TITLE:

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CITATION:

Sotani, Hajime. Observational discrimination of Eddington-inspired Born-Infeld gravity from general relativity. Physical Review D 2014, 89(10): 104005.

ISSUE DATE:

2014-05-02

URL:

<http://hdl.handle.net/2433/187791>

RIGHT:

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Observational discrimination of Eddington-inspired Born-Infeld gravity from general relativity

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(Received 27 January 2014; published 2 May 2014)

Direct observations of neutron stars could tell us an imprint of modified gravity. However, it is generally difficult to resolve the degeneracy due to the uncertainties in the equation of state of neutron star matter and in gravitational theories. In this paper, we have successfully found the observational possibility to distinguish Eddington-inspired Born-Infeld gravity (EiBI) from general relativity. We show that the radii of neutron stars with $0.5M_{\odot}$ are strongly correlated with the neutron skin thickness of ^{208}Pb independently of the equation of state, while this correlation depends on the coupling constant in EiBI. As a result, via the direct observations of the radius of the neutron star with $0.5M_{\odot}$ and the measurements of a neutron skin thickness of ^{208}Pb by the terrestrial experiments, one could not only discriminate EiBI from general relativity but also estimate the coupling constant in EiBI.

DOI: [10.1103/PhysRevD.89.104005](https://doi.org/10.1103/PhysRevD.89.104005)

PACS numbers: 04.40.Dg, 04.50.Kd, 04.80.Cc

I. INTRODUCTION

Up to now, several modified theories of gravity are proposed in spite of the fact that general relativity has been successful in explaining the phenomena and experiments in a weak-field regime such as the Solar System [1]. Meanwhile, the tests of general relativity in a strong-field regime are quite poor. This could be one of the reasons why the modified gravitational theories are considered. Additionally, in order to explain the unsolved issues such as singularities in cosmology and/or inside black holes, one might take into account the correction due to the higher order curvature. Anyway, since the technology is developing more and more, one will be able to observe compact objects with high accuracy and use it as tests of modified gravity [2–5].

Among the several modified gravitational theories, Eddington-inspired Born-Infeld gravity (EiBI) [6] has recently attracted attention in the context to avoid the big bang singularity [7,8], while EiBI becomes equivalent to general relativity in vacuum. EiBI is based on the Eddington action [9] and the nonlinear electrodynamics of Born and Infeld [10], where the metric and the connection are considered as independent fields, as in the Palatini-type approach to general relativity. EiBI can deviate from general relativity only when the matter exists, and one can expect the significant deviation especially in a high-density region. That is, the compact objects might be suitable laboratories to probe the gravitational theory. Previously, there are several attempts to examine the structures of compact objects in EiBI [11–15], which showed the significant deviations in stellar properties from the predictions in general relativity, depending on the coupling constant. We remark on some of the problems associated with the EiBI, i.e., the appearance

of the curvature instabilities at the surface of polytropic stars is pointed out [16], while the validity of the continuous fluid approximation adopted in astrophysical and cosmological studies is also discussed [17].

However, the stellar structures also depend on the unfixed equation of state (EOS), which is a relation between the pressure and density of nuclear matter. That is, it must be generally difficult to resolve the degeneracy due to the uncertainties in the EOS and in gravitational theory, even if one would measure the mass and radius of the neutron star.

In this paper, we find the observational possibility to distinguish EiBI from general relativity via the measurements of neutron skin thickness by the terrestrial experiments, in addition to the astronomical observations of neutron stars. Since the neutron stars are also regarded as neutron-rich giant nuclei, the neutron star radius could be correlated with the properties of neutron-rich nuclei. In fact, in general relativity, it is suggested that the radii of neutron stars with $0.5M_{\odot}$ are strongly correlated with the neutron skin thickness [18].

