

1     **Coupled thermo-hydro-mechanical-chemical modeling of permeability change in porous**  
2                     **rocks: The significant role of the pressure solution**

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9

10 **Abstract**

11       When considering the safe isolation of high-level radioactive wastes, the long-term  
12 evolution of the hydraulic and transport behavior of the rocks of interest should be predicted prior  
13 to its operation because coupled thermal-hydraulic-mechanical-chemical (THMC) processes  
14 should be significantly active in such situations where relatively high ground pressure and  
15 temperature are induced. In this study, a coupled THMC numerical model has been developed to  
16 examine the long-term change in permeability of the porous sedimentary rocks that are assumed  
17 to be composed purely of quartz. Specifically, the chemo-mechanical process of the pressure  
18 solution was incorporated into the model. The developed model was validated by replicating the  
19 existing experimental measurements of the porosity reduction and the evolving silica  
20 concentration. Subsequently, by simulating the burial of high-level radioactive wastes in the deep  
21 subsurface, namely, by applying the simulated confining pressure and temperature conditions, the  
22 long-term evolution of the rock permeability was predicted. The model predictions clearly  
23 showed a significant influence of the pressure dissolution on the change in permeability with time.  
24 The predicted permeability of the rocks close to the wastes decreased by one order of magnitude  
25 in  $10^4$  years when considering the pressure dissolution, while the permeability changed little  
26 during the same period when the pressure dissolution was not considered. This reduction should  
27 delay the dispersion of the radioactive materials dissolved in the groundwater.

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30 **Keywords: Rock permeability, Coupled THMC model, Mineral dissolution, Pressure**  
31 **solution**

32

33 **Highlights:**

34 ➤ **A coupled THMC numerical model was developed to predict the long-term change in**  
35 **permeability.**

36 ➤ **The developed model considers the pressure solution.**

37 ➤ **The model was validated by replicating the existing experiments.**

38 ➤ **The model enables the long-term evolution of rock permeability to be predicted under**  
39 **arbitrary pressure and temperature conditions.**

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41

## 42 **1. Introduction**

43 When disposing high-level radioactive wastes in the deep subsurface, the influence of the  
44 disposal on the hydraulic property of the rocks of interest must be examined in advance and  
45 should be estimated with a certain level of precision. The rocks that work as natural barriers to the

46 migration of radionuclides should be influenced by the convolved phenomena, including the  
47 transfer of heat from the wastes, the groundwater flow, the variation in induced stresses, and the  
48 geochemical reactions, such as mineral dissolution and precipitation [1], [2]. Therefore, in order  
49 to predict the long-term evolution of the hydraulic property, a numerical model that can account  
50 for the coupled Thermo-Hydro-Mechanical-Chemical (THMC) processes is required. In particular,  
51 the precise modeling of the geochemical reactions, occurring at the interface between the grain  
52 particles composing the rocks and the pore water, is of significant importance to achieving precise  
53 predictions. To date, THMC numerical models have been developed to address such engineering  
54 issues as the geological isolation of CO<sub>2</sub> and radioactive wastes and energy recovery from  
55 geothermal reservoirs [3]-[9]. By using some of the above models, the long-term phenomena  
56 taking place in the artificial and natural barriers have been predicted by considering the specific  
57 geological conditions, the heat transfer, the water flow, the stress/deformation, and the  
58 geochemical reactions. In the geochemical calculations of the THMC models, the mineral  
59 dissolution and precipitation occurring on the free surfaces of the rocks [10] are typically  
60 considered, but the dissolution active at the grain contacts (e.g., pressure dissolution [11]-[18]) is  
61 not taken into account. In the literature, it is indicated that the pressure dissolution may change the  
62 hydraulic property over a long duration; and therefore, the phenomenon must be incorporated into  
63 the modeling process when evaluating the long-term integrity of the rocks in terms of the

64 hydraulic property. Recently, several THMC numerical models that can consider the process of  
65 the pressure dissolution have been proposed [7]-[9], but these models mostly address fracture  
66 media and do not estimate the evolution of the hydraulic property in porous rocks.

67 In this study, a new coupled THMC numerical model that incorporates the important process  
68 of the pressure dissolution, as well as the free-face dissolution and precipitation, was developed,  
69 and the validity of the model was examined by replicating the experimental measurements  
70 obtained from Elias and Hajash (1992) [19]. Subsequently, the long-term evolution of the  
71 permeability in porous rock was predicted under the expected stress and temperature conditions  
72 where high-level radioactive wastes are disposed. In particular, the influence of the pressure  
73 dissolution on the change in the rock permeability was examined intensively.

74 When any numerical model is developed, it may be dilemmatic to consider the balance  
75 between the simplicity and the precision of the model. Complex models that incorporate a number  
76 of equations to be solved may require time-consuming handling during pre- and post-processing,  
77 and lengthy calculation time. Therefore, simpler or more straightforward numerical models with  
78 satisfactory precision are preferred for general users. By focusing selectively on the geochemical  
79 process of the pressure dissolution, the minor objective of this study is to develop a relatively  
80 simple model.

