

Origin of the Tetragonal-to-Orthorhombic Phase Transition in FeSe: A Combined Thermodynamic and NMR Study of Nematicity

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The nature of the tetragonal-to-orthorhombic structural transition at $T_s \approx 90$ K in single crystalline FeSe is studied using shear-modulus, heat-capacity, magnetization, and nuclear magnetic resonance measurements. The transition is shown to be accompanied by a large shear-modulus softening, which is practically identical to that of underdoped $\text{Ba}(\text{Fe}, \text{Co})_2\text{As}_2$, suggesting a very similar strength of the electron-lattice coupling. On the other hand, a spin-fluctuation contribution to the spin-lattice relaxation rate is only observed below T_s . This indicates that the structural, or “nematic,” phase transition in FeSe is not driven by magnetic fluctuations.

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One of the most intriguing questions in the study of iron-based superconductors concerns the relation between structure, magnetism, and superconductivity [1–10]. Stripe-type antiferromagnetic order often occurs at the same or at a slightly lower temperature than the tetragonal-to-orthorhombic structural distortion and the two types of order are closely related by symmetry. They break the fourfold rotational symmetry of the high-temperature phase, which can be associated with a nematic degree of freedom [4,6]. Superconductivity typically is strongest around the point where the structural transition (T_s) and the antiferromagnetic transition (T_N) are suppressed by pressure or chemical substitution. Whether the magnetic or the structural instability is the primary one is still under intense debate [10], also because of its relevance to the pairing mechanism [5,6]. Recently, scaling relations between the shear modulus related to the structural distortion, C_{66} , and the spin-lattice relaxation time T_1 , as a measure of the strength of spin fluctuations, have been proposed [7,8] in order to address the above question. They were found to be well satisfied in the $\text{Ba}(\text{Fe}, \text{Co})_2\text{As}_2$ system [7,8], where T_s and T_N are in close proximity to each other, suggesting a magnetically driven structural transition [7]. Clearly, it is of great interest to see if a relation between shear modulus and spin fluctuations is universally observed in other iron-based materials.

FeSe is structurally the simplest iron-based superconductor and has attracted a lot of attention because of a nearly fourfold increase of its $T_c \approx 8$ K under pressure [11,37]. Moreover, this system is particularly interesting with respect to the relation of structure and magnetism, since it undergoes a tetragonal-to-orthorhombic structural phase transition at $T_s \sim 90$ K, similar to that found in the 1111- and 122-type parent compounds [2], but does not order magnetically at ambient pressure [12,13]. Spin fluctuations at low temperatures were, however, observed in nuclear

magnetic resonance (NMR) measurements [14]. Surprisingly, the orthorhombic distortion of FeSe is not reduced upon entering the superconducting state [9] in strong contrast to underdoped BaFe_2As_2 [3,15], indicating different couplings between structure and superconductivity. This strongly motivates further study of the interplay of structure, magnetism, and superconductivity in FeSe.

In this Letter, we study FeSe using shear-modulus, specific-heat, magnetization, and NMR measurements in vapor-grown [9] single crystals and compare our results to those of underdoped $\text{Ba}(\text{Fe}, \text{Co})_2\text{As}_2$. We find that the magnetic fluctuations observed in the NMR data cannot be the driving force for the structural transition, since they set in only below T_s . Further, the shear-modulus softening above T_s is found to be nearly identical in FeSe and underdoped $\text{Ba}(\text{Fe}, \text{Co})_2\text{As}_2$, possibly suggesting a common origin of the structural transition in both systems.