In particular, we adopt the realistic EOS, which are consistent with the empirical data of the masses and radii of stable atomic nuclei obtained from the terrestrial experiments, and show that the radii of neutron stars with $0.5M_{\odot}$ can be written as a linear function of the neutron skin thickness of ^{208}Pb independently of the adopted EOS. Additionally, this linear correlation depends strongly on the coupling constant in EiBI. Therefore, one could distinguish EiBI from general relativity via the measurements of neutron skin thickness and the radii of neutron stars with $0.5M_{\odot}$. Furthermore, we are also successful in eliminating the value of the coupling constant in EiBI as a function of the neutron skin thickness of ^{208}Pb and stellar radius with $0.5M_{\odot}$. With this estimation, at least, one may be able to observationally see how valid general relativity is. In this

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paper, we adopt geometric units, $c = G = 1$, where c and G denote the speed of light and the gravitational constant, respectively, and the metric signature is $(-, +, +, +)$.

II. EDDINGTON-INSPIRED BORN-INFELD GRAVITY

EiBI proposed by Bañados and Ferreira [6], is described with the action

$$S = \frac{1}{8\pi\kappa} \int d^4x \left(\sqrt{|g_{\mu\nu} + \kappa R_{\mu\nu}|} - \lambda \sqrt{-g} \right) + S_M[g, \Psi_M], \quad (1)$$

where $R_{\mu\nu}$ is the symmetric part of the Ricci tensor constructed with the connection $\Gamma_{\alpha\beta}^\mu$, while S_M denotes the matter action depending on the metric and matter field. $|g_{\mu\nu} + \kappa R_{\mu\nu}|$ means the absolute value of the determinant of the matrix of $(g_{\mu\nu} + \kappa R_{\mu\nu})$. It should be remarked that this action for $S_M = 0$ can recover the Einstein-Hilbert action; i.e., EiBI in vacuum is identical to general relativity [6]. The dimensionless constant λ is associated with the cosmological constant as $\Lambda = (\lambda - 1)/\kappa$. In this paper, we adopt $\lambda = 1$ to focus on the relativistic stars with asymptotically flatness. Additionally, the constraints on the Eddington parameter κ are also discussed in term of the solar observations, big bang nucleosynthesis, and the existence of neutron stars [6,11,19,20]. We should remark that the stellar structures could depend on the value of λ , which should be considered somewhere.

As a feature of this theory, the metric $g_{\mu\nu}$ and the connection $\Gamma_{\alpha\beta}^\mu$ are considered as the independent fields. Then, the field equations can be obtained by varying the action [6];

$$\Gamma_{\alpha\beta}^\mu = \frac{1}{2} q^{\mu\sigma} (q_{\sigma\alpha,\beta} + q_{\sigma\beta,\alpha} - q_{\alpha\beta,\sigma}), \quad (2)$$

$$q_{\mu\nu} = g_{\mu\nu} + \kappa R_{\mu\nu}, \quad (3)$$

$$\sqrt{-q} q^{\mu\nu} = \sqrt{-g} g^{\mu\nu} - 8\pi\kappa \sqrt{-g} T^{\mu\nu}, \quad (4)$$

where $q_{\mu\nu}$ is an auxiliary metric and $T^{\mu\nu}$ is the standard energy-momentum tensor with indices raised with the metric $g_{\mu\nu}$. In addition to the above field equations, the energy-momentum conservation should be satisfied, i.e., $\nabla_\mu T^{\mu\nu} = 0$, where ∇_μ is defined with the physical metric $g_{\mu\nu}$. It is noticed that $q^{\mu\nu}$ is the matrix inverse of $q_{\mu\nu}$, which is different from $g^{\mu\alpha} g^{\nu\beta} q_{\alpha\beta}$ if matter exists.

Now, we consider the spherically symmetric relativistic stars. Previously, the structures of compact objects in EiBI have already been examined by several groups [11–15]. The metric describing the spherically symmetric objects can be written as

$$g_{\mu\nu} dx^\mu dx^\nu = -e^{\nu(r)} dt^2 + e^{\lambda(r)} dr^2 + f(r) d\Omega^2, \quad (5)$$

$$q_{\mu\nu} dx^\mu dx^\nu = -e^{\beta(r)} dt^2 + e^{\alpha(r)} dr^2 + r^2 d\Omega^2, \quad (6)$$

