<table>
<thead>
<tr>
<th>Title</th>
<th>A CR-HYDRO-NEI MODEL OF MULTI-WAVELENGTH EMISSION FROM THE VELA JR. SUPERNOVA REMNANT (SNR RX J0852.0–4622)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Author(s)</td>
<td>Lee, Shiu-Hang; Slane, Patrick O.; Ellison, Donald C.; Nagataki, Shigehiro; Patnaude, Daniel J.</td>
</tr>
<tr>
<td>Citation</td>
<td>The Astrophysical Journal (2013), 767(1)</td>
</tr>
<tr>
<td>Issue Date</td>
<td>2013-03-21</td>
</tr>
<tr>
<td>URL</td>
<td><a href="http://hdl.handle.net/2433/173353">http://hdl.handle.net/2433/173353</a></td>
</tr>
<tr>
<td>Right</td>
<td>© 2013. The American Astronomical Society.; This is not the published version. Please cite only the published version. この論文は出版社版ではありません。引用の際には出版社版をご確認ご利用ください。</td>
</tr>
<tr>
<td>Type</td>
<td>Journal Article</td>
</tr>
<tr>
<td>Textversion</td>
<td>author</td>
</tr>
</tbody>
</table>
A CR-HYDRO-NEI MODEL OF MULTI-WAVELENGTH EMISSION FROM THE VELA JR. SUPERNOVA REMNANT
(SNR RX J0852.0-4622)

SHU-HANG LEE1, PATRICK O. SLANE 2, DONALD C. ELLISON3, SHIGEHIRO NAGATAKI4 AND DANIEL J. PATNAUDE 2

Received 28 December 2012; Accepted 18 Feb 2013

ABSTRACT

Based largely on energy budget considerations and the observed cosmic-ray (CR) ion composition, supernova remnant (SNR) blast waves are the most likely sources of CR ions with energies at least up to the “knee” near $10^{15}$ eV. Shocks in young shell-type TeV-bright SNRs are surely producing TeV particles, but the emission could be dominated by ions producing $\pi^0$-decay emission or electrons producing inverse-Compton (IC) gamma-rays. Unambiguously identifying the GeV-TeV emission process in a particular SNR will not only help pin down the origin of CRs, it will add significantly to our understanding of the diffusive shock acceleration (DSA) mechanism and improve our understanding of supernovae and the impact SNRs have on the circumstellar medium. In this study, we investigate the Vela Jr. SNR, an example of TeV-bright non-thermal SNRs. We perform hydrodynamic simulations coupled with non-linear DSA and non-equilibrium ionization near the forward shock (FS) to confront currently available multi-wavelength data. We find, with an analysis similar to that used earlier for SNR RX J1713.7-3946, that self-consistently modeling the thermal X-ray line emission with the non-thermal continuum in our one-dimensional model strongly constrains the fitting parameters, and this leads convincingly to a leptonic origin for the GeV-TeV emission for Vela Jr. This conclusion is further supported by applying additional constraints from observation, including the radial brightness profiles of the SNR shell in TeV gamma-rays, and the spatial variation of the X-ray synchrotron spectral index. We will discuss implications of our models on future observations by the next-generation telescopes.

Subject headings: acceleration of particles, shock waves, ISM: cosmic rays, ISM: supernova remnants

1. INTRODUCTION

Young shell-type supernova remnants (SNRs) with strong non-thermal emission, such as RX J1713.7-3946, HESS J1731-347 and Vela Jr., have been in the spotlight in recent years due to their presumed close relation to the origin of Galactic cosmic rays (CRs). These remnants show high luminosities in TeV gamma-rays and synchrotron dominated X-rays with no sign of thermal emission from the ejecta or shell. Vela Jr. is a typical example of a TeV-bright SNR where emission in the X-ray band is strongly non-thermal. It lies along the line-of-sight of the crowded Vela complex, comprising the Vela SNR, the Vela-X pulsar wind nebula (PWN), the Vela pulsar, the Pencil Nebula, and the Puppis A SNR. While Vela Jr. was first discovered by the ROSAT satellite at X-ray energies above ~ 1.3 keV (Aschenbach 1998), it is coincident with the southeastern part of the more diffuse Vela SNR and is totally obscured by the latter in the soft X-ray band.

The age of and distance to this remnant have been debated with the current most-agreed-on values being $d_{\text{SNR}} \gtrsim 750$ pc and $t_{\text{age}} \sim 1700 - 4300$ yr (e.g., Slane et al. 2001; Katuda et al. 2008). The progenitor has been suggested to be the core-collapse of a massive star due to the discovery of a central compact object AX J0851.9-4617.4 near the center of the SNR (Slane et al. 2001) with a consistent age and distance (Kargaltsev et al. 2007), although no pulsation has yet been detected.

Detection of the 1.157 MeV radioactive decay line of the short-lived $^{44}$Ti along the same line-of-sight has been claimed (Iyudin et al. 1998), suggestive of an extremely short distance of about 200 pc, and a young age of around 700 yr. However, the line detection suffers from low statistical significance at the $2 \sim 4 \sigma$ level (Schönfelder et al. 2000), and from the non-detection of the associated Ca(Sc) K line in X-rays by the Advanced Satellite for Cosmology and Astrophysics (ASC) GIS (Slane et al. 2001) and Suzaku XIS (Hiraga et al. 2009) imaging spectrometers. Moreover, using the distance and age deduced directly from proper-motion measurements (Katsuda et al. 2008), it can be shown that the required initial mass of $^{44}$Ti has to be $\sim 1 M_\odot$, orders of magnitude larger than that expected by supernova nucleosynthesis models. Hence, we consider the association of the $^{44}$Ti flux with Vela Jr. unlikely.

Sharp synchrotron filamentary structures in X-rays have been resolved by Chandra in the bright northwestern shell (Bamba et al. 2005). An explanation of the small effective width of these filaments by fast synchrotron cooling of CR electrons requires a local magnetic field strength of about 100 $\mu$G (e.g., Berezhko et al. 2009), probably indicating magnetic field amplification (MFA) induced by efficient CR ion acceleration (e.g., Bell 2004; Vladimirov, Bykov, & Ellison 2008; Bykov, Ospov, & Ellison 2011).

The radio remnant (Combi et al. 1999; Stupar et al. 2005) is relatively faint ($\sim 30 \sim 50$ Jy at 1 GHz) with a flat spectral index $\sim 0.3$. The morphology is ring-like and shows a good overall correlation with the X-ray remnant, suggesting a common synchrotron origin for the radio and X-ray emission. Spatially extended emission in the GeV and TeV bands has also been discovered by Fermi LAT (Tanaka et al. 2011) and H.E.S.S. (Aharonian et al. 2007) along the line-of-sight. The gamma-ray spectra can be described by a single power-law.
with index $\sim 1.85$ and a cutoff energy at a few TeV. As we will discuss in more detail below, Vela Jr. shares some striking similarities with another well-studied non-thermal SNR RX J1713.7-3946 in both spectral and morphological characteristics. We believe these similarities are important for understanding the physical nature of Vela Jr.

