Experimental and numerical investigation of screening currents induced in Bi-2223/Ag double pancake coil for space applications

Y Nagasaki1, T Nakamura2, I Funaki3, Y Ashida1 and H Yamakawa1

1 Research Institute of Sustainable Humanosphere, Kyoto University, Gokasho, Uji, Kyoto 611-0011, Japan
2 Graduate School of Engineering, Kyoto University, Kyotodaigakukatsura, Nishikyo, Kyoto 615-8510, Japan
3 Institute of Space and Astronautical Science, Japan Aerospace Exploration Agency, Sagamihara, Kanagawa 252-5210, Japan

E-mail: nagasaki@rish.kyoto-u.ac.jp

Abstract. We modelled screening currents (I_s) induced in high-temperature superconducting (HTS) coils to develop a method for the characterization and design of HTS magnets for space applications. The analysis made use of the so-called percolation depinning and flux creep models to describe the current density versus electric field in HTS tapes. We compared model results with experimental data obtained from a Bi-2223/Ag double pancake coil. The experimental residual magnetization due to I_s in the Bi-2223/Ag coil can be effectively modelled assuming an equivalent loop length of approximately 9 mm for I_s in the coil. The values calculated from the method quantitatively agreed with the results for various experimental conditions. We also successfully modelled the hysteresis of the magnetization due to I_s. These results demonstrate the validity of our model for I_s, which considers the effects of flux creep and smaller I_s loops in the multi-filamentary Bi-2223/Ag tape.

1. Introduction

There is much interest in developing high-temperature superconducting (HTS) coils for space applications [1], such as for a magnetic sail and electric propulsion. The space propulsion systems with HTS coils can have more thrust, since HTS coils weigh less, use less power and produce larger magnetic fields [2–9] than non-HTS coils. Since the acceleration of a magnetic sail is proportional to the magnetic moment/mass ratio of the installed coil, our purpose is to develop a light-weight HTS coil system with a higher magnetic moment, radiative and/or conductive cooling and light-weight DC/DC converters for the regulation of power supply in a spacecraft. A detailed explanation of the propulsion mechanism of a magnetic sail has been given by Yamakawa et al [5].

Space missions attach great importance to the reliability of instruments installed in a spacecraft. For HTS coils, great care is needed to avoid coil quench in space. To that end, we previously developed a thermo-electromagnetic field analysis method [10] that can evaluate the thermal stability of the HTS coil. The analysis is based on the so-called percolation depinning model [11], which can quantitatively express the current density versus electric field in HTS tapes as a function of temperature and magnetic field vector.

However, one potential problem can arise from AC ripples in the output current of the DC/DC converter, which could generate screening currents (I_s) and AC losses in the HTS coil. Since a spacecraft cannot be equipped with any refrigerants, mostly because of mass considerations, the AC loss could become a serious problem for the reliability of an HTS coil. Moreover, the induced I_s could have large effects on the magnetic field distribution and current transport characteristics of the HTS coil itself [12–15]. These effects must be estimated to design optimal HTS coil systems for space missions. In addition, understanding I_s is highly important for terrestrial applications, e.g. magnetic resonance imaging, nuclear magnetic resonance imaging and cyclotrons, which require stable magnetic fields [12–15].
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In this study, we investigated a Bi-2223/Ag coil, which is a candidate for magnetic sail spacecraft [10]. It has been reported that multi-filamentary Bi-2223/Ag tapes have superconducting connections (bridging) between neighbouring filaments [16–21]. The filament bridging can have effects on the loop length and inductance of \( I_s \) in the coil, and as a result, the AC loss and magnetic field distribution generated by the coil itself. Koyama et al. reported that due to the filament bridging, flux creep was a dominant factor for \( I_s \) induced in a Bi-2223/Ag coil [22]. To analyse the AC loss, magnetic field distribution and optimal design for the Bi-2223/Ag coil, it is essential to develop an analytical method that considers flux creep and understands how \( I_s \) is induced in the Bi-2223/Ag coil.

To evaluate the AC loss and magnetic field distribution of HTS coils accurately, we developed an analytical method to investigate \( I_s \) in a Bi-2223/Ag coil that considers the effect of flux creep. We validated the method by comparing calculated results to measured magnetic fields generated by \( I_s \).

| Table 1. Specifications of the Bi-2223/Ag coil and tape. |
|----------------|------------------|
| Items          | Scaled-down model coil [10] |
| Shape          | Double pancake coil |
| Turn number    | 130 Layer × 2 Stack |
| Inner diameter | 0.200 m           |
| Outer diameter | 0.274 m           |
| Tape width     | 4.2 mm            |
| Tape thickness | 0.28 mm           |
| Tape length    | 200 m             |
| Critical current \( I_{c\text{min}} \) of the coil | 200 A (50 K, \( E_{\text{max}} \): 1 μV/cm) |