where $d\Omega^2 = d\theta^2 + \sin^2\theta d\phi^2$. We remark that we use the gauge freedom to fix that $q_{\theta\theta} = r^2$. In particular, we consider the neutron stars composed of the perfect fluid, which is given by

$$T^{\mu\nu} = (\epsilon + p) u^\mu u^\nu + p g^{\mu\nu}, \quad (7)$$

where ϵ and p denote the energy density and pressure, while u^μ corresponds to the four velocity of matter given as $u^\mu = (e^{-\nu/2}, 0, 0, 0)$. Using Eq. (4), one can obtain the relation

$$abf = r^2, \quad e^\alpha = e^\lambda ab, \quad e^\beta = e^\nu b^3/a, \quad (8)$$

where $a \equiv \sqrt{1 + 8\pi\kappa\epsilon}$ and $b \equiv \sqrt{1 - 8\pi\kappa p}$. On the other hand, using Eq. (3), one can get the equations describing the structures of relativistic stars;

$$(re^{-\alpha})' = 1 - \frac{r^2}{2\kappa} \left[\frac{a}{b^3} - \frac{3}{ab} + 2 \right] \quad (9)$$

$$e^{-\alpha}(1 + r\beta') = 1 + \frac{r^2}{2\kappa} \left[\frac{a}{b^3} + \frac{1}{ab} - 2 \right], \quad (10)$$

where the prime denotes a derivative with respect to r . In addition to these equations, the energy-momentum conservation law gives us the additional equation:

$$\nu' = -\frac{2p'}{\epsilon + p}. \quad (11)$$

At last, combining Eqs. (8)–(11), one can derive the Tolman-Oppenheimer-Volkoff (TOV) equations in EiBI;

$$m' = \frac{r^2}{4\kappa} \left[\frac{a}{b^3} - \frac{3}{ab} + 2 \right], \quad (12)$$

$$e^{-\alpha} = 1 - \frac{2m}{r},$$

$$p' = -e^\alpha \left[\frac{2m}{r^2} + \frac{r}{2\kappa} \left(\frac{a}{b^3} + \frac{1}{ab} - 2 \right) \right] \times \left[\frac{2}{\epsilon + p} + 4\pi\kappa \left(\frac{3}{b^2} + \frac{1}{a^2 c_s^2} \right) \right]^{-1}, \quad (13)$$

where c_s denotes the sound speed. We remark that these equations in the limit of $\kappa \rightarrow 0$ can reduce to the standard TOV equations in general relativity. With the relation between ϵ and p , i.e., the EOS, the equation system is closed. After one adopts the central density ϵ_c , the TOV equations are integrated outward with the conditions $m(0) = 0$. Then, the stellar surface should become the position where the pressure vanishes. Since EiBI is

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equivalent to general relativity in vacuum and $\epsilon = p = 0$ at the stellar surface ($r = R$), one can find that $e^{-\alpha} = e^{-\lambda} = 1 - 2M/R$ at $r = R$. As a result, the stellar mass is defined as $M = m(R)$. Additionally, in order to allow for self-gravitating objects, the condition of κ is obtained [11] as

$$8\pi p_c \kappa < 1 \quad \text{for } \kappa > 0 \quad (14)$$

$$8\pi \epsilon_c |\kappa| < 1 \quad \text{for } \kappa < 0, \quad (15)$$

where p_c denotes the central pressure. Hereafter, we adopt $8\pi \epsilon_0 \kappa$ as a normalized constant, where ϵ_0 is the nuclear saturation density given by $2.68 \times 10^{14} \text{ g cm}^{-3}$. We remark that $\epsilon_0 = 1.99 \times 10^{-4} \text{ km}^{-2}$ in geometric units with $c = G = 1$.