81

82

## 83 **2. Model description**

84 The coupled THMC model developed in this work enables the change in permeability of  
85 porous rocks to be followed with time by considering the interactions of the thermal, hydraulic,  
86 mechanical, and geochemical processes (i.e., heat transfer, groundwater flow in saturated porous  
87 media, stress/deformation, mass transport, and mineral dissolution/precipitation). The processes  
88 considered in this model are schematically summarized in **Figure 1**. As is apparent from this  
89 figure, the two-way interactions are taken into account between the T and H, the H and C, and the  
90 C and T components. In the M component, the stress distribution is calculated and then rendered  
91 to calculate a chemo-mechanical process, which is referred to as CM in **Figure 1**. In the C  
92 components, two different chemical processes are incorporated into the model; one is the  
93 free-surface dissolution/precipitation (CF) and the other is the pressure solution (CM). The  
94 pressure solution includes three serial processes - mineral dissolution at the stressed contacts,  
95 diffusive transport through the thin film of water, and re-precipitation of the mineral matter at the  
96 pore wall. The mineral dissolution at the stressed contacts is explicitly integrated into the  
97 proposed model as the CM component. It should be noted that we have proposed conceptual  
98 chemo-mechanical models to predict the change in permeability of porous and fractured rocks  
99 [20]-[24], and that this work is an attempt to fit the conceptual model into the coupled numerical

100 model and to conduct numerical simulations at a field scale instead of a representative element  
101 scale. It should be also noted that the interactions between the H and M and the M and T  
102 components are intentionally omitted in this work. These processes may influence the change in  
103 permeability, but the main focus of the current work is to examine the effects of the geochemical  
104 reactions (i.e., free-face dissolution/precipitation and pressure dissolution) on the change in  
105 permeability by simplifying the developed model.

106

## 107 *2.1 Governing equations*

108 The equations used to model each of the THMC processes are presented in this section. In  
109 this work, COMSOL Multiphysics [25] is utilized to solve the differential equations describing  
110 the THMC processes. The calculation procedure is shown in **Figure 2** and the details are  
111 described hereinafter. The coupled THMC processes are solved sequentially by exchanging the  
112 dependent variables (i.e., porosity/permeability, flow velocity, stress, temperature, and  
113 dissolution/precipitation rate constants).

114 The groundwater flow in saturated rocks is simply modeled by the conservation of water  
115 mass and by assuming the Darcian flow, given by

116 
$$\frac{\partial(\rho_w \phi)}{\partial t} + \nabla \cdot (\rho_w \mathbf{u}) = f_m, \quad (1)$$

117 
$$\mathbf{u} = -\frac{\mathbf{k}}{\mu}(\nabla p + \rho_w g \nabla D), \quad (2)$$

118 where  $\rho_w$  [kg m<sup>-3</sup>] is the density of the fluid,  $\phi$  [-] is the porosity,  $\mathbf{u}$  [m s<sup>-1</sup>] is the fluid velocity  
 119 tensor,  $f_m$  [kg m<sup>-3</sup> s<sup>-1</sup>] is the source term for the flow,  $\mathbf{k}$  [m<sup>2</sup>] is the rock permeability tensor,  $\mu$  [Pa  
 120 s] is the fluid dynamic viscosity,  $p$  [Pa] is the fluid pressure,  $g$  [m s<sup>-2</sup>] is the gravity acceleration,  
 121 and  $D$  [m] is the potential head. The temperature-dependent variables of  $\rho_w$  and  $\mu$  are evaluated at  
 122 arbitrary temperatures within the calculation scheme [25].

123 The heat transfer is evaluated by considering thermal convection and conduction without the  
 124 radiation effect, as follows:

125 
$$(\rho C_p)_{eq} \frac{\partial T}{\partial t} + \rho_w C_{p,w} \mathbf{u} \cdot \nabla T = \nabla \cdot (\mathbf{k}_{eq} \nabla T) + Q_h, \quad (3)$$

126 where  $T$  [K] is the temperature,  $(\rho C_p)_{eq}$  [J K<sup>-1</sup> m<sup>-3</sup>] is the equilibrium volumetric heat capacity,  
 127  $C_{p,w}$  [J kg<sup>-1</sup> K<sup>-1</sup>] is the heat capacity of the fluid,  $\mathbf{k}_{eq}$  [W m<sup>-1</sup> K<sup>-1</sup>] is the equilibrium thermal  
 128 conductivity tensor, and  $Q_h$  [W m<sup>-3</sup>] is the heat source.  $(\rho C_p)_{eq}$  and  $\mathbf{k}_{eq}$  can be obtained from the  
 129 following equations:

130 
$$(\rho C_p)_{eq} = (1 - \phi) \rho_m C_{p,m} + \phi \rho_w C_{p,w}, \quad (4)$$

131 
$$\mathbf{k}_{eq} = (1 - \phi) \mathbf{k}_m + \phi \mathbf{k}_w, \quad (5)$$

132 where  $\rho_m$  [kg m<sup>-3</sup>] is the density of the solid,  $C_{p,m}$  [J kg<sup>-1</sup> K<sup>-1</sup>] is the heat capacity of the solid, and  
 133  $\mathbf{k}_m$  and  $\mathbf{k}_w$  [W m<sup>-1</sup> K<sup>-1</sup>] are the thermal conductivity tensors of the solid and the fluid, respectively.



134 The numerical model enables the temperature-dependent variables of  $C_{p,m}$ ,  $C_{p,w}$ ,  $k_m$ , and  $k_w$  to be  
 135 followed at arbitrary temperatures [25].

136 The mechanical process of the rock structure is evaluated by the quasi-static equilibrium  
 137 equation and the typical Hooke's law, given by

$$138 \quad -\nabla \cdot \boldsymbol{\sigma} = \mathbf{F}_v, \quad (6)$$

$$139 \quad \boldsymbol{\sigma} = \mathbf{E} : \boldsymbol{\varepsilon}, \quad (7)$$

140 where  $\boldsymbol{\sigma}$  [Pa] is the stress tensor,  $\mathbf{F}_v$  [Pa m<sup>-1</sup>] is the body force,  $\mathbf{E}$  [Pa] is the elasticity tensor, and  $\boldsymbol{\varepsilon}$   
 141 [-] is the strain tensor. In this work, the thermal stress and the inelastic behavior are disregarded  
 142 for simplicity. A self-weight analysis is conducted to obtain the initial stress field, while the  
 143 change in stress distribution by the cavity excavation is calculated using these equations.

