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Kyoto University
Odd-parity superconductivity by competing spin-orbit coupling and orbital effect in artificial heterostructures

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We show that odd-parity superconductivity occurs in multilayer Rashba systems without requiring spin-triplet Cooper pairs. A pairing interaction in the spin-singlet channel stabilizes the odd-parity pair-density-wave (PDW) state in the magnetic field parallel to the two-dimensional conducting plane. It is shown that the layer-dependent Rashba spin-orbit coupling and the orbital effect play essential roles for the PDW state in binary and tricolor heterostructures. We demonstrate that the odd-parity PDW state is a symmetry-protected topological superconducting state characterized by the one-dimensional winding number in the symmetry class $BDI$. The superconductivity in the artificial heavy-fermion superlattice CeCoIn$_5$/YbCoIn$_5$ and bilayer interface SrTiO$_3$/LaAlO$_3$ is discussed.

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I. INTRODUCTION

Parity is an essential quantum number of quantum phases unless inversion symmetry is broken. Classification of superconducting states is based on the parity of the order parameter [1]. According to the conventional understanding [1], even-parity superconductivity is realized by the condensation of spin-singlet Cooper pairs, while odd-parity superconductivity is induced by spin-triplet Cooper pairs because of the anticommutation relation of fermions. Even-parity superconductivity has been observed in a variety of materials, e.g., archetypal strongly correlated electron systems such as high-$T_c$ cuprate superconductors (SCs) [2,3] as well as conventional SCs stabilized by electron-phonon coupling. On the other hand, only a few materials are considered as possible hosts of odd-parity superconductivity. This is probably because the conditions for spin-triplet pairing are unfavorable in most materials. Since electron-phonon coupling mostly stabilizes spin-singlet $s$-wave superconductivity, strong electron correlation is required for the glues of spin-triplet Cooper pairs. However, $d$-wave superconductivity is stable in most strongly correlated electron systems [4].

Odd-parity superconductivity has been attracting attention because of its multicomponent order parameters that give rise to multiple superconducting/superfluid phases and intriguing phenomena related to spontaneous symmetry breaking [1,5–9]. Furthermore, a great deal of attention has recently been paid to odd-parity SCs because they are candidates for topological superconductivity [10–15]. However, only Sr$_2$RuO$_4$ [8,9] and some uranium-based heavy-fermion compounds such as UPt$_3$ [6,7], UGe$_2$ [16], URhGe, and UCoGe [17,18] show strong evidence for spin-triplet pairing.

Recent theoretical studies have presented another way to stabilize the odd-parity superconducting state. It has been shown that odd-parity superconductivity may occur through spin-singlet Cooper pairs in crystals lacking local inversion symmetry. Such locally noncentrosymmetric crystals have a sublattice degree of freedom in electronic structures, allowing the odd-parity spin-singlet superconducting state [19,20]. Although this state is not allowed in the absence of spin-orbit coupling according to the BCS theory, such an exotic superconducting state may be stabilized by the sublattice-dependent spin-orbit coupling arising from the relativistic effect [20]. It has been shown that a long-range Coulomb interaction stabilizes odd-parity superconductivity in combination with spin-orbit coupling [21,22]. On the other hand, two of the authors have shown that the odd-parity spin-singlet superconducting state is stabilized by spin-orbit coupling and the paramagnetic effect without relying on the particular electron correlation effect [23]. Therefore, conventional electron-phonon coupling or antiferromagnetic spin fluctuation leading to spin-singlet Cooper pairing may induce odd-parity superconductivity when both spin-orbit coupling and the paramagnetic effect play important roles.

In a previous study, we focused on two-dimensional (2D) multilayer SCs in which global inversion symmetry is preserved but some of the layers lack local inversion symmetry. Then, by applying a magnetic field along the $c$ axis, the order parameter of spin-singlet superconductivity changes sign across the center layer, as shown in Fig. 1(a) [23]. The order parameter spatially modulated in the atomic length scale ensures the odd parity of superconductivity. Such a superconducting state is called the pair-density-wave (PDW) state. Interestingly, the PDW state is classified into topological crystalline superconductivity protected by mirror reflection symmetry when the number of superconducting layers is odd [24]. A nontrivial topological invariant in the symmetry class $D$, the mirror Chern number ensures the appearance of the Majorana edge mode at the edge. A promising candidate for realizing such a topological superconducting state is the recently grown artificial superlattice CeCoIn$_5$/YbCoIn$_5$ composed of the quasi-2D heavy-fermion SC CeCoIn$_5$ and the conventional metal YbCoIn$_5$ [25]. The superconductivity occurs in CeCoIn$_5$ multilayers, and YbCoIn$_5$ plays the role of spacer layers. Thus, the superlattice is regarded as a 2D multilayer SC when the number of YbCoIn$_5$ layers is large. The strong spin-orbit coupling and the large paramagnetic...
maintained by solving the linearized mean-field equation are introduced. We introduce the model for multilayer SCs possessing the topological invariant, i.e., the one-dimensional winding number in the symmetry class $BDI$. We will show a nontrivial $BDI$.

FIG. 1. (Color online) Illustration of superlattice structures studied in this paper. We show examples of the trilayer system ($M = 3$). (a) Binary superlattice that has been realized in CeCoIn$_5$/YbCoIn$_5$. Closed (blue) and open (red) circles show the superconducting layers and spacer layers, respectively. The layer-dependent order parameters in the BCS and PDW states are described on the left. (c) Tricolor superlattice. Thick (red) and thin (green) open circles show the two kinds of spacer layers.

The organization of this paper is as follows. In Sec. II we introduce the model for multilayer SCs possessing the layer-dependent RSOC. Various superconducting states obtained by solving the linearized mean-field equation are illustrated. We study the binary superlattices in Sec. III and discuss the superconducting states in the artificial superlattice CeCoIn$_5$/YbCoIn$_5$. The tricolor superlattice in Fig. 1(b) is also investigated in Sec. IV. In Secs. III and IV, it is shown that the odd-parity PDW state is stabilized through the RSOC and the orbital effect. In Sec. V, the topologically nontrivial properties of the PDW state are clarified, and the Majorana edge state is demonstrated. A brief summary and discussions are provided in Sec. VI.