III. RELATIVISTIC STELLAR MODELS IN EIBI

In order to construct relativistic stellar models, we need to prepare the EOS. In this paper, we adopt the realistic EOS proposed by the different theoretical approaches, i.e., the phenomenological models, the relativistic mean field models, and the ones based on the Skyrme-type effective interactions (see [21] for more information about EOS adopted here). As the phenomenological models, we adopt the EOS constructed by Oyamatsu and Iida [22,23], where they made EOS for various values of incompressibility K_0 and the density dependence of the nuclear symmetry energy at the saturation point L . K_0 and L are parameters characterizing the stiffness of neutron-rich nuclear matter. Hereafter, we refer to this phenomenological EOS as OI (a, b), where a and b denote the adopted values of K_0 and L . As the relativistic mean field models, we adopt two EOS, i.e., the Shen EOS [24] and the Miyatsu EOS [25]. We also adopt five EOS based on the Skyrme-type effective interactions, i.e., FPS [26], SLy4 [27], BSk19, BSk20, and BSk21 [28–30]. We remark that every EOS adopted in this paper is consistent with the terrestrial experimental data for masses and radii of stable nuclei. It is important to consider the neutron stars with $0.5M_\odot$, because the density inside such objects is less than a few times the saturation density, which should be strongly constrained from the terrestrial experiments [21].

As an example of neutron star models in EiBI, we show the mass and radial relations constructed from the FPS EOS in Fig. 1, where the solid line denotes the results in general relativity ($\kappa = 0$), while the broken and dotted lines correspond to those in EiBI with $8\pi \epsilon_0 \kappa = 0.01$ and 0.02 , respectively. From this figure, one can observe the obvious deviation from the predictions in general relativity. However, as mentioned the above, this difference, depending on the coupling constant κ , must be buried in the uncertainties due to the EOS of neutron star matter. That is, it could be quite difficult to distinguish EiBI from general relativity only if one would measure the mass and radius of neutron stars.

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FIG. 1 (color online). Neutron star mass-radius relations in EiBI constructed from FPS EOS. The labels on lines denote the values of $8\pi \epsilon_0 \kappa$. The solid line corresponds to that in general relativity.

With respect to such a difficulty, we are successful in finding an observational possibility to discriminate EiBI from general relativity, i.e., via the terrestrial experiments for the neutron skin thickness of neutron-rich atomic nuclei. Using the various realistic EOS mentioned above, we determine the radii of neutron stars with $0.5M_\odot$ by varying the value of $8\pi \epsilon_0 \kappa$ and then show it in Fig. 2 as a function of the neutron skin thickness of ^{208}Pb , where R_{05} and ΔR denote the stellar radii with $0.5M_\odot$ and the neutron skin thickness of ^{208}Pb . In particular, in order to estimate the value of ΔR for each EOS, we adopt the formula proposed by Oyamatsu and Iida [22], where the neutron skin thickness can be expressed as functions of neutron excess, the atomic mass number, and the value of L . Since the estimation of ΔR could depend a little on theoretical models, the plots in Fig. 2 may be slightly modified. Anyway, the value of ΔR does not depend on κ at all. From this figure, one clearly observes that R_{05} can be written as a linear function of ΔR almost independently of the adopted

FIG. 2 (color online). Radii of neutron stars with $0.5M_\odot$, R_{05} , as a function of neutron skin thickness of ^{208}Pb for $8\pi \epsilon_0 \kappa = -0.02, 0$, and 0.02 , using the various EOS. The solid line denotes the fitting line in general relativity, while the broken and dotted lines denote that in EiBI for $8\pi \epsilon_0 \kappa = 0.02$ and -0.02 , respectively.

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EOS, while the correlation between R_{05} and ΔR strongly depends on the coupling constant κ . In practice, one can write the linear fitting with each value of $8\pi\epsilon_0\kappa$ as

$$R_{05} = c_0 + c_1 \Delta R, \quad (16)$$

where c_0 and c_1 are constants depending on the value of $8\pi\epsilon_0\kappa$. Since the units of R_{05} and ΔR in this fitting are km and fm, the units of c_0 and c_1 become km and km/fm. Regarding the suitability of this fitting, we can estimate that the root mean fractional variation (RMFV) from the original values are 1.44%, 1.09%, and 0.90% for $8\pi\epsilon_0\kappa = -0.02, 0$, and 0.02 , respectively. Here, RMFV for each κ is calculated as

$$\text{RMFV} = \sqrt{\frac{1}{N} \sum_N \frac{(R_{05}^{\text{ex}} - R_{05}^{(16)})^2}{R_{05}^{\text{ex}2}}}, \quad (17)$$

where R_{05}^{ex} and $R_{05}^{(16)}$ denote the stellar radius with $0.5M_\odot$ calculated with each EOS and that estimated with Eq. (16), while N is the number of adopted EOS, i.e., $N = 11$ in this paper. The number of RMFV expresses how good the fits are. Thus, we consider that the linear fitting (16) is enough to distinguish the gravitational theory.

