

Physical origin of hydrophobicity studied in terms of cold denaturation of proteins: Comparison between water and simple fluids

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A clue to the physical origin of the hydrophobicity is in the experimental observations manifesting that it is weakened at low temperatures. By considering a solvophobic model protein immersed in water and three species of simple solvents, we analyze the temperature dependences of the changes in free energy, energy, and entropy of the solvent upon protein unfolding. The angle-dependent and radial-symmetric integral equation theories and the morphometric approach are employed in the analysis. Each of the changes is decomposed into two terms which depend on the excluded volume and on the area and curvature of solvent-accessible surface, respectively. The excluded-volume term of the entropy change is further decomposed into two components representing the protein-solvent pair correlation and the protein-solvent-solvent triplet and higher-order correlation, respectively. We show that water crowding in the system becomes more serious upon protein unfolding but this effect becomes weaker as the temperature is lowered. If the hydrophobicity originated from the water structuring near a nonpolar solute, it would be strengthened upon the temperature lowering. Among the three species of simple solvents, considerable weakening of the solvophobicity at low temperatures is observed only for the solvent where the particles interact through strongly attractive potential and the particle size is as small as that of water. Even in the case of this solvent, however, cold denaturation of a protein cannot be reproduced. It would be reproducible if the attractive potential was substantially enhanced, but such enhancement causes the appearance of the metastability limit for a single liquid phase.

1 Introduction

The hydrophobic effect at ambient temperature is powerful enough to drive a variety of self-assembly processes in aqueous environments such as micelle formation, protein folding and aggregation, receptor-ligand binding, and lipid membrane formation^{1–7}. However, there is much experimental evidence showing that the hydrophobicity is weakened at low temperatures for small nonpolar solutes, amphiphilic molecules, and biomolecules like proteins. For example, upon the temperature lowering, the solubility of methane increases^{3,5,6}, the critical micelle concentration becomes higher, the average size of micelles for nonionic amphiphilic molecules becomes smaller⁸, most of the proteins unfold at 250 ~ 260 K^{9–11} (this unfolding is referred to as cold denaturation; yeast frataxin⁹ unfolds at the exceptionally high temperature, ~ 280 K), and protein aggregation is dissociated¹². Despite the crucial importance of the hydrophobicity, its physical origin still remains rather ambiguous. A prevailing view is that the hydrophobicity originates from the inability of nonpolar solutes to participate in hydrogen bonds of water molecules and the resultant water structuring near the solutes giving rise to entropic loss¹.

If this was true, the hydrophobicity would be strengthened due to the enhanced hydrogen bonding when the temperature is lowered, which clearly conflicts with the experimental observations described above⁶. We believe that a clue to the physical origin of the hydrophobicity is in its weakening at low temperatures.

In a previous study⁶, we calculated hydration thermodynamic quantities (hydration free energy μ , entropy S_V , and energy U_V) of small hard-sphere solutes using the angle-dependent integral equation theory^{6,13–16} combined with a multipolar water model^{13,14}. The calculation was performed under the isochoric condition. The dependence of $\beta\mu$ on T ($\beta = 1/(k_B T)$, k_B is the Boltzmann constant, and T is the absolute temperature) was discussed because the Ostwald coefficient $\exp(-\beta\mu)$ is a measure of the hydrophobicity. As the measure increases, the hydrophobicity becomes weaker. In what follows, we recapitulate the significant results obtained. When the number density of bulk water is taken to be that of real water along the saturation curve, $\beta\mu$ possesses the maximum value at ~ 323 K, which is consistent with the experimental result known for methane^{3,5,6}. The measure becomes larger monotonically as T decreases from ambient temperature. This temperature dependence of the measure arises primarily from that of the translational component of S_V . The orientational component of S_V exhibits the opposite temperature

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dependence, which can be associated with the enhanced hydrophobicity at low temperatures and understood indisputably on the basis of the conventional picture¹. The translational component is substantially larger than the orientational component. Here, the translational and orientational components represent the contributions from the translational and orientational freedoms of water molecules restricted by solute insertion, respectively. The proposition reached is the following: What is responsible for the hydrophobic effect is not the hydrogen-bonding property but the interplay of the exceptionally small molecular size and strongly attractive interaction of water⁶. However, the relation between this proposition and the physical origin of the hydrophobicity exhibiting the characteristic temperature dependence mentioned above is to be elucidated further.

It has been pointed out for spherical solutes that the behavior of a sufficiently large solute is qualitatively different from that of a small one⁴. The hydration free energy μ of the former at ambient pressure is scaled by the water-accessible surface area (ASA) A as expressed by

$$\mu \simeq \gamma A \quad (1)$$

where γ is the surface tension of water that is positive. The water-accessible surface is the surface that is accessible to the centers of water molecules¹⁷. On the other hand, it is well known that μ of a small solute is substantially dependent on the excluded volume (EV) which is the volume enclosed by the water-accessible surface¹⁷. One might think that a protein is large enough to obey the scaling of Eq. (1), but this thought is inconsistent with cold denaturation caused by the weakening of the hydrophobicity at low temperatures. This inconsistency arises from the fact that as T becomes lower, γ increases: The scaling indicates that the hydrophobicity would become stronger. A protein possesses hydrophobic regions of widely varying length scales due to its complex polyatomic structure, which may distinguish it from a large spherical solute.

In the present study, we investigate the physical origin of the hydrophobicity by revisiting cold denaturation of a protein. Considering a completely solvophobic model protein^{18–23} immersed in water and three species of simple solvents for which the same solvent packing fraction is assumed, we analyze the temperature dependences of the changes in free energy, energy, and entropy of the solvent upon protein unfolding. The angle-dependent^{6,13–16} and radial-symmetric^{24–27} integral equation theories and the morphometric approach^{28–30} are employed in the analysis. The three species of simple solvents considered are (i) a solvent in which the particles interact through strongly attractive potential and the particle diameter is as small as that of water (simple solvent 1); (ii) a solvent in which the particles interact through strongly attractive potential but the particle diameter is about 1.9 times

larger than that of water (simple solvent 2); and (iii) a hard-sphere solvent whose particle diameter is the same as that of water. The microscopic mechanism of cold denaturation of a protein was studied in earlier works^{20,21,23}, but the consideration of these simple solvents in the present work is expected to give a much larger amount of physically insightful information on the nature of the hydrophobicity. The morphometric approach allows us to decompose any of solvation thermodynamic quantities or its change upon protein unfolding into two terms which depend on the EV (term 1) and on the area and curvature of solvent-accessible surface (term 2), respectively. Effects due to the formation of ordered structure by the solvent molecules near the protein surface are included in term 2. Term 1, on the other hand, represents the contribution from the solvent molecules in the system with the proviso that the solvent molecules near the protein surface, which are influenced by the solute-solvent potential, are not included; See Subsection 2.5). For water and simple solvent 1, term 1 of the solvent-entropy change is further decomposed into two components representing the protein-solvent pair correlation and the protein-solvent-solvent triplet and higher-order correlation, respectively. The former is relevant to the total volume available to the translational displacement of solvent molecules. The latter is related to solvent crowding in the system. We note that the presence of a solvent molecule also generates an EV for the other solvent molecules, thus causing the solvent crowding. Such correlation among solvent molecules is not included in the protein-solvent pair correlation component.

The principal results can be summarized as follows. For water, the protein-solvent-solvent triplet and higher-order correlation component of term 1 of the negative entropy change upon protein unfolding becomes markedly smaller as T decreases, which leads to cold denaturation of a protein induced by the weakening of the hydrophobicity. Water crowding in the system becomes more serious upon protein unfolding, but this effect becomes weaker as T becomes lower. If the hydrophobicity originated from the structuring of water near a nonpolar solute as in the conventional view, it would be strengthened upon the temperature lowering. The rotational-entropy loss upon solute insertion is often emphasized for water, but only the water molecules near the solute contribute to it. Its effect is much less important than that of the translational entropy. Term 1 of the hydration free energy plays essential roles for a protein like for small nonpolar solutes such as methane. Among the three species of simple solvents, considerable weakening of the solvophobicity at low temperatures is observed only for simple solvent 1. Even in the case of this solvent, however, cold denaturation cannot be reproduced. It would be reproducible if the attractive potential was substantially enhanced, but such enhancement gives rise to the appearance of the spinodal point beyond which the liquid state

cannot exist as a single phase even in a metastable state. Water is unique in the sense that the hydrophobicity is powerful enough to form self-assembled structures at ambient temperature but substantially weakened when the temperature is lowered, leading to the collapse of the structures. We argue that the weakening of the solvophobicity at low temperatures is ascribed to enhanced local associations of solvent molecules in the bulk, causing more inhomogeneity followed by the formation of more void space: Due to the presence of more void space, the solvent can accommodate a solvophobic solute with less difficulty.