II. MODEL AND FORMULATION
A. Model

First, we introduce the model for 2D multilayer SCs. By simply neglecting the spacer layers, the binary and tricolor superlattices in Fig. 1 are described by the multilayer model. By taking into account the layer-dependent RSOC, the orbital effect, and Zeeman coupling, the Hamiltonian is described as

$$
\mathcal{H} = \sum_{k,k',m,m'} \xi(k + p_m) c_{k,m}^\dagger c_{k',m'} + t_\perp \sum_{k,k',[m,m']} c_{k,m}^\dagger c_{k',m'}
\quad + \sum_{k,k',q,m} V(k,k') c_{k,m}^\dagger c_{k',m-q} + \sum_{k,k',s,m} \mu_B H \cdot \sigma \sigma_{k,m}^\dagger c_{k,m}
\quad + \sum_{k,k',s,m} g(k + p_m) \cdot \sigma \sigma_{k,m}^\dagger c_{k,m},
$$

(1)

where $k$, $s$, and $m (=1, \ldots, M)$ are indexes of momentum, spin, and layer, respectively. The number of superconducting layers is $M$.

The first term is the energy dispersion in the single-layer limit. We adopt the nearest-neighbor hopping term in the square lattice for simplicity,

$$
\xi(k) = -2t(\cos k_x a + \cos k_y a) - \mu,
$$

(2)

where $a$ is the lattice constant. The orbital effect induced by the applied magnetic field is taken into account through the Peierls phase. When we consider the magnetic field along the [100] axis, $H = H \hat{x}$, we can choose the vector potential $A = (0, -H z, 0)$. Then, the orbital effect leads to the layer-dependent shift of momentum, $k \rightarrow k + \frac{\pi}{a} \hat{x}$. Thus, we obtain $p_m = \vec{H} d[m - (M + 1)/2]$, where $d$ is the lattice spacing between the nearest-neighbor superconducting layers. For binary superlattices, $d = c$, with $c$ being the lattice constant along the $c$ axis. Later we adopt the lattice constant of CeCoIn$_5$, $a = 4.6$ Å, and $c = 7.5$ Å since we focus on the artificial superlattice CeCoIn$_5$/YbCoIn$_5$ [25]. The second term of Eq. (1) is the interlayer hopping term. Since we consider the heterostructures composed of quasi-2D SCs, the interlayer hopping $t_\perp$ is assumed to be much smaller than the in-plane hopping, $t_\perp \ll t$.

The third term describes the pairing interaction. We assume $s$-wave superconductivity for simplicity, and thus

$$
V(k,k') = -V_s.
$$

(3)

We have confirmed that qualitatively the same results are obtained for $d$-wave superconductivity. As we will show later, a spatially nonuniform superconducting state may be stabilized. Thus, we take into account the finite center-of-mass momentum of Cooper pairs $q$, and $k_\pm = k \pm q/2$. The
fourth term is the Zeeman coupling term giving rise to the paramagnetic effect on the superconducting state.

We show that exotic superconducting states are stabilized by the layer-dependent RSOC represented in the last term of Eq. (1), which arises from the local violation of inversion symmetry [20]. Ensured by the global inversion symmetry in the crystal structure, the RSOC is odd with respect to the mirror reflection on the center layer, and thus $a_{M-I-m} = -a_m$. For example, the layer-dependent coupling constant is $(a_1, a_2) = (a, -a)$ for bilayers and $(a_1, a_2, a_3) = (a, 0, -a)$ for trilayers. We assume a $g$-vector characterizing the RSOC [32], $g(k) = (-\sin k_a, \sin k_a, 0)$, so as to satisfy the periodicity in momentum space.

For bilayers, a similar model has been investigated by noticing the twin boundary of noncentrosymmetric SCs [33–36]. Then, the intriguing superconducting phase with broken time-reversal symmetry was investigated by assuming comparable pairing interactions for the spin-singlet Cooper pairs and spin-triplet ones [33–35]. We avoid such fine-tuning of pairing interactions here and consider the dominantly spin-state that is the focus of this paper is not obtained.

As shown by previous studies [20, 23, 31], exotic superconducting states near the transition temperature by otherwise. As shown by previous studies [20, 23, 31], exotic superconducting states near the transition temperature by otherwise.

We study the superconducting state by means of the linearized BdG equation. As we will show later, various superconducting states may be stabilized when the center-of-mass momentum of Cooper pairs is finite. It is expected that the double-$q$ state is stable in our model because the order parameter almost disappears in one of the outermost layers in the single-$q$ state with a small condensation energy. For instance, $\Delta_m \ll \Delta_1$ for momentum $q$ while $\Delta_1 \ll \Delta_M$ for the opposite momentum $-q$. In the double-$q$ state, the order parameter is described as $\Delta_m(r) = \Delta_m^+ e^{iq r} + \Delta_m^- e^{-iq r}$, where $\Delta_m^\pm$ is the eigenvector of $V_n \tilde{\chi}_0(q)$ for the momentum $\pm q$, respectively. We confirmed that the bosonic Matsubara frequency is always zero, $\Omega_n = 0$. 

C. Superconducting states

In this subsection, we classify the solution of the linearized BdG equation. As we will show later, various superconducting states are stabilized in our model. They are illustrated for the bilayer system in Fig. 2. We discuss the bilayer system for simplicity, since the extension to more-than-two-layer systems is straightforward.