144 The advection-diffusion equation is used to calculate the solute transport behavior. The  
 145 mechanical dispersion and the retardation due to the sorption processes are not considered here.

$$146 \quad \frac{\partial(c_i \phi)}{\partial t} + \mathbf{u} \cdot \nabla c_i = \nabla \cdot (\phi \tau \mathbf{D}_{b,i} \nabla c_i) + R_i, \quad (8)$$

147 where  $c_i$  [mol m<sup>-3</sup>] is the concentration of solute  $i$ ,  $\tau$  [-] is the coefficient related to tortuosity,  $\mathbf{D}_{b,i}$   
 148 [m<sup>2</sup> s<sup>-1</sup>] is the diffusion coefficient tensor, and  $R_i$  [mol m<sup>-3</sup> s<sup>-1</sup>] is the solute source or sink of solute  
 149  $i$ . The diffusion coefficient is controlled by the system temperature and can be defined by an  
 150 Arrhenius-type equation [26], as

151 
$$D_{b,i} = D_{b,i}^0 \exp(-E_{D,i} / RT), \quad (9)$$

152 where  $D_{b,i}^0$  [ $\text{m}^2 \text{s}^{-1}$ ] and  $E_{D,i}$  [ $\text{J mol}^{-1}$ ] are the pre-exponential factor and the activation energy of  
153 the diffusion of solute  $i$ , respectively, and  $R$  [ $\text{J mol}^{-1} \text{K}^{-1}$ ] is the gas constant.

154 The source/sink term,  $R_i$ , is calculated by considering both free-face dissolution/precipitation  
155 and pressure dissolution, and can be expressed by

156 
$$R_i = R_i^{FF} + R_{diss,i}^{PS}, \quad (10)$$

157 where  $R_i^{FF}$  and  $R_{diss,i}^{PS}$  [ $\text{mol m}^{-3} \text{s}^{-1}$ ] are the rates of free-face dissolution/precipitation and  
158 pressure dissolution, respectively. They are the physical quantities that describe the mineral  
159 dissolution and precipitation per volume and time. The rate of the free-face  
160 dissolution/precipitation is defined by [10]

161 
$$R_i^{FF} = k_+ A (a_{H^+})^n (1 - Q / K), \quad (11)$$

162 where  $k_+$  [ $\text{mol m}^{-2} \text{s}^{-1}$ ] is the mineral dissolution rate constant,  $A$  [ $\text{m}^2 \text{m}^{-3}$ ] is the specific surface  
163 area,  $a_{H^+}$  [-] is the activity of  $H^+$ , and  $n$  [-] is the constant, which may be obtained from  
164 experimental observations in the literature.  $Q$  [-] is the ionic activity product and  $K$  [-] is the  
165 equilibrium constant. When  $Q/K < 1$ , free-face dissolution occurs; when  $Q/K > 1$ , free-face  
166 precipitation occurs. The specific surface area is obtained by the measurement using the BET  
167 method, given as follows:

168 
$$A = A_{BET} \rho_m, \quad (12)$$

169 where  $A_{BET}$  [ $\text{m}^2 \text{kg}^{-1}$ ] is the specific surface area determined by the BET method.

170 In this work, the rock is assumed to be composed purely of quartz, and subscript  $i$  in Eqs. (8)

171 - (10) is omitted hereinafter. The equilibrium and the dissolution rate constants in Eq. (11) are

172 obtained from PHREEQC [27] and Rimstidt and Barnes (1980) [28], respectively. These

173 constants are temperature-dependent and are given via polynomial approximation and by an

174 Arrhenious expression, as follows:

175 
$$K = \sum_{m=0}^7 \alpha_m T^m, \quad (13)$$

176 
$$k_+ = k_+^0 \exp(-E_{k_+} / RT), \quad (14)$$

177 where  $\alpha_m$  ( $m=0-7$ ) [-] is the constant,  $k_+^0$  [ $\text{mol m}^{-2} \text{s}^{-1}$ ] is the pre-exponential factor, and  $E_{k_+}$  [J

178  $\text{mol}^{-1}$ ] is the activation energy of the mineral dissolution.

179 Incorporating the process of pressure dissolution into the developed model is the most

180 important task in this work. As described above, we have developed conceptual models that

181 describe the process [20]-[24]. The flux that represents the pressure dissolution is driven by the

182 gradient in the chemical potential between the highly-stressed contacts and the less-stressed site

183 of the pore walls [13], [26]. Dissolution is most conveniently defined in terms of a dissolution

184 mass flux,  $\dot{M}_{diss}^{PS}$ , the rate of addition of dissolved mass into solution at the interface, given as

185 [20]

186 
$$\dot{M}_{diss}^{PS} = \frac{3V_m^2(\sigma_a - \sigma_c)k_+ \rho_g A_c}{RT}, \quad (15)$$

187 where  $V_m$  is the molar volume of the solid ( $2.27 \times 10^{-5} \text{ m}^3 \text{ mol}^{-1}$  for quartz),  $\sigma_a$  [Pa] is the  
 188 disjoining pressure [29] equal to the amount by which the pressure acting at the contacts exceeds  
 189 the hydrostatic pore pressure,  $\rho_g$  is the grain density ( $2650 \text{ kg m}^{-3}$  for quartz),  $A_c$  [ $\text{m}^2$ ] is the area  
 190 of the grain contact, and  $\sigma_c$  [Pa] is the critical stress, which defines the stress state where the  
 191 compaction of the grain aggregate will effectively halt [20]. This stress is determined by  
 192 considering the energy balance under applied stress and temperature conditions, given by [26],  
 193 [30]

194 
$$\sigma_c = \frac{E_m(1 - T/T_m)}{4V_m}, \quad (16)$$

195 where  $E_m$  and  $T_m$  are the heat and temperature of fusion, respectively ( $E_m = 8.57 \text{ kJ mol}^{-1}$ ,  $T_m =$   
 196  $1883 \text{ K}$  for quartz).