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2. Experimental Method

2.1 Scaled-down model coil

As a scaled-down model for space applications, a double pancake coil was fabricated with a Bi-2223/Ag tape of 200 m length and was set at the second cold-stage in a conduction-cooled experimental system [10], as depicted in figure 1. The specifications of the coil are shown in table 1, and current, \( I_{\text{op}} \), versus voltage, \( V \), for the coil are shown in figure 2; we obtained these values in a previous study [10]. The minimum critical current, \( I_{c\text{min}} \), of the coil at 50 K was about 200 A (maximum electric field, \( E_{\text{max}} \), in the coil was 1 μV/cm at 200 A in self-field).

2.2 Experimental procedure

To investigate \( I_s \) induced in the coil during the coil excitation, we measured the axial magnetic fields generated by \( I_s \) with Hall sensors. The Hall sensors were installed at (I) the centre and (II) the top surface of the coil, as shown in figure 1. The residual magnetic fields due to \( I_s \) were obtained by subtracting the fields for the transport current (e.g. 1.17 mT/A at the centre of the coil, calculated by the integration of the Biot–Savart law without any screening currents) from the measured values. We measured the loop inductance and magnitude of \( I_s \) in the Bi-2223/Ag coil and compared them with the analytical results from the model.

To evaluate the inductance and loop length of \( I_s \), the decay time constant, \( \tau \), was estimated. We measured the decay behaviour of the magnetic field due to \( I_s \) by pausing the increase of the operational current, \( I_{\text{op}} \), for several times during the excitation of the coil up to 200 A. The measurements were conducted under various conditions: at different temperatures from 4 to 50 K and with different sweep rates from 40 to 80 A/min.
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To investigate the maximum ratio of the magnetic fields from $I_s$ to those from the coil current, the hysteresis loops of the magnetization during charging and discharging of the coil were measured. The transport current was applied up and down to ±200 A at 50 K with a 40 A/min sweep rate.

3. Analytical Model

We enhanced a thermo-electromagnetic field analysis method [10] by including the effects of flux flow and flux creep on $I_s$ induced in HTS coils. Figure 3 shows the analysis model of the Bi-2223/Ag double pancake coil, whose features are described in table 1. $I_s$ is induced by the temporal variation of the self-magnetic field, $B_r$, during the coil excitation and flow between filaments via the filament interconnections or silver sheath in the Bi-2223/Ag tape. We assumed $I_s$ is induced by a single equivalent loop length, $l$, along the tape in the coil, as shown in figure 3. $I_s$ was analysed using Faraday’s law, the percolation depinning model, the flux creep model and the equivalent circuit of the HTS coil.

The electric field, $E_s$, induced by the temporal variation of the radial component of $B_r$ linked with the operational current, $I_{op}$, and $I_s$ is expressed as follows:

$$\nabla \times E_s = -\frac{\partial B_r}{\partial t}. \tag{1}$$

$B_r$, at each time, $t$, is calculated using the Biot–Savart law. Based on the percolation depinning model, the current density, $J$, versus the electric field, $E$, due to the flux flow relationship in HTS tapes can be described as a function of temperature, $T$, magnetic field and its applied angle [23–26] [equation (2)], where $\rho_{FF}$ is the resistivity for uniform flux flow; $J_{cm}$, $J_0$ and $m$ denote the minimum value, the scaling factor and the statistical parameter characterizing the shape of the local critical current density distribution, respectively, and $B_{eq}$ denotes the equivalent perpendicular magnetic flux density, which describes the magnetic field anisotropy of HTS tapes [26].

Considering the influence of thermally activated vortex hopping, i.e. flux creep, the relationship between $J$ and $E$, especially in a lower load factor region, can be written as follows [24]:

$$E_{fc} = \begin{cases} E_{0}\exp\left[-\frac{U(j)}{kT}\right] & \text{for } J < J_c, \\ E_{0}\left[1 - \exp\left(-\frac{\pi U_{eff}}{kT}\right)\right] & \text{for } J \geq J_c, \end{cases} \tag{3}$$

where $U(j) = U_0 \left[1 - j^2 \right]^{1/2} - j \cos j$, $E_{0} = B a v_0$ and $j = J / J_c$. $a_1$ is the flux line lattice spacing, $v_0$ is the attempt frequency, $U_0$ is the height of the pinning potential for $j = 0$ and $k$ is the Boltzmann constant. The total electric field from the flux flow and the flux creep can be calculated as the sum of the electric fields obtained from (2) and (3): $E(J) = E_{FF}(J) + E_{fc}(J)$ [27].