The uniform superconducting state [$\Delta_m(r) = \Delta_m^\pm$] is stable at zero magnetic field as expected from conventional BCS theory. Thus, we call the uniform state the “BCS state” [Fig. 2(a)]. On the other hand, the vortex state or the double-$q$ state may be stabilized when the center-of-mass momentum of Cooper pairs is finite.
the other hand, a variety of spatially nonuniform states may be stabilized in the magnetic field. First, the orbital effect induces the vortex state illustrated in Fig. 2(b). When the quantum vortices penetrate through multilayers, the order parameter is described as

$$\Delta_1(\mathbf{r}) = \Delta_0(e^{-i\mathbf{q}\cdot\mathbf{r}} + \delta e^{i\mathbf{q}\cdot\mathbf{r}}),$$  \hspace{1cm} (8)

$$\Delta_2(\mathbf{r}) = \Delta_0(\delta e^{-i\mathbf{q}\cdot\mathbf{r}} + e^{i\mathbf{q}\cdot\mathbf{r}}),$$  \hspace{1cm} (9)

where $|\delta| < 1$, and $\mathbf{q} = q(\hat{x} \times \hat{H})$ with $\hat{H} = H/|H|$ and $q > 0$. Second, the layer-dependent RSOC stabilizes the CS state through the paramagnetic effect [31]. The CS state is also described by Eqs. (8) and (9), however the sign of the center-of-mass momentum $\alpha$ depends on the band structure and the sign of RSOC. For our choice of parameters, the RSOC favors $q < 0$ when $\alpha > 0$ while $q > 0$ when $\alpha < 0$. Thus, the CS state is regarded as an antivortex state [Fig. 2(c)] and is distinguished from the vortex state when $\alpha > 0$. Then the spin-orbit coupling competes with the orbital effect and gives rise to an intriguing superconducting phase diagram, as we show later. We focus on this case in the following, although the other case, $\alpha < 0$, is briefly discussed.

Finally, Fig. 2(d) illustrates the PDW state, where $[\Delta_1(\mathbf{r}), \Delta_2(\mathbf{r})] = (\Delta, -\Delta)$ [23]. The order parameter is uniform in the 2D conducting plane, but it changes sign between layers. As we mentioned before, the PDW state is an odd-parity superconducting state, although the superconductivity is induced by the spin-singlet $s$-wave Cooper pairs. Although we have shown that the PDW state is stabilized in the c-axis magnetic field near the Pauli limit [23], in this paper we show that the PDW state is also stabilized in the in-plane magnetic field when the RSOC competes with the orbital effect.

The BCS, PDW, vortex, and CS states are distinguished from each other in more-than-two-layer systems too. In Table I, we summarize the order parameter of these states in trilayers as well as in bilayers. The order parameter of the so-called Fulde-Ferrell-Larkin-Ovchinnikov (FFLO) state [37,38] is also shown for comparison.

**Table I.** Layer-dependent order parameter of the BCS, PDW, FFLO, vortex, and CS states in bilayers and trilayers.

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<th>Trilayer</th>
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<td>$\Delta_1(\mathbf{r}) = \Delta$</td>
<td>$\Delta_1(\mathbf{r}) = \Delta$</td>
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<tr>
<td></td>
<td>$\Delta_2(\mathbf{r}) = \Delta$</td>
<td>$\Delta_2(\mathbf{r}) = \Delta'$</td>
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<td></td>
<td>$\Delta_3(\mathbf{r}) = \Delta$</td>
<td>$\Delta_3(\mathbf{r}) = \Delta$</td>
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<tr>
<td>PDW</td>
<td>$\Delta_1(\mathbf{r}) = \Delta$</td>
<td>$\Delta_1(\mathbf{r}) = \Delta$</td>
</tr>
<tr>
<td></td>
<td>$\Delta_2(\mathbf{r}) = -\Delta$</td>
<td>$\Delta_2(\mathbf{r}) = 0$</td>
</tr>
<tr>
<td></td>
<td>$\Delta_3(\mathbf{r}) = -\Delta$</td>
<td>$\Delta_3(\mathbf{r}) = -\Delta$</td>
</tr>
<tr>
<td>FFLO</td>
<td>$\Delta_1(\mathbf{r}) = \Delta \cos(\mathbf{q} \cdot \mathbf{r})$</td>
<td>$\Delta_1(\mathbf{r}) = \Delta \cos(\mathbf{q} \cdot \mathbf{r})$</td>
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<td>$\Delta_2(\mathbf{r}) = \Delta \cos(\mathbf{q} \cdot \mathbf{r})$</td>
<td>$\Delta_2(\mathbf{r}) = \Delta' \cos(\mathbf{q} \cdot \mathbf{r})$</td>
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<td></td>
<td>$\Delta_3(\mathbf{r}) = \Delta \cos(\mathbf{q} \cdot \mathbf{r})$</td>
<td>$\Delta_3(\mathbf{r}) = \Delta \cos(\mathbf{q} \cdot \mathbf{r})$</td>
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<tr>
<td>Vortex</td>
<td>$\Delta_1(\mathbf{r}) = \Delta e^{-i\mathbf{q}\cdot\mathbf{r}} + \delta e^{i\mathbf{q}\cdot\mathbf{r}}$</td>
<td>$\Delta_1(\mathbf{r}) = \Delta (e^{-i\mathbf{q}\cdot\mathbf{r}} + \delta e^{i\mathbf{q}\cdot\mathbf{r}})$</td>
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<td>$\Delta_2(\mathbf{r}) = \Delta (e^{-i\mathbf{q}\cdot\mathbf{r}} + \delta e^{i\mathbf{q}\cdot\mathbf{r}})$</td>
<td>$\Delta_2(\mathbf{r}) = \Delta' \cos(\mathbf{q} \cdot \mathbf{r})$</td>
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<td>$\Delta_3(\mathbf{r}) = \Delta (e^{-i\mathbf{q}\cdot\mathbf{r}} + \delta e^{i\mathbf{q}\cdot\mathbf{r}})$</td>
<td>$\Delta_3(\mathbf{r}) = \Delta (e^{-i\mathbf{q}\cdot\mathbf{r}} + \delta e^{i\mathbf{q}\cdot\mathbf{r}})$</td>
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<tr>
<td>CS</td>
<td>$\Delta_1(\mathbf{r}) = \Delta (e^{i\mathbf{q}\cdot\mathbf{r}} + \delta e^{-i\mathbf{q}\cdot\mathbf{r}})$</td>
<td>$\Delta_1(\mathbf{r}) = \Delta (e^{i\mathbf{q}\cdot\mathbf{r}} + \delta e^{-i\mathbf{q}\cdot\mathbf{r}})$</td>
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### III. Binary Superlattice