Figure 1 shows thermodynamic data of FeSe and, for comparison, of lightly co-substituted BaFe_2As_2 . A clear mean-field-like anomaly with $\Delta C_p/T_s \approx 5.5$ mJ mol⁻¹ K⁻² is observed at $T_s = 87$ K in the specific heat of FeSe. The discontinuity is similar in magnitude to the low-temperature Sommerfeld coefficient $\gamma_L = 5.7$ mJ mol⁻¹ K⁻², suggesting an electronic instability consistent with a recently observed reconstruction of the Fermi surface at T_s [16–18]. A similar steplike specific-heat anomaly is also seen at T_s of $\text{Ba}(\text{Fe}_{0.98}\text{Co}_{0.02})_2\text{As}_2$ [see inset in Fig. 1(a)], where T_s is well separated from T_N . The temperature dependence of the orthorhombic distortion $\delta = (a - b)/(a + b)$, derived from thermal-expansion data [9], [Fig. 1(b); a and b are the in-plane lattice constants of the orthorhombic unit cell] also provides a clear indication of the structural transition and is very similar to that of BaFe_2As_2 [9].

Shear-modulus measurements offer another powerful method for studying the structural transition [4,19–21]. If there is an electronic origin of the tetragonal-to-orthorhombic

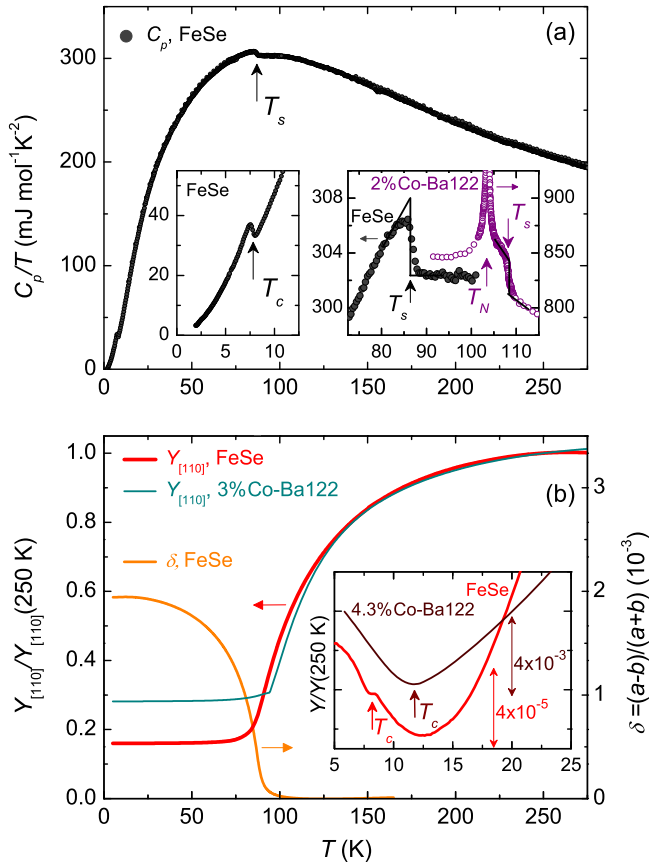


FIG. 1 (color online). (a) Specific heat C_p divided by T vs T of an FeSe single crystal. Insets show data around T_c and T_s on an enlarged scale revealing relatively sharp, mean-field-like transitions. Data for 2% Co-substituted BaFe₂As₂ are shown for comparison. (b) Young's modulus Y (left scale) and orthorhombic distortion δ (right scale) of FeSe single crystals vs T , compared with slightly underdoped Ba(Fe, Co)₂As₂. The inset shows data around T_c of FeSe and 4.3% Co-substituted BaFe₂As₂. Note the different vertical scales in the inset.

transition, it can phenomenologically be ascribed to the divergence of the susceptibility χ_φ of an electronic and, by symmetry, nematic order parameter φ , irrespective of its microscopic nature [22]. In this case, the Landau-type free energy is written as

$$F = \frac{1}{2}(\chi_\varphi)^{-1}\varphi^2 + \frac{B}{4}\varphi^4 + \frac{C_{66,0}}{2}\delta^2 - \lambda\varphi\delta, \quad (1)$$

with bilinear coupling, λ , between φ and the orthorhombic distortion δ , allowed by symmetry, and a bare shear modulus $C_{66,0}$. In consequence, the effective elastic shear modulus, given by

$$C_{66} = \frac{d^2F}{d\delta^2} = C_{66,0} - \lambda^2\chi_\varphi, \quad (2)$$

is determined by the ‘‘phenomenological’’ nematic susceptibility χ_φ and the coupling constant λ [4,21,23,24].