2 Models and Theories

2.1 Change in system free energy upon protein unfolding

We first consider a real protein immersed in aqueous solution. Diluted proteins are considered. The free-energy difference between the unfolded state and the native structure ΔG can be written as

$$\Delta G(T) = \Delta E_I + \Delta \mu(T) - T\Delta S_C(T). \quad (2)$$

Here, E_I is the protein intramolecular energy and $S_C(T)$ is the conformational entropy of the protein. $\Delta Z \equiv Z_D - Z_N$ denotes the change in a thermodynamic quantity upon the unfolding. The subscripts “N” and “D” represent the values for the native structure and for the unfolded (denatured) state, respectively. ΔG , which is positive at ambient temperature, turns negative below the cold denaturation temperature. Under the isochoric condition, μ is expressed by

$$\mu(T) = U_V(T) - TS_V(T). \quad (3)$$

The justification of considering the isochoric condition is discussed in Subsection 2.5. Equation (2) is then written as

$$\Delta G(T) = \Delta E_I + \Delta U_V(T) - T\Delta S_V(T) - T\Delta S_C(T). \quad (4)$$

We decompose $\Delta U_V(T)$ into three terms as

$$\Delta U_V(T) = \Delta U_{IN}(T) + \Delta U_{RO}(T) + \Delta U_{V,HS}(T), \quad (5)$$

where $\Delta U_{V,HS}(T)$ is the change in the hydration energy calculated by replacing all the protein atoms by hard spheres (i.e., by modeling the protein as a set of fused hard spheres). $\Delta U_{IN}(T)$ and $\Delta U_{RO}(T)$ correspond to the changes in the protein-water interaction energy and in the water reorganization energy, respectively. These changes arise from the incorporation of the protein-water van der Waals and electrostatic interactions. Only the water molecules near the protein surface contribute to them. According to a recent experimental study³¹, $\Delta E_I + \Delta U_{IN}(T) + \Delta U_{RO}(T) + \Delta U_{V,HS}(T)$ is negative at ambient temperature and it decreases further as T becomes

lower. For a solvent in which the solvent molecules interact through strongly attractive potential like water, $\Delta U_{V,HS}(T)$ is negative and its absolute value becomes larger as the EV of a solute increases or T decreases⁶. Since the EV of the unfolded state is much larger than that of the native structure, $\Delta U_{V,HS}(T)$ takes a large, negative value. Moreover, it decreases as T becomes lower. The experimentally known behavior of $\Delta E_I + \Delta U_{IN}(T) + \Delta U_{RO}(T) + \Delta U_{V,HS}(T)$ mentioned above is reproducible by $U_{V,HS}(T)$. We assume that $\Delta E_I + \Delta U_{IN}(T) + \Delta U_{RO}(T)$ can be neglected for the following reason. When the protein unfolds, the protein intramolecular hydrogen bonds and van der Waals interactions are lost, leading to a positive value of ΔE_I . However, due to the protein-water hydrogen bonds and van der Waals interactions gained, $\Delta U_{IN}(T)$ takes a negative value. For the exposure of nonpolar groups $\Delta U_{RO}(T)$ remains almost unchanged, while for that of polar and charged groups $\Delta U_{RO}(T)$ becomes positive¹⁶. The three terms, ΔE_I , $\Delta U_{IN}(T)$, and $\Delta U_{RO}(T)$ are somewhat compensating^{32–34}. As argued in our earlier work²⁰, the neglect of $\Delta E_I + \Delta U_{IN}(T) + \Delta U_{RO}(T)$ simply leads to a small shift of the cold denaturation temperature.

In general, U_V and μ are largely dependent on the solute-water interaction potentials, while S_V is considerably insensitive to them^{35,36}. For example, using the three-dimensional reference interaction site model (3D-RISM) theory combined with all-atom potentials comprising Lennard-Jones (LJ) and Coulomb terms and the SPC/E water model, Imai *et al.*³⁵ calculated S_V of the native structures of a total of eight peptides and proteins. Even when the protein-water electrostatic potentials, which are quite strong, are shut off and only the LJ potentials are retained, S_V decreases merely by less than 5%. In our earlier work³⁶, μ , S_V , and U_V at 298.15 K were calculated for a hard-sphere solute with diameter of water molecule using the angle-dependent integral equation theory^{6,13,14,16} combined with the multipolar water model^{13,14}. The calculated values are $\mu = 5.95k_B T$, $S_V = -9.22k_B$, and $U_V = -3.27k_B T$. When the point charge $-0.5e$ (e is the electronic charge) is embedded at its center, the calculated values are $\mu = -32.32k_B T$, $S_V = -10.11k_B$, and $U_V = -42.43k_B T$: μ and U_V exhibit large decreases while S_V remains roughly unchanged. Thus, S_V can be approximated by $S_{V,HS}$ representing the hydration entropy calculated for the model protein, a set of fused hard spheres.

On the basis of the above discussion, Eq. (4) is approximately given by

$$\Delta G(T) \simeq \Delta \mu_{HS}(T) - T\Delta S_C(T), \quad (6)$$

where $\mu_{HS}(T) = U_{V,HS}(T) - TS_{V,HS}(T)$ is the hydration free energy of the protein modeled as a set of fused hard spheres. Hereafter, the subscript “HS” is omitted (e.g., $\mu_{HS}(T)$ is denoted simply by $\mu(T)$). We employ Eq. (6) by adopting a set of fused hard spheres which is completely solvophobic as

the protein model for all the solvents considered. It should be noted that the details of the polyatomic structure, which is crucially important, are fully taken into account. $T\Delta S_C(T)$ and $\Delta\mu(T)$ take large, positive values. $\Delta G(T)$ is positive at ambient temperature. $\Delta S_C(T)$ is almost constant³⁷ or a slightly increasing function of T ³⁸. In either case, $-T\Delta S_C(T)$ increases as T becomes lower, shifting $\Delta G(T)$ in a more positive direction. Therefore, $\Delta\mu(T)$ must decrease to a sufficiently large extent for $\Delta G(T)$ to turn negative below the cold denaturation temperature. $\Delta\mu(T)$ is the key quantity for describing the stability of the native structure of a protein.

The heat-capacity change for the entire system upon protein denaturation has experimentally been shown to be positive^{9–11}. It comprises the contributions from the hydration of nonpolar, polar, and charged groups and from the protein intramolecular energy. The contribution from the hydration of polar and charged groups is negative^{39,40} and that from the intramolecular energy is negligibly small^{41,42}. Therefore, the contribution from the hydration of nonpolar groups, which is positive^{41,43}, is dominant. This gives another justification of considering a completely hydrophobic model protein in the present study. Completely hydrophobic model proteins were considered in previous studies^{18–23} as well.

2.2 Protein and solvent models

The protein we consider is protein G with 56 residues [PDB code: 2GB1]. As explained above, the protein is modeled as a set of fused hard spheres. The (x, y, z) coordinates of all the protein atoms (hydrogen, carbon, nitrogen, oxygen, etc.) in the backbone and side chains are used as part of the input data to account for the characteristics of each structure on the atomic level. The diameter of each atom is set at the σ -value of the LJ potential parameters of AMBER99. We assume that the unfolded state comprises a set of random coils⁹. As in our earlier work²⁰, 32 random-coil structures³² are employed as the unfolded state.

A water molecule is modeled as a hard sphere with diameter $d_S = 0.28$ nm in which a point dipole and a point quadrupole of tetrahedral symmetry are embedded^{13,14}. The influence of molecular polarizability of water is included by employing the self-consistent mean field (SCMF) theory^{13,14}. At the SCMF level the many-body induced interactions are reduced to pairwise additive potentials involving an effective dipole moment. The number density of the bulk water ρ_S is taken to be that of real water along the saturation curve. The four temperatures, 258.15, 263.15, 273.15, and 298.15 K, are examined and

the values of $\rho_S d_S^3$ at these temperatures are 0.7312, 0.7325, 0.7338, and 0.7317, respectively.

Particles of the simple solvents interact through

$$u_{SS} = \infty \quad \text{for } r < d_S, \quad (7a)$$

$$u_{SS} = -\epsilon_{SS} \left(\frac{d_S}{r} \right)^6 \quad \text{for } r > d_S. \quad (7b)$$

For “simple solvent 1”, d_S and $\epsilon_{SS}/(k_B T)$ are set at 0.28 nm and 1.6 at 298.15 K, respectively. When ϵ_{SS} is set at zero, the solvent is formed by hard spheres and referred to as “hard-sphere solvent”. In simple solvent 1 and the hard-sphere solvent, $\rho_S d_S^3$ at each temperature is taken to be the same as that of water. It is physically insightful to look at the effect of the solvent diameter. To this end, we consider a simple solvent whose molecular diameter d'_S is set at 0.53 nm that equals the σ -value of the LJ potential parameters for carbon tetrachloride (CCl₄)⁴⁵. The number density ρ'_S is evaluated so that $\rho'_S d'^3_S$ at each temperature becomes the same as $\rho_S d^3_S$ of water, and $\epsilon_{SS}/(k_B T)$ is set at 1.6 at 298.15 K (the same as that for simple solvent 1). We refer to this solvent as “simple solvent 2”. We note that all the four solvents share the same packing fraction at each temperature.

2.3 Integral equation theories

The quantities we calculate are the hydration free-energy μ , entropy S_V , and energy U_V (they are referred to as the solvation free-energy, entropy, and energy, respectively, when all the solvents are simultaneously considered) for a protein with a prescribed structure. They are obtained through the integral equation theories and the morphometric approach^{28–30} described in the next subsection.

A hard-sphere solute of diameter d_U is immersed in solvent at infinite dilution. The solute-solvent correlation functions are calculated by the integral equation theory for the simple fluids^{24–27} and by its angle-dependent version for water^{6,13–16}, and μ is obtained using the Morita-Hiroike formula^{46,47} or its extension to molecular liquids^{6,48}. S_V is evaluated through the numerical differentiation of μ with respect to T ^{6,48} as

$$S_V = - \left(\frac{\partial \mu}{\partial T} \right)_V = - \frac{\mu(T + \delta T) - \mu(T - \delta T)}{2\delta T}, \quad \delta T = 5 \text{ K}. \quad (8)$$

U_V is obtained from $U_V = \mu + TS_V$. In the hard-sphere solvent, U_V is zero and μ equals $-TS_V$. The solvation thermodynamic quantities are calculated for sufficiently many different values of d_U for determining the coefficients in the morphometric form (Eqs. (9) and (10)).

S_V can be expressed as an expansion in terms of multiparticle correlation functions for a solute immersed in solvent⁴⁹. On the basis of the expansion, we can decompose S_V into the

*It has recently been shown that yeast frataxin, which is denatured at 280 K, possesses the properties of an unfolded protein at 272 K though a small amount of local, residual secondary structure is retained⁴⁴. Our conclusions are not likely to be altered even when a completely unfolded state is considered as the cold-denatured one.

two components: the solute-solvent pair correlation component, $S_{V,\text{Pair}}$, and the solute-solvent-solvent triplet and higher-order correlation component, $S_{V,\text{Multi}}$ ^{50,51}. $S_{V,\text{Pair}}$ is calculated using the solute-solvent pair correlation function and $S_{V,\text{Multi}}$ is obtained as $S_V - S_{V,\text{Pair}}$. Details of the decomposition were described in our previous papers^{50,51}.