197 Based on Eq. (15), the rate of the pressure dissolution,  $R_{diss}^{PS}$ , is derived through the following  
 198 procedure. Firstly, the strain rate due to the pressure dissolution is given as [20]

199 
$$\dot{\epsilon}_{diss}^{PS} = \frac{\dot{M}_{diss}^{PS}}{d \rho_g A_c} = \frac{3V_m^2 k_+}{RTd} \left( \frac{\sigma_{eff}}{R_c} - \sigma_c \right), \quad (17)$$

200 
$$\sigma_a = \frac{\sigma_{eff}}{R_c}, \quad (18)$$

201 where  $\dot{\epsilon}_{diss}^{PS}$  [-] is the strain state,  $d$  [m] is the grain diameter,  $\sigma_{eff}$  [Pa] is the effective stress  
 202 exerted in the representative element, and  $R_c$  ( $0 < R_c < 1$ ) [-] is the contact-area ratio. In this work,

203 the FE analyses are conducted with 2-D meshes in the following sections. To this end, the  
 204 effective stress is replaced with the von Mises stress that can boil any complex stress conditions  
 205 down to a single representative scalar value. Therefore, Eq. (17) may be expressed as

$$206 \quad \dot{\epsilon}_{diss}^{PS} \approx \frac{3V_m^2 k_+}{RTd} \left( \frac{\sigma_{VM}}{R_c} - \sigma_c \right), \quad (19)$$

$$207 \quad \sigma_{VM} = \sqrt{\frac{3}{2} \boldsymbol{\sigma} : \boldsymbol{\sigma}}, \quad (20)$$

208 where  $\sigma_{VM}$  [Pa] is the von Mises stress. When the system is assumed to be simple cubic packing  
 209 with uniformly sized contacting spheres (**Figure 3**), the volumetric rate induced by the pressure  
 210 dissolution can be defined by

$$211 \quad \dot{V}_{diss}^{PS} = \frac{\Delta d \cdot d^2}{\Delta t} = \dot{\epsilon}_{diss}^{PS} d^3 = \frac{3V_m^2 k_+ d^2}{RT} \left( \frac{\sigma_{VM}}{R_c} - \sigma_c \right), \quad (21)$$

212 where  $\dot{V}_{diss}^{PS}$  [ $\text{m}^3 \text{s}^{-1}$ ] is the volumetric rate of the pressure dissolution. The dissolution rate, with  
 213 respect to the representative element, can be simply evaluated by dividing the volumetric rate by  
 214 the molar volume, as

$$215 \quad \frac{\dot{V}_{diss}^{PS}}{V_m} = \frac{3V_m k_+ d^2}{RT} \left( \frac{\sigma_{VM}}{R_c} - \sigma_c \right). \quad (22)$$

216 The volume of the representative element (**Figure 3**) is  $d^3$  [ $\text{m}^3$ ], and the number of grains per unit  
 217 volume should be  $d^{-3}$  [ $\text{m}^{-3}$ ]. Finally, the rate of pressure dissolution is defined by multiplying Eq.  
 218 (22) by  $d^{-3}$ , as follows:

219 
$$R_{diss}^{PS} = \frac{3V_m k_+}{RTd} \left( \frac{\sigma_{VM}}{R_c} - \sigma_c \right). \quad (23)$$

220 As the pressure dissolution proceeds, contact-area ratio  $R_c$  increases and corresponding porosity  $\phi$   
 221 decreases. Therefore, the relation between  $R_c$  and  $\phi$  should be obtained to solve Eq. (23) with time.

222 By considering the geometrical scheme (see **Figure 3** and more details in Appendix A), it is given  
 223 by

224 
$$R_c = \frac{12}{\pi} (1 - \phi) - 2. \quad (24)$$

225 Consequently, the rate of pressure dissolution is rearranged by substituting Eq. (24) into Eq. (23),  
 226 as follows:

227 
$$R_{diss}^{PS} = \frac{3V_m k_+}{RTd} \left( \frac{\sigma_{VM}}{(12/\pi)(1-\phi)-2} - \sigma_c \right). \quad (25)$$

228

## 229 2.2 Modification of porosity and related permeability

230 In this work, the change in porosity is only induced by the free-face dissolution/precipitation  
 231 and the pressure dissolution. The porosity rates evaluated by the two geochemical processes are  
 232 defined by

233 
$$\dot{\phi}^{FF} = V_m R^{FF}, \quad (26)$$

234 
$$\dot{\phi}_{diss}^{PS} = -V_m R_{diss}^{PS}, \quad (27)$$

235 where  $\dot{\phi}^{FF}$  and  $\dot{\phi}_{diss}^{PS}$  [ $s^{-1}$ ] are the porosity rates of the free-face dissolution/precipitation and the

236 pressure dissolution, respectively. Therefore, the porosity at an arbitrary time is evaluated using

237 Eqs. (26) and (27), given by

$$238 \quad \phi = \phi_i + \int \dot{\phi}^{FF} dt + \int \dot{\phi}_{diss}^{PS} dt, \quad (28)$$

239 where  $\phi_i$  [-] is the initial porosity. Once the porosity is calculated, the related permeability is also

240 evaluated by the Kozeny-Carman equation [31], as

$$241 \quad k = k_i \frac{(1-\phi_i)^2}{(1-\phi)^2} \left( \frac{\phi}{\phi_i} \right)^3, \quad (29)$$

242 where  $k$  and  $k_i$  [ $m^2$ ] are the permeability at an arbitrary time and the initial permeability,

243 respectively.

244

245

### 246 3. Model verification

247 In the previous section, we proposed a coupled THMC model to describe the evolution of

248 porosity/permeability in porous media. In order to verify the proposed model, the model

249 predictions are compared with the laboratory experiments performed by Elias and Hajash (1992)

250 [19]. The compaction of quartz sand, with a mean grain diameter of 180-250  $\mu m$ , has been

251 completed under the constant effective stresses of 69.0, 34.5, and 17.2 MPa at 150°C. The

252 changes in porosity and the silica concentrations in the pore fluid were measured over time to

253 examine the chemical and physical processes associated with the pressure solution [19]. In this  
254 work, both the rates of porosity reduction and the evolving concentrations of silica in the pore  
255 fluid were predicted. The parameters utilized in the calculations are summarized in **Table 1**.