In Fig. 1(b), we show the Young modulus along the tetragonal [110] direction, $Y_{[110]}$, whose temperature dependence was previously shown to be dominated by C_{66} [21], of FeSe and Ba(Fe_{0.97}Co_{0.03})₂As₂, as measured in a three-point bending setup in a capacitance dilatometer [21]. The significant softening on approaching T_s from above is characteristic of the elastic soft mode, i.e., C_{66} [25,26]. Strikingly, this softening is practically identical in the two systems, which shows that $\lambda^2\chi_\varphi/C_{66,0}$ of FeSe is practically identical to that of Ba(Fe_{0.97}Co_{0.03})₂As₂, implying that the coupling between nematic order parameter and lattice $\lambda^2/C_{66,0}$ has nearly the same value in the two systems.

Below T_s , the Young modulus is nearly constant and does not show the increase expected for a second-order phase transition, presumably due to the formation of structural twins within the orthorhombic phase [27]. Nevertheless, small anomalies around T_c can still be resolved [see inset in Fig. 1(b)]. $Y_{[110]}$ of Ba(Fe_{0.957}Co_{0.043})₂As₂ ($T_c = 12$ K) hardens anomalously by $\sim 4 \times 10^{-3}$ below T_c , an effect previously observed in overdoped Ba(Fe, Co)₂As₂ [4,20] and interpreted as a consequence of the competition between magnetic fluctuations and superconductivity in the spin-nematic scenario [4]. In strong contrast, $Y_{[110]}$ of FeSe only shows a small steplike softening by $\Delta Y_{[110]} \approx 8.5 \times 10^{-6}$ at T_c . The steplike softening is the normal behavior expected at a superconducting transition and is related to the uniaxial pressure derivative of T_c and the specific-heat anomaly via a thermodynamic relation [28]. Importantly, the absence of any anomalous hardening of $Y_{[110]}$ related to T_c demonstrates again [9] that the orthorhombic phase and superconductivity do not compete in FeSe, as they do in substituted BaFe₂As₂ [4,20,21]. We note that $Y_{[110]}$ hardens slightly by $\sim 5 \times 10^{-5}$ below ~ 12.5 K $> T_c$, which correlates well with the anomalous thermal expansion below roughly the same temperature [9].

In order to investigate the microscopic physics, we have performed ⁷⁷Se NMR measurements on a collection of ~ 10 single crystals, aligned by eye, in a constant field of 9 T. ⁷⁷Se has a nuclear spin of $I = 1/2$ and therefore no quadrupolar interactions. The resonance lines in the NMR spectra, observed at a fixed frequency of $f = 73.28$ MHz, are very narrow with FWHM of only 5–8 kHz [Figs. 2(a) and 2(b)]. Interestingly, the resonance lines split below $T_s \sim 87$ –90 K under an in-plane field, which was confirmed by measurements on only one single crystal. Since NMR is a local probe, this clearly shows the existence of two types of domains having different Knight shift, or spectral shift, K in which the field is aligned parallel to either the orthorhombic a axis or the b axis. We arbitrarily assign the smaller K to domains with $H \parallel a$ (‘‘a’’) and the larger K to domains with $H \parallel b$ (‘‘b’’). Note that a similar observation was reported for LaFeAsO, but was attributed to quadrupolar effects [29].