The radial-symmetric integral equation theory has been applied to a number of problems for simple fluids with successful results^{24–27}. The reliability of the angle-dependent integral equation theory has also been verified in a number of studies. For example, the hydration free energies of small nonpolar solutes calculated by the theory combined with the multipolar water model are in perfect agreement with those from Monte Carlo simulations with the SPC/E and TIP4P water models⁶. The dielectric constant for bulk water, which is determined from the water-water orientational correlation functions, is in good agreement with the experimental data⁶. The theory is also capable of elucidating the hydrophilic hydration experimentally known¹⁶.

2.4 Morphometric approach: decomposition of thermodynamic quantities of solvation and their changes upon protein folding

In this approach, any of the solvation thermodynamic quantities is expressed using only four geometric measures of a solute with a fixed structure and corresponding coefficients^{28–30}. The resultant morphometric form for the quantity Z is given by

$$Z = C_1 V_{\text{ex}} + C_2 A + C_3 X + C_4 Y. \quad (9)$$

Here, V_{ex} is the EV, A is the ASA, and X and Y are the integrated mean and Gaussian curvatures of the water-accessible surface, respectively, and they form the four geometric measures. We calculate them for a protein with a prescribed structure by means of the extension²⁹ of Connolly's algorithm^{52,53}. In Eq. (9), the solute shape enters Z only via the four geometric measures. Therefore, the four coefficients (C_1 – C_4) can be determined in simple geometries: They are determined from the values of Z for hard-sphere solutes with various diameters (those in the range $0 \leq d_U \leq 5d_S$; changing $5d_S$ to $10d_S$, for example, leads to no changes in the four coefficients determined). For the determination, we employ the angle-dependent (for water) or radial-symmetric (for the three species of simple solvents) integral equation theory. More details of the determination were described in our earlier publications^{21,48,51}. Once the four coefficients are determined, Z of a protein with any structure can be obtained by calculating only its four geometric measures.

For Z , we consider such quantities as μ , S_V , and U_V . Z can be decomposed into two terms. One of them consists of the second, third, and fourth terms in Eq. (9). This term, which is referred to as term 2, depends only on the area and curvatures

of the solvent-accessible surface of the protein. It represents the contribution from the solvent molecules near the protein surface. The other is the first term in Eq. (9) which is referred to as term 1. The solvent molecules in the system, excluding those near the protein surface, contribute to term 1 depending on the EV of the protein. Terms 1 and 2 of Z are denoted by Z_{Term1} and Z_{Term2} , respectively.

We are concerned with ΔZ denoting the change in Z upon protein unfolding. Z of the unfolded state is calculated as its average value for the 32 random coils. With the present protein model, $\Delta\mu$, ΔU_V , and ΔS_V correspond to the changes in free energy, energy, and entropy of the solvent upon the unfolding, respectively. It follows from Eq. (9) that ΔZ is expressed as:

$$\Delta Z = C_1 \Delta V_{\text{ex}} + C_2 \Delta A + C_3 \Delta X + C_4 \Delta Y. \quad (10)$$

As in the case of Z , we can discuss ΔZ by decomposing it into two terms, terms 1 and 2^{20,21}. Term 2, which consists of the second, third, and fourth terms in Eq. (10), is dependent only on the changes in the area and curvatures of the solvent-accessible surface upon the unfolding. Term 1 is the first term in Eq. (10) which is influenced by the change in the EV. Terms 1 and 2 of ΔZ are denoted by $(\Delta Z)_{\text{Term1}}$ and $(\Delta Z)_{\text{Term2}}$, respectively.

In the case of water, any of the hydration thermodynamic quantities can be decomposed into translational and orientational components⁶. We emphasize that the translational component of $-T\Delta S_V$ possesses the EV term (term 1) while the orientational component does not^{48,50}. The physical meaning of these components of ΔS_V , for instance, is the following: Upon solute insertion, the translational and orientational freedoms of water molecules are reduced, causing losses of translational and rotational entropy of water, respectively. Only the water molecules near the solute undergo the orientational reduction, while the translational reduction reaches the water molecules in the bulk as well.

The usefulness of the morphometric approach has already been demonstrated. For example, the results from the three-dimensional integral equation theory^{54,55} applied to the same model protein immersed in a simple solvent can be reproduced with sufficient accuracy by the morphometric approach applied to the same solvent^{29,48}. By a hybrid of the angle-dependent integral equation theory combined with the multipolar water model and the morphometric approach, the experimentally measured changes in thermodynamic quantities upon apoPC folding are quantitatively reproduced⁴⁸. Moreover, great progresses have been made in elucidating the microscopic mechanisms of pressure^{50,51}, cold^{20,21}, and heat^{56,57} denaturing of proteins, developing a physical picture for the rotation of F₁-ATPase⁵⁸, and discrimination of a native fold from misfolded decoys^{59–61} by our theoretical methods in which the morphometric approach is combined with

the radial-symmetric integral equation theory or the angle-dependent version.

2.5 Isochoric and isobaric conditions

We consider the isochoric condition while the experiments are performed under the isobaric condition. This can be justified as follows. Under the isobaric condition, the changes in the solvent entropy and enthalpy upon protein unfolding, ΔS_P and ΔH , are related to ΔS_V and ΔU_V through the thermodynamic relations^{15,62–64}

$$\Delta S_P/k_B = \Delta S_V/k_B + \frac{\alpha^*}{\kappa_T^*} \frac{\Delta V_P}{d_S^3}, \quad (11a)$$

$$\Delta H/(k_B T) = \Delta U_V/(k_B T) + \frac{\alpha^*}{\kappa_T^*} \frac{\Delta V_P}{d_S^3}, \quad (11b)$$

where V_P is the partial molar volume of the protein (i.e., change in the system volume upon protein insertion under the isobaric condition). The dimensionless parameters with the superscript “*”, which depend only on the properties of bulk solvent, are defined as

$$\alpha^* = \alpha T, \quad (12a)$$

$$\kappa_T^* = \kappa_T k_B T / d_S^3, \quad (12b)$$

where α is the isobaric thermal expansion coefficient and κ_T is the isothermal compressibility.

We write ΔS_V and ΔU_V in Eq. (11) as

$$\begin{aligned} \Delta S_V &= (\Delta S_V)_{\text{Term1}} + (\Delta S_V)_{\text{Term2}} \\ &= C_{1,S_V} \Delta V_{\text{ex}} + (\Delta S_V)_{\text{Term2}}, \end{aligned} \quad (13a)$$

$$\begin{aligned} \Delta U_V &= (\Delta U_V)_{\text{Term1}} + (\Delta U_V)_{\text{Term2}} \\ &= C_{1,U_V} \Delta V_{\text{ex}} + (\Delta U_V)_{\text{Term2}}. \end{aligned} \quad (13b)$$

Here, C_{1,S_V} or C_{1,U_V} is the first coefficient in Eq. (10) applied to S_V or U_V . ΔV_P can be expressed by

$$\Delta V_P = \Delta V_{\text{ex}} + (\Delta V_P)_{\text{Term2}}. \quad (14)$$

Equation (11) is then given by

$$\begin{aligned} \Delta S_P/k_B &= \left(C_{1,S_V}/k_B + \frac{\alpha^*}{\kappa_T^*} \frac{1}{d_S^3} \right) \Delta V_{\text{ex}} \\ &+ (\Delta S_V/k_B)_{\text{Term2}} + \frac{\alpha^*}{\kappa_T^*} \frac{1}{d_S^3} (\Delta V_P)_{\text{Term2}}, \end{aligned} \quad (15a)$$

$$\begin{aligned} \Delta H/(k_B T) &= \left(C_{1,U_V}/(k_B T) + \frac{\alpha^*}{\kappa_T^*} \frac{1}{d_S^3} \right) \Delta V_{\text{ex}} \\ &+ (\Delta U_V/(k_B T))_{\text{Term2}} + \frac{\alpha^*}{\kappa_T^*} \frac{1}{d_S^3} (\Delta V_P)_{\text{Term2}}. \end{aligned} \quad (15b)$$

Since ΔV_P is experimentally known to be essentially zero in a wide range of T ^{31,65}:

$$\Delta V_P \simeq 0, \quad (16a)$$

$$(\Delta V_P)_{\text{Term2}} \simeq -\Delta V_{\text{ex}}. \quad (16b)$$

It follows that

$$\Delta S_P/k_B \simeq (C_{1,S_V}/k_B) \Delta V_{\text{ex}} + (\Delta S_V/k_B)_{\text{Term2}}, \quad (17a)$$

$$\Delta H/(k_B T) \simeq C_{1,U_V}/(k_B T) \Delta V_{\text{ex}} + (\Delta U_V/(k_B T))_{\text{Term2}}. \quad (17b)$$

It is apparent from Eq. (17) that

$$(\Delta S_P)_{\text{Term1}} \simeq (\Delta S_V)_{\text{Term1}}, \quad (18a)$$

$$(\Delta S_P)_{\text{Term2}} \simeq (\Delta S_V)_{\text{Term2}}, \quad (18b)$$

$$(\Delta H)_{\text{Term1}} \simeq (\Delta U_V)_{\text{Term1}}, \quad (18c)$$

$$(\Delta H)_{\text{Term2}} \simeq (\Delta U_V)_{\text{Term2}}. \quad (18d)$$

Namely, ΔS_P , ΔH , and their terms 1 and 2 are approximately equal to ΔS_V , ΔU_V , and their terms 1 and 2, respectively. Due to the fact that $|\Delta V_P|$ is much smaller than $|\Delta V_{\text{ex}}|$ as in Eq. (16), ΔS_P as well as ΔS_V possesses term 1 (i.e., the EV-dependent term). As shown in Sec. 3, term 1 plays essential roles even in μ . This gives another evidence that the behavior of a sufficiently large solute expressed as Eq. (1), which is based on the assumption that term 1 of μ is negligibly small at ambient pressure^{4,15}, is not applicable to a protein.