Recently, Tanaka et al. (2011) have fitted the broadband spectra of Vela Jr. using both hadronic ($\pi^{0}$-decay dominated) and leptonic (IC dominated) scenarios. They assumed single power-law spectra with exponential cut-offs for the underlying proton and electron distributions. To obtain the best fits, they varied the spectral indices of the particles and the environmental parameters including the downstream (DS) B-field strength and gas density. They concluded that reasonable spectral fits can be obtained under both scenarios by invoking different parameter choices. In some cases, however, the interpretation of their parameters can be non-trivial, such as an unrealistically large energy in the accelerated proton population ($\sim 10^{51}$ erg) in the hadronic model for a low-density ($n \sim 0.01$ cm$^{-3}$) ambient medium, and a small downstream B-field ($B_{2} \sim 10$ $\mu$G) required in the leptonic case which seems to contradict with the sharpness of the X-ray filaments found in the brighter NW rim (but see our arguments for such a possibility in Section 5).

While DSA models predict the acceleration of both electrons and ions, determining the total energy appearing in relativistic particles depends crucially on the correct interpretation of which particles are responsible for any observed gamma-ray emission. In addition, models for which the gamma-ray emission is produced predominantly by hadrons necessarily produce observable signatures in the luminosity and ionization state of the thermal X-ray emission. We believe that disentangling the emission origin requires a more self-consistent SNR model, as we have developed and used to model SNR RX J1713.7-3946 (e.g., Ellison et al. 2012; Lee et al. 2012, and references therein). In our CR-hydro-NEI model, the thermal X-ray emission is determined self-consistently using the dynamical information of the forward shock. Furthermore, the SNR dynamics is calculated self-consistently with DSA including the feedback effects from NL-DSA on the SNR evolution. We include spatial profiles of the multi-wavelength emission which provide more stringent constraints on the parameters and lead to a better differentiation between the $\pi^{0}$-decay and IC dominated cases.

Within the approximations of our one-dimensional model, we find that leptonic models clearly fit the broadband observations better than $\pi^{0}$-decay ones in a fashion strikingly similar to broadband models of SNR RX J1713.7-3946. We emphasize that regardless of the approximations intrinsic to our model; our results clearly show that including a self-consistent calculation of the thermal X-ray emission is essential for any broadband model of a young SNR. For Vela Jr., as for SNR RX J1713.7-3946, hadronic scenarios are excluded with high confidence in homogeneous models.

This paper is organized as follows: The first section provides a brief description of the latest version of the CR-hydro-NEI simulation code we use as our modeling platform; the second section describes our models for Vela Jr. and the various constrains from observation data; and in the last part, we discuss the implications of our models on our understanding of the environment of Vela Jr., the acceleration of CR particles at the blast wave, and the possible production mechanism(s) of the observed broadband emission from radio to the TeV band. Some concluding remarks follow.

2. THE CR-HYDRO-NEI SIMULATION CODE

When it comes to modeling emission from young shell-type SNRs with strong forward shocks, it is very important to take into account the non-linear aspects of DSA and its coupling to the hydrodynamics and plasma conditions in the shocked gas. The high Mach number shocks in young SNRs are expected to be efficient particle accelerators and with efficient DSA, the CR production, shock structure, shocked gas temperature, and magnetic fields are coupled and feedback effects cannot be ignored. Here we employ a CR-hydro-NEI code which can effectively model young, shell-type SNRs like Vela Jr. with these non-linear effects accounted for self-consistently. In this section, we briefly describe a generalized version of the CR-hydro-NEI code that includes several updates and additional functions not included in the description given in Lee et al. (2012).

2.1. Coupled SNR hydrodynamics, NL-DSA, and NEI

The development of the CR-hydro-NEI code used here has been described in detail in a number of recent papers (e.g., Ellison et al. 2007; Pataquade et al. 2009, 2010; Ellison et al. 2010, 2012), with the most recent “generalized” version given in Lee et al. (2012). Briefly, the SNR hydrodynamics are modeled with a one-dimensional hydro simulation based on VH-1 (e.g., Blondin & Ellison 2001). The SNR simulation provides the evolving shock speed, sonic and Alfvén Mach numbers, and other quantities necessary for the shock acceleration calculation. The NL-DSA calculation is done with a semi-analytic solution based largely on the work of P. Blasi and co-workers (e.g., Blasi et al. 2005; Caprioli et al. 2009) (see Lee et al. 2012, for a full list of references). With suitable parameters, the semi-analytic calculation provides the shock compression ratio, amplified magnetic field, and full proton and electron spectra which are used to calculate the broadband continuum radiation from synchrotron, bremsstrahlung, IC, and $\pi^{0}$-decay emission.

The SNR evolution is coupled to the CR production by modifying the standard hydrodynamic equations through a change in the equation of state from the influence of relativistic CRs, energy loss from escaping CRs, and magnetic pressure. The changes produced in the hydrodynamics by NL-DSA also modify the evolution and ionization state of the shocked thermal plasma and these changes are self-consistently included in our non-equilibrium ionization (NEI) calculation of the thermal X-ray emission.

We thus obtain a model of an evolving SNR where the non-thermal continuum and thermal line emission are calculated self-consistently. Treating thermal and non-thermal processes consistently is required when CR production is efficient because the production of relativistic CRs can strongly influence the density and temperature of the shock-heated thermal plasma (e.g., Ellison 2000). In such a self-consistent calculation, it is not possible, for instance, to adjust parameters so

5 As in our models of SNR RX J1713.7-3946, we only calculate emission from the shocked region between the contact discontinuity (CD) and FS and neglect emission from the reverse shock. Including additional thermal X-ray emission from the shocked ejecta would strengthen the case for a leptonic dominated model for the $\gamma$-ray emission.

6 We note that only a “scalar” magnetic pressure is used in our 1D hydro simulation.
that $\pi^0$-decay matches GeV-TeV observations without modifying the fit to thermal X-ray line emission. As we have demonstrated in our fits to SNR RX J1713.7-3946 (e.g., Ellison et al. 2012; Lee et al. 2012), this coupling strongly constrains broadband emission models.

