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EFFECTIVE LEAF AREA INDEX RETRIEVING FROM TERRESTRIAL POINT CLOUD DATA: COUPLING COMPUTATIONAL GEOMETRY APPLICATION AND GAUSSIAN MIXTURE MODEL CLUSTERING

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KEY WORDS: Point Cloud Data, Effective Leaf Area Index, Curvature Threshold, Clustering Analysis

ABSTRACT:

Leaf area index (LAI) is one of the most important structural parameters of forestry studies which manifests the ability of the green vegetation interacted with the solar illumination. Classic understanding about LAI is to consider the green canopy as integration of horizontal leaf layers. Since multi-angle remote sensing technique developed, LAI obliged to be deliberated according to the observation geometry. Effective LAI could formulate the leaf-light interaction virtually and precisely. To retrieve the LAI/effective LAI from remotely sensed data therefore becomes a challenge during the past decades. Laser scanning technique can provide accurate surface echoed coordinates with densely scanned intervals. To utilize the density based statistical algorithm for analyzing the voluminous amount of the 3-D points data is one of the subjects of the laser scanning applications. Computational geometry also provides some mature applications for point cloud data (PCD) processing and analysing. In this paper, authors investigated the feasibility of a new application for retrieving the effective LAI of an isolated broad leaf tree. Simplified curvature was calculated for each point in order to remove those non-photosynthetic tissues. Then PCD were discretized into voxel, and clustered by using Gaussian mixture model. Subsequently the area of each cluster was calculated by employing the computational geometry applications. In order to validate our application, we chose an indoor plant to estimate the leaf area, the correlation coefficient between calculation and measurement was 98.28%. We finally calculated the effective LAI of the tree with 6 × 6 assumed observation directions.

1. INTRODUCTION

Leaf area index (LAI) is a key variable used to model many physical processes, such as canopy photosynthesis and transpiration. It determines the size of the plant-atmosphere interface and thus plays a critical role in the exchange of energy and mass between the canopy and the atmosphere (Weiss et al., 2004). Therefore, obtaining LAI effectively and accurately by using remote sensing data has been discussed for decades.

LAI is first defined as one-sided of photosynthetic tissue per unit ground horizontal area (Watson, 1947). At the beginning of the LAI studies the canopy structural parameters are measured directly. It is accurate, however, time consuming and destructive to plants (Lang and Xiang, 1986). According to the botanical structure of the vegetation, we only consider the green plants on the ground; leaves from the canopy are with low visible light reflectance except of green light. Theoretically it is possible to retrieve the leaf area from the canopy using optical sensed data. Since 1960s people attempt to indirectly retrieve canopy structural parameters from optical images (Jonckheere et al., 2004). Several ground-based commercial instruments for LAI collection have been testified, the advantages and drawbacks of each instrument have been presented as well; moreover the potential of the laser instruments for LAI measurement has been pointed out acutely (Welles and Cohen, 1996). Landsat TM data and ground-based measurements of LAI have been correlated for estimating effective LAI, which is the product of LAI and clumping index. Some issues have been discussed for the LAI estimation, which were correlated to the LAI retrieving from Landsat images in spite the limitations of TM image (Chen and Cihlar, 1996).

The development of the optical sensor resolution improves LAI measurement accuracy and mathematical modeling. An application with spectral and textural information was used for mapping the LAI of different vegetation types, has been presented by using IKONOS images (Colombo et al., 2003). Moreover when the land cover is stratified, spectral and textural relations are considerably better for mapping LAI spatial variability for different crop types. Encouraging result in LAI estimation by using optical data has been obtained via data fusion process for high spatial resolution images of the LAI. For achieving reliable result over a large area, LAI measurement with auxiliary variables such as NDVI computed from Landsat images have been combined (Hernandez et al., 2014). However, due to the assumption of randomly located foliage elements within the canopy, LAI obtained from gap fraction (Pearcy et al., 1989) theory is not the actual LAI (Zheng and Moskal, 2009), thus effective LAI has been proposed to describe the result more accurately, which is obtained by considering the clumping index affection.