2.6 Estimation of conformation-entropy change upon protein unfolding at 298.15 K

The conformational-entropy change upon protein unfolding, ΔS_C , at 298.15 K can be estimated in the following manner. It is experimentally known for a number of proteins that ΔG in aqueous solution is approximately ~ 50 kJ/mol at 298.15 K⁶⁶. We assume that protein G is no exception. Equation (6) applied to the case of $T = 298.15$ K then becomes

$$\Delta \mu(298.15\text{K}) - 298.15 \times \Delta S_C = 50\text{kJ/mol}. \quad (19)$$

We can estimate ΔS_C using Eq. (19) into which $\Delta \mu(298.15\text{K})$ calculated for water through Eq. (10) is substituted. It is assumed that ΔS_C takes the same value for all the solvents considered. Further, unless otherwise mentioned, ΔS_C is treated as a constant that is independent of T . The value of ΔG for any of the three species of simple solvents is given by $\Delta \mu(298.15\text{K}) - 298.15 \times \Delta S_C$ where $\Delta \mu(298.15\text{K})$ is calculated for the particular solvent.

3 Results and discussion

3.1 Temperature dependence of protein solvophobicity

The Ostwald coefficient $\exp(-\beta\mu)$ is a measure of the hydrophobicity, and we first look at the temperature dependence

of $\beta\mu$. In Figures 1(a) and (b), $\beta\mu$ of the native structure of protein G, which is modeled as a set of fused hard spheres, is plotted against T for water and the three species of simple solvents. The decomposition of $\beta\mu$ into terms 1 and 2 is shown in Figure 1(c) (water), (d) (simple solvent 1), (e) (simple solvent 2), and (f) (hard-sphere solvent). We note that $\beta\mu$ of the unfolded state displays qualitatively the same characteristics (the data is not shown).

For water, $\beta\mu$ takes a large positive value (~ 630) at 298.15 K but decreases as T becomes lower. It is observed in Figure 1(c) that this temperature dependence stems from that of term 1. Term 2, which is emphasized in the conventional view¹, exhibits the opposite temperature μ , term 1, and term 2 for simple solvent 1 are qualitatively similar to those for water, though $\beta\mu$ and term 1 for simple solvent 1 are significantly larger.

The behavior for simple solvent 2 is substantially different from that for simple solvent 1 (compare Figures 1(d) and (e)) despite that these two simple solvents share the same attractive potential parameter. For the is essentially constant. The very minor change in $\beta\mu$ is merely due to the change in the solvent number density. Thus, the hydrophobicity can never be reproduced even in a qualitative sense when the strongly attractive potential is shut off. Sufficiently large $\beta\mu$ at ambient temperature and the appreciable reduction in $\beta\mu$ upon the lowering of T is attributed to the interplay of the exceptionally respectively.

As observed in Figure 2(a) for water, $\Delta\mu$ decreases as T becomes lower: It decreases by ~ 115 kJ/mol upon the lowering of T from 298.15 K to 258.15 K. Both of ΔU_V (Figure 2(b)) and ΔS_V (Figure 2(c)) are negative and they decrease further as T becomes lower. It has experimentally been shown that the changes in enthalpy and entropy for the entire system upon protein unfolding are negative at ambient temperature and decrease further as T becomes lower³¹. The temperature dependences of ΔU_V and ΔS_V are consistent with this experimental result. It is observed in Figure 3(a) for simple solvent 1 that ΔS_V and ΔU_V , which are both negative, decrease further as T becomes lower. $\Delta\mu$ decreases by ~ 110 kJ/mol upon the lowering of T from 298.15 K to 258.15 K. These characteristics are qualitatively similar to those observed for water.

We now discuss the temperature dependences of terms 1 and 2 of $\Delta\mu$, ΔU_V , and $-T\Delta S_V$ or ΔS_V . It is found that the two terms exhibit similar dependences on T for water and simple solvent 1. The temperature dependence of $-T\Delta S_V$ or that of ΔU_V is governed by that of term 2. Term 2 of $-T\Delta S_V$ increases while that of ΔU_V decreases as T becomes lower. The increase and decrease are somewhat compensating but the increase is more or less larger: Term 2 of $\Delta\mu$ does not decrease as T becomes lower. Thus, cold denaturation cannot be induced by term 2 of $\Delta\mu$. A closer look at Figures 2 and 3 allows us to appreciate the following difference between water

and simple solvent 1. For water, term 2 of ΔU_V or ΔS_V decreases more sharply with decreasing T : the sign of term 2 of ΔS_V turns negative at ~ 265 K and that of ΔU_V is also likely to turn negative at a temperature lower than 258.15 K. This behavior, which is not shared by simple solvent 1, is attributable to the formation of highly ordered structure of water near the protein surface due to the enhancement of hydrogen bonding or increase in the number of hydrogen bonds. Compared with the native structure, the unfolded state possesses much larger ASA and more water molecules participating in the ordered-structure formation, leading to larger entropic loss and energy decrease upon the unfolding at lower temperatures. However, this entropic loss and energy decrease are almost cancelled out and term 2 of $\Delta\mu$ remains almost unchanged.

As argued in our earlier publications^{20,21}, the decrease in $\Delta\mu$ by ~ 115 kJ/mol mentioned above for water induces cold denaturation of our model protein at ~ 259 K. This behavior originates from the temperature dependence of term 1. The decrease in term 1 of $-T\Delta S_V$, which surpasses the increase in term 1 of ΔU_V , is the cause of cold denaturation. Here we decompose term 1 of $-T\Delta S_V$ into the two components, $-T\Delta S_{V,\text{Pair}}$ and $-T\Delta S_{V,\text{Multi}}$, representing the protein-water pair correlation and the protein-water-water triplet and higher-order correlation, respectively. A similar decomposition is performed for simple solvent 1. The results for water and simple solvent 1 are compared in Figures 4(a) and (b). We note that C_1 of $S_{V,\text{Pair}}$ is ρ_S ^{50,51} (only $S_{V,\text{Pair}}$ is incorporated in the Asakura-Oosawa theory^{67,68}). For both of the two solvents, $-T\Delta S_{V,\text{Multi}}$ is substantially larger than $-T\Delta S_{V,\text{Pair}}$. The temperature dependence of term 1 of $-T\Delta S_V$ arises from that of $-T\Delta S_{V,\text{Multi}}$. As a significant difference, for water, $-T\Delta S_{V,\text{Multi}}$ decreases more sharply as T becomes lower. The weakening of the hydrophobicity followed by cold denaturation in water is induced by the EV-dependent term of the hydration entropy at the protein-solvent-solvent triplet and higher-order correlation level.

The EV term (term 1) of $-T\Delta S_V$ is nothing but its translational component (the orientational component possesses no EV term^{48,50}; see Subsection 2.4). It should be emphasized that the presence of a water molecule generates an EV for the other water molecules, thus causing water crowding. The EV of the native structure is much smaller than that of the unfolded state^{48,69}. Upon protein folding, the water crowding in the system is substantially reduced, leading to a large gain in the translational entropy of water^{48,69}. This gain is a consequence of the protein-solvent-solvent triplet and higher-order correlation and the driving force of protein folding. However, this force becomes much less powerful at low temperatures, giving rise to cold denaturation.

As mentioned above, it is experimentally known that the heat-capacity change for the entire system upon protein denaturation is positive^{9–11}, implying the dominant contribution

from the hydrophobic hydration. Since ΔU_V and ΔS_V for water is an increasing function of T as shown in Figures 2(b) and (c), ΔC_V is positive, which is consistent with the experimental result. As far as the temperature dependence of ΔU_V or ΔS_V is concerned, it is governed by term 2. This indicates that ΔC_V is determined primarily by the contribution from hydrogen bonds of the water molecules near the protein surface. Our result never conflicts with the empirical picture that the change in the heat capacity upon protein denaturation can be scaled by that in the ASA⁷⁰. It is worthwhile to note that ΔC_V is much larger for water than for simple solvent 1 probably due to the hydrogen-bonding property (see Figures 2 and 3).

3.2 Temperature dependences of changes in thermodynamic quantities of simple solvent 2 and hard-sphere solvent upon protein unfolding

The temperature dependences of the changes in thermodynamic quantities of simple solvent 2 and hard-sphere solvent upon protein unfolding are shown in Figures 5 (simple solvent 2) and 6 (hard-sphere solvent). For the hard-sphere solvent, $\Delta U_V = 0$ and $\Delta\mu = -T\Delta S_V$.

By comparing Figures 3 and 5, we notice that the increase of the solvent diameter by 1.9 times leads to a drastic change in the behavior of thermodynamic quantities: The absolute values of $\Delta\mu$, ΔU_V , ΔS_V , and $-T\Delta S_V$ become substantially smaller and they exhibit much weaker temperature dependences. Qualitatively the same characteristics are observed for their terms 1 and 2. As for the hard-sphere solvent (Figure 6), ΔS_V is essentially independent of T and $\Delta\mu = -T\Delta S_V$ decreases simply in proportion to T as T becomes lower. The absolute value of ΔS_V for the hard-sphere solvent is much larger than for simple solvent 2, which should be due to the smaller solvent diameter. However, the hard-sphere solvent and simple solvent 2 share the behavior that ΔS_V remains almost constant against a temperature change. The experimentally known result³¹, “the changes in enthalpy and entropy for the entire system upon protein unfolding exhibit considerable decrease with lowering T ”, can never be explained.

In summary, with respect to the temperature dependences of changes in thermodynamic quantities of solvation upon protein unfolding, water and simple solvent 1 exhibit qualitatively similar behavior. The increase in the solvent diameter by 1.9 times or removal of the solvent-solvent attractive interaction potential in simple solvent 1 leads to drastically different behavior. The interplay of the exceptionally small molecular size and strongly attractive interaction of the solvent is important in reproducing the behavior of water. However, there are certainly some differences in details of the behavior between water and simple solvent 1, which is further discussed in a later subsection.