256 In the predictions, the domain whose porosity initially starts with 0.35, equivalent to that of  
257 the experiments [19], was set to be a square with side lengths of 0.01 m. The uniaxial confining  
258 pressures of 69.0, 34.5, and 17.2 MPa and the temperature of 150°C were applied as the boundary  
259 conditions and as the initial condition, respectively. The silica concentration within the domain  
260 was initially fixed at the equilibrium concentration of quartz at 150°C, which was obtained by Eq.  
261 (13), and was followed over time by considering the free-face dissolution/precipitation and/or the  
262 pressure dissolution of quartz. All the boundaries were assumed to be thermally and hydraulically  
263 the outflow boundaries. The initial contact-area ratio,  $R_{c0}$ , was evaluated by assuming the Herzian  
264 contacts, given by

$$265 \quad R_{c0} = \left( \frac{3\sigma_{eff} \pi (1-\nu)^2}{4E} \right)^{2/3}, \quad (30)$$

266 where  $\sigma_{eff}$  [Pa] is the effective stress (i.e., 69.0, 34.5, or 17.2 MPa),  $\nu$  [-] is Poisson's ratio, and  $E$   
267 [Pa] is Young's modulus. When the pressure dissolution proceeds, the contact-area ratio increases.

268 The change is obtained using Eqs. (24), (26), and (27), as



$$\begin{aligned}
R_c &= R_{c0} + \int \dot{R}_c dt \\
&= R_{c0} - \frac{12}{\pi} \int \dot{\phi} dt \\
&= R_{c0} - \frac{12}{\pi} \int (\dot{\phi}^{FF} + \dot{\phi}^{PS}) dt \\
&= R_{c0} - \frac{12}{\pi} (\int V_m \cdot R^{FF} dt - \int V_m \cdot R^{PS} dt)
\end{aligned} \tag{31}$$

269  
270 After every time step, the new  $R_c$  was updated and used for calculating the rate of the pressure  
271 dissolution,  $R_{diss}^{PS}$ , in the following time step (see **Figure 2**). Note that in these verification  
272 predictions,  $R_{diss}^{PS}$  was evaluated over time with Eq. (23) instead of Eq. (25) because  $R_c$  can be  
273 evaluated directly with Eq. (31). It should also be noted that the specific surface area in Eq. (11)  
274 cannot be obtained from the literature [19]. Therefore, by introducing roughness factor  $f_r$  [32],  
275 which is the ratio of the true (microscopic) surface area over the apparent (geometric) surface area,  
276 the model predictions were conducted. The relation between specific surface area  $A$  and  
277 roughness factor  $f_r$  is defined as follows:

$$A = f_r A_{geo}, \tag{32}$$

279 where  $A_{geo}$  [ $m^2 m^{-3}$ ] is the apparent specific surface area, which is simply given by the ratio of the  
280 surface area of the spherical grain of diameter  $d$  over the volume, as

$$A_{geo} = \frac{\pi d^2}{\frac{\pi d^3}{6}} = \frac{6}{d}. \tag{33}$$

282 In the model predictions, three kinds of roughness factors, namely, 10, 20, and 80, were utilized.  
283 The values are congruent with the magnitude indicated by Anbeek [1992] [33], who concluded

284 that it ranged from 2.5 to 11 for freshly created surfaces, and Sverdrup [1990] [34], who reported  
285 that it varied between 1.5 and 71 for 28 silicate minerals.

286 Predictions of the porosity reduction rates and the silica concentration rates normalized by  
287 the initial values are shown in **Figure 4** and **Figure 5**, respectively, together with the data  
288 measured in the experiments. Surprisingly, all the predicted porosity reduction rates with time  
289 closely match the experimental measurements (**Figure 4**). Note that changing the roughness factor  
290 has little effect on the evolution of the porosity; and thus, the predictions with different roughness  
291 factors are not shown in **Figure 4**. In contrast, the predicted silica concentrations are clearly  
292 dependent on which roughness factors are applied (**Figure 5**). The utilization of higher roughness  
293 factors results in the prediction of lower silica concentrations. The system in the pore fluid is  
294 always oversaturated with silica because that is initially equivalent to the equilibrium  
295 concentration, and the additional solute is supplied from the grain contacts via the pressure  
296 dissolution. Therefore, the rates of precipitation are augmented by the higher roughness factors,  
297 resulting in the lower silica concentrations. The predictions show some variations because of the  
298 different roughness factors, but they follow the tendency observed in the experiments well (i.e.,  
299 the abrupt increase after applying the pressures and the gradual decrease with time). Overall, a  
300 comparison of the results of the porosity reduction and the evolving silica concentrations between  
301 the predictions and the experimental measurements gives us confidence to use the developed

302 model to examine the long-term evolution of the porosity/permeability in porous media due to the  
303 free-face dissolution/precipitation and the pressure dissolution, dependent on the applied pressure,  
304 temperature, and flow conditions.

305

306

#### 307 **4. Long-term predictions of permeability**

308 The developed model was applied to predict the long-term evolution of the permeability in  
309 sedimentary rock near radioactive wastes within a simulated repository. It should be noted that  
310 although we used actual data from related literature in the following predictions, we do not  
311 anticipate any specific sites for high-level radioactive waste repositories.