Recent studies propose to utilize laser scanner for LAI estimation since it holds good performance at range detection and the consistency of the precision. Morsdorf and his colleagues evaluated the potential of deriving effective LAI proxy by estimating a fraction of first and last echo types inside the canopy. Based on the regression results, LAI has been computed for a region, and compared qualitatively to the result based on imaging spectrometry, revealing similar spatial patterns and ranges of values (Morsdorf et al., 2006). Effective LAI has been calculated by referring empirical model from airborne LiDAR data. Due to the narrow scan angle of the LiDAR, the parameters of the model have been estimated from the field investigation (Korhonen et al., 2011). An accurate application has been developed for calculating leaf area density (LAD) and cumulative LAI profiles of small trees (Hosoi and Omasa, 2006). This voxel based 3-D modeling application is implemented in the study. This model allows the LAD and LAI of trees, which have complex spatial distributed foliage, to be computed by direct counting of the beam-contact frequency in...
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Five parts are presented in this paper. In the second part we introduce the data collection, theoretical foundations and data processing. Thirdly, we show some results, including the validation experiment and retrieved effective LAI of an isolated broad leaf tree. We discuss several issues related to the study in the fourth part; finally a conclusion will be made.
2. MATERIALS AND METHODOLOGY

2.1 Data Collection

A well-isolated broad leaf tree (Cinnamomum Camphora, Figure 1a) was used in this study, which is located in Kyoto University Katsura Campus (N34°58′55.61″, E135°40′43.54″) in Kyoto Prefecture, Japan. We set six directions around the tree for collecting data. Raw data were assigned to an assumed coordinate system, in which the original point was set to the first station (ScanPose001). Cartesian coordinates (x, y, z) units were in meters (m) (Figure 1b). Both vertical and horizontal scanning intervals were set to 0.02°.

2.2 Methodology

2.2.1 Simplified Curvature Estimation: PCD give the average Cartesian or polar coordinates of the surface patch. The curvature of a point can therefore be estimated by considering the normals of its neighboring points. Assume there is a point set $P_n$ which contains $N$ points, whose element $p_i$ is the 3-D coordinates (x, y, z) of the Cartesian space. The amount of the point is determined by both vertical and horizontal scanning intervals. The set of neighboring points $P_k$ is determined by the searching radius $r$ centering on the query point $p_k$, which is $P_k = \{ p_i : \| p_i - p_k \|_2 \leq r \}, (i = 1, 2, ..., n)$. A simplified curvature $c_q$ of point $p_i$ is given by (Rusu, 2009):

$$c_q = \frac{\lambda_1}{\lambda_1 + \lambda_2 + \lambda_3}, \quad (\lambda_1 \leq \lambda_2 \leq \lambda_3), \quad (1)$$

where $\lambda_j (j = 1, 2, 3)$ is the eigenvalue given by $\text{Cov} \cdot x_i = \lambda_j \cdot x_i$, $\text{Cov}$ is the covariance matrix of $P_i$, determined by $\text{Cov} = \frac{1}{n} \sum_{i=1}^{n} (p_i - \bar{p})(p_i - \bar{p})^T$, $x_j$ is the eigenvector of $\text{Cov}$. $\bar{p}$ is the center of $P_k$, which is given by:

$$\bar{p} = \frac{1}{n} \sum_{i=1}^{n} p_i. \quad (2)$$

2.2.2 Gaussian Mixture Model: Voluminous points amount and complexity are the principal property of PCD. PCD carry the Cartesian coordinates from the patch of an object interacting with the laser impulse by receiving objects surface echo. Points therefore correspond to heterogeneous distributions, like multivariate clusters, of discrete objects within a sample space according to their positions. Exploring constructional information is one of the majority purposes for PCD users. We used the mclust package of the R platform to cluster the point set observations for reducing the complexity of the PCD. It provides functions for model-based clustering (covariance parameterization and number of clusters selected via Bayesian information criterion (BIC)), which gives the maximized loglikelihood for the number of components in the data. In general, the larger value of BIC, the stronger the evidence for the number of clusters (Fraley et al., 2012). It attempted to iterate group sets of objects according to a rule stating that objects within the same cluster were more optimized to each other than those in other groups. The detailed algorithm explanation was presented by the articles (Fraley and Raftery, 1998, Fraley and Raftery, 2002).