3.3 Change in thermodynamic quantities of entire system upon protein unfolding at ambient temperature

Table 1 shows $\Delta\mu$, $-T\Delta S_C$, and ΔG upon protein unfolding at 298.15 K calculated for water and the three species of simple solvents in accordance with the procedure described in Subsection 2.6. According to the argument described in ref 48, $-T\Delta S_C$ of protein G should be in the range, $-541 \text{ kJ/mol} < -T\Delta S_C < -173 \text{ kJ/mol}$. The value of $-T\Delta S_C$ in Table 1 is certainly in this range, proving the validity of the value. For simple solvent 1 or the hard-sphere solvent ΔG takes a larger positive value than for water. For simple solvent 2, $\Delta\mu$ is much smaller than for any of the other solvents, leading to the negative sign of ΔG . This means that the unfolded state is more stable than the native structure even at ambient temperature. A solvent with too large a value of the molecular diameter is not capable of driving a protein to fold. Simple solvent 1 and the hard-sphere solvent possess this capability, but cold denaturation, which can be caused by the weakening of the solvophobicity at low temperatures, is not reproducible for the model protein immersed in these solvents as discussed below.

3.4 Possibility of cold denaturation of a protein in water, simple solvent 1, and hard-sphere solvent

Since $\Delta G = \Delta\mu - T\Delta S_C$, the cold denaturation temperature is the temperature at which $\Delta\mu = T\Delta S_C$. We assume that ΔS_C is independent of T ³⁷. The temperature dependence of $\Delta\mu$ for water and that of $T\Delta S_C$ are illustrated in Figure 7(a). The two lines intersect at $\sim 259 \text{ K}$ being the denaturation temperature. This temperature is quite consistent with the experimentally observed one ($250 \text{ K} \sim 260 \text{ K}$)^{9–11}. Even if ΔS_C is treated as an increasing function of T , $T\Delta S_C$ decreases a little more rapidly as T becomes lower, leading to only a small shift of the denaturation temperature in a lower direction.

Figure 7(b) shows the temperature dependence of $\Delta\mu$ for simple solvent 1 and that of $T\Delta S_C$. By extrapolating the data of $\Delta\mu$ to the temperatures lower than 258.15 K, we estimate that the two lines intersect at $\sim 160 \text{ K}$. This temperature is unrealistically low. Moreover, using the radial-symmetric integral equation theory, we find that the spinodal point at which the isothermal compressibility diverges is encountered at $\sim 222 \text{ K}$ when T is progressively lowered. This means that simple solvent 1 cannot exist as a single liquid phase even in the metastable state below $\sim 222 \text{ K}$. It is concluded that cold denaturation is not reproducible in this solvent.

In the hard-sphere solvent, $\Delta\mu$ is equal to $-T\Delta S_V$ and ΔG is expressed as

$$\Delta G(T) = -T(\Delta S_V + \Delta S_C). \quad (20)$$

$\Delta S_V/k_B$ and $\Delta S_C/k_B$ at ambient temperature are -284.2 and 111.2 , respectively, as given in Table 1. We note that ΔS_V

remains almost constant against the temperature lowering (see Figure 6(a)). Hence, cold denaturation cannot occur when ΔS_C is assumed to be independent of T . Even if we consider that ΔS_C decreases as T becomes lower, ΔG can never become 0 because $|\Delta S_V/k_B| > \Delta S_C/k_B$ at ambient temperature and ΔS_V remains almost constant. Thus, cold denaturation is not likely to occur in the hard-sphere solvent.

3.5 Further comparison between water and simple solvent 1

The solvophobicity is considerably weakened at low temperatures for simple solvent 1 as well as for water. However, we find the following differences between these solvents. As discussed above, for water at low temperatures, highly ordered structure is formed near the protein surface due to the enhancement of hydrogen bonding or increase in the number of hydrogen bonds. For simple solvent 1, on the other hand, we find no appreciable sign of such solvent structuring near the protein surface.

Cold denaturation of a protein is reproducible in water but not in simple solvent 1. This is partly because the temperature dependence of the EV-dependent term of the hydration entropy at the protein-solvent-solvent triplet and higher-order correlation level is stronger for water. Another reason is in $\Delta\mu$ of simple solvent 1 at ambient temperature which is significantly larger than that of water (see Table 1). The difference between water and simple solvent 1 in $\Delta\mu$ can be explained as follows. As shown in Figures 2(d) and 3(d), the two solvents share essentially the same value of $-T\Delta S_V$. On the other hand, ΔU_V is substantially more negative for water than for simple solvent 1 (see Figures 2(b) and 3(b)). For a solvent whose particles interact through attractive interaction, the solute insertion causes the internal energy to decrease. Since the direct solvent-solute interaction does not contribute energetically for our solute model, the energy decrease is due to the structural changes induced in the solvent. $U_V = 0$ for the hard-sphere solvent but U_V take a large, negative value for simple solvent 1 or water. U_V of the unfolded state of a protein ($U_{V,D}$) is more negative than that of its native structure ($U_{V,N}$): $\Delta U_V = U_{V,D} - U_{V,N} < 0$. Further, $U_{V,D}$, $U_{V,N}$, and ΔU_V for water are substantially more negative than $U_{V,D}$, $U_{V,N}$, and ΔU_V for simple solvent 1, respectively, due to the considerably stronger attractive interaction. Thus, the difference between the two solvents in $\Delta\mu$ arises from that in the strength of the solvent-solvent attractive interaction giving rise to the internal-energy decrease upon solute insertion. (When the temperature is lowered from 298.15 K to 258.15 K, the decrease in ΔU_V for water is larger than that for simple solvent 1 as expected, while the increase in $-T\Delta S_V$ for water is also larger than for simple solvent 1 by almost the same magnitude: Due to the cancellation, the two solvent share almost the

same decrease in $\Delta\mu$. The larger increase in $-T\Delta S_V$ for water originates from the enhanced hydrogen bonding near the protein surface occurring in the very low temperature range as discussed above.)

We find that $\Delta\mu$ of simple solvent 1 at ambient temperature becomes closer to that of water when the solvent-solvent attractive potential is enhanced by increasing ϵ_{SS} ($\rho_S d_S^3$ is fixed at 0.7317). However, the radial-symmetric integral equation theory loses its solution before $\beta\mu$ for simple solvent 1 becomes sufficiently close to that for water when ϵ_{SS} is progressively increased: The divergence of the isothermal compressibility of the bulk solvent is encountered. Thus, there are certainly some aspects in the water behavior which cannot be reproduced by a simple model solvent with no hydrogen bonds.

As pointed out above, the interplay of the exceptionally small molecular size and strongly attractive interaction of the solvent is essential in mimicking the water behavior. At the same time, hydrogen bonds are necessitated for the complete elucidation of the hydrophobicity. Water is unique in the sense that its hydrophobicity is powerful enough to form self-assembled structures at ambient temperature but substantially weakened when the temperature is lowered, leading to the collapse of the structures. This feature cannot be reproduced even by simple solvent 1 that is far closer to water in solvation thermodynamics than simple solvent 2 and the hard-sphere solvent.

3.6 Physical origin of weakening of solvophobicity at low temperatures for water and simple solvent 1

It is clear that a sufficiently strong attractive interaction between solvent particles is required for reproducing the weakening of the solvophobicity at low temperatures. Consider first the bulk solvent. As the temperature becomes lower, the effect of the attractive interaction becomes stronger, reducing the number of accessible translational configurations of solvent particles due to the constraints caused by the effect. For water, the contact value of the solvent-solvent pair correlation function $g(d_S)$ is 18.2 at 298.15 K but it increases to 22.1 at 258.15 K. For the simple solvent 1, it is 6.11 at 298.15 K but it increases to 6.56 at 258.15 K. This type of increase represents that associations of solvent molecules are *locally* enhanced at low temperatures. Since the solvent number densities at 298 K and at 258 K share almost the same value (i.e., the system volume remains almost unchanged), the enhanced associations accompany an increase in the inhomogeneity of the solvent, producing more void space. Due to the presence of more void space, the decrease in the number of accessible translational configurations of solvent molecules upon the solute insertion becomes smaller, the degree of the enhancement of solvent crowding reduces, and the entropic loss becomes less serious. Thus, the solvent can accommodate a solvopho-

bic solute with less difficulty (i.e., the solvophobicity is weakened) at low temperatures. Judging from the values of $g(d_S)$ given above, this temperature effect is much larger for water than for simple solvent 1, because the solvent-solvent attractive interaction in simple solvent 1 is considerably weaker.

Matubayasi and Nakahara investigated the effect of the dipole moment of water molecules on μ of a nonpolar solute using a computer simulation⁷¹. The simulation was performed under the isochoric condition. They found that μ decreases as the dipole moment becomes larger. It was then argued that the enhanced hydrogen bonding arising from the increased dipole moment gives rise to more void space, leading to a reduction in μ . This interpretation is closely related and similar to ours described above.

The water density decreases as the temperature becomes lower from 277 K. However, this decrease is very minor and cannot cause cold denaturation of a protein by itself. To demonstrate this, we calculate $\Delta\mu$ for water at 258.15 K with two number densities: the values pertinent to 258.15 K ($\rho_S d_S^3=0.7312$) and 298.15 K ($\rho_S d_S^3=0.7317$), respectively. The result is given as Table 2: $\Delta\mu$ and its terms 1 and 2 with $\rho_S d_S^3=0.7317$ are almost indistinguishable from those with $\rho_S d_S^3=0.7312$. Thus, the weakening of the hydrophobicity at low temperatures and cold denaturation of a protein are ascribed solely to the solvent-solvent attractive interaction coupled with the temperature lowering. Graziano succeeded in reproducing cold denaturation of a protein using the classical scaled particle theory (SPT)²³. The SPT, in which the solvent is always formed by hard spheres, is capable of explicitly incorporating neither the solvent-solvent attractive interaction nor the temperature effect. In his work, however, the hard-sphere diameter for the solvent is adjusted so that the experimental value of the isothermal compressibility of water can be fitted with respect to the SPT relationship. The resulting diameter is referred to as “effective diameter”. The effective diameter decreases as the temperature becomes lower below 20 °C. The decrease in the total packing fraction of the solvent at low temperatures, which leads to the reduction in the work of cavity creation and the occurrence of cold denaturation, arises mostly from the smaller effective diameter. The decrease in the solvent density itself has only very minor effects. In our view, the effects of the solvent-solvent attractive interaction coupled with the temperature lowering are implicitly incorporated in the treatment of Graziano through the adjustment of the diameter. In this sense, our argument is never inconsistent with that of Graziano.