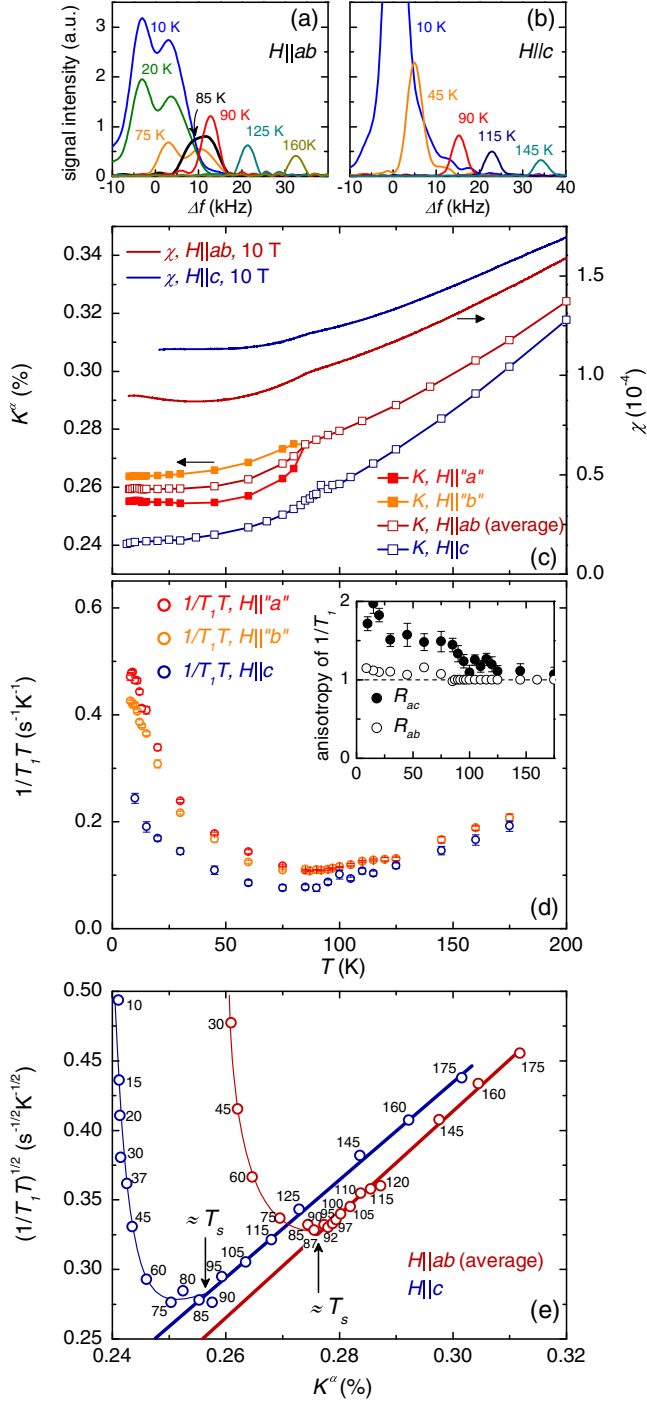


FIG. 2 (color online). (a),(b) NMR spectra of a collection of ~ 10 FeSe single crystals with field $H||ab$ and $H||c$, respectively, at $H = 9$ T. (c) K^α (left scale) and uniform magnetic susceptibility (right scale) for the indicated field directions. (d) $1/T_1T$ and its anisotropy with respect to the applied field $R_{ac} = [(1/T_1)_{H||"a"} + (1/T_1)_{H||"b"}]/2/(1/T_1)_{H||c}$ and $R_{ab} = (1/T_1)_{H||"a"}/(1/T_1)_{H||"b"}$ (inset). (e) Square root of $1/T_1T$ vs K^α with temperature as implicit parameter, indicated in units of K. Bold straight lines show a linear fit to the data for $T > T_s$, Eq. (3), deviations from which demonstrate the emergence of spin fluctuations. Thin lines are a guide to the eye. $K^\alpha(T_s)$ is indicated by vertical arrows.