#### A. Bilayer system

In this section we study the binary superlattices [see Fig. 1(a)], which have been fabricated in CeCoIn$_5$/YbCoIn$_5$ [25]. We begin with the simplest case, namely the bilayer system ($M = 2$) illustrated in Fig. 2. Then, the strength of the orbital effect is controlled by the Fermi energy $E_F$, which is proportional to the in-plane hopping $t$. The orbital effect is estimated from the dimensionless quantity $\mu_B H/|H|$, with $\mu_B = \hbar/2\pi$ being the flux quantum. Since the coherence length of superconductivity is $\xi \approx \hbar v_F/|H| T_c$, the orbital effect is enhanced by increasing the Fermi energy. On the other hand, the paramagnetic effect of the magnetic field is estimated from another dimensionless quantity $\mu_B H/|H| T_c$, which is independent of the Fermi energy. Thus, the orbital effect (paramagnetic effect and RSOC) plays an important role in the superconducting state for large (small) in-plane hopping $t$. Note that the RSOC induces the CS state through the paramagnetic effect.

When we assume small in-plane hopping $t = 20$ meV consistent with the heavy effective mass of CeCoIn$_5$, the orbital effect is negligible. Indeed, we obtain the phase diagram in Fig. 3(a), which resembles the result in the paramagnetic limit [31]. The CS state is stable in the high magnetic field region, but the PDW state is not stabilized. Upon increasing the magnetic field, the center-of-mass momentum of Cooper pairs gradually increases through the BCS-CS phase transition [Fig. 3(b)], indicating the second-order phase transition. Figure 3(c) shows that $\Delta_1 = \Delta_2$ in the BCS state while $\delta$ in Eqs. (8) and (9) decreases upon increasing the magnetic field in the CS state. These behaviors are consistent with the previous study on the same model [31] where the orbital effect is simply neglected. Thus, the previous study that was focused on the heavy-fermion superlattice CeCoIn$_5$/YbCoIn$_5$ is justified.

On the other hand, the orbital effect significantly affects the superconducting state for large in-plane hopping, $t = 200$ meV. Figure 4(a) shows that the vortex state is stable in the high magnetic field region, as expected. The BCS-vortex phase transition is second order as indicated by the continuous change of the center-of-mass momentum [Fig. 4(b)] and $\delta$ [Fig. 4(c)]. Although the RSOC and the paramagnetic effect play less important roles than the orbital effect, they induce a characteristic magnetic field dependence in the center-of-mass momentum around the Pauli-Chandrasekhar-Clogston limit $\mu_B H/|H| T_c = 1.25$. The RSOC and paramagnetic effect suppress the orbital effect and thus decrease the center-of-mass momentum above the Pauli-Chandrasekhar-Clogston limit.

A main result of our study is obtained when the RSOC competes with the orbital effect. Such a situation is realized for moderate in-plane hopping $t = 80$ meV. Then the PDW state is stabilized in the high magnetic field region, as shown in Fig. 5. Note that the PDW state is induced neither by the orbital effect nor by the paramagnetic effect and RSOC. The PDW state is stable due to a balance of these effects. We explain this mechanism in detail here. The order parameter of the CS and vortex states is described by Eqs. (8) and (9), and these two states are differentiated by the sign of $\delta$. The positive $q$ (vortex state) is favored by the orbital effect, although the negative $q$ (CS state) is induced by the RSOC. Thus, $q \sim 0$.
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FIG. 3. (Color online) (a) Transition temperatures of various superconducting states in the bilayer system. We assume small in-plane hopping, \( t = 20 \text{ meV} \). Thin (red), moderate (blue), and thick (green) lines show the \( T_c \) of BCS, CS, and PDW states, respectively. The highest transition temperature is observable and indicated by the solid line, while the dashed and dot-dashed lines show the fictitious transition temperatures. (b) Magnetic field dependence of the center-of-mass momentum \(|\mathbf{q}|\). (c) Layer dependence of the order parameter. We show \( \Delta_1/\Delta_2 \) for the BCS state and \( \delta \) for the CS state. In this subsection, we choose the pairing interaction \( V_s/t = 1.5 \), which gives the transition temperature \( k_B T_{c0} = 0.0124t \) in the absence of the spin-orbit coupling and magnetic field. The temperature and magnetic field are scaled by \( T_{c0} \) in the figures.

when these two effects are in balance. Then, the interlayer Josephson coupling stabilizes the uniform superconducting state along the conducting plane, and thus \( q = 0 \). The \( \pi \) phase difference between layers is favored so that the paramagnetic depairing effect is avoided as in the \( c \)-axis magnetic field \[23\]. In this way, the PDW state is stabilized by the orbital effect, the paramagnetic effect, RSOC, and interlayer coupling.

B. More-than-two-layer system

Although it is hard to experimentally control the Fermi energy, the number of superconducting layers \( M \) can be tuned by using the artificial superlattice \[25,28,29\]. Thus, we may be able to control the orbital effect by tuning \( M \). Since the shift of momentum on the outermost layers, \(|p_1| = |p_M| = eHc(M - 1)/2\hbar\), increases with \( M \), the orbital effect is enhanced by increasing the number of superconducting layers. This is reasonable because vortices easily penetrate inside of thick SCs. We demonstrate here that the competing region of the RSOC and the orbital effect is realized by tuning \( M \), and then the PDW state is stabilized.

We take into account the RSOC on the outermost layers, \((\alpha_1, \alpha_M) = (\alpha, -\alpha)\), while the RSOC on the other layers is neglected for simplicity. This is a reasonable assumption for the layer dependence of RSOC because the spin-orbit coupling is determined by the local environment of atoms \[39\], and thus the outermost layers contain the largest spin-orbit coupling.

We fix the in-plane hopping, \( t = 21 \text{ meV} \), and the pairing interaction, \( V_s/t = 1.3 \). Then, the orbital effect is negligible in the bilayer system as in Fig. 3. The trilayer system shows the phase diagram (Fig. 6) similar to Fig. 3, and thus the trilayer system is still close to the Pauli limit.