4 Conclusions

We have investigated the physical origin of the hydrophobicity by revisiting cold denaturation of a protein. There are a number of phenomena manifesting that the hydrophobicity is weakened at low temperatures, and cold denaturation is a typical example. In order to explore the feature of water, three species of simple solvents as well as water are considered in the investigation. Considering a completely solvophobic model protein, we analyze the temperature dependences of the solvation free energy multiplied by $\beta = 1/(k_B T)$ ($\beta\mu$) of a folded protein, a measure of the solvophobicity. Those of the changes in free energy $\Delta\mu$, energy ΔU_V , and entropy ΔS_V (or $-T\Delta S_V$) of the solvent upon protein unfolding are also analyzed. The angle-dependent^{6,13–16} and radial-symmetric^{24–27} integral equation theories and the morphometric approach^{28–30} are employed in the analysis. The three species of simple solvents considered are as follows: simple solvent 1 in which the particles interact through strongly attractive potential and the particle diameter is as small as that of water; simple solvent 2 in which the particles interact through strongly attractive potential but the particle diameter is about 1.9 times larger than that of water; and a hard-sphere solvent whose particle diameter is the same as that of water. The four solvents share the same packing fraction at each temperature. The changes in thermodynamic quantities of the solvent upon protein unfolding are decomposed into two terms, term 1 which is scaled by the excluded volume (EV) and term 2 depending on the area and curvature of solvent-accessible surface, using the morphometric approach. The solvent molecules near the protein surface and those in the system (excluding those near the protein surface) contribute to term 2 and to term 1, respectively. Term 2 includes the effects due to the formation of ordered structure by the solvent molecules near the protein surface. For water and simple solvent 1, term 1 of $-T\Delta S_V$ is further decomposed into the protein-solvent pair correlation component and the protein-solvent-solvent triplet and higher-order correlation component. The former is relevant to the total volume available to the translational displacement of solvent molecules. The latter is related to the solvent crowding in the system which is caused by the physical factor that the presence of a solvent molecule also generates an EV for the other solvent molecules. Such correlation among solvent molecules is not included in the protein-solvent pair correlation component.

The following characteristics of water can qualitatively be reproduced by simple solvent 1: (i) $\beta\mu$ decreases (i.e., the hydrophobicity is weakened) considerably as T becomes lower; (ii) $\Delta\mu$ reduces considerably with lowering T due to the decrease in its term 1 which is ascribed to the reduction in term 1 of $-T\Delta S_V$; and (iii) the reduction in term 1 of $-T\Delta S_V$ originates from that in its protein-solvent-solvent triplet and

higher-order correlation component. For water, term 1 of μ plays essential roles for a protein just as it does for small nonpolar solutes such as methane. This is an important point suggesting that the scaling behavior of Eq. (1) does not hold for a protein. The results for simple solvent 2 and the hard-sphere solvent are substantially different from those for water and simple solvent 1: The temperature dependences of $\beta\mu$, $\Delta\mu$, ΔU_V , and ΔS_V (or $-T\Delta S_V$) are much weaker. It is suggested that the water characteristics are ascribed to the interplay of the two factors, the exceptionally small molecular size and strongly attractive interaction. If one of the two factors is absent, the characteristics of water are lost. Even between water and simple solvent 1, the following differences are appreciated in the behavior: (i) The temperature dependences of term 1 of $-T\Delta S_V$ and its protein-solvent-solvent triplet and higher-order correlation component are significantly stronger for water; (ii) though the two solvents share the result that the temperature dependences of ΔU_V and ΔS_V are governed by their term 2 but they are compensating, the dependences for water are much stronger; and (iii) there is a clear sign of water structuring arising from the enhanced hydrogen bonding near the protein surface at low temperatures whereas such a sign is not found for simple solvent 1.

Not only water but also simple solvent 1 and the hard-sphere solvent are capable of driving a protein to fold while simple solvent 2 is not. Only in water, the solvophobicity becomes weak enough to give rise to protein unfolding at low temperatures. Cold denaturation is not reproducible even in simple solvent 1 due to the insufficient weakening of the solvophobicity despite that water and this solvent share some qualitatively similar characteristics as described above. It would be reproducible if the attractive potential was substantially enhanced, but such enhancement causes the appearance of the metastability limit for a single liquid phase. In this sense, the hydrogen bonds are related to the exhibition of the hydrophobicity. However, this never implies the importance of the orientational component of the hydration entropy. It is relevant only to the water molecules near the protein surface and much smaller than the translational component. Water is unique in the sense that the hydrophobicity is powerful enough to form a variety of self-assembled structures of solute molecules at ambient temperature but substantially weakened when the temperature is lowered, leading to the collapse of the structures. This uniqueness is ascribed to the reduction in the EV term of the hydration entropy at the solute-solvent-solvent triplet and higher-order correlation level. It should be emphasized that the presence of a water molecule generates an EV for the other water molecules, thus causing water crowding. Upon a self-assembly process, the water crowding in the system is substantially reduced with the result of a large gain in the translational entropy of water. However, this force driving the process becomes much less powerful at low temperatures,

giving rise to the collapse of the self-assembled structures. In our view, the weakening of the hydrophobicity at low temperatures leading to cold denaturation of a protein is attributable to enhanced local associations of water molecules in the bulk, giving rise to more inhomogeneity followed by the formation of more void space: Due to the presence of more void space, water can accommodate a hydrophobic solute with less difficulty. We believe that the same physical origin is shared by the following phenomena at low temperatures: The solubility of methane increases, the critical micelle concentration becomes higher, the average size of micelles for nonionic amphiphilic molecules becomes smaller, most of the native structures of proteins unfold, and protein aggregation is dissociated.

As described in Introduction, the behavior of the hydration free energy μ (the solvent is water) of a sufficiently large solute is quite different from that of a small solute⁴: While μ of the former is scaled by the water-accessible surface area, μ of the latter is largely dependent on the excluded volume. We note that the four coefficients in the morphometric form for μ are determined by the fitting to the hydration free energies of hard-sphere solutes. The resulting values of the four coefficients can largely be influenced by the solute sizes chosen in the fitting. C_1 and C_2 could be approximated by P (the pressure) and γ (the surface tension), respectively, when only sufficiently large hard-sphere solutes are employed in the fitting. On the other hand, the coefficients adopted in our studies are determined from small hard-sphere solutes (see Sec. 2.4). In this case, C_1 and C_2 are substantially different from P and γ , respectively. Our proposition is that the coefficients determined using sufficiently small hard-sphere solutes should be employed for proteins in order to reproduce the experimentally observed behavior of cold denaturation. Namely, the first term of the morphometric form for μ is not the pressure-volume work. We have tackled a number of problems related to solvation thermodynamics of a variety of solutes. On the basis of the results obtained, we now believe that the large-solute limit is inapplicable to proteins as well as to small solutes like methane (this was already stated in our paper, Ref. 20) when the solvent is water. At the large-solute limit, with $P = 1$ atm, the first term in the morphometric form can be neglected. With the absence of the first term, however, many of the important problems (e.g., the very large entropic gain upon folding of apoplastocyanin, cold and pressure denaturation of a protein, and thermal stability of a protein) cannot be elucidated. In summary, the first term in the morphometric form for μ is quite large even for water with $P = 1$ atm; and the second and third terms of the morphometric form also make significantly large contributions to μ . On the other hand, for the hard-sphere solvent, when the four coefficients are determined using hard-sphere solutes with diameter d_U ranging from d_{U1} to d_{U2} , the resulting values are almost completely independent of d_{U1} and d_{U2} chosen. Since the large-solute

limit seems to be applicable to a protein immersed in the hard-sphere solvent, the morphometric form in Refs. 29 and 72 was written for this limit. We remark that the large-solute limit is not applicable to a protein immersed in simple solvent 1 as in the case of water.

It is of great interest and importance to further examine whether or not the proposition given in the present study is universally applicable to the behavior of diverse self-assembly processes. Work in this direction is in progress.

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Table 1 Changes in solvation free energy $\Delta\mu$, contribution to free energy from conformational entropy of protein $-T\Delta S_C$, and free energy of the entire system ΔG upon protein unfolding at $T=298.15$ K (in kJ/mol).

	$\Delta\mu$	$-T\Delta S_C$	ΔG
Water	479.1	-429.1	50.0
Simple solvent 1	622.3	-429.1	193.2
Simple solvent 2	204.5	-429.1	-224.6
Hard-sphere solvent	532.7	-429.1	103.6

Table 2 Changes in hydration free energy $\Delta\mu$ (i.e., free-energy changes of water) upon protein unfolding and in its terms 1 and 2 calculated at $T=258.15$ K (in kJ/mol). The two values pertinent to 258.15 K ($\rho_S d_S^3 = 0.7312$) and 298.15 K ($\rho_S d_S^3 = 0.7317$), respectively, are employed for the number densities of water.

