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Kyoto University
Compressed Sensing based Protocol for Interfering Data Recovery in Multi-Hop Sensor Networks

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Abstract—We consider a multi-hop wireless sensor network that measures sparse events and propose a novel protocol based on Compressed Sensing (CS) as an alternative to traditional Media Access Control (MAC) scheduling and routing protocol. Instead of avoiding collisions, our CS-based protocol exploits interferences by superimposing the data measurements "over-the-air", simultaneously received at any node. Thanks to our protocol design, each node is able to recover and forward only new data towards the sink. Our protocol achieves near zero reconstruction errors at the sink, while greatly reducing overhead and delays compared to conventional methods. These results reveal a new and promising approach to protocol design through CS.

I. INTRODUCTION

Recently, the groundbreaking theory of Compressed Sensing (CS) was developed, enabling a vector with correlated entries, i.e., that can be transformed into a sparse vector through a transformation basis, to be recovered with high accuracy from a few random projections onto another, incoherent basis [1]. Widely used in the domains of digital signal and image processing, CS is also a highly promising tool for improving the performance of wireless networks. Several works have exploited CS in wireless sensor networks with space-time correlated data as in [2][3][4][5]. By contrast, [6] considers a one-hop sensor network where multiple nodes transmit their measurement simultaneously to the sink. As sparse events are assumed, i.e., the number of measurements received at the sink is much smaller than the number of sensors, each measurement can be recovered from few observations with CS. A similar approach is taken for developing new multiple access schemes as in [7] or downlink scheduling [8].

In this work, we consider a multi-hop wireless sensor network and take the approach of [6]–[8] where the events to be reported occur sparsely. We develop a protocol based on CS and flooding that enables the sink to obtain and reconstruct the sparse measurement data with high accuracy without any heavy routing nor MAC protocol, by exploiting collisions. In a one-hop network, the interfering/superimposed data measurements due to packet collisions may be resolved by the CS-based algorithms in [6]–[8], but they pose major problems in a multi-hop network where every node forwards all received packets, as the number of interfering measurements may increase drastically, thereby causing the CS-based algorithms to perform poorly due to loss of sparsity. Moreover, if different measurements of a same source but generated at different times are contained in the same packet, they would hardly be resolvable. Note also that our goal is radically different from the existing CS data recovery schemes in sensor networks: here, the generated events themselves are assumed to be sparse as in [6], which happens whenever only a few sensors are allowed to send significant data, such that these sparse data have no correlation between themselves. In that case, the existing CS based techniques as in [2][3][4][5] will not be applicable, since there is no data correlation to be exploited: each data would be simply forwarded to the sink by usual MAC and routing protocols, which are actually assumed in these works to guarantee collision-free transmissions. Instead, the novelty of our work is to take advantage of CS techniques to enable efficient delivery of sparse data superimposed “over-the-air” by exploiting flooding and interferences, as opposed to conventional collision-avoiding MAC scheduling and routing. Simulation results show that our CS based protocol achieves excellent data reconstruction at the sink, while greatly reducing overhead and delays compared to conventional protocols.

II. SYSTEM MODEL

We consider a multi-hop wireless sensor network with \( N \) nodes and one sink, forming a lattice as shown in Fig. 1. If a sensor \( S_n \) detects an event, the measurement is forwarded to the sink based on the proposed protocol. As in [6] which considers a one-hop sensor network, we assume digital transmissions with measurements \( x \in \{-1, 1\} \), and that there may be up to \( K \) events occurring simultaneously within the whole network, but these events are considered to be sparse compared to the number of nodes, namely \( K << N \).

Given the lattice structure of the network, each node only communicates with its closest neighbors at distance \( d \), so there may be 2, 3 or 4 neighbors depending on the node’s location. For example, a packet sent by node \( S_1 \) in Fig. 1 will be received by nodes \( S_2 \) and \( S_6 \) only, while a packet sent by node \( S_7 \) will be received by nodes \( S_2, S_6, S_8 \) and \( S_{12} \). For simplicity, it will be assumed that nodes take turns for being in transmit or receive mode: if at time \( t \), a node at position \((i, j)\) in the grid is in transmit mode, then at time \( t + 1 \) it will be in receive mode while its four neighbors in positions \((i \pm 1, j), (i, j \pm 1)\) will be in transmit mode. Nodes are assumed to be synchronized as in [6]. Channels are considered

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Fig. 1. Multi-Hop Wireless Sensor Network Model (1)

III. PROPOSED PROTOCOL

To exploit "over-the-air" data aggregation, we consider a routing based on a simple flooding procedure whereby upon packet reception, each node broadcasts this packet locally until it reaches the sink. However, unlike the single-hop case, there are major issues to be resolved in this multi-hop setting. If each node simply forwards all received packets, the number of superimposed measurements will increase drastically, leading to poor CS recovery due to loss of sparsity in each packet. Moreover, if each source node is assigned a signature sequence as in the single-hop case, it will not be possible to distinguish whether the multiple received packets are due to self-interference, i.e., they are copies of a same original packet, or if they originate from the same source but at different times.