2.2. Precursor CR populations and emission

To determine the CR proton distribution function $f^{\text{cr}}(x, p)$ at a certain position $x$ in the precursor upstream of the forward shock, we follow the recipe described in Lee et al. (2012) [see equation (17)] and references therein. As for the electrons, we implicitly assume that they do not affect the shock structure and dynamics due to their low energy density compared to the protons, which we have checked to be the case a posteriori for all models presented here. We also assume that radiative cooling of the electrons occurs mainly in the downstream region where the B-field is highest and the electrons spend most of their time scattering per shock-crossing. As a result, this allows us to calculate the electron distribution in the precursor easily using the precursor profile and the distribution function at the subshock in the same way as for the protons after the DSA solution has been obtained at every time step.

At each position $x$ in the precursor, we read off the local environment variables such as the gas density, the B-field strength and the temperature as provided by the DSA solution to calculate the local photon emissivity. The total emission spectrum from the CR precursor is thus obtained by an integration over the precursor volume.

2.3. Secondary particle production and emission in the SNR shell

Accelerated protons and heavier ions will interact with the background gas and produce charged pions through p-p interactions. These pions further decay into secondary particles such as $e^+$, $e^-$ and $\nu$'s. The charged secondaries can accumulate in the SNR shell and radiate as the shock propagates into the upstream medium. We have implemented this process in the CR-hydro-NEI code by following the continuous production of the secondaries in the post-shock region, as well as the adiabatic and radiative losses of the $e^+e^-$. We only consider secondary production and radiation in the post-shock region because the density and magnetic field are considerably higher than in the shock precursor. The relevant inclusive secondary cross-sections are obtained using the parameterized model by Kamae et al. (2006), as we do for the gamma-rays. Contribution from heavy ions like p-He is taken into account via an effective enhancement factor. These secondaries contribute to the photon emissivity via synchrotron, IC and bremsstrahlung and is estimated at the end of a simulation.

We note that there is a possibility that these secondary $e^+e^-$ can be injected into DSA and be ‘reaccelerated’ in the same manner as the primary electrons. This is especially true for those being generated in the CR precursor. However, since most of the secondary particles are produced and accumulated in the DS region, and the probability of these populations traveling back to the shock from their production sites in order to be injected into acceleration is relatively low, we will ignore the process of reacceleration. We will show that, whilst the secondary particles do not contribute significantly to the volume-integrated broadband photon spectrum for all models presented in this work, the production of these particles in the shocked gas and their accumulation can have important effects on the spatial variation of synchrotron emission in some specific X-ray bands for a hadronic model. This result will be discussed in detail in Section 4.3.

2.4. Multi-wavelength emission profiles

Using the spatial information from the CR-hydro-NEI code, it is relatively straightforward to obtain model predictions for multi-wavelength emission profiles. Line-of-sight projection effects are calculated assuming spherical symmetry. The projected radial (i.e., outward from the SNR center) profiles, integrated over a set of chosen wavebands, are convolved with gaussian kernels to mimic the point-spread-functions of various instruments and facilitate direct comparison with data.

3. MODELS

The radio-to-TeV spectral and morphological features of Vela Jr. largely resemble SNR RX J1713.7-3946. The observed similarities between Vela Jr. and SNR RX J1713.7-3946 include: (i) relatively dim radio emission with a flat spectral index; (ii) radio and X-ray emission which are predominantly synchrotron in origin with ring-like morphologies, and with no evidence of thermal emission from either the shell or the ejecta (central) region; (iii) luminous in TeV energies, but relatively faint in the GeV band when compared to other gamma-ray SNRs, especially the middle-aged remnants like W51C, W44, and IC 443 (e.g., Abdo et al. 2009, 2010a,b); and (iv) TeV emission is spatially resolved to a shell-like structure and correlates well with the X-ray and radio images. As might be expected, the observational similarities between Vela Jr. and SNR RX J1713.7-3946 lead naturally to a similar conclusion from our CR-hydro-NEI model that IC dominates the GeV-TeV emission process.

3.1. Input parameters

We have constructed two representative models: a “hadronic” model where the GeV-TeV emission is $\pi^0$-decay dominated, and a “leptonic” model where it is IC dominated. For both models we assume: (i) the associated supernova (SN) had a kinetic energy of $E_{\text{SN}} = 10^{51}$ erg; (ii) the age of the remnant is 2500 yr to match the observed size of the SNR at the distances assumed in Table 1; (iii) the injection parameter which determines the acceleration efficiency of DSA is set at $X_{\text{ej}} = \frac{\text{pinj}}{\text{pth}} + 2f_{\text{inj}} = 3$, corresponding to a fraction $\eta \sim 2 \times 10^{-4}$ of thermal particles being injected in DSA at any time (note that our $X_{\text{inj}}$ is $\xi$ in Blasi et al. 2005); (iv) we have conservatively assumed that the electron temperature equilibrates with the proton temperature through Coulomb collisions otherwise mentioned; (v) the spectrum of the background photon fields that are up-scattered by the relativistic electrons to gamma-ray energies (IC) is taken from Porter et al. (2006) at the position of the SNR, which contains the cosmic microwave background (CMB) and the local interstellar radiation fields in the infrared and optical bands; (vi) the upstream gas temperature is fixed at $T_0 = 10^4$ K regardless of the gas density gradient; (vii) a number fraction of helium $f_{\text{He}} = 0.0077$ is specified for the plasma, which contributes additionally to the various photon emission. However, other than this scaling, we ignore the acceleration of heavy ions in this paper; (viii) we assume that the ambient B-field is oriented quasi-parallel to the shock normal over the whole surface, that is, we assume that the magnetic field geometry is unimportant as would be the case for efficient DSA where the self-generated magnetic turbulence mediating DSA is totally tangled in the CR precursor and downstream from the
shock, i.e., the Bohm limit for CR diffusion is obtained. For full details of the formulation, see Lee et al. (2012).

An important difference between our hadronic and leptonic models is that the hadronic model evolves in a uniform upstream medium, typical of a Type Ia SN, and the leptonic model evolves in a wind cavity, typical of a core-collapse SN. While the observational evidence favors a core-collapse origin for the Vela Jr. SNR, we could not find a set of core-collapse parameters that would produce a reasonable fit to the broadband data for a hadronic model radiating in a pre-SN wind. This is because the hadronic model needs a high ambient gas density and high B-field strength in order to simultaneously explain the radio/X-ray synchrotron emission and the gamma-ray flux. We thus used a uniform ISM model for our hadronic fit. On the other hand, a leptonic model requires a lower ambient gas density to suppress the \( \pi^0 \)-decay gamma-rays, and this is naturally realized by a wind bubble environment for a remnant sitting close to the Galactic plane. More details will be given in Section 4 where we will further discuss this point. Consistent with the different SN scenarios, we assume an ejecta mass \( M_{ej} = 1.4 M_\odot \) for our hadronic model and \( M_{ej} = 3 M_\odot \) for our leptonic model.