On the other hand, the orbital effect plays an important role in the five-layer system \((M = 5)\). Then, the orbital effect competes with the RSOC, and therefore the PDW state is stabilized as expected from the results in Sec. III A. Indeed, Fig. 7 shows that the BCS state, the CS state, and the PDW state are stabilized in the low, intermediate, and high magnetic field regions, respectively. Because the CS-PDW transition is a first-
order phase transition, the upper critical field shows a kink, although the kink may be weak in some cases [see Figs. 5(a) and 10(a)]. Generally speaking, a distinct kink appears when the transition temperature of the PDW state is small. Then, the $H_{c2}$ of the CS state is suppressed while that of the PDW state shows an upward curvature. The observation of the kink will be an experimental test for the presence of the PDW state.

When we furthermore increase the number of superconducting layers, the superconducting state is dominated by the orbital effect, and thus the vortex state is stabilized in the high magnetic field region. For example, we show the phase diagram of the seven-layer system ($M = 7$) in Fig. 8. It is shown that the PDW state is not stabilized.

We focus here on the five-layer system, and we emphasize the cooperative role of the RSOC, the orbital effect, and the paramagnetic effect on the thermodynamic stability of the PDW state. Figure 9(a) shows the phase diagram in the absence of the orbital effect. The CS state is more stable than the PDW state, as in the bilayer and trilayer systems. On the other hand, the vortex state is stable in the high magnetic field region when we neglect the paramagnetic effect, as shown in Fig. 9(b). Note that the RSOC does not play an important role in the absence of the paramagnetic effect.

It should be noticed that the orbital limit of the upper critical field [Fig. 9(b)] is much larger than the paramagnetic limit [see Fig. 9(a)], indicating the large Maki parameter. This means that the upper critical field of five-layer systems is mainly determined from the paramagnetic effect. In this sense, the PDW state occurs near the paramagnetic limit, although a weak orbital effect is needed. Stars in Figs. 6, 7, 8, and 9(a) show the crossover induced by the paramagnetic effect [23]. Because the center layer is not protected against the paramagnetic effect by the RSOC, the order parameter in the center layer $\Delta_1/(M+1)/2$ suddenly decreases by increasing the magnetic field through the crossover. We see that the paramagnetic effect appears even in the seven-layer system, where the orbital effect is larger than the effect of RSOC.

C. CeCoIn$_5$/YbCoIn$_5$

In the previous subsections, we designed the odd-parity PDW state using the artificial heterostructures. It has been shown that the orbital effect is controlled by the number of superconducting layers. Indeed, various superlattices CeCoIn$_5$/YbCoIn$_5$ with $M > 2$ are superconducting, and we can tune the number of layers $M$ [25,28,29]. Thus, the artificial superlattice CeCoIn$_5$/YbCoIn$_5$ may be a new platform for odd-
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FIG. 5. (Color online) Transition temperatures (a) and layer dependence of the order parameter (b) for a moderate in-plane hopping, $t = 80\text{ meV}$. The other parameters are the same as those in Fig. 3. It is shown that the PDW state is stable in the high magnetic field region.

parity superconductivity. A reasonable parameter $t \sim 20\text{ meV}$ leads to the PDW state in the five-layer system.

![Graph](image)

FIG. 6. (Color online) Transition temperatures of the BCS, CS, and PDW states in the trilayer system ($M = 3$) for small in-plane hopping, $t = 21\text{ meV}$. In this subsection, we assume $V_c/t = 1.3$, which gives rise to the transition temperature at zero magnetic field, $T_{c0} = 0.00487t/k_B$, in the absence of RSOC.

![Graph](image)

FIG. 7. (Color online) Transition temperatures of the BCS, CS, and PDW states in the five-layer system ($M = 5$) for a small in-plane hopping, $t = 21\text{ meV}$.

We comment here on the recent experimental observations of the paramagnetic effect in the superlattice CeCoIn$_5$/YbCoIn$_5$ [28]. Goh et al. observed the strong paramagnetic effect by measuring the field-angle dependence of the upper critical field. They also showed that the paramagnetic effect is suppressed in a few-layer system $M \leqslant 3$. Their experimental results are consistent with our model; the paramagnetic effect is suppressed with decreasing $M$ because the superconductivity in surface layers, $m = 1$ and $M$, is substantially protected against the paramagnetic effect due to the RSOC [20,28]. Indeed, the upper critical field of the trilayer system is larger than that of the five-layer system near $T = T_{c0}$ (see Figs. 6 and 7). Note that the upper critical field is dominantly determined from the paramagnetic effect even when the orbital effect competes with the RSOC (see the discussion in Sec. III B).

Considering the consistency between our calculation and experiments for CeCoIn$_5$/YbCoIn$_5$ at low magnetic fields, it is expected that the PDW state may be realized in the artificial superlattice with $M \simeq 5$ at high magnetic fields. However, any indication of the presence of a high-field superconducting phase has not been reported. For instance, the kink and the upturn of the upper critical field shown in our calculations have

![Graph](image)

FIG. 8. (Color online) Transition temperatures of the BCS, the vortex, and the PDW states in the seven-layer system ($M = 7$) for small in-plane hopping, $t = 21\text{ meV}$.

CeCoIn$_5$/YbCoIn$_5$ indeed contains substantial disorders. Section II.FLO state is suppressed [40]. The artificial superlattice disorders suppress the high-field superconducting phase, as not taken into account in our model. First, it is expected that discrepancy may be attributed to the two ingredients that are not taken into account in our model. One is the Zeeman term in the Hamiltonian [Eq. (1)]. The other parameters are the same as those in Fig. 5.