Figure 2(c) shows K^α [$\alpha = (a, b, c)$] and the uniform magnetic susceptibility χ_α measured in a vibrating sample magnetometer at 10 T. The relatively strong temperature dependence of K and χ is presumably due to the small Fermi-surface pockets [30] found in FeSe [18,31,32]. In general, K is given by $K^\alpha = K_{\text{spin}}^\alpha + K_{\text{chem}}^\alpha$ with $K_{\text{spin}}^\alpha = A_{\text{hf}}^{\alpha\alpha} \chi_\alpha / N_A \mu_B$ and a temperature-independent chemical shift K_{chem}^α . $A_{\text{hf}}^{\alpha\alpha}$ is the relevant component of the hyperfine coupling tensor. Scaling of K^α and χ_α for $T > T_s$ yields $A_{\text{hf}}^{aa} = 2.49(1) \mu_B/T$ and $A_{\text{hf}}^{cc} = 3.77(4) \mu_B/T$.

Figure 2(d) shows the spin-lattice relaxation rate divided by T , $1/T_1T$ and Fig. 2(e) an analysis of its temperature dependence. The data agree qualitatively well with the early data by Imai *et al.* on polycrystalline samples [14]. Here, we study, in particular, the region around T_s and the magnetic-field anisotropy of $1/T_1$. In general, there are several contributions to $1/T_1$. For a Fermi liquid, the hyperfine coupling between nuclear spins and conduction electrons results in the Korringa contribution, following the relation

$$\left(\frac{1}{T_1T}\right)_{\text{FL}} \propto K_{\text{spin}}^2. \quad (3)$$

Fluctuating transverse magnetic fields provide an additional relaxation process, which adds to the total relaxation rate $1/T_1T = (1/T_1T)_{\text{FL}} + (1/T_1T)_{\text{sf}}$. In order to discriminate between these two contributions, we show in Fig. 2(e) $\sqrt{1/T_1T}$ plotted versus K^α with temperature as an implicit parameter. From Eq. (3), one would expect the data to fall on a straight line, which indeed holds for $T > T_s$. Importantly, deviations from the Korringa behavior, which signal the emergence of significant magnetic fluctuations, occur only below T_s .

Information about the nature of the magnetic fluctuations may be obtained from the field anisotropy of $1/T_1T$ within the orthorhombic phase. Namely, the *ab*-anisotropy ratio

$$R_{ab} = \frac{(1/T_1)_{H||"a"}}{(1/T_1)_{H||"b"}} \approx 1.1-1.2 \quad (T < T_s) \quad (4)$$

is found to be quite small and nearly temperature independent. The ratio of the in-plane average of $1/T_1$ and its *c*-axis value,

$$R_{ac} = \frac{[(1/T_1)_{H||"a"} + (1/T_1)_{H||"b"}]/2}{(1/T_1)_{H||c}}, \quad (5)$$

is $\sim 1.5-2$ at low T where spin fluctuations dominate $1/T_1$. These results are in strong contrast to LaFeAsO, where R_{ab} nearly doubles [29] and R_{ac} increases strongly from ≈ 1.5 to ≈ 3 [33] on decreasing T between T_s and T_N . The former observation has been taken as a characteristic of the spin-nematic state, in which spin fluctuations are at the origin of