In Table 1, we summarize the main input parameters and output quantities measured at the end of the simulation for each model. We constrain the input parameters via a satisfactory fit to the observed broadband spectrum from radio to TeV energies, as well as a general agreement of the dynamical variables (e.g., radius of the forward shock) with current observations. The distance to the SNR is recently constrained by Katsuda et al. (2008) using proper-motion measurements over a 7-year time period. They provided the estimate equivalent to \( d_{SNR} \geq (750 \pm 205) \times (v_{pk}/3000 \text{ km s}^{-1}) \) pc. We will adopt \( d_{SNR} \) for our models which is consistent with this limit.

4. RESULTS AND DISCUSSION

4.1. Dynamics

We plot the time evolution of selected important physical quantities for the hadronic and leptonic models in Figures 1 and 2. The very different undisturbed upstream environments give rise to large differences in the dynamical behavior of the two models. With the lower B-field and gas density in the wind cavity for the leptonic model, the following are expected and observed compared to the hadronic model: (1) the shock sweeps up material at a much lower rate, so that the shock speed and Mach numbers decay slower, and shock radius increases faster, with time; (2) the acceleration efficiency, and hence the fraction, \( f_{SN} \), of supernova explosion energy, \( E_{SN} \), converted into CR particles at the current age is much lower (\( f_{SN} \approx 0.14 \) vs 0.48) due to the slower injection rate of thermal particles from the shocked gas into DSA. This is also reflected in the much more moderate shock modification (i.e., smaller \( R_{tot} \)) than for the hadronic model on average. The high \( f_{SN} \) fraction of the hadronic model is consistent with the result of Tanaka et al. (2011); (3) the lower B-field in the DS region \( (B_3) \) results in a longer synchrotron loss time-scale, in this case longer than the acceleration time-scale throughout the age of 2500 yr, resulting in a common \( p_{\text{max}} \) for electrons and protons. On the contrary, the hadronic model has a much higher ambient B-field strength in the uniform ISM, such that \( p_{\text{max}} \) of electrons becomes limited by the synchrotron loss (and IC loss to a lesser extent) starting from about 200 yr. These evolutionary differences relate directly to the broadband emission of the SNR, as we will discuss in the upcoming sections.

4.2. Broadband Photon Spectrum

As mentioned in Section 3, to obtain reasonable fits to the observed photon spectra, the two models require that the SNR evolves within very different surrounding environments. For the hadronic model, in order for the \( \pi^0 \)-decay photons to dominate over the IC component in the gamma-ray band, the gas density has to be high and the number ratio between electrons and protons \( (K_{ep}) \) has to be particularly low \( (K_{ep} \sim 10^{-4}) \). The high density requirement argues against the SNR propagating into a pre-SN wind with rapidly decreasing density and we are forced to assume the blast wave runs into an interstellar medium (ISM) with uniform gas density and magnetic field strength.

In contrast, the leptonic model requires that the forward shock propagates into a magnetized pre-SN wind region. This introduces a descending gradient for the gas density and B-field. The low shocked gas density in the downstream photon-emitting region suppresses the \( \pi^0 \)-decay and bremsstrahlung, as well as the X-ray line emission, relative to the IC component.

![Fig. 1. Time evolution of output quantities for our leptonic model (solid lines) and hadronic model (dashed lines). From the top panel: (1) shock radius \( R_{peak} \); (2) shock velocity \( V_{sh} \); (3) sonic Mach number \( M_S \) (black) and Alfvén Mach number \( M_A \) (red) of the forward shock; and (4) B-field strength in the far upstream \( B_0 \) (black), right in front of the subshock \( B_1 \) (green), and immediately behind it \( B_2 \) (red).](image-url)
Figure 3 shows the corresponding fits of the broadband spectra to currently available observations. We see that both models can explain the radio and GeV-to-TeV gamma-ray data reasonably well under the respective choices of parameters. In the X-ray band, however, the hadronic model has difficulty reproducing the X-ray photon index observed by ASCA, mainly due to the much faster synchrotron loss rate caused by the higher B-field in the hadronic model. The higher ambient gas density required for π0-decay dominance in the gamma-ray band is also accompanied by a high flux from thermal X-ray lines, which exceeds the X-ray flux observed by ASCA in the soft X-ray energy range below a few keV, despite the adoption of a conservative model of electron heating via Coulomb collisions in the post-shock region. The self-consistently calculated thermal X-ray emission provides a strong additional model constraint.

Another important difference between the two models is the overall normalization factor required for the broadband emission to match the observed flux. For the leptonic model this factor is close to unity, but the hadronic model has to be boosted by a factor \( \sim 5 \) to explain the observed flux level. This factor \( \sim 5 \) is included in all of the model spectra shown in the lower panel of Figure 3.

### 4.3. X-ray Spectrum and Its Spatial Properties

A more in-depth comparison with the currently available X-ray data is valuable to differentiate SNR models. Firstly, to see the general agreement of the models with data, we plot the calculated non-thermal and thermal X-ray spectra against the ASCA result (e.g., Slane et al. 2001; Aharonian et al. 2007) in Figure 4. For the hadronic model, to show the possible range of variance of the thermal spectrum based on different equilibration models for the electron temperature, we also show the calculated thermal spectrum assuming that the electron temperature equilibrates instantaneously with the proton temperature behind the FS. Coulomb equilibration and instant equilibration are two extremes for electron heating and the actual heating is very likely to lie somewhere in between. For either extreme in heating, the hadronic model predicts a thermal X-ray flux substantially higher than what observation implies (especially below \( \sim 2 \) keV), in addition to its failure to reproduce the non-thermal spectral index. The leptonic model, on the other hand, shows a general good fit to the data without an over-prediction of the thermal emission.
Fig. 4.— X-ray spectra for our leptonic model (upper panel) and hadronic model (lower panel). In both panels, the blue and black solid lines correspond to the synchrotron (including secondary contribution if any) and thermal line emission respectively, while the dashed lines are the thermal continuum spectra. The red band is from ASCA GIS observation. In the lower panel for the hadronic model, the light grey lines also show the thermal spectra corresponding to a model with instantaneous equilibration between the electron and proton temperatures right behind the subshock, but is otherwise the same. In the top panel for the leptonic model, the grey line shows the total spectrum. As in Figure 3, the hadronic model spectra are multiplied by \(~ 5\) to match the observed broadband flux level.

In this regard, we notice that Berezhko et al. (2009) have proposed a hadronic model in which the shock is running into a wind bubble region created by the progenitor star embedded inside a high density gas cloud. We do not consider such a situation in this work since, in such a high density environment (\(n_{\text{gas}} \geq 0.01\,\text{cm}^{-3}\)), the resultant thermal X-ray lines are expected to violate the observation data even more than is the case for our hadronic model.