On the other hand, Figs. 10(a) and 10(b) show the phase diagram for $t_{\perp}/t = 0.05$ and 0.01, respectively. Since the high-field phase may have not been observed [25,28,29]. The high-field phase may have been missed because the measurement has not been carried out in the low-temperature region. On the other hand, the discrepancy may be attributed to the two ingredients that are not taken into account in our model. First, it is expected that disorders suppress the high-field superconducting phase, as the FFLO state is suppressed [40]. The artificial superlattice CeCoIn$_5$/YbCoIn$_5$ indeed contains substantial disorders. On the other hand, Figs. 10(a) and 10(b) show the phase diagram for $t_{\perp}/t = 0.05$ and 0.01, respectively. Since the

IV. TRICOLOR SUPERLATTICE

Next, we discuss the tricolor superlattice illustrated in Fig. 1(b). As we have shown in Sec. III B, the orbital effect is controlled by the spacing between the outermost layers. Thus, the PDW state may be stabilized in a tricolor superlattice by intercalating the spacer layers into the superconducting layers. Then, the spacing of neighboring superconducting layers is multiplied to $d = (m_d + 1)c$, with $m_d$ being the number of intercalated spacer layers [green open circles in Fig. 1(b)]. We assume here that the interlayer spacing between the spacer layer and the superconducting layer is $c$. A similar situation in the bilayer $\delta$-doped SrTiO$_3$ [41] has been realized, and superconductivity in the bilayer interface LaAlO$_3$/SrTiO$_3$/LaAlO$_3$ has been studied [22].

Multiplying the interlayer spacing by $(m_d + 1)$ is equivalent to increasing the in-plane hopping to $(m_d + 1)t$ while keeping the ratio, $t_{\perp}/t$, $\mu/t$, $\alpha/t$, and $V_s/t$. For instance, we obtain the same results for the binary superlattice with $t = 80$ meV and for the tricolor superlattice with $t = 20$ meV and $m_d = 3$. Thus, the PDW state may be stabilized in the tricolor bilayer superlattice. However, in reality, the interlayer hopping $t_{\perp}$ between the nearest-neighbor superconducting layers is significantly decreased by intercalating a spacer layer. For instance, we obtain $t_{\perp} \sim t_{\perp}^m/(E_s - E_b)$ in the presence of a single spacer layer ($m_d = 1$), where $t_{\perp}^m$ is the hopping integral between the superconducting layer and the spacer layer and $E_s - E_b$ is the potential difference between these layers. Therefore, the stability of the PDW state in the tricolor superlattice should be examined by investigating the superconducting state for small $t_{\perp}$.

We study here the tricolor bilayer superlattice for simplicity. The in-plane hopping is set to $t = 20$ meV by considering the heavy-fermion superlattice. As we discussed above, we obtain the same phase diagram as Fig. 5 when $m_d = 3$ and $t_{\perp}/t = 0.1$. On the other hand, Figs. 10(a) and 10(b) show the phase diagram for $t_{\perp}/t = 0.05$ and 0.01, respectively.
interlayer Josephson coupling decreases with $t_{ij}/t$, the uniform states, namely the BCS and PDW states, are suppressed. It is shown that the PDW state is stable at high magnetic fields, but the transition temperature of the PDW state is significantly decreased for $t_{ij}/t = 0.01$. The PDW state will be furthermore suppressed by further decreasing $t_{ij}/t$. Thus, it may be hard to realize the PDW state in a tricrystal superlattice by intercalating many spacer layers.

It should be noticed that Fig. 10(b) is similar to the phase diagram of the binary five-layer superlattice (Fig. 7). We now understand that the reduced transition temperature of the PDW state in the five-layer system is due to the reduced Josephson coupling between the outermost layers. In other words, the superconducting inner layers play a role of the spacer layers. Indeed, the PDW state is mainly induced by the outermost layers where the superconductivity is protected against the paramagnetic effect by the RSOC. For example, we obtain the layer-dependent order parameter $(\Delta_1, \Delta_2, \Delta_1, \Delta_4, \Delta_5) \simeq \Delta(1, 0.18, 0, -0.18, -1)$ in the five-layer PDW state.

Finally, we discuss the superconductivity in the bilayer $\delta$-doped SrTiO$_3$ [41] and the bilayer interface LaAlO$_3$/SrTiO$_3$/LaAlO$_3$ [22]. The Fermi velocity estimated for a carrier density $n \approx 10^{14}$ cm$^{-2}$ on the basis of the three-orbital tight-binding model [42] is approximately twice as large as that in our model. Since the lattice constant along the $c$ axis, $c = 3.9$ Å, is nearly half of CeCoIn$_5$, the orbital effect in the SrTiO$_3$ heterostructures is comparable to our model. Thus, the bilayer system sandwiching three nonsuperconducting layers may be a platform of the odd-parity PDW state. Then, the interlayer coupling between superconducting layers may be small, and therefore the PDW state may appear in the low-temperature region, as shown in Fig. 10(b). The kink in the upper critical field would be a signature of the PDW state.

V. TOPOLOGICAL SUPERCONDUCTIVITY

Topologically nontrivial insulators and SCs have evolved into one of the major research topics of modern condensed-matter physics recently [43,44]. In particular, topological superconductivity attracts a great deal of attention since the Majorana state satisfying the non-Abelian statistics appears in the low-temperature region, as shown in Fig. 10(b). The kink in the upper critical field would be a signature of the PDW state.