	$\Delta\mu$	Term 1	Term 2
$\rho_S d_S^3 = 0.7312$	369.4	80.93	288.4
$\rho_S d_S^3 = 0.7317$	370.7	82.18	288.5

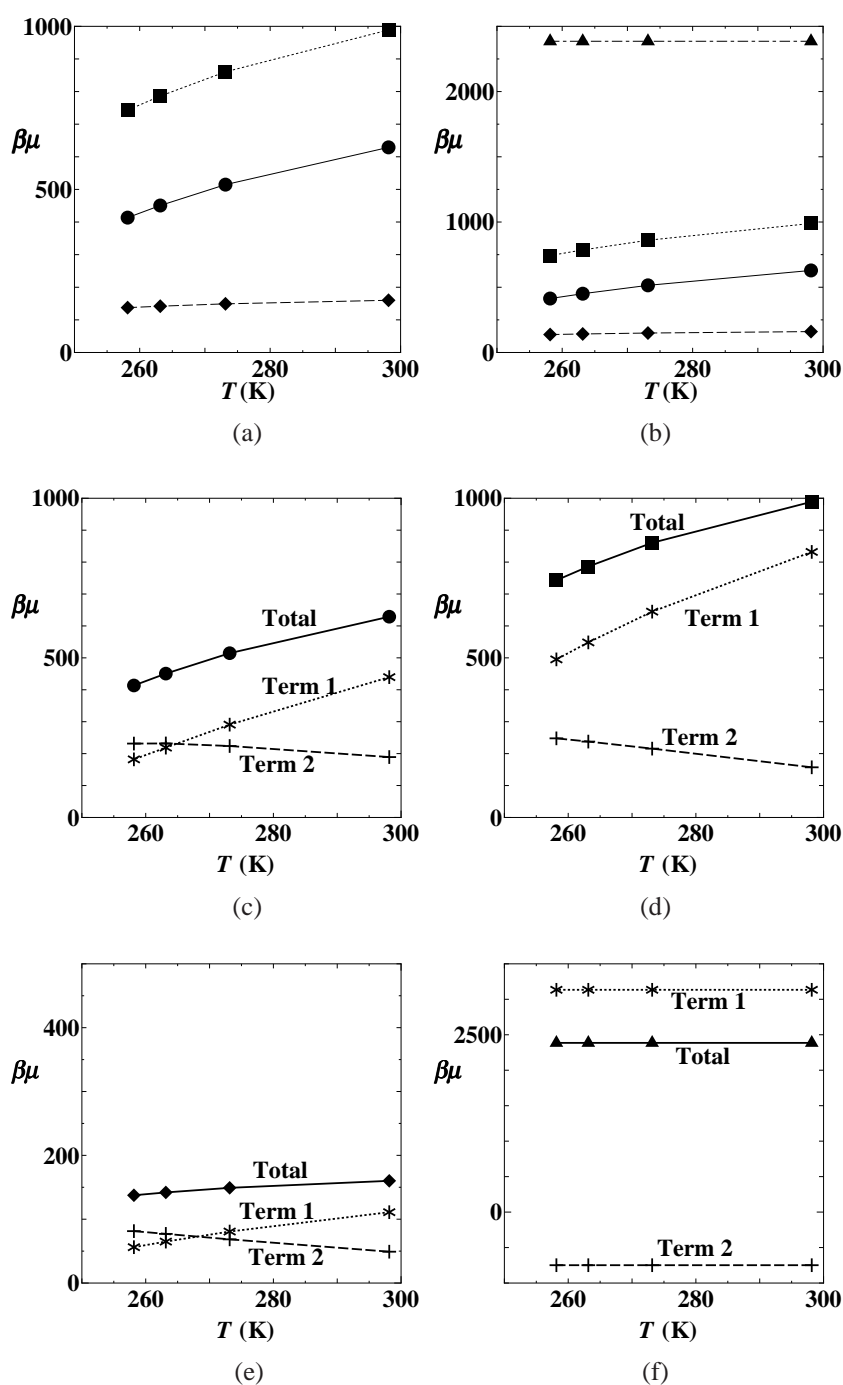


Fig. 1 (a) and (b): Temperature dependence of $\beta\mu$ of the native structure of protein G for water (circles), simple solvent 1 (squares), and simple solvent 2 (rhombuses). The result for the hard-sphere solvent (triangles) is given in (b). Temperature dependences of $\beta\mu$ and its terms 1 and 2 are shown for water (c), simple solvent 1 (d), simple solvent 2 (e), and the hard-sphere solvent (f). “Total” is the sum of terms 1 and 2 and equal to $\beta\mu$ itself.

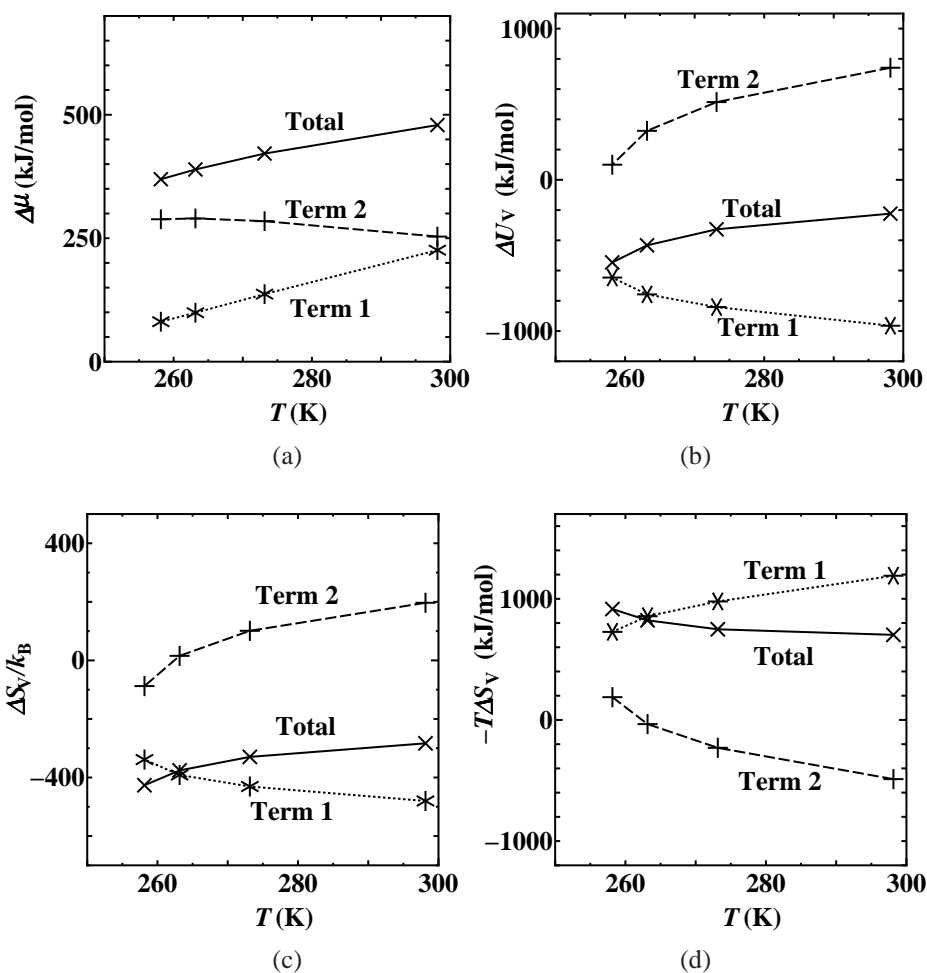


Fig. 2 Temperature dependences of changes in thermodynamic quantities of water upon protein unfolding: (a) free energy, (b) energy, (c) entropy, and (d) entropy multiplied by $-T$ (i.e., contribution to free energy from entropy). Term 1 is the first term in the right hand of Eq. (10) and term 2 is the sum of the other three terms. “Total” denotes the sum of terms 1 and 2.

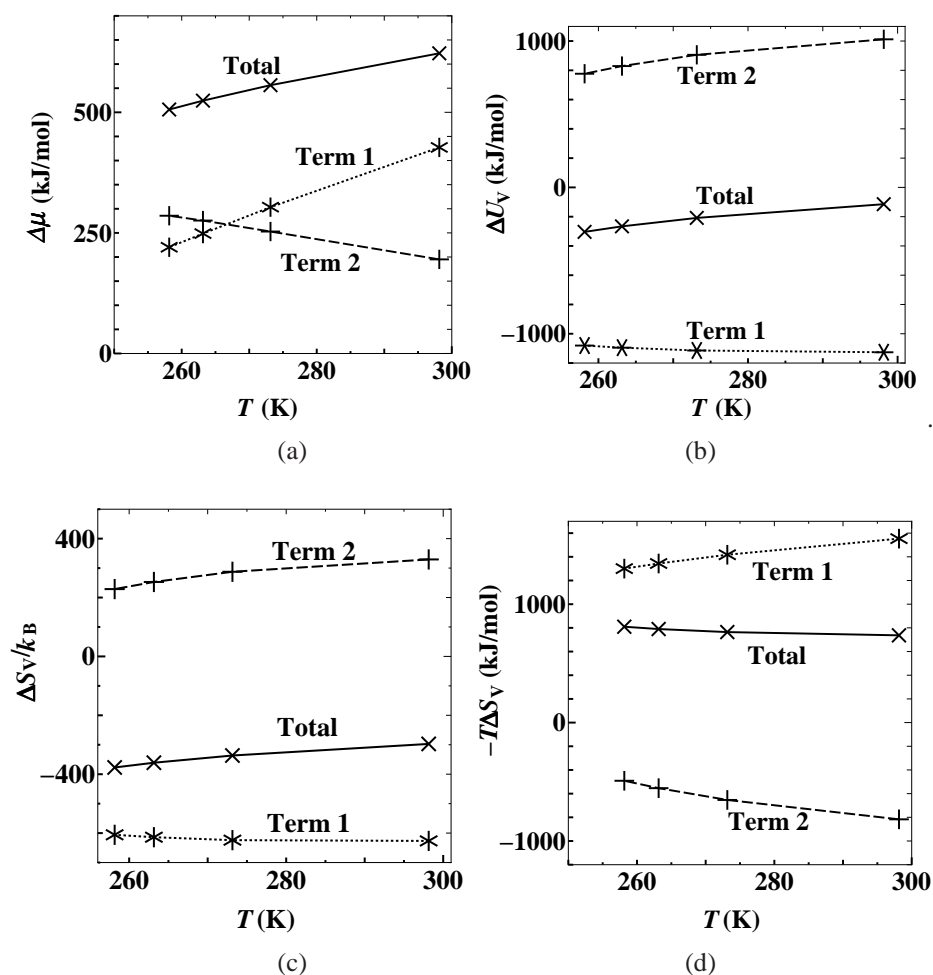


Fig. 3 Temperature dependences of changes in thermodynamic quantities of simple solvent 1 upon protein unfolding: (a) free energy, (b) energy, (c) entropy, and (d) entropy multiplied by $-T$ (i.e., contribution to free energy from entropy). Term 1 is the first term in the right hand of Eq. (10) and term 2 is the sum of the other three terms. “Total” is the sum of terms 1 and 2.