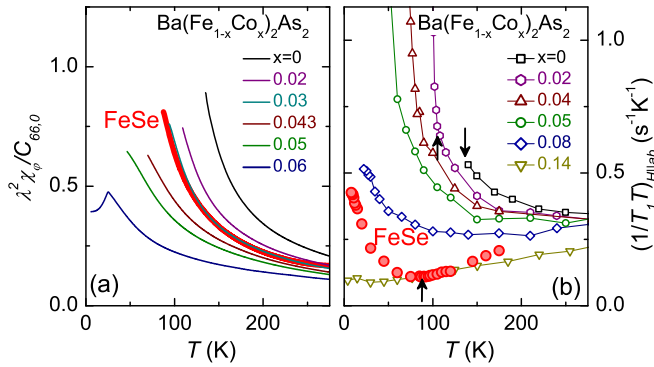


FIG. 3 (color online). (a) Normalized nematic susceptibility $\lambda^2\chi_\phi/C_{66,0} = 1 - C_{66}/C_{66,0}$ of FeSe and $\text{Ba}(\text{Fe}, \text{Co})_2\text{As}_2$ (from Ref. [21]). Data on FeSe are found to be practically identical to $\text{Ba}(\text{Fe}, \text{Co})_2\text{As}_2$ with the same T_s . (b) $1/T_1T$ of FeSe and $\text{Ba}(\text{Fe}, \text{Co})_2\text{As}_2$ (from Refs. [35,36]) in in-plane field, demonstrating very distinct behavior in the two systems. Arrows mark T_s of BaFe_2As_2 , $\text{Ba}(\text{Fe}_{0.98}\text{Co}_{0.02})_2\text{As}_2$, and FeSe.

ab anisotropy [29]. The small value of R_{ab} in FeSe hence suggests that a possible spin-nematic state at low T in FeSe is much weaker than in LaFeAsO just above T_N .

Figure 3 summarizes our results concerning the phenomenological nematic susceptibility χ_ϕ , derived from the Young-modulus data [34] and $1/T_1T$, which are closely related in the spin-nematic scenario [6,7]. Remarkably, $\lambda^2\chi_\phi/C_{66,0}$ of FeSe fits very well into the $\text{Ba}(\text{Fe}, \text{Co})_2\text{As}_2$ series [Fig. 3(a)], showing that the nematic susceptibility and the electron-lattice coupling are very similar, as already argued above. The temperature dependence of $1/T_1T$ of FeSe, on the other hand, clearly does not fit into the $\text{Ba}(\text{Fe}, \text{Co})_2\text{As}_2$ series [Fig. 3(b)]. In particular, the large spin-fluctuation contribution to $1/T_1T$, observed up to room temperature in lightly doped $\text{Ba}(\text{Fe}, \text{Co})_2\text{As}_2$ [35], is not found in the FeSe data. Our results for FeSe therefore put the spin-nematic scenario, in which the lattice softening is the result of increased spin fluctuations [4,6,7], into question, even if the scaling of C_{66} and T_1 of Ref. [7] needs not be strictly valid if T_N is not finite [7].

The NMR relaxation data show that the onset of magnetic fluctuations coincides approximately with T_s and that FeSe appears to be close to a magnetic instability at low temperatures. The result seems to suggest that the structural transition triggers the emergence of magnetism. This, however, does not hold under hydrostatic pressure, where spin fluctuations are enhanced [14], while T_s is rapidly suppressed [37]. Possibly, FeSe tends to a tetragonal-type magnetic order, which naturally would not couple strongly to the orthorhombic distortion, as is also suggested by the magnetic-field anisotropy of $1/T_1T$. A magnetic state within a quasitetragonal structure has, for example, been observed in Na-substituted BaFe_2As_2 [38,39].

In summary, we have shown that FeSe exhibits a surprisingly similar shear-modulus softening as found in the 122 compounds, suggesting a common origin of the

structural transition in these systems. In FeSe, spin fluctuations emerge only below T_s and are therefore argued not to be the driving force of its structural transition. This leaves orbital ordering as a possible driving force and, in fact, ARPES measurements [16,18] find evidence for the orbital ordering scenario. Namely, a strong orbital anisotropy, which is greater than expected from the small structural distortion δ alone, is observed below T_s . Finally, our results naturally raise the question of the origin of superconductivity in FeSe, since both orbital and magnetic fluctuations have been considered as a pairing glue for superconductivity in the iron-based materials. If superconductivity were mediated by orbital fluctuations, one might expect a strong coupling between δ , C_{66} , and T_c , which is, however, not observed. Spin fluctuations, on the other hand, may be candidates to mediate superconductivity, which is also suggested by their close correlation with T_c under pressure [14]. They appear not to be of the typical stripe-type nature and, thus, not strongly coupled to the structural distortion. Inelastic neutron scattering would be useful in order to clarify the exact nature of the incipient magnetism in FeSe.

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Note added.—After submission of our manuscript an NMR study of single-crystalline FeSe, consistent with our results, was published by Baek et al. [42].

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