Hamiltonian,
\[
\mathcal{H}_{\text{BdG}} = \sum_{k,s,m} \xi(k + p_m) c_{ksm}^\dagger c_{ksm} + t_{ij} \sum_{k,s,(m',m)} c_{ksm}^\dagger c_{ks'm'} \\
- \sum_{k,s,s',m} \mu_B H \cdot \sigma_{ss'}^\dagger c_{ksm} c_{ks'm} \\
+ \sum_{k,s,s',m} a_m g(k + p_m) \cdot \sigma_{ss'}^\dagger c_{ksm} c_{ks'm} \\
+ \frac{1}{2} \sum_{k,s,s',m} [\Delta_{ss'}^\dagger(k)c_{ks'm}^\dagger c_{k'sm} + \text{H.c.}],
\]
where $\Delta_m(k) = |\Delta_{ss'}^\dagger(k)| = |\psi_m + d_m(k) \cdot \sigma | |\sigma\rangle$ describes the layer-dependent order parameter of superconductivity [1]. Although the purely $s$-wave superconductivity is considered in Secs. III and IV, the $p$-wave component is admixed through the layer-dependent RSOC by the local violation of inversion symmetry [51]. The layer dependence of the order parameter is obtained as
\[
(\psi_1, \psi_2, \psi_3, \psi_4, \psi_5) = (\psi_{\text{out}}, \psi_{\text{in}}, 0, -\psi_{\text{in}}, -\psi_{\text{out}}),
\]
\[
(d_{1}(k), d_{2}(k), d_{3}(k), d_{4}(k), d_{5}(k)) = (d_{\text{out}}, d_{\text{in}}, d_{\text{in}}, d_{\text{in}}, d_{\text{out}}) \cdot g(k)
\]
in the five-layer PDW state. The BdG Hamiltonian is represented in Nambu space,
\[
\mathcal{H}_{\text{BdG}} = \frac{1}{2} \sum_k c_k^\dagger \mathcal{H}_{\text{BdG}}(k) c_k,
\]
\[
\mathcal{H}_{\text{BdG}}(k) = \begin{pmatrix} \hat{H}_0(k) & \hat{\Delta}(k) \\ \hat{\Delta}^\dagger(k) & -\hat{H}_0(-k)^T \end{pmatrix},
\]
where $\hat{H}_0(k)$ is the Hamiltonian in the normal state and $\hat{\Delta}(k)$ is the order parameter.

Although the mirror symmetry with respect to the $ab$ plane $M_{ab}$ is broken in the in-plane magnetic field, the magnetic mirror symmetry $T = T M_{ca}(T M_{bc})$ is preserved in the $a$-axis ($b$-axis) magnetic field. For instance, in the magnetic field along the $a$ axis, the BdG Hamiltonian is invariant under magnetic mirror symmetry,
\[
T \hat{H}_{\text{BdG}}(k_0, k_0) T^{-1} = \hat{H}_{\text{BdG}}(-k_0, k_0),
\]
where $M_{ca} = i\sigma_y$ is the mirror reflection operator and $T = i\sigma_y K$ is the time-reversal operator, with $K$ being the complex-conjugate operator. Combining with the particle-hole symmetry $C \mathcal{H}_{\text{BdG}}(k) C^\dagger = -\mathcal{H}_{\text{BdG}}(-k)$, we get $C = \tau_x K$ and $\tau_z$ is the Pauli matrix in the particle-hole space, we can define the mirror chiral symmetry $\Gamma \mathcal{H}_{\text{BdG}}(k_0, k_0) \Gamma^{-1} = -\mathcal{H}_{\text{BdG}}(k_0, -k_0)$ with $\Gamma^{-1} = -CT = \tau_z$. Thus, the BdG Hamiltonian satisfies the chiral symmetry
\[
[\Gamma, \hat{H}_{\text{BdG}}(k)] = 0
\]
at $k_1 = 0$ and $k_2 = \pi/a$. The chiral symmetry ensures that the one-dimensional winding number
\[
\omega_{k_y} = \frac{1}{4\pi i} \int \frac{d^2 k_{1,2}}{2\pi} Tr \left[ \hat{q}(k)^{-1} \partial_{k_1} \hat{q}(k) - \hat{q}^\dagger(k)^{-1} \partial_{k_1} \hat{q}^\dagger(k) \right]
\]
from which we obtain the topological Chern numbers.
is a topological invariant [52–57] when a finite gap is open at $k_y = 0$ and $k_x = \pi/a$. The $2M \times 2M$ matrix $\hat{q}(k)$ is obtained by carrying out the unitary transformation

$$U\hat{H}_{BDG}(k)U^\dagger = \begin{pmatrix} 0 & \hat{q}(k) \\ \hat{q}^\dagger(k) & 0 \end{pmatrix}. \quad (18)$$

When we regard the magnetic mirror symmetry $T'$ as pseudo-time-reversal symmetry [58,59], the one-dimensional Hamiltonian $\hat{H}_{BDI}^{k_y=0}(k_x) = \hat{H}_{BDG}(k_x,0)$ and $\hat{H}_{BDI}^{\nu_{BDI}/a}(k_x) = \hat{H}_{BDG}(k_x,\pi/a)$ belong to the symmetry class $BDI$ because $T'^2 = +1[13,14]$. Thus, we can define the integer topological numbers of the $BDI$ class,

$$v_0^{BDI} = \frac{1}{\pi i} \int_0^\pi dk_x \text{Tr}[\hat{q}(k_x,0)^{-1}\partial_{k_x}\hat{q}(k_x,0)], \quad (19)$$

$$v_{\pi/a}^{BDI} = \frac{1}{\pi i} \int_0^\pi dk_x \text{Tr}[\hat{q}(k_x,\pi/a)^{-1}\partial_{k_x}\hat{q}(k_x,\pi/a)]. \quad (20)$$

Indeed, these winding numbers are equivalent to Eq. (17), namely $v_{\pi/a}^{BDI} = \omega_0,\pi/a$. The pseudo-time-reversal symmetry considered here has been used for the definition of the integer topological number in one-dimensional semiconductor nanowires [58] and quasi-one-dimensional $d$-wave superconductors [59]. The magnetic mirror symmetry is the physical origin of this “hidden” time-reversal symmetry. The difference of two winding numbers, $v_0^{BDI} = v_{\pi/a}^{BDI}$, is the strong index of 2D topological crystalline SCs protected by the magnetic mirror symmetry [48].