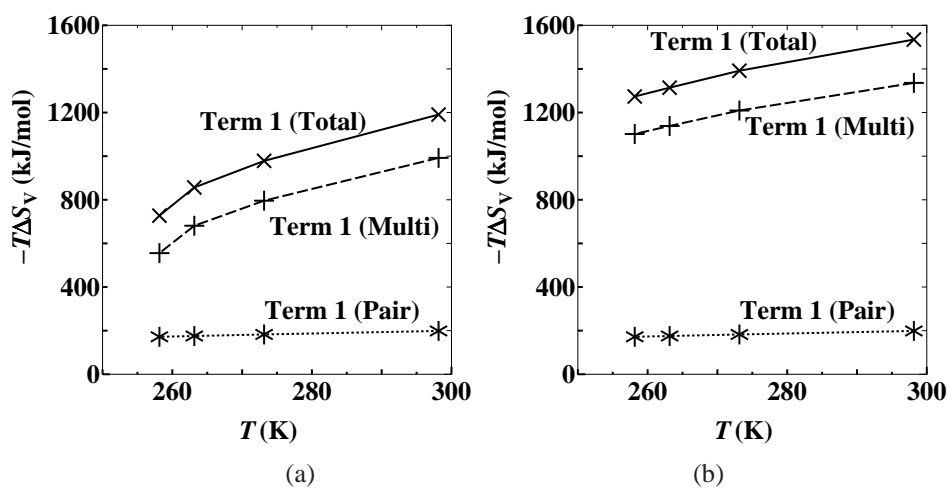


Fig. 4 Temperature dependences of term 1 of $-T\Delta S_V$ at the protein-solvent pair correlation level [“Term 1 (Pair)”] and that at the protein-solvent-solvent triplet and higher-order correlation level [“Term 1 (Multi)”]. The sum is indicated by “Term 1 (Total)”. (a) Water. (b) Simple solvent 1.

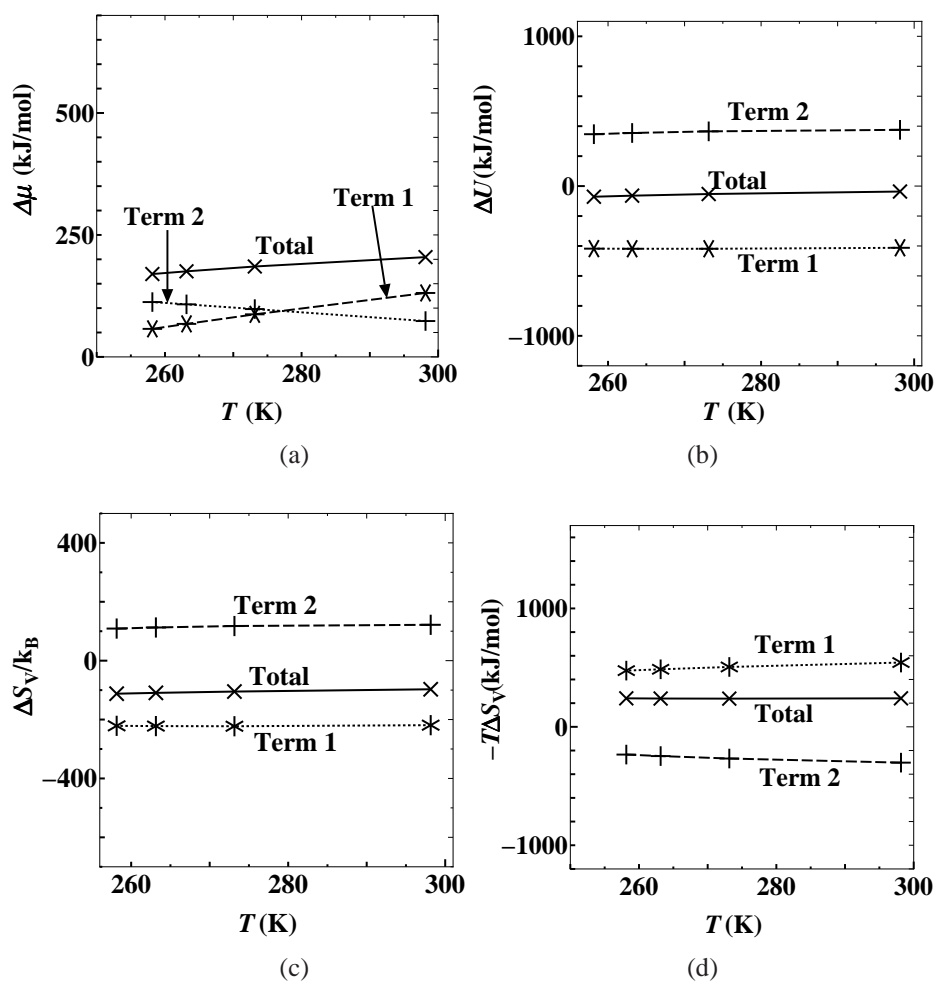


Fig. 5 Temperature dependences of changes in thermodynamic quantities of simple solvent 2 upon protein unfolding: (a) free energy, (b) energy, (c) entropy, and (d) entropy multiplied by $-T$ (i.e., contribution to free energy from entropy). Term 1 is the first term in the right hand of Eq. (10) and term 2 is the sum of the other three terms. “Total” is the sum of terms 1 and 2.

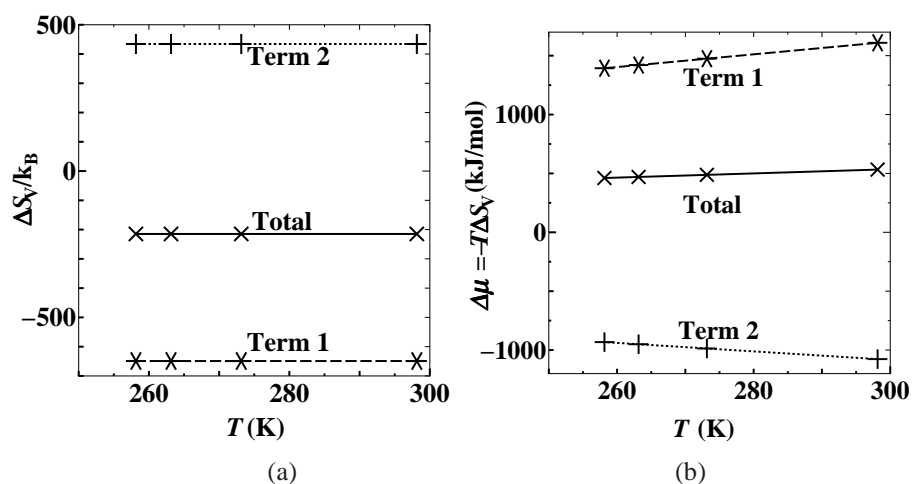


Fig. 6 Temperature dependences of changes in thermodynamic quantities of hard-sphere solvent upon protein unfolding: (a) entropy and (b) entropy multiplied by $-T$ corresponding to $\Delta\mu$. Term 1 is the first term in the right hand of Eq. (10) and term 2 is the sum of the other three terms. “Total” is the sum of terms 1 and 2.

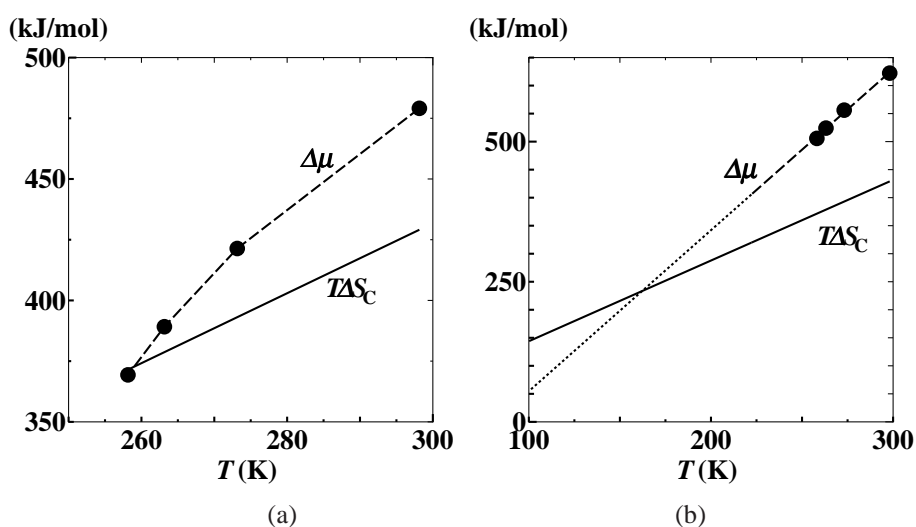


Fig. 7 Temperature dependences of changes in solvation free energy, $\Delta\mu$, and in protein conformational entropy multiplied by T , $T\Delta S_C$. (a) Water. (b) Simple solvent 1. The temperature at which the two lines intersect represents the cold denaturation temperature. In (b), we linearly extrapolate $\Delta\mu$ for temperatures lower than 258.15 K. The dashed and dotted lines represent the extrapolated lines above and below the spinodal point (~ 222 K), respectively.