To alleviate these issues, the proposed protocol is designed as follows. First, the length of the signature sequences is increased so that each sequence simultaneously codes over ID space and time space, i.e., each measurement is associated with a unique sequence $a_{n,l}$, vector of size $M$, that identifies the pair (origin node ID $S_n$, number of hops $l$). Here $S_n$ is the sensor that originally detected this measurement, and $l$ is its time stamp parameter, defined as the number of hops elapsed by forwarding the packet bearing this measurement, counted from its origin node up to its current location in the network. Each sensor $S_n$ receives and forwards all packets bearing this measurement, and the packet reception at each node is denoted by $p_{nl}$. For example, assuming $S_1$ and $S_2$ to be source nodes in Fig. 1, at time $t = 0$, packet $p_1 = x_{1,0}a_{1,0}$ is received by $S_1$'s neighbors $S_2, S_3$ and packet $p_3 = x_{3,0}a_{3,0}$ by $S_2$'s neighbors $S_2, S_4, S_6$.

At a time $t$, if sensor node $S_k$ is in receive mode, it receives signal $y_k$ containing all simultaneous transmissions from its neighbor nodes $n \in N(S_k)$. The received signal at node $S_k$ is

$$y_k = \sum_{n \in N(S_k)} p_{nl} = \sum_{j,l} x_{j,l}a_{j,l} + z_k,$$

where $x_{j,l}$ is the measurement with source node $S_j$ transmitted in packet $p_n$.

2Among NL, two equal or opposite sequences may be chosen from the total of $2^M$. But as $NL \leq 300 < 2^M \approx 10^{10}$, here, such events rarely occur.

3If a new event was detected during the node’s receive mode, it will store the measurement and send it in the next transmit slot with hop count $l = 1$. 

Fig. 2. Multi-Hop Wireless Sensor Network Model (2)
so the received signal at receiver node $S_2$ is written $y_2 = A x_2 + z_2$, where $x_2 = [x_{1,0} \ldots x_{3,0} \ldots 0]^T$.

3. Receiver node $S_k$ decodes each measurement contained in the received signal $y_k$, using CS principles. In particular, this problem can be formulated by $\ell_1-\ell_2$ optimization as

$$\hat{x}_k = \arg \min_{x_k} \frac{1}{2} \|y_k - Ax_k\|^2 + \lambda \|x_k\|_1,$$

where Lagrange Multiplier $\lambda$ makes a trade-off between representation error and sparsity of the solution. The main computational effort of the proposed scheme arises from this step (3), solved by the Iterative Shrinkage-Thresholding Algorithm (ISTA) as it only requires very low complexity [9].

4. The reconstructed vector $\hat{x}_k$ is renormalized so that each component belongs to $\{-1, 1\}$.

5. After decoding the received measurements at node $S_k$, their respective (source ID, time stamp)-sequence $a_{j,l}$ could be identified. Node $S_k$ then compares the sequence $a_{j,l}$ of each newly decoded measurement to the sequences of previously received ones that are stored in its local table $Q(S_k) = \{a_{k,l}^{\text{out}} \text{ received by } S_k \mid 0 \leq l' \leq L\}$.

- if there exists a sequence $a_{j,l'}$ in $Q(S_k)$, $q = j$, $l' \leq l$: as fading is not assumed, any new data from $S_j$ should have a smaller hop count $l < l'$ unless the new data packet that followed the shortest path was lost, which rarely occurs in this setting. So with high probability, this data was already received. Thus, $S_k$ discards the decoded data $\tilde{x}_{j,l}a_{j,l}$, from the set of data to be forwarded next.

- if there exists a sequence $a_{j,l'}$ in $Q(S_k)$, $q = j$, $l' > l$: although both share the same origin node $S_j$, this is a new data as it has a smaller hop count than the one stocked. Therefore, $S_k$ will forward the decoded data $\tilde{x}_{j,l}a_{j,l}$.

- in all other cases, $S_k$ will forward $\tilde{x}_{j,l}a_{j,l}$.

For example, in Fig. 1, node $S_2$ reconstructs $x_{1,0}, x_{3,0}$ from $y_2$ based on Steps 3 and 4. Both measurements will be forwarded since they are the first ones to be received, but the local table is updated to $Q(S_2) = \{a_{1,0}, a_{3,0}\}$.