We now discuss the superconducting gap. Figure 11 shows the gap of the single-particle excitation spectra in the five-layer PDW state for each $k_y$, which is defined as $E_{\text{min}}(k_x) = \min_{\alpha,E} |E_i(k)|$, with $E_i(k)$ being eigenvalues of the BdG Hamiltonian $\hat{H}_{BDG}(k)$. We assume here $\mu/t = -2$ so that the Fermi surface encloses the $\Gamma$ point ($k = 0$). Since there is no Fermi surface along $k_y = \pi/a$, the winding number is trivial, $v_{\pi/a}^{BDI} = 0$. Therefore, we focus on $v_0^{BDI}$. The superconducting gap is finite at $k_y = 0$, ensuring the topological protection of the winding number $v_0^{BDI}$. At low magnetic fields, the superconducting gap is finite in the whole Brillouin zone (thin solid line in Fig. 11), and thus $v_0^{BDI}$ is the strong topological index. Although the gap at finite $k_y$ is closed at high magnetic fields due to the paramagnetic effect, the winding number is regarded as a topological number of an effective one-dimensional Hamiltonian.

As we show in Fig. 12(a), $v_0^{BDI}$ discretely changes upon increasing the $p$-wave component in the order parameter, $d = d_{\text{out}} = d_{\text{in}} = d'_{\text{in}}$. The superconducting gap is closed for special values of $d$ where the winding number jumps [Fig. 12(b)]. We ignore here the layer dependence of the $p$-wave component for simplicity. This assumption has been justified by the BdG equation, which shows the nearly layer-independent $p$-wave component in the PDW state [51].

Switching on a small $p$-wave component $|d| > 0.05\psi_{\text{out}}$, we obtain a finite winding number indicating the topologically nontrivial properties [see Fig. 12(a)]. This is in sharp contrast to the 2D Rashba SC, where the $p$-wave component overwhelming the $s$-wave component is required for topological superconductivity [52,60]. This condition is hardly realized in real materials. On the other hand, a small $p$-wave component induced by the RSOC causes the PDW state to be
the Majorana edge state according to the bulk-edge correspondence.

Although the bilayer system ($M = 2$) is trivial, the topologically nontrivial superconducting state is induced by a small $p$-wave component for $M \geq 3$. According to the random-phase-approximation (RPA) analysis of the three-dimensional Rashba-Hubbard model, the induced spin-triplet component is approximately 20% of the spin-singlet component for a moderate RSOC [39,61]. Thus, the $p$-wave component is likely to be large enough to realize the topological crystalline superconductivity protected by the magnetic mirror symmetry for $M \geq 3$. Note that these conditions are different from those for the topological superconductivity in the magnetic field along the $c$ axis. The PDW state is a topological crystalline superconductor in the $c$-axis magnetic field when the number of superconducting layers $M$ is odd [24]. Then, the $p$-wave component is not required.

A nontrivial winding number may ensure the presence of the Majorana edge state according to the bulk-edge correspondence. When the magnetic field is applied along the $a$ axis, the magnetic mirror symmetry $T M_{ca}$ is preserved at the edge perpendicular to the $[010]$ axis ($[100]$ edge). Therefore, the winding number protected by this symmetry corresponds to the number of zero-energy edge states according to the index theorem [53]. Indeed, we show the Majorana edge states in Fig. 14. The trilayer PDW state with a large superconducting gap is considered for simplicity of numerical calculation. The energy spectrum is calculated in the open boundary condition along the $a$ axis. The layer-dependent order parameters are $(\psi_1, \psi_2, \psi_3) = (1, 0, -1)\psi_{out}$ and $(d_{1}(k), d_{2}(k), d_{3}(k)) = (1, 1, 1)\hat{d}g(k)$. We see the two Majorana modes around $k_\mu = 0$ [Fig. 14(a)] when we assume a small $p$-wave component leading to the winding number $v_0^{BDM} = 2$. The Majorana states have a linear dispersion since the chiral symmetry defined in Eq. (16) is not preserved at $0 < |k| < \pi/a$. Because another pseudo-time-reversal symmetry, $T'' = T M_{ab}$, is preserved, the two Majorana states form “Kramers pairs.”

Finally, we comment on the anisotropic response to the external magnetic field. The magnetic mirror symmetry $T M_{ca}$ is broken when we apply the magnetic field along the $b$ axis. Then, the zero-energy Majorana states disappear at the $(100)$ edge, as expected [Fig. 14(b)]. This field angle dependence is attributed to the Ising character of the Majorana state. Similarly, the Majorana mode appears (disappears) at the $(010)$ edge in the magnetic field along the $b$ axis ($a$ axis), because the mirror symmetry along the $bc$ plane $M_{bc}$ is preserved at the edge.

VI. SUMMARY AND DISCUSSION

In this paper, we studied 2D multilayer SCs influenced by the layer-dependent RSOC. We showed that the odd-parity PDW state is stabilized by competing spin-orbit coupling and...
the orbital effect in the magnetic field along the 2D conducting plane. We also showed that the PDW state is a topological crystalline SC protected by the magnetic mirror symmetry when a small $p$-wave component is induced by the RSOC. The Majorana state has been demonstrated at the (100) edge ([010] edge) in the magnetic field along the $a$ axis ($b$ axis).

Our finding paves the way toward realizing odd-parity superconductivity without a considerable pairing interaction in the spin-triplet channel. Although spin-triplet superconductivity is hardly stabilized in most SCs except for a few exceptions, our proposal provides an alternative way to create odd-parity SC by using the sublattice degree of freedom.

Indeed, recent developments in the technology of artificial heterostructures may enable the design of the odd-parity PDW state. Superconducting 2D electron systems have been fabricated in the oxide interfaces SrTiO$_3$/LaAlO$_3$ [62] and SrTiO$_3$/LaTiO$_3$ [63], gate-tuned SrTiO$_3$ [64] and MoS$_2$ [65], and the heavy-fermion superlattice CeCoIn$_5$/YbCoIn$_5$ [25]. It has been reported that interfacial (intrinsic) spin-orbit coupling significantly affects the superconducting state in SrTiO$_3$ heterostructures [42,66–68] and CeCoIn$_5$/YbCoIn$_5$ [28,29] (MoS$_2$ [69,70]). Furthermore, the multilayer structure has been artificially controlled in CeCoIn$_5$/YbCoIn$_5$ [29] and $\delta$-doped SrTiO$_3$ [41]. Thus, we expect that odd-parity topological superconductivity will be created in these systems by tuning the multilayer structure and the magnetic field.

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