Figure 4 illustrates the equivalent circuit of the HTS coil. $I_s$ can be obtained by satisfying the following equation:

$$J = \begin{cases} J_{cm}(T, B_{eq}) + \left(\frac{m + 1}{\rho_{FF}} E_{11} J_0(T, B_{eq})^n\right)^{1/n+1} & \text{for } J_{cm} \geq 0, \\ -J_{cm}(T, B_{eq}) + \left(\frac{m + 1}{\rho_{FF}} E_{11} J_0(T, B_{eq})^n + \left[J_{cm}(T, B_{eq})\right]^{1/n+1}\right) & \text{for } J_{cm} < 0. \tag{2} \end{cases}$$
4. Results and Discussion

4.1 Decay behaviour of $I_s$ in the Bi-2223/Ag coil

We first measured the decay behaviour of $I_s$ with long-term operation of the coil. Figure 5 shows the experimental result of the temporal variation of the residual magnetization due to $I_s$, which was obtained by subtracting the magnetic field generated by the coil current from the measured one at Hall sensor (I). In this experiment, we increased $I_{op}$ from 0 to 80 A at a rate of 40 A/min. At 80 A ($t = 0$ in figure 5), $I_{op}$ was fixed and the decay of the magnetization was measured. A typical logarithmic decay in the magnetization is shown by a dashed line in figure 5. This result indicates that the decay behaviour of $I_s$ in the Bi-2223/Ag coil is controlled by flux creep, as discussed by Koyama et al. [22] and Pust [29]. The result also suggests that much of $I_s$ flows as persistent currents via the filament interconnections in the Bi-2223/Ag coil without any normal resistance [22]. Conversely, the rapid decay of the magnetization at $t < 3$ s in figure 5 suggests that some $I_s$ in the Bi-2223/Ag coil flow across the silver sheath and rapidly disappear due to the resistance, $R_N$, of the silver sheath, as suggested by Koyama et al [22]. Approximately 46% of the magnetic field generated by $I_s$ rapidly diminished at $t < 3$ s. Because of this decay behaviour, we continued to consider both the flux creep and the silver sheath resistance in our analysis of $I_s$ in the coil, as described in section 3.

As mentioned in section 2.2, we investigated the inductance and loop length, $l$, of $I_s$ induced in the Bi-2223/Ag coil. We measured the decay time constant, $\tau$, of the magnetic field generated by $I_s$ due to the normal resistance, $R_N$, and fitted the model result to the measured one. The fitting parameter was $l$ for $I_s$ in the Bi-2223/Ag tape. The corresponding inductance, $L_s$, was obtained by calculating $B_r$ from only $l$ of the loop itself and $\tau = L_s/R_N$.

Figure 6(a) shows the temporal variation of the experimental residual magnetization due to $I_s$ at Hall sensor (I). $I_{op}$ and $T$ were 80 A and 50 K, respectively. The experimental results (solid circles) indicate that the magnetic field from $I_{op}$ for various load factors, $I_{op}/I_{cmin}$, for the HTS coil, $I_{op}$ was increased up to the minimum critical current, $I_{cmin} = 200$ A (when $E_{max} = 1.0$ μV/cm), with a fixed 40 A/min sweep rate and $T = 50$ K, and the magnetic field was measured every 0.5 s. The experimental results (solid circles) indicate that the magnetic field from $I_s$ drastically decreased under constant current conditions with no induced electric field due to $E_c$. In addition, the decay ratio and $\tau$ of the magnetic field slightly decreased with increasing load factor, i.e. increasing resistance of the HTS tape, $R_{HTS}$. The fact that this rapid decay was observed even at an extremely low load factor, i.e. at a no flux flow region, suggests that the decay is caused mainly by the influence of $R_N$ and the flux creep, as in the case shown in figure 5. At $I_{op} = 20$ A, for example, $\tau$ of $I_s$ is estimated to be approximately 0.9 s.

Figure 6(b) and table 2 depict the model fitting results assuming various values for $l$ for $I_s$. The maximum value and decay time constant of the magnetic field for each $l$ are shown in table 2. Considering the standard deviation of the measurements, the experimental results can be successfully modelled using $l = 0 \pm 3$ mm. This value of $l$ is of the same order as the length of the filament bridging in a Bi-2223/Ag tape of approximately 5 mm,
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This may imply that $I_s$ flows through the filament bridging in the Bi-2223/Ag tape, as discussed for the results of figure 5. In addition, these results suggest that in Bi-2223/Ag tape, $I_s$ is induced in smaller current loops compared to those in RE-system-coated conductors, such as GdBa2Cu3O7 tapes.