312

##### 313 *4.1 Modelling conditions*

314 The calculation domain, of the rock density of  $1700 \text{ kg/m}^3$ , was set to be a rectangle with  
315 vertical and horizontal lengths of 700 and 12.2 m, respectively. The canisters of radioactive  
316 wastes were virtually installed as a heat source by setting them laterally at a depth of 450 m [35].  
317 The horizontal length of 12.2 m was chosen for the domain because it may be one-half of the  
318 center-to-center spacing of each cavity, of the diameter 2.22 m [35] (**Figure 6**). The rock for the  
319 calculations was assumed to have been fully-saturated with water and to have been composed

320 purely of quartz, with the initial porosity of 0.40 [36]. The hydraulic and thermal gradients were  
321 set to be 1/1000 and 5°C/100 m, respectively [37]. The surface temperature was fixed at 15°C.  
322 The initial silica concentrations within the domain were assumed to be the equilibrium values,  
323 which were evaluated by Eq. (13). The change in pH was not considered and the initial value was  
324 set at  $\text{pH} = 7$ .

325 In this work, the Excavation Distributed Zone (EDZ) was modeled explicitly with respect to  
326 the rock permeability. The scientific and technical report, summarizing the HLW disposal  
327 construction in Japan [38], indicates that the EDZ in both sedimentary and crystalline rocks may  
328 range, in the radial direction, from the periphery of the excavated cavity to roughly 1 m. Therefore,  
329 the range of 0.8 m was modeled as the EDZ in our calculations (**Figure 6**). The permeability in  
330 the EDZ was increased by two orders of magnitude greater than the sound rock [35], [39]. Note  
331 that the thermal and the mechanical properties in the EDZ were assumed to be equivalent to those  
332 of sound rock, because those in the EDZ were ill-defined, and examining the changes in  
333 permeability due to geochemical processes is the most significant task in this work. In the actual  
334 calculations, the changes in the von Mises stresses, due to the excavation, were predicted by  
335 conducting a self-weight analysis (**Figure 7**). The evolved von Mises stresses, greater around the  
336 periphery of the cavity, as is apparent in **Figure 7**, are the driving-force for the pressure  
337 dissolution (see Eq. (25)). The heat source from the radioactive wastes was modeled by applying

338 the temperatures at the periphery of the cavity as the boundary conditions. The applied  
339 temperatures over time were obtained from the literature [38], as shown in **Figure 8**. The  
340 prediction period was set at  $10^4$  years after the excavation. All the boundaries, excluding the  
341 periphery of the cavity, were assumed to be thermally and hydraulically the outflow boundaries.  
342 The parameters utilized in the calculations are summarized in **Table 2**.

343

#### 344 *4.2 Prediction results*

345 In this work, the predictions were conducted for two different cases – one was done by  
346 considering the full processes illustrated in **Figure 2**, and the other was done by excluding only  
347 the pressure dissolution, in order to examine the effect of the pressure dissolution on the change in  
348 permeability with time. The former and the latter cases are called the “PS” and the “no-PS”  
349 conditions hereinafter. Calculations for the no-PS condition were performed by merely making  
350  $R_{diss}^{PS}$  in Eq. (25) zero at all the calculation steps.

351 The change in the temperature distribution with time, predicted under the PS condition, is  
352 shown in **Figure 9**. The temperature in the EDZ increases with time; it increases to more than  
353  $80^{\circ}\text{C}$  between  $10^1$  and  $10^2$  years. Subsequently, it decreases with time and reaches a steady  
354 temperature (i.e.,  $\sim 45^{\circ}\text{C}$ ) after  $10^4$  years. This tendency is quite similar to the change in Si  
355 concentration with time (**Figure 10**), which is reasonable. As the equilibrium concentration of Si

356 is only controlled by the induced temperature, the changes over time should be similar. It should  
357 be noted that the predicted changes in both temperature and the Si concentration with time, under  
358 the no-PS condition, show no great difference from those under the PS condition. This is because  
359 the concentrations in the whole system approach the equilibrium values in a relatively short  
360 period, through free-face precipitation, when additional solute is supplied in the pore fluid due to  
361 the pressure dissolution, and through free-face dissolution, when the system temperature and the  
362 related equilibrium concentration increase. Consequently, the Si concentrations are equivalent to  
363 the equilibrium values throughout most of the calculation period.

364 The changes in permeability with time under the no-PS and the PS conditions are compared  
365 (**Figure 11** and **Figure 12**). Note that the permeability is normalized by the initial value. As is  
366 apparent from the figures, it changes little with time under the no-PS condition, while it decreases  
367 with time and the reduction appears after  $10^2$  years under the PS condition. Specifically, the  
368 reduction is significant within the EDZ. This is because the pressure dissolution, resulting in  
369 porosity reduction, is enhanced by the increase in the von Mises stress due to the cavity  
370 excavation (see **Figure 7**), and an additional reduction in porosity is caused by the free-face  
371 precipitation induced by the supply of the dissolved silica through the pressure dissolution. In  
372 order to further investigate the influence of the pressure dissolution on the permeability change  
373 within the EDZ, the changes with time at four specific locations, shown in **Figure 13**, are depicted

374 in **Figure 14**. Three of the four points are located within the EDZ, and the fourth one is 5 m away  
375 from the periphery of the cavity. No change in permeability is observed under the no-PS condition.  
376 In reality, the free-face precipitation of the secondary minerals, induced by the dissolution of the  
377 cement materials, may cause changes in the porosity/permeability, but it is not the case in this  
378 work. On the other hand, the permeability at No. 1 decreases by one order of magnitude in  $10^4$   
379 years. However, the reduction is locally limited and is not observed at No. 4, which is located at  
380 one-fourth of the center-to-center spacing of each cavity (**Figure 14**). In the current predications,  
381 the decrease in permeability was observed only under the PS condition. This should result in the  
382 delay of the transportation of radioactive materials, and the influence needs to be examined  
383 quantitatively.