6. For all data $\tilde{x}_{j,l}a_{j,l}$ to be forwarded, the hop count is incremented to $l + 1$. All decoded measurements as well as sequences in $Q(S_k)$ for which $l > L$ are discarded. Then, $S_k$ superimposes all the remaining data to be forwarded into a packet $p_k$ composed of $M$ bits, $p_k = A \tilde{x}_k = \sum_{j,l} \tilde{x}_{j,l}a_{j,l}$, and forwards it. In Fig. 2, among all even nodes sending at $t = 1$, $S_2$ sends $p_2 = \tilde{x}_{1,1}a_{1,1} + \tilde{x}_{3,1}a_{3,1}$, which is received by $S_1, S_3, S_7$. Based on Step 5, $S_1$ discards $\tilde{x}_{1,1}$ and $S_3, \tilde{x}_{3,1}$. Similarly, $S_8$ sends $p_8 = \tilde{x}_{3,1}a_{3,1}$, received by the Sink $S$.

7. The Sink runs the reconstruction algorithm for all incoming packets during the session of duration $T_{\text{out}}$. If multiple versions of the same data are received, diversity gain may be achieved. The measurement time is given by the first received packet if $\tilde{x}_{j,l}$ is received for the first time, then its time is given by $T-(l+1)$, where $T$ is the actual time at the Sink in hop counts. Given the procedure of Step 5, it is very unlikely that multiple versions of a given measurement with different hop counts are simultaneously received at the Sink for the first time. Thus, if several measurements from a node are received, they will correspond to different measurements of that node. That is, if the Sink receives $p_k = \tilde{x}_{j,l}a_{j,l} + \tilde{x}_{j,m}a_{j,m}$, with $l < m$ and has a local table $Q(S) = \{a_{j,l'}\}$, then most probably $l \leq l' < m$, i.e., $\tilde{x}_{j,l'}$ is the same as $\tilde{x}_{j,l}$, but received through a longer route in the network. Then, $\tilde{x}_{j,l}$ will be considered as a new measurement with time $T-(l+1)$ and $\tilde{x}_{j,m}$ as a replica of $\tilde{x}_{j,l'}$, providing diversity. 4

IV. NUMERICAL RESULTS

In a network of 49 nodes within a regular 7 by 7 grid, $K$ sources generate measurements. These sparse generation events occur at random times during each session, e.g., they may occur simultaneously. Each session ends after time out $T_{\text{out}}$ in hop counts, at which point the measurements collected by the sink are evaluated. The Signal-to-Noise Ratio (SNR) for each link is fixed to 30 dBs. Each simulated point is averaged over 300 sessions. Note that here only one measurement is generated by a source node per session, in order to focus on the reconstruction performance of the measurements as in [4], while measurement times can be retrieved as described in Step 7. Thus, we evaluate the reconstruction error averaged over all sessions as in [2][4], defined for one session as $\epsilon = \|s - x_0\|_2^2/\|s\|_2^2$, where $s_0$ is the vector of size $N$ containing the original measurements for all $N$ sensors, i.e., its corresponding components are in $\{-1, +1\}$ if sensor $S_j$ is an origin node, and zero otherwise, while $s$ denotes the reshaped vector of collected measurements at the sink at the end of a session.

Fig. 3 shows the average reconstruction error of our protocol for $K=\{2, \ldots, 10\}$, for sequence length $M=\{35, 40\}$, $L=\{6, 7\}$ and $T_{\text{out}}=\{25, 30\}$. We observe that in both cases, excellent reconstruction is achieved even for larger values of $K$ which imply lower sparsity in the number of superimposed data. By increasing $T_{\text{out}}$ and $M$, more diversity gain and reconstruction accuracy are achieved, respectively.

As explained in the introduction, in the absence of data correlations to exploit, benchmark CS-based recovery algorithms as in [2][4] reduce to conventional forwarding protocols such as AODV routing and MAC scheduling that guarantee no collisions. Therefore, we compare the proposed protocol

\[4\text{If } Q(S) = \{a_{j,l'}\text{, }l' \leq m\text{, }l' < m\text{, }\tilde{x}_{j,l'}\text{, }\tilde{x}_{j,m}\text{ may be equal to }\tilde{x}_{j,l}\text{, }\tilde{x}_{j,m}\text{. Such cases rarely occur given the sparsity, and as packets with }l \geq L\text{ are discarded. But if they do, ambiguous packets are discarded.}\]
required amount of transmitted packets for reconstruction. The packet format is based on the IEEE 802.15.4 standard. Performance is only compared to conventional algorithms that guarantees no collisions. The packet format is based on the IEEE 802.15.4 standard. Performance is only compared to conventional routing and MAC scheduling strategies, as well as CDMA and flooding based protocol. The protocol will be extended to more general systems, with various topologies and asynchronous nodes.

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REFERENCES