Secondly, we consider the X-ray spectrum near the bright NW rim of the remnant. Vela Jr. was observed with the Chandra X-ray Observatory on 2003 January 5 and 6 (ObsIDs 3446 and 4414) using the Advanced CCD imaging Spectrometer (ACIS). Standard cleaning and data reduction were performed using CIAO version 4.4. The merged observations yielded a total exposure time of 73.9 ks. Spectra, extracted using the specextract software, were obtained from a narrow region encompassing the forward shock of the SNR (solid box in Figure 5) and from a background region (dashed box) used to account for projected emission from the Vela SNR as well as internal, Galactic, and extragalactic background emission.

The predicted thermal and nonthermal emission from CR-hydro-NEI for the projected spectral region indicated was converted into a table model for use in xspec for both the hadronic and leptonic models. The tbabs model for interstellar absorption was applied, and the model was convolved with the instrument response function and fit to the data. To account for possible excess foreground emission from the Vela SNR, a thermal nonequilibrium ionization model (nei) with a distinct tbabs absorption component was included.

The best-fit results are shown in Figure 6, where the leptonic model fit is shown as a black histogram, and the hadronic model is shown in red. The dashed histogram corresponds to the additional tbabs\(\times\)nei model. It is clear that the hadronic model provides a poor representation of the X-ray data, both at low energies, where the predicted line emission is not observed, and at high energies, where the model is much steeper than the observed spectrum. The leptonic model provides an excellent fit to the data (\(\chi^2 = 1.05\) for 327 degrees of freedom). The column density is \(n_H = (4.3 \pm 0.2) \times 10^{21}\,\text{cm}^{-2}\), in good agreement with previous measurements (Slane et al. 2001; Pannuti et al. 2010) and the accompanying thermal component has a temperature of \(0.26^{+0.32}_{-0.08}\,\text{keV}\) with a column density of \((0 - 3.3) \times 10^{21}\,\text{cm}^{-2}\), consistent with observed properties for soft thermal emission from the Vela SNR. The best-fit normalization for the CR-hydro-NEI component is about 15% higher than the ratio of the spectral extraction region length to the entire SNR circumference, which is reasonable given that the rim is somewhat brighter at this position (see Figure 5).

Thanks to the high angular resolution of Chandra, it is also possible to study spatial variation of the spectral properties near the FS (see, e.g., Pannuti et al. 2010). Correspondingly, we calculate the synchrotron photon index for a series of line-of-sight projected regions from the models which have different radial distances from the FS. The results are shown in Figure 7. Besides the absolute difference of the index values, the hadronic and leptonic models show very distinct trends of the index variation as a function of distance from the FS. For our leptonic model, the synchrotron spectrum softens as we look inward from the FS, whereas our hadronic model exhibits a much weaker dependence on position.

The major factors which determine the spectral index of the non-thermal X-rays at a certain distance from the SNR center are the following: (1) Energy loss history of the primary accelerated electrons, which is critical to the high-energy cutoff of the primary synchrotron component; and (2) the relative importance of the secondary e\(^+\)-e\(^-\) to the primary electrons at that position. These secondaries are produced by the
trapped accelerated protons interacting with the shocked gas, which lose energy radiatively like the primaries and meanwhile accumulate in number with time. Different from the primaries, which are accelerated by the shock and then advected downstream without replenishment, the secondaries at each position in the shocked gas are continuously generated by the advected high-energy protons whose spectra do not evolve with time significantly other than from adiabatic losses. The spectral shapes of the secondary and primary synchrotron components are hence typically different. For our leptonic model, the effect from secondaries is obviously small due to the very low ambient gas density in the wind bubble. As a result, the energy loss of the primaries dominates the spatial behavior of the synchrotron radiation. Since primary electrons accelerated by the shock at an earlier phase and now residing further inward in the SNR shell have suffered from synchrotron/IC and adiabatic losses for a longer period of time than those just being freshly accelerated, the cutoffs of their spectra are found at lower energies. In addition, due to the falling B-field strength with radius in our wind model, those primary electrons accelerated earlier have experienced a higher synchrotron loss rate on average than those residing closer to the FS at the current age. These lead to the softening of the synchrotron spectrum as shown by our result.

For the hadronic model, the secondaries cannot be neglected. In the volume integrated photon spectrum (Figure 3), the primary component dominates over the secondary one until around 10 keV. However, by looking deeper towards the SNR center where the number of secondary particles is larger due to accumulation and the primaries have a lower cut-off energy from a longer period of radiative loss, the secondary spectrum can dominate over the primary spectrum at a few keV and harden the resultant total spectrum in the 1 – 5 keV energy range. We find that this effect can compensate the energy loss of the primaries in the SNR shell and, for the relatively moderate ambient gas density we assume, lead to a weak variation of the synchrotron index with radius after projecting our spherically symmetric model along the line-of-sight. With a higher ambient gas density, a spectral hardening can be expected as we look inward from the shock. Using Chandra and XMM Newton data respectively, Pannuti et al. (2010) and Kishishita et al. (2013) have recently discovered a trend of softening for the non-thermal spectrum as the line-of-sight is moved inward from the FS towards the SNR center. This trend provides further support for our leptonic scenario. For a direct comparison, we overlaid in Figure 7 the fitted photon indices given by Kishishita et al. (2013) and found a reasonable agreement with our result. Additionally, the phenomenological spectral evolution model invoked by Kishishita et al. (2013) shows that the typical downstream B-field should be around a few μG in order to explain the observed softening trend, which is highly consistent with the field strength obtained in our leptonic model.

**4.4. Gamma-ray Morphology**

The current generation of ground-based Imaging Atmospheric Cherenkov Telescopes (IACTs) possesses sufficient angular resolution to discern the spatial structures of SNRs with large angular sizes in sub-TeV to multiple TeV energies. Recent HESS observations of Vela Jr. (Aharonian et al. 2007) have measured the radial surface brightness profiles of its shell-like emission from 300 GeV to 20 TeV with a resolution of about 0.06°. We compare our model profiles with the HESS measurements for the brightest northern part in Figure 8. The profiles are extracted from the model gamma-ray image after convolution with the PSF of the observation. The results show that both models predict gamma-ray emission profiles reasonably compatible with the data, and unlike the X-ray result, closely resemble each other after PSF smoothing.

The reason behind this relative similarity in the gamma-ray band can be explained by the following: X-ray synchrotron
emission produced by relativistic electrons is highly sensitive to the radiative loss rate. Electrons experience much faster energy loss in our hadronic model than the leptonic model, as mentioned above, which results into a sharp X-ray profile close to the FS for the hadronic case, and a more spread out profile behind the FS for the leptonic case. In the gamma-ray band, however, radiative loss plays a much less important role. In the hadronic model, the gamma-ray photons mainly originate from CR protons where losses can be ignored, while in the leptonic model the electrons responsible for the IC emission are only subject to minor losses due to the low magnetic fields.