384 As a parametric study, predictions are made by varying the parameters of initial porosity  $\phi_i$   
385 and critical stress  $\sigma_c$ , that should control the rate of the pressure dissolution (see Eq. (25)) to  
386 examine the influence on the change in permeability. Two different initial porosities, 0.40 and  
387 0.45, are selected to simulate Horonobe mudstone in Japan [36], and three levels of critical stress,  
388 15, 50, and 80 MPa, are set for the analysis. The change in permeability at observation point No. 1,  
389 shown in **Figure 13**, is shown in **Figure 15**. It is obvious that when a higher critical stress is  
390 applied, less change in permeability is observed. This is because the effect of the pressure  
391 dissolution becomes smaller when the difference between the von Mises stress and the critical

392 stress is smaller, as is clear from Eq. (25). In particular, at 80 MPa, the permeability hardly  
393 changes in the case of  $\phi_i = 0.40$ , and it decreases roughly 30 % for  $10^4$  years in the case of 0.45.  
394 From the above calculations, we have confirmed that choosing the right values for the critical  
395 stress is of great importance to achieving precise predictions.

396

397

## 398 **5. Conclusions**

399 A coupled THMC model was developed to investigate the long-term evolution of the  
400 permeability in sedimentary rocks. The model solves the heat transfer, the groundwater flow, the  
401 variation in induced stresses, and the geochemical reactions (i.e., the free-face  
402 dissolution/precipitation and the pressure dissolution), and their interactions. The changes in  
403 porosity and silica concentration in the quartz aggregates were examined to test the adequacy of  
404 the developed model in representing the experimentally observed behavior [19]. The predictions  
405 showed an excellent agreement with the experimental observations. Subsequently, the verified  
406 model was applied to examine the influence of the pressure dissolution on the evolution of the  
407 permeability in sedimentary rocks where a radioactive waste repository may be constructed, in  
408 considering the expected temperature, flow, and stress conditions. The predictions confirmed that  
409 the process of the pressure dissolution decreased the permeability especially close to the



410 excavated cavity by one order of magnitude smaller than the initial value, which should delay the  
411 transportation of the radioactive materials.

412 The developed model is straightforward and relatively simple because some interactions  
413 among the THMC processes are omitted, but it enables the long-term evolution of the  
414 permeability under arbitrary stress and temperature conditions to be followed over time with some  
415 precision. Generally, when considering coupling processes for solving complicated nonlinear  
416 problems, the uncertainty should be significant. Therefore, it is always important to ponder  
417 whether complex, fully-coupled models are necessary for achieving sufficiently high precision. In  
418 the near future, we will update the current model by taking into account the omitted processes  
419 among the THMC interactions (e.g., the hydraulic-mechanical interactions; see **Figure 1**), and  
420 examine whether or not the updates are indeed meaningful to the problems of interest.

421

422

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429

430

### 431 **APPENDIX A: Relation between contact-area ratio and porosity**

432 Solid volume  $V_s$ , in the representative elementary volume, is obtained by subtracting the  
433 sums of the volumes truncated between the contacts of two hemispheres from the volume of a  
434 sphere of diameter  $d$ , given by

$$435 \quad V_s = \frac{1}{6} \pi h \left( 3a^2 + \frac{3d^2}{4} + h^2 \right), \quad (\text{A1})$$

436 where  $h$  is one-half of the domain height and  $a$  is the radius of the contact area. One-half of the  
437 domain height,  $h$ , is given by

$$438 \quad h = \sqrt{\frac{d^2}{4} - a^2}. \quad (\text{A2})$$

439 The porosity,  $\phi$ , is obtained by subtracting the solid volume,  $V_s$ , divided by the total volume of the  
440 domain,  $V_t$ , from one, as follows:

$$441 \quad \phi = 1 - \frac{V_s}{V_t} = 1 - \frac{\frac{1}{6} \pi \sqrt{\frac{d^2}{4} - a^2} (2a^2 + d^2)}{d^2 \sqrt{\frac{d^2}{4} - a^2}} = 1 - \frac{\pi(2a^2 + d^2)}{6d^2}. \quad (\text{A3})$$

442 The radius of the contact area is expressed by

$$443 \quad a^2 = \frac{d^2}{4} R_c. \quad (\text{A4})$$

444 By substituting Eq. (A3) into Eq. (A2), porosity  $\phi$  is rearranged as

445 
$$\phi = 1 - \frac{\pi \left( \frac{d^2}{2} R_c + d^2 \right)}{6d^2} = 1 - \left\{ \frac{\pi}{12} (R_c + 2) \right\}. \quad (\text{A5})$$

446 
$$\Rightarrow R_c = \frac{12}{\pi} (1 - \phi) - 2. \quad (\text{A6})$$

447

448

449 **Nomenclature**

450	$A$	specific surface area [ $\text{m}^2 \text{m}^{-3}$ ]
451	$A_{BET}$	specific surface area determined by the BET method [ $\text{m}^2 \text{kg}^{-1}$ ]
452	$A_c$	area of the grain contact [ $\text{m}^2$ ]
453	$A_{geo}$	apparent specific surface area [ $\text{m}^2 \text{m}^{-3}$ ]
454	$a_{H^+}$	activity of $H^+$ [-]
455	$C_i$	concentration of the solute $i$ [ $\text{mol m}^{-3}$ ]
456	$C_{p,m}$	heat capacity of the solid [ $\text{J kg}^{-1} \text{K}^{-1}$ ]
457	$C_{p,w}$	heat capacity of the fluid [ $\text{J kg}^{-1} \text{K}^{-1}$ ]
458	$D$	potential head of the fluid [m]
459	$\mathbf{D}_{b,i}$	diffusion coefficient tensor [ $\text{m}^2 \text{s}^{-1}$ ]
460	$d$	grain diameter [m]
461	$\mathbf{E}$	elasticity tensor [Pa]
462	$E_{D,i}$	activation energy of the diffusion of the solute $i$ [ $\text{J mol}^{-1}$ ]
463	$E_{k^+}$	activation energy of the mineral dissolution [ $\text{J mol}^{-1}$ ]
464	$E_m$	heat of fusion [ $\text{kJ mol}^{-1}$ ]
465	$\mathbf{F}_v$	body force [ $\text{Pa m}^{-1}$ ]
466	$f_m$	source term for flow [ $\text{kg m}^{-3} \text{s}^{-1}$ ]
467	$f_r$	roughness factor [-]
468	$g$	gravity acceleration [ $\text{m s}^{-2}$ ]
469	$K$	equilibrium constant [-]
470	$\mathbf{k}$	rock permeability tensor [ $\text{m}^2$ ]
471	$\mathbf{k}_{eq}$	equilibrium thermal conductivity tensor [ $\text{W m}^{-1} \text{K}^{-1}$ ]