2.2.3 Leaf Orientation Retrieving: This study assumed that one leaf is a fitting plane retrieved from point cluster which was obtained by mclust (see 2.2.2). We chose the principal component analysis routine from CGAL to calculate the plane (Aliez et al., 2014). Suppose the plane equation we computed is: $Ax + By + Cz + D = 0$. The orientation of the plane can be calculated by:

$$\theta_L = \begin{cases} \arccos \left( \frac{C_{n,p}^T}{|C_{n,p}|^2} \right) : C \geq 0 \\ \pi - \arccos \left( \frac{C_{n,p}^T}{|C_{n,p}|^2} \right) : C < 0 \end{cases}, \quad (3)$$

$$\varphi_L = \arccos \left( \frac{A}{\sqrt{A^2 + B^2}} \right),$$

where $\|n_p\|_2 = \sqrt{A^2 + B^2 + C^2}$, $\theta_L$ and $\varphi_L$ are the zenith and azimuth angle of the plane normal, respectively. Leaf normal calculation is a key step to retrieve the leaf area we discuss in following section.

2.2.4 Effective Leaf Area Calculation: In order to find the geometrical boundary of the cluster, the 3-D convex hull function of CGAL for generating the convex hull, which contained all the points of the cluster, was selected (Hert and Schirra, 2014). Assume the convex hull contains $m$ points as vertices, the leaf area can be approximately calculated as the topological closure of the points that vertices projected on the fitting plane which we computed from section 2.2.3.

Suppose $P_V = \{ p_k(x_v, y_v, z_v) : k = 1, 2, ..., m \}$ are the vertices projection on the fitting plane, the center of $P_v(x_v, y_v, z_v)$ of $P_V$ can be calculated by (2). If the points are ordered sequentially, according to the triangulation mesh function of CGAL, the leaf area could be computed by accumulating the triangles:

$$S = \sum_{i=1}^{m} s_i, \quad (4)$$

where $s_i$ is the triangle area constructed by $p_i$, $p_k$ and $p_{k+1}$. When $k = m$, $p_{k+1} = p_1$. Those points inside the closure are skipped. The effective leaf area $S^*$ can be computed by considering the projection coefficient (Ross, 1981):

$$S^* = \cos \bar{r}_v \bar{r}_v S, \quad (5)$$

where $\bar{r}_v(\theta_v, \varphi_v)$ and $\bar{r}_L(\theta_L, \varphi_L)$ are view direction and leaf normal, respectively.

2.3 Data Processing

Effective leaf area retrieving algorithm was designed as follows (Figure 2). We calculated the simplified curvature of each point, see (1), and then defined the searching radius $r (r = 4cm)$ according to the average long axis of the leaves. Points whose $c_q > T_1 (T_1 = 0.21)$ were taken as $D_1$, which were mostly from leaves, and points whose $c_q \leq T_1$ were taken as $D_2$ (Figure 3c). In $D_2$, there were points from leaves as well, which should be restored to $D_1$. Hence we detected the $D_2$ points within a sphere (the radius is $T_2 = 0.01m$), which centered at each point of $D_1$. The point(s) in $D_2$ located in each sphere were merged to $D_1$ as leaf data (Figure 3d). The leaf data were voxelized with each lattice size 8 x 8 x 8 cm, which could contain the maximum leaf size. The data within each voxel were clustered according to section 2.2.2. Those clusters containing less than thirty $(T_3 = 30)$ points
were rejected due to the possibility of low reliability. The leaf area were calculated for each cluster according to section 2.2.4, and then the accumulated area for entire canopy was calculated. Finally the effective LAI was computed according to proposed $6 \times 6$ observation directions.