The analytical results in figure 6(b) and table 2 also show the tendency of the smaller $I_s$ loops to generate smaller magnetic fields. This result derives from the fact that in the case of a smaller loop, the maximum value of $I_s$ becomes lower because of the smaller loop area and smaller $E_s$ in (4). Consequently, $I_s$ induced in Bi-2223/Ag tape with smaller loops due to the effect of the...
filament bridging has less effect on the magnetic field distribution from the coil current than $I_s$ in a coated conductor.

4.2 Effect of sweep rate and $T$

We also conducted experiments and analyses with varying sweep rates and $T$, examples of which are shown in figure 7. The horizontal axis is $I_{op}$ in figure 7(a) and time in figure 7(b). The modelling for both figures assumes $l = 9$ mm. In figure 7(a), with increasing sweep rate, the temporal variation ratio of $B_r$ and $E_s$ increase, and as a result, the maximum value of the induced $I_s$ increases according to (4). In the case of figure 7(b), with a decrease in $T$, $R_N$ of the silver sheath decreases [28], and as a result, the maximum value and time constant, $\tau = L_s/R_N$, of $I_s$ increases according to (4). These tendencies can be seen in the experimental results in figure 7 and can be modelled assuming $l = 9$ mm. This result indicates that the maximum value of $I_s$ and its time constant in the Bi-2223/Ag coil are affected by the operational conditions of the coil and can be well described by the model.

4.3 Hysteresis effect of the magnetization due to $I_s$

As mentioned in section 2.2, we measured the hysteresis of the magnetic field generated by $I_s$, and investigated the maximum ratio of the induced magnetic field to that of the coil current itself. Figure 8 illustrates the experimental data and the modelling of the magnetization due to $I_s$ at Hall sensors (I) and (II). The measured data are the solid circles, and the polarity of the hysteresis loops is dependent on the position of the sensor relative to the coil [22]. $I_s$ in the coil tends to saturate at specific values in a higher load factor region due to the increasing resistance of the HTS tape, $R_{HTS}$. Since the sweep rate of 40 A/min, which corresponds to 46 mT/min at Hall sensor (I), is much higher than $\tau$ due to the flux creep, which is of the order of nT/min–μT/min, the decay effect due to flux creep is not detected in these hysteresis curves. The saturation values at the Hall sensors are (I) $-2.85$ mT and (II) 9.6 mT, which are only 1.2% and 1.8% of the magnetic field from $I_{op}$, respectively.

The modelling of the hysteresis loops are depicted in figure 8 as lines. We used $l = 9$ mm, as estimated in the previous section, and $l = 100$ mm for $I_s$. As shown in the figures, the modelling assuming $l = 9$ mm agrees well with the experimental data. These results also support the validity of the developed model, and suggest that $l$ for $I_s$ in the Bi-2223/Ag coil can be assumed as approximately 9 mm, which agrees well with the bridging length of the filament in the Bi-2223/Ag tape.

As also shown in figure 8, the saturation values of the magnetic field due to $I_s$ greatly increase with the increasing loop length of $I_s$. This result indicates that the amount of the influence of $I_s$ on the magnetic field generated by $I_{op}$ depends on the loop length of $I_s$ in the coil. Our model considering the loop length of $I_s$ is surely helpful to estimate the effect of $I_s$ on the magnetic field from $I_{op}$, which is directly related to the propulsive force of the magnetic sail. Our future work is to enhance the model in order to clarify the effect of the loop length of $I_s$ on AC loss in HTS coils for space applications.

The developed model can also be applied to a coil made from RE-system-coated conductors. In this type of coil, a more complicated screening current will flow in the thin film superconducting area, and the influence of such a current upon the residual magnetic field will be a
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5. Conclusion
To characterise and design optimal HTS coils for space missions, we developed a numerical analysis method based on the percolation depinning and the flux creep models, considering screening currents, $I_s$, induced in the coil. In this study, $I_s$ induced in a Bi-2223/Ag double pancake coil was investigated and modelled. We measured the decay behaviour of the magnetic field due to $I_s$ and then modelled the results assuming an equivalent loop length, $l$, for $I_s$ in the coil. The experimental and analytical results suggest that the decay behaviour of $I_s$ in the Bi-2223/Ag tape was dominated by the silver sheath resistance and the flux creep, especially at a lower load factor. In addition, the experimental results under varying conditions could be quantitatively modelled assuming an equivalent $l$ of approximately 9 mm for $I_s$ in the coil. The good agreement between the measurements and the analyses proved the validity of our model, which considered the effects of the flux flow and flux creep on $I_s$ induced in the HTS coil. The precise identification of the mechanism for the smaller loops of $I_s$ and the effects of such loops on AC loss in the coil for space applications is our future work.

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