Moreover, we also examine the dependence of c_0 and c_1 on $8\pi\epsilon_0\kappa$ in the range of $-0.02 \leq 8\pi\epsilon_0\kappa \leq 0.04$. Figure 3 shows the values of c_0 and c_1 as a function of $8\pi\epsilon_0\kappa$. From this figure, one finds that the coefficients in the linear fitting (16), i.e., c_0 and c_1 , can be written as linear functions of $8\pi\epsilon_0\kappa$. In fact, we can derive such linear functions as

$$c_0/\text{km} = 8.21 + 60.3 \times (8\pi\epsilon_0\kappa), \quad (18)$$

$$c_1/\text{km/fm} = 31.0 - 125.8 \times (8\pi\epsilon_0\kappa). \quad (19)$$

Consequently, combining Eqs. (16), (18), and (19), one can obtain the value of $8\pi\epsilon_0\kappa$ as a function of R_{05} and ΔR ;

FIG. 3 (color online). Coefficients in the fitting formula (16) as a function of $8\pi\epsilon_0\kappa$, where the circles and squares denote the obtained coefficients c_0 and c_1 , respectively.

$$8\pi\epsilon_0\kappa = \frac{(R_{05}/\text{km}) - 8.21 - 31.0(\Delta R/\text{fm})}{60.3 - 125.8(\Delta R/\text{fm})}. \quad (20)$$

Using this empirical formula, at least, one must be able to check how valid general relativity is. Namely, with the observational values of R_{05} and ΔR , one can estimate the value of κ , where κ should be zero in general relativity. On the other hand, we should also emphasize that this empirical formula could be adopted to distinguish EiBI from most of the modified theories of gravity, because the stellar properties with $0.5M_\odot$ in most of the modified theories of gravity are almost the same as those in general relativity.

At last, we should also mention an uncertainty in $8\pi\epsilon_0\kappa$ due to the observational uncertainties in R_{05} and ΔR . If the observations of R_{05} and ΔR have $\pm 10\%$ variances, one can estimate that the variances on $8\pi\epsilon_0\kappa$ arise up to ± 0.04 for $R_{05} = 12$ km and ± 0.06 for $R_{05} = 14$ km, using Eq. (20), even if general relativity is the correct gravitational theory.

IV. CURRENT OBSERVATIONAL STATUS

In order to estimate the coupling constant κ with Eq. (20), one needs to measure the neutron skin thickness of ^{208}Pb , ΔR , and the radius of the $0.5M_\odot$ neutron star, R_{05} . That is, depending on some finite precision in the measurements of ΔR and R_{05} , the estimation of κ could become blurry. In this section, we discuss the current observational status and how well κ may be constrained with ΔR and R_{05} .

The current best measurement of ΔR could be the data by PREX experiment [31], which tells us that $\Delta R = 0.33^{+0.16}_{-0.18}$ fm. Unfortunately, within this precision of ΔR , we cannot constrain κ even if the exact value of R is known. In fact, since $\Delta R = 0.33$ fm is out of Fig. 2, it may be questionable to adopt Eq. (20) in such region to estimate κ .