3. RESULTS AND VALIDATION

Raw data points amount was over $9.7 \times 10^6$ (Figure 3a). After curvature estimation (Figure 3b), 76.13% data were rejected according to the threshold, many of them were from leaves. Therefore, we employed the method in 2.3 to restore the excessively removed points. The result of rejected data and leaf data are shown in Figure 3c and 3d, individually. The leaf data accordingly increased to 52.33% and the opposite data were 47.67%. The leaf data were effectively restored.

The algorithm of data processing within a voxel is indicated in Figure 4. The initial condition of the data in the voxel is shown in Figure 4a, which is out-of-order arranged. After mclust function (see 2.2.2) processing, points were distinguished into four clusters: $c_1, c_2, c_3$ and $c_4$ (Figure 4b). We picked one ($c_3$) of them as an example for retrieving the cluster area, red plane (Figure 4c) was obtained by using PCA function of CGAL (see 2.2.3). First, we generated the convex hull of this cluster by using 3-D convex hull generation function from CGAL, then obtained the vertices of this convex hull. Vertices were projected on the fitting plane of the cluster and those points within the convex hull were removed. Finally the area of this cluster was calculated by accumulating the triangles which are constructed from each two vertices and the center (red point in Figure 4d). The volume of this canopy was calculated as $V = 33.918 \text{ m}^3$ from 3-D convex hull as well. For the light travel length we assumed the canopy was contained by a sphere, according the maximum and minimum coordinates of the PCD, we calculated the effective LAI by:

$$ELAI = \frac{D\eta}{V},$$

$$D = \frac{\Delta x + \Delta y + \Delta z}{3},$$

$$\eta = \sum_{\chi=1}^{I} \sum_{\omega=1}^{J} S^*_{\chi\omega},$$

$$\Delta x = x_{\max} - x_{\min},$$

$$\Delta y = y_{\max} - y_{\min},$$

$$\Delta z = z_{\max} - z_{\min}.$$  \hspace{1cm} (6)

where $D$ is the average light traveling distance, $\eta$ is the effective leaf area of the entire canopy, $\chi$ is the index of the voxel (from 1 to $I$), $\omega$ is the index of the cluster within the $\chi$th voxel (from 1 to $J$), $S^*_{\chi\omega}$ is the effective area of each cluster within a voxel, $\Delta x = 4.64 \text{ m}$, $\Delta y = 4.61 \text{ m}$, $\Delta z = 4.79 \text{ m}$, respectively.

The effective LAI of the tree was calculated from $6 \times 6$ assumed observation directions (Table 1). It was indicated that our calculation can precisely provide effective LAI estimation according to the variation of the observation directions. Due to the lack of the resource we cannot accurately measure the total leaf area of the tree we selected. We assessed the application using an indoor plant (Figure 5a) and marked down nine well-isolated leaves before this plant was scanned (Figure 5b). We manually measured...
Figure 3: (a) The raw point cloud data of the tree with scale bar 1 m. (b) The curvature estimation of the raw data, scale bar shows in 0.9 m, color various according to the curvature, which ranged from 0 to 0.33. (c) The data ($D_2$) contain branches after curvature filtering. The scale bar shows in 0.5 m. (d) Leaf data after merging leaf points from $D_2$ and data $D_1$; the scale bar shows in 0.5 m (see section 2.3).

the area of the leaves to compare with the calculation results. A high correlation coefficient up to 98.28% was achieved (Figure 5c).