Nevertheless, the gamma-rays originate from totally different mechanisms for the hadronic and leptonic cases so differences are predicted for more precise measurements. Future ground-based gamma-ray observatories, such as the upcoming Cherenkov Telescope Array (CTA), will be able to differentiate the models with unprecedented spatial resolving power and sensitivity. For illustration, we include in Figure 8 our model profiles using the advertised best angular resolution of CTA (about 0.02°). The thin curves imply that future gamma-ray observations will be able to differentiate between the predicted radial profiles of Vela Jr.

4.5. Possible Thermal X-ray Line Detection by Astro-H

TeV-bright SNRs like Vela Jr. and RX J1713.7-3946 have shown no sign of strong thermal emission with current X-ray observations. However, with the advent of future instruments of superior spectral resolution, it is very possible that thermal X-ray lines will be discerned in the non-thermal dominated spectrum. As a first look, we plot the calculated X-ray spectrum in Figure 9 for our leptonic model in the energy range of 0.3 to 12 keV where the IC flux $f_{\text{IC}} \propto n_0 K_{\text{ep}}$ (e.g. Ellison et al. 2010), we explore an altered model where $K_{\text{ep}}$ is lowered by a factor of 5 (i.e. $3 \times 10^{-3}$) and the wind matter density increased by the same factor to

For comparison, we show the leptonic model spectrum with a resolution of 60 eV (a typical ballpark value for currently operating X-ray observatories). We see that using the resolving power of SXS, the stronger sub-keV lines can be recognized very visibly on top of the synchrotron spectrum, and it is very possible that they will be detected by Astro-H. Detection of such lines will be important to further constrain our model parameters such as the local gas compositions and the ion temperatures and densities. In a follow-up paper in preparation, we will perform a more detailed study of the X-ray spectrum by performing formal Astro-H SXS spectral simulations based on our models, and take into account thermal Doppler broadening of the emission lines.

4.6. Sensitivity of Results on Model Parameters

We emphasize that while small variations in parameters in either of our “best-fit” models do not strongly modify the results for that model, the parameter sets for the two scenarios are well separated and it is not possible to go smoothly from one set to the other while maintaining a satisfactory fit to the observations. To illustrate this point and see how our models respond to parameter changes, we create modified versions for each of our models in which we purposely tune a set of important parameters so that it is positioned closer to the parameter space of the competing best-fit model. Two of the most important parameters that distinguish our leptonic and hadronic scenarios include the electron-to-proton number ratio at relativistic energies $K_{\text{ep}}$, and the upstream gas density $n_0$ (or the mass loss rate $dM/dt$ and wind speed $V_{\text{wind}}$ when a pre-SN wind is present). For the leptonic case with a massive star as progenitor and a wind cavity, by recalling that the IC flux $f_{\text{IC}} \propto n_0 K_{\text{ep}}$ (e.g. Ellison et al. 2010), we explore an altered model where $K_{\text{ep}}$ is lowered by a factor of 5 (i.e. $3 \times 10^{-3}$) and the wind matter density increased by the same factor to

7 We assume a pure spherical expansion of the SNR shell, such that near the FS (i.e., the SNR rim) the line broadening/shifting effect from expansion is negligible.

8 For the typical post-shock temperature in our leptonic model, the broadening by thermal motion of the ions is around 1%, assuming that the temperature ratios among the ion species are mass-proportional. Therefore, roughly speaking, SXS with a FWHM of at most 7 eV will be able to identify thermal broadening of the stronger lines above approximately 0.7 keV, where there are a few. We will perform a more detailed calculation of the ion temperatures in our follow-up paper to better assess this possibility.
roughly maintain the level of $f_{\text{IC}}$.\(^9\) The wind magnetization is fixed so as to keep the synchrotron-to-IC flux ratio $f_{\text{syn}}/f_{\text{IC}}$ roughly unchanged. On the other hand, we explore an altered model for the hadronic case where $K_{ep}$ is boosted up by a factor of 5 while $n_0$ is decreased by a factor of 1.7, so that the model is now leaning toward the leptonic parameter space. Note that since the $\pi^0$-decay flux $f_{\pi^0} \propto n_0^2$, this will decrease $f_{\pi^0}$ and increase $f_{\text{IC}}$ by roughly the same factor. For both cases, we also adjust the assumed age of the remnant, within the allowable range of $1700 \sim 4000$ yr implied by observations, from the default age of 2500 yr in order to achieve the same SNR angular size as the original model. Otherwise what described above, all other parameters are kept fixed.

The effect on the total broadband spectrum is shown in Figure 10. We can see that the modified leptonic model produces a non-thermal spectrum with an acceptable fit to the data except the highest energy TeV points and a X-ray spectral index a little too soft. But most importantly, it already starts to face the difficulty of over-predicting the thermal emission in the X-ray band due to the enhanced ambient gas density, which is the same problem encountered by our hadronic model. Another surfacing problem not shown in this plot is that the spatial dependence of the synchrotron index now fails to explain the XMM \textit{Newton} data by showing a softening trend too strong towards the SNR center (see Figure 7). For the modified hadronic model, although the thermal X-ray reduces back to a flux level more compatible with data than the original model, the broadband spectral fit becomes unacceptable by failing to explain the non-thermal X-ray flux level simultaneously with the gamma-rays, due to the enhanced leptonic contributions which worsen the fit. To achieve a good fit again, we find that a much lower B-field must accompany the increased $K_{ep}$ and decreased $n_0$, which is simply what being realized in the wind model we are employing for the leptonic model. The conclusion from this analysis is hence that it is impossible to maintain a good fit to data by continuously tuning some influential parameters from the leptonic to the hadronic case (and vice versa) unless a drastic change of the underlying SNR environment is involved, i.e. a rarified wind cavity against a uniform ISM model for the ambient medium.

