Takayuki Morifuji

## RIMS Seminar

### Twisted topological invariants and topology of low-dimensional manifolds

Akita Shirakami Taiken Center, September 13–17, 2010

#### Program

##### September 13 (Mon)

16:30–17:30 Stefan Friedl (Cologne)  
Twisted Alexander polynomials - an overview

##### September 14 (Tue)

9:00–9:40 Masaaki Suzuki (Akita)  
Epimorphisms between knot groups: determination of the partial order

10:00–11:00 Taehee Kim (Seoul)  
Twisted Alexander polynomials and character varieties for 2-bridge knots

11:20–12:00 Yoshikazu Yamaguchi (Tokyo)  
On the twisted Alexander polynomial for metabelian  $SL(2, \mathbb{C})$ -representations with the adjoint action

14:30–15:30 Shicheng Wang (Beijing)  
Graph manifolds have virtually positive Seifert volume

16:00–17:30 Makoto Sakuma (Hiroshima)  
Epimorphisms between 2-bridge links: Essential simple loops on 2-bridge spheres

##### September 15 (Wed)

9:00–9:40 Yuya Koda (Sendai)  
On the Reidemeister-Turaev torsion of standard  $\text{Spin}^c$ -structures on Seifert fibered 3-manifolds

10:00–11:00 Jae Choon Cha (Pohang)  
Why is the twisted invariant related to fiberability?

11:20–12:20 Masaaki Wada (Osaka)  
Twisted Alexander polynomial revisited

14:30–17:30 Problem Session

##### September 16 (Thu)

9:00–9:40 Yuichi Yamada (Tokyo)  
Lens space surgeries along certain 2-component links, and Reidemeister-Turaev torsion

10:00–11:00 Shicheng Wang (Beijing)  
Finiteness of gluing under domination

11:20–12:00 Taehee Kim (Seoul)  
Cobordism on homology cylinders and combinatorial torsions

14:30–15:30 Takuya Sakasai (Tokyo)  
The Magnus representation and homology cobordism groups of homology cylinders

16:00–17:30 Stefan Friedl (Cologne)  
Detecting the Thurston norm and fibered classes

**September 17 (Fri)**

9:00–9:40 Takahiro Kitayama (Tokyo)

On the leading coefficients of higher-order Alexander polynomials

10:00–11:00 Jae Choon Cha (Pohang)

$L^2$ -signatures: twisted invariants from duality

Organizers: Takayuki Morifuji (Tokyo)  
Masaaki Suzuki (Akita)  
Teruaki Kitano (Tokyo)

Twisted topological invariants and topology of low-dimensional manifolds  
RIMS 合宿型セミナー報告集

2010年9月13日～9月17日

研究代表者 森藤 孝之 (Takayuki Morifuji)

副代表者 鈴木 正明 (Masaaki Suzuki)

目 次

1. RECENT RESULTS ON AMENABLE $L^2$ -THEORETIC METHODS FOR HOMOLOGY COBORDISM AND KNOT CONCORDANCE -----	1
POSTECH	Jae Choon Cha
2. COBORDISM ON HOMOLOGY CYLINDERS AND COMBINATORIAL TORSIONS -----	17
POSTECH	Jae Choon Cha
U. Köln	Stefan Friedl
Konkuk U.	Taehee Kim
3. CENTRALIZERS IN 3-MANIFOLD GROUPS -----	23
U. Köln	Stefan Friedl
4. APPROXIMATIONS TO THE VOLUME OF HYPERBOLIC KNOTS -----	35
U. Köln	Stefan Friedl
U. Warwick	Nicholas Jackson
5. JOHNSON HOMOMORPHISMS AS FIBERING OBSTRUCTIONS OF HOMOLOGICALLY FIBERED KNOTS -----	47
東京農工大・工学 (Tokyo U. Agri. Tech.)	合田 洋 (Hiroshi Goda)
東工大・理工学 (Tokyo Inst. Tech.)	逆井 卓也 (Takuya Sakasai)
6. LENS SPACE SURGERIES ALONG TWO COMPONENT LINKS AND REIDEMEISTER-TURAEV TORSION -----	67
East China Normal U.	門上 晃久 (Teruhisa Kadokami)
電通大 (U. Electro-Communications)	山田 裕一 (Yuichi Yamada)
7. TWISTED ALEXANDER POLYNOMIALS AND CHARACTER VARIETIES FOR 2-BRIDGE KNOTS -----	77
Konkuk U.	Taehee Kim
東京農工大・工学 (Tokyo U. Agri. Tech.)	森藤 孝之 (Takayuki Morifuji)

8.	SOME PROBLEMS ON EPIMORPHISMS BETWEEN KNOT GROUPS	81
	創価大・工 (Soka U.)	北野 晃朗 (Teruaki Kitano)
9.	ON METABELIAN REIDEMEISTER TORSION	87
	東大・数理科学 (U. Tokyo)	北山 貴裕 (Takahiro Kitayama)
1 0.	ON THE REIDEMEISTER-TURAEV TORSION OF STANDARD SPIN <sup>C</sup> STRUCTURES ON SEIFERT FIBERED 3-MANIFOLDS	93
	東北大・理学 (Tohoku U.)	古宇田 悠哉 (Yuya Koda)
1 1.	EPIMORPHISMS BETWEEN 2-BRIDGE LINK GROUPS: ESSENTIAL SIMPLE LOOPS ON 2-BRIDGE SPHERES	109
	Pusan Nat. U.	Donghi Lee
	広島大・理学 (Hiroshima U.)	作間 誠 (Makoto Sakuma)
1 2.	A NOTE ON DEGREES OF TWISTED ALEXANDER POLYNOMIALS	121
	東京農工大・工学 (Tokyo U. Agri. Tech.)	森藤 孝之 (Takayuki Morifuji)
1 3.	THE MAGNUS REPRESENTATION AND ABELIAN QUOTIENTS OF GROUPS OF HOMOLOGY CYLINDERS	126
	東工大・理工学 (Tokyo Inst. Tech.)	逆井 卓也 (Takuya Sakasai)
1 4.	AN EPIMORPHISM BETWEEN KNOT GROUPS WHICH DOES NOT MAP A MERIDIAN TO A MERIDIAN	135
	秋田大・教育文化 (Akita U.)	鈴木 正明 (Masaaki Suzuki)
1 5.	TWISTED ALEXANDER POLYNOMIAL REVISITED	140
	阪大・情報科学 (Osaka U.)	和田 昌昭 (Masaaki Wada)
1 6.	ON THE MAPPING DEGREE SETS FOR 3-MANIFOLDS	145
	Peking U.	Shicheng Wang
1 7.	ON THE TWISTED ALEXANDER POLYNOMIAL FOR METABELIAN SL <sub>2</sub> (C)-REPRESENTATIONS WITH THE ADJOINT ACTION	157
	東工大・理工学 (Tokyo Inst. Tech.)	山口 祥司 (Yoshikazu Yamaguchi)