The measurement of R_{05} must be more difficult than that of ΔR , because $0.5M_\odot$ is an exceptionally small mass for the neutron star and the measurement of the stellar radius itself is quite challenging. The masses of neutron stars in a binary system have been determined [32,33]. Among them, the lowest mass of a neutron star observed so far could be $0.87 \pm 0.07M_\odot$ with an eccentric orbit or $1.00 \pm 0.10M_\odot$ with a circular orbit observed in the high-mass x-ray binary 4U1538-52 [34]. We hope that the measurement of an extremely low-mass neutron star will be successful in the future. In that time, perhaps, we may not need the exactly $0.5M_\odot$ neutron star, because the stellar radius is theoretically predicted to be quasiconstant for the neutron star with $M = 0.5 - 0.7M_\odot$, where the difference in radius could be less than a few percent [35]. In fact, in a similar way in Sec. III, we find that the radii of $0.7M_\odot$ stellar models, R_{07} , can be also expressed as a linear function of ΔR almost independently of the adopted EOS, although the values of RMFV become slightly worse, i.e., 2.00%, 1.44%, and 1.08% for $8\pi\epsilon_0\kappa = -0.02, 0$, and 0.02 , respectively.

Using the obtained linear relation between R_{07} and ΔR with Eq. (16), the relative deviations between R_{05} and R_{07} for $\Delta R = 0.1$ fm become 1.16%, 2.24%, and 3.32%, while those for $\Delta R = 0.22$ fm become 0.33%, 0.79%, and 1.41% for $8\pi\epsilon_0\kappa = -0.02, 0$, and 0.02 , respectively. Thus, one might estimate the value of $8\pi\epsilon_0\kappa$ on some level from Eq. (20) with R_{07} instead of R_{05} .

On the other hand, the measurement of the stellar radius is notoriously difficult. Recently, the stellar radius of a neutron star has been estimated with the observations of thermonuclear x-ray bursts and thermal spectra from quiescent low-mass x-ray binaries [36–39]. However, it is still quite difficult to determine the stellar radius with less than $\sim \pm 10\%$ accuracy. In order to determine the value of $8\pi\epsilon_0\kappa$ within the range of ± 0.01 , one should measure the stellar radius at least with $\pm$ a few % accuracy, even if ΔR will be exactly measured.

V. CONCLUSION

Compact objects must be suitable laboratories to test the gravitational theory. However, due to the uncertainties of the EOS of neutron star matter, it is generally difficult to distinguish the gravitational theory by only using the observations of neutron stars. To solve this difficulty, we find an observational possibility to discriminate EiBI from general relativity via the measurements of a neutron skin thickness of ^{208}Pb by the terrestrial experiments, in addition to the astronomical observations of neutron stars. We show that the stellar radii with $0.5M_\odot$ can be written as a linear function of the neutron skin thickness almost independently of the adopted EOS, which strongly depends on the coupling constant in EiBI. Additionally, we show that the coupling constant can be estimated with the observable

properties, such as the stellar radii with $0.5M_\odot$ and a neutron skin thickness of ^{208}Pb . This estimation could be also useful to observationally probe how valid general relativity is.

In this paper, we especially focus on the neutron skin thickness of ^{208}Pb , but the linear correlation between the stellar radii with $0.5M_\odot$ and neutron skin thickness could be satisfied for the different neutron-rich nuclei. If so, one could make estimations of the coupling constant in EiBI via the different measurements of neutron skin thickness of various nuclei, which tells us a more accurate value of the coupling constant. On the other hand, it could be difficult to discuss the similar correlation by using the radius with a massive neutron star, because the density inside the massive neutron star becomes much higher than the nuclear saturation density, where there exist many theoretical uncertainties to construct EOS models and the additional components such as hyperon and/or quark could appear.

ACKNOWLEDGMENTS

We are grateful to K. Yagi, K. Iida, K. Oyamatsu, and our referees for their fruitful comments. We also acknowledge the hospitality of members of the University of Mississippi, especially E. Berti. This work was supported by Grants-in-Aid for Scientific Research on Innovative Areas through Grants No. 24105001, and No. 24105008 provided by MEXT, by a Grant-in-Aid for Young Scientists (B) through Grants No. 24740177 and No. 26800133 provided by JSPS, by the Yukawa International Program for Quark-hadron Sciences, by the Grant-in-Aid for the global COE program “The Next Generation of Physics, Spun from Universality and Emergence” from MEXT, and by a grant from Yukawa Institute for Theoretical Physics, Kyoto University.

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