5. CONCLUSIONS

We have investigated the TeV bright SNR Vela Jr. with a comprehensive modeling of its multi-wavelength emission from the radio to TeV band. Our one-dimensional, spherically symmetric NL-DSA model indicates that the SNR originated from the core-collapse explosion of a massive star inside a wind cavity with rarified gas density and magnetic fields. Based on the broadband continuum emission, with the added constraint from the self-consistently determined thermal X-ray emission, we show that the GeV-TeV gamma-rays are predominately produced by IC emission from shock accelerated electrons with a much smaller hadronic contribution from shock accelerated ions. Despite the fact that the leptons radiate more efficiently, here, as in all self-consistent DSA models of SNRs we are aware of, far more energy is put into relativistic ions than electrons. In summary, these conclusions are supported by the following results:

- In order for $\pi^0$-decay gamma-rays from shock accelerated ions to dominate IC emission from electrons, the ambient pre-shock density must be above some limit. Despite a wide range in possible thermal equilibration models for electron heating and the non-equilibrium ionization of the shocked plasma, the density required for $\pi^0$-decay dominance is accompanied by strong thermal line emission in the X-ray band which is well above \textit{ASCA GIS} observations (see the lower panel of Figure 3). This conclusion is similar to what we found previously for another non-thermal SNR RX J1713.7-3946.

- Even if the inconsistency with the thermal X-ray line emission is ignored, the hadronic model, with the SNR forward shock moving into a uniform ISM, fails to reproduce the spectral index of the observed X-ray synchrotron emission, as measured by \textit{ASCA GIS} and \textit{Chandra ACIS}. While the hadronic model can produce a reasonable match to the spectral shapes of data in other wavelengths, the overall normalization of the broadband emission requires a boosting factor of $\sim 5$ to bring the model spectra to the observed flux levels.

- Another possible problem with the hadronic model is that our best fit hadronic result predicts a spatial (i.e., radial) variation of the X-ray synchrotron photon index around the FS that is incompatible to the trend suggested by data from X-ray satellites (see Figure 7).

- The Vela Jr. SNR most likely originated from a core-collapse SN but the “best-fit” hadronic model requires

---

\(^9\) Only decreasing $K_{ep}$ by such a factor will not visibly change the broadband spectral shape, but will require an overall normalization factor substantially larger than 1, thus excluding such an option.
a relatively high-density, high-magnetic field environment more typical of a thermonuclear Type Ia SN.

In contrast to the above problems with the hadronic model, our pre-SN wind leptonic model can self-consistently explain the broadband continuum emission, the lack of thermal X-ray line emission, the overall normalization assuming \( d_{\mathrm{SNR}} \sim 1 \) kpc, and the spatial variation of the non-thermal X-ray spectral index.

It is important to note that while our calculations assume a uniform ambient ISM, any real SNR may have a highly inhomogeneous upstream medium containing clumped gas. Recently, radio observations of SNR RX J1713.7-3946 (Sano et al. 2010; Fukui et al. 2012) have revealed clumpy atomic/molecular cloud distributions surrounding the SNR shell, indicating a possible interaction of the shock and the accelerated protons with the gas clouds. Concentrating the mass in small, dense clumps can considerably enhance the gamma-ray flux. Inoue et al. (2012) have investigated this possibility using 3-D MHD simulations of a shock running into an inhomogeneous medium. They pointed out the possibility that a hadronic model can avoid the problem of an over-prediction of the thermal X-ray flux, since the denser cores of the gas that carry most of the mass fraction can survive the shock passing without being ionized and hence will not contribute to the thermal emission, but still can interact with the accelerated protons and produce gamma-rays. While definitively ruling out hadronic scenarios in homogeneous broadband models of Vela Jr., our 1-D model cannot rule out hadronic dominated GeV-TeV emission in more complex clumpy environments. In fact, although not pursued in this work, it is possible that the gamma-rays are contributed by a two-component mixture of IC and \( \pi^0 \)-decay photons from the interaction of dense gas clumps and the accelerated CR protons. Future high-resolution observations of the surrounding interstellar gas distribution and 3-D hydro simulations self-consistently coupled to DSA will provide a quantitative estimate on this possible \( \pi^0 \)-decay component from clumps.

To explain the broadband spectrum of the SNR as a whole, our leptonic model requires a low B-field (\( \sim a few \mu G \)) on average in the SNR shell, which is one of the reasons why the presence of a wind cavity is necessary to provide a weak B-field in the upstream medium. The fact that magnetic field amplification in the shock precursor is taken into account in our models only strengthens this need. This low downstream B-field is highly consistent with those inferred from measurements of the X-ray/TeV brightness ratio (Aharonian et al. 2007) and more recently the radial variation of X-ray synchrotron spectral indices (Pannuti et al. 2010; Kishishita et al. 2013). However, as briefly mentioned earlier, it disagrees with some previous claims of large post-shock B-fields (\( \sim 0.1 \) mG) based on the discovery of sharp X-ray filaments in the NW shell. The argument for such large field strength is built on the assumption that the narrow widths of such filaments are realized by a short synchrotron loss time-scale for the electrons. Our broadband analysis and supporting observational data essentially show that an alternative explanation for the sharp filamentary structures without the need to invoke large B-field strengths may be necessary (see e.g., Bykov et al. 2008; Ellison & Vladimirov 2008, and references therein). We leave this important point as an open question to be answered by future works.

A fundamental question for DSA in SNRs is the fraction of SN explosion energy, \( f_{\mathrm{SN}} \), channeled into CRs. Our two models show that this fraction can be very different, at a given age, depending on whether the gamma-ray production mechanism is assumed to be \( \pi^0 \)-decay or IC. For Vela Jr., at \( t_{\mathrm{SNR}} = 2500 \) yr, \( f_{\mathrm{SN}} \approx 0.14 \) for our leptonic model and \( f_{\mathrm{SN}} \approx 0.48 \) for our hadronic model. In both cases, of course, CR protons contain the large majority of the CR energy. The ratio of CR electron to CR proton energy density is given by \( K_{\mathrm{ep}} \) and \( K_{\mathrm{ep}} \approx 0.015 \) for our leptonic model and \( K_{\mathrm{ep}} \approx 1.5 \times 10^{-4} \) for our hadronic model.

The determination of the gamma-ray origin, therefore, relates directly to the long postulated but unproven link between SNRs and Galactic CRs, that is, whether or not the Galactic ensemble of SNRs can meet the energy budget of the CR spectrum. Because the \( \pi^0 \)-decay and IC mechanisms are so different, a mis-interpretation of the multi-wavelength data including the gamma-rays can yield a very wrong prediction for the contribution of SNRs to the Galactic CRs. Of course, the CR energy budget depends ultimately on \( f_{\mathrm{SN}} \) over the full age of the remnant so it will be interesting to see how \( f_{\mathrm{SN}} \) evolves from very young ages up to the radiative phase of a SNR. In particular, the recent discovery of gamma-ray bright middle-aged SNRs by Fermi LAT may imply active particle acceleration at radiative shocks running into molecular clouds despite their slow speeds.

Another important point is that the evolution of a SNR in a changing ambient environment may shift the dominating gamma-ray production mechanism with age. It is hence critical to understand observations from SNRs of different ages and try to link them together into a self-consistent evolutionary picture. We will pursue this line of work in a series of follow-up papers.