4. DISCUSSION

Curvature is a common parameter during PCD processing in computational geometry. Different from the Gaussian curvature and mean curvature, the simplified curvature we utilized in this study is the approximation of the change of curvature in a neighborhood $P_n$ centered at $p_q$, and it is invariant under rescaling. It can be computed conveniently as well. Small values indicate that the neighborhood points $P_n$ are on the plane tangent to the surface (Rusu, 2009). This simplified curvature was an effective parameter for identifying whether the point was on trunk or leaf by using a properly defined search radius $r$. In our study we defined the searching radius as the average long axis of the leaves. However, we did not discuss how the searching radius affects the curvature. Different searching radius settings would definitely change the point normal result, which was determined by the surface
complexity of the object. Smaller searching radius corresponded higher curvature fluctuation, and bigger searching radius causes that the distinction of leaf points and non-photosynthetic tissue points was not obvious. A future study for investigating the optimized searching radius setting method should be attempted so that to develop this application into an unsupervised function.

Our clustering strategy was to first discrete the PCD into voxel matrices, for reducing the computational complexity of the PCD. The voxel size was set according to the maximum single-leaf size observed in the canopy. Other applications for determining the voxel size should be considered in line with different leaf patterns. We then clustered the points within each voxel using Gaussian mixture model. Estivill-Castro has pointed out that one cannot precisely define clusters, so the clustering results almost certainly contain errors (Estivill-Castro, 2002). They showed weak correlations and the amount of these points were not big. Therefore we remove those clusters which held less than thirty points. It caused the loss of leaf area we retrieved from PCD, but the reducing area of thirty points is very small according to the scan-

Figure 4: (a) Point data with in a voxel. (b) After *mclust* clustering, the data were indicated into four subsets (*c1*, *c2*, *c3*, *c4*) each symbol indicates one cluster. (c) One cluster (*c3*) from (b), red plane is the fitting plane retrieved from PCA algorithm. (d) After CGAL convex hull generation, we obtain the vertices of the volume of the cluster, then projected these vertices on PCA fitting plane of this cluster and remove those points within the closure. Finally the area of this cluster is calculated by accumulating the triangles which construct from each two vertices and the center (red point).
Calculated leaf area (m$^2$)
Measured leaf area (m$^2$)
Correlation coefficient: 98.28%

Figure 5: (a) The picture of the indoor plant for validation. (b) PCD of the plant, different color shows components of the plant. (c) Comparison between measurements and calculated each leaf area of the plant, which have a correlation coefficient of 98.28%.

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<td>75</td>
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<td>3.141</td>
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Table 1: The effective LAI (m$^2$/m$^2$) result which is calculated from 6 x 6 assumed observation directions.

This study adapted dense PCD with millimeter resolution, permitting reliable scanned points Cartesian coordinates. There should be at least three directional observations under similar conditions so that the whole canopy can be covered, with minimal disturbance from wind and beam absorption by the canopy. The PCD should be calibrated with geo-references for calculating the actual relative angle between leaf normal and observation angles.
5. CONCLUSION

This study retrieved effective LAI, a key canopy structure parameter, using terrestrial scanned PCD. It is an important factor in vegetation structural investigations and canopy radiative transfer simulations. In contrast to previous studies, we innovatively utilized simplified curvature as the threshold for filtering the non-photosynthetic components. PCD were clustered by mclust, which is a Gaussian mixture model based package of the R platform. An important aspect of this method was the manipulation of computational geometry algorithm for curvature estimation and effective leaf area retrieving. Good agreements between measurement and our calculation were obtained by conducting an indoor experiment of a plant. The correlation coefficient was in the range of 98.28%. Due to the sufficient accuracy of TLS, the results of this study could be taken as a validation of optical sensor based LAI estimation. In future research, we will attempt to apply our curvature-cluster application on investigating forest effective LAI. We believe that laser scanning based phytometric techniques have more advantages than many optical sensor based applications. With the development of laser scanning techniques, the efficiency and accuracy of TLS will be improved; and forest parameterization and investigation techniques will be substantially improved as well.

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