Finally, we discussed the implications of our models for Vela Jr. on future observations by the next-generation of observatories, including CTA and Astro-H. We showed that CTA may be able to distinguish broadband emission models by measuring TeV brightness profiles with its unprecedented angular resolving power. This is especially valuable to distinguish leptonic and hadronic models for Vela Jr., as we have illustrated in Figure 8. In the X-ray band, the soon to be commissioned Astro-H space telescope possesses an extremely powerful calorimeter for high-resolution spectral studies, and we have postulated that there is a high possibility that SXS will be able to detect the more prominent thermal lines (see Figure 9) from non-thermal dominated SNRs such as Vela Jr. and RX J1713.7-3946. We expect future multi-wavelength observations will put extremely precise constraints on our model parameters, allowing us to firmly pin down the origin of the high-energy emission and to gain further insight on the particle acceleration mechanism in young SNR shocks.

The authors acknowledge important discussions with Takaaki Tanaka and Hidetoshi Sano concerning this work. They also thank the anonymous referee for providing valuable suggestions on improving the quality of this manuscript. D.C.E. acknowledges support from NASA grants ATP02-0042-0006, NNNH04Zs001N-LTSA, 06-ATP06-21, and NNX11AE03G. P.S. acknowledges support from NASA Contract NAS8-03060. S.N. acknowledges support from Ministry of Education, Culture, Sports, Science and Technology (No. 23105709), Japan Society for the Promotion of Science (No. 19104006 and No. 23340069), and the Global COE Program, The Next Generation of Physics, Spun from Universality and Emergence, from MEXT of Japan.
REFERENCES

<table>
<thead>
<tr>
<th>Input parameters</th>
<th>Hadronic $^a$</th>
<th>Leptonic $^b$</th>
<th>Remarks</th>
</tr>
</thead>
<tbody>
<tr>
<td>$d_{\text{SNR}}$ [kpc]</td>
<td>0.74</td>
<td>0.88</td>
<td>Distance to SNR</td>
</tr>
<tr>
<td>$n_0$ [cm$^{-3}$]</td>
<td>0.033</td>
<td>(0.002)</td>
<td>Far upstream gas density</td>
</tr>
<tr>
<td>$B_0$ [$\mu$G]</td>
<td>0.5</td>
<td>(0.14)</td>
<td>Far upstream B-field</td>
</tr>
<tr>
<td>$dM/dt$ [$10^{-6}$ $M_\odot$ yr$^{-1}$]</td>
<td>7.5</td>
<td>Pre-SN mass loss rate</td>
<td></td>
</tr>
<tr>
<td>$V_{\text{wind}}$ [km s$^{-1}$]</td>
<td>50</td>
<td>Pre-SN wind speed</td>
<td></td>
</tr>
<tr>
<td>$\sigma_{\text{wind}}$</td>
<td>0.02</td>
<td>Wind magnetization</td>
<td></td>
</tr>
<tr>
<td>$K_{\text{ep}}$</td>
<td>1.5 $\times$ 10$^{-4}$</td>
<td>(e$^-$/p) ratio at $p_{\text{max}}$ of e$^-$</td>
<td></td>
</tr>
<tr>
<td>$\alpha_{\text{cut}}$</td>
<td>0.75</td>
<td>Exp. cut-off index $^c$</td>
<td></td>
</tr>
<tr>
<td>$f_{\text{FEB}}$</td>
<td>0.15</td>
<td>Width of FEB over $R_{\text{FS}}$ $^d$</td>
<td></td>
</tr>
<tr>
<td>$f_{\text{all}}$</td>
<td>0.10</td>
<td>$x$-dependance of $v_A$ $^e$</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Output quantities</th>
<th>Hadronic $^a$</th>
<th>Leptonic $^b$</th>
<th>Remarks</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R_{\text{FS}}$ [pc]</td>
<td>12.7</td>
<td>15.2</td>
<td>Forward shock radius</td>
</tr>
<tr>
<td>$R_{\text{CD}}$ [pc]</td>
<td>10.3</td>
<td>12.5</td>
<td>Contact discontinuity radius</td>
</tr>
<tr>
<td>$V_{\text{FS}}$ [km s$^{-1}$]</td>
<td>2130</td>
<td>4700</td>
<td>Forward shock velocity</td>
</tr>
<tr>
<td>$p_{\text{max}}$ (p) [TeV/c]</td>
<td>26.7</td>
<td>5.2</td>
<td>Proton max. momentum</td>
</tr>
<tr>
<td>$p_{\text{max}}$ (e$^-$) [TeV/c]</td>
<td>13.3</td>
<td>5.2</td>
<td>Electron max. momentum</td>
</tr>
<tr>
<td>$R_{\text{tot}}$</td>
<td>9.30</td>
<td>4.69</td>
<td>Total compression ratio</td>
</tr>
<tr>
<td>$R_{\text{sub}}$</td>
<td>3.69</td>
<td>3.99</td>
<td>Subshock compression ratio</td>
</tr>
<tr>
<td>$B_2$ [$\mu$G]</td>
<td>34.1</td>
<td>4.8</td>
<td>Downstream B-field</td>
</tr>
<tr>
<td>$T_2$ [$10^8$ K]</td>
<td>0.16</td>
<td>3.62</td>
<td>Downstream temperature</td>
</tr>
<tr>
<td>$\epsilon_{\text{acc}}$</td>
<td>0.84</td>
<td>0.36</td>
<td>Total accel efficiency</td>
</tr>
<tr>
<td>$\epsilon_{\text{esc}}$</td>
<td>0.34</td>
<td>0.12</td>
<td>Escaped accel efficiency</td>
</tr>
<tr>
<td>$E_{\text{CR}}/E_\text{SN}$ ($f_{\text{SN}}$)</td>
<td>0.48</td>
<td>0.14</td>
<td>SN energy converted to CR</td>
</tr>
</tbody>
</table>

$^*$ For all models listed in this Table, Bohm diffusion is assumed in the DS and precursor region, and MFA is included. These models all have $E_\text{SN} = 10^{51}$ erg, $T_0 = 10^4$ K, and $f_{\text{He}} = 0.0977$.  
$^†$ Values in parentheses are taken at $t = t_{\text{age}} (= 2500$ yr).  
$^a$ Best-fit model under the ‘hadronic-dominated’ scenario with a uniform upstream medium.  
$^b$ Best-fit model under the ‘leptonic-dominated’ scenario with a pre-SN magnetized wind.  
$^c$ See e.g. equation (24) in Lee et al. (2012) for definition.  
$^d$ See e.g. equation (1) and description in Ellison & Vladimirov (2008).  
$^e$ See e.g. equation (14) in Lee et al. (2012) for definition.