472	$\mathbf{k}_m$	thermal conductivity tensor of the solid [ $\text{W m}^{-1} \text{K}^{-1}$ ]
473	$\mathbf{k}_w$	thermal conductivity tensor of the fluid [ $\text{W m}^{-1} \text{K}^{-1}$ ]
474	$k_+$	dissolution rate constant [ $\text{mol m}^{-2} \text{s}^{-1}$ ]
475	$\dot{M}_{diss}^{PS}$	rate of addition of dissolved mass into solution at the interface [ $\text{kg s}^{-1}$ ]
476	$p$	fluid pressure [Pa]
477	$Q$	ionic activity product [-]
478	$Q_h$	heat source [ $\text{W m}^{-3}$ ]
479	$R$	gas constant [ $\text{J mol}^{-1} \text{K}^{-1}$ ]
480	$R_c$	contact-area ratio [-]
481	$R_i^{FF}$	rate of free-face dissolution/precipitation of the solute $i$ [ $\text{mol m}^{-3} \text{s}^{-1}$ ]
482	$R_{diss,i}^{PS}$	rate of pressure dissolution of the solute $i$ [ $\text{mol m}^{-3} \text{s}^{-1}$ ]
483	$R_i$	solite source or sink of the solute $i$ [ $\text{mol m}^{-3} \text{s}^{-1}$ ]
484	$T$	system temperature [K]
485	$T_m$	temperature of fusion [K]
486	$\mathbf{u}$	fluid velocity tensor [ $\text{m s}^{-1}$ ]
487	$\dot{V}_{diss}^{PS}$	volumetric rate of the pressure dissolution [ $\text{m}^3 \text{s}^{-1}$ ]
488	$V_m$	molar volume [ $\text{m}^3 \text{mol}^{-1}$ ]
489	$V_s$	solid volume [ $\text{m}^3$ ]
490		
491	<u>Greek letters</u>	
492	$\boldsymbol{\varepsilon}$	strain tensor [-]
493	$\dot{\boldsymbol{\varepsilon}}_{diss}^{PS}$	strain rate due to the pressure dissolution [ $\text{s}^{-1}$ ]

494	$\phi$	porosity [-]
495	$\dot{\phi}^{FF}$	porosity rate of the free-face dissolution/precipitation [ $s^{-1}$ ]
496	$\dot{\phi}_{diss}^{PS}$	porosity rate of the pressure dissolution [ $s^{-1}$ ]
497	$\mu$	dynamic viscosity of the fluid [Pa s]
498	$\nu$	Poisson's ratio [-]
499	$\rho_g$	grain density [ $kg\ m^{-3}$ ]
500	$\rho_m$	density of the solid [ $kg\ m^{-3}$ ]
501	$\rho_w$	density of the fluid [ $kg\ m^{-3}$ ]
502	$(\rho C_p)_{eq}$	equilibrium volumetric heat capacity [ $J\ K^{-1}\ m^{-3}$ ]
503	$\sigma$	stress tensor [Pa]
504	$\sigma_a$	stress acting at the contact area [Pa]
505	$\sigma_c$	critical stress [Pa]
506	$\sigma_{eff}$	effective stress [Pa]
507	$\sigma_{VM}$	von Mises stress [Pa]
508	$\tau$	tortuosity [-]
509		

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608

609

610 List of Tables

611

612 Table 1. Calculation parameters to simulate experimental results.

613 Table 2. Calculation parameters to simulate long-term permeability.

614

615

616

Table 1. Calculation parameters to simulate experimental results.

Diameter $d$ [ $\mu\text{m}$ ]	Temperature $T$ [ $^{\circ}\text{C}$ ]	Effective stress $\sigma_{eff}$ [MPa]	Critical stress $\sigma_c$ [MPa]	Equilibrium constant $K$ [ $\text{mol m}^{-3}$ ]
215	150	69.0, 34.5, 17.2	73.2	1.79
Diffusion coefficient $D_b$ [ $\text{m}^2\text{s}^{-1}$ ]	Dissolution rate constant $k_+$ [ $\text{mol m}^{-2}\text{s}^{-1}$ ]	Young's modulus $E$ [GPa]	Poisson's ratio $\nu$ [-]	
$1.12 \times 10^{-9}$	$2.51 \times 10^{-9}$	72.4	0.17	

617

618

619

Table 2. Calculation parameters to simulate long-term permeability.

Rock type	Initial permeability $k_i$ [ $\text{m}^2$ ]	Young's modulus $E$ [GPa]	Poisson's ratio $\nu$ [-]	Initial porosity $\phi_i$ [-]	Thermal conductivity $k_{eq}$ [ $\text{W m}^{-1}\text{K}^{-1}$ ]	Heat capacity $C_p$ [ $\text{J kg}^{-1}\text{K}^{-1}$ ]
EDZ	$1.0 \times 10^{-13}$	2.5	0.30	0.40	1.60	1500
Sound	$1.0 \times 10^{-15}$	2.5	0.30	0.40	1.60	1500

620

621

622 List of Figures

623

624 Figure 1. THMC interactions considered in the developed numerical model.

625 Figure 2. Sequential procedure to conduct consistent calculations of porosity change with time.

626 Figure 3. Geometrical model of grain-to-grain contact. Initially, two grains contact each other

627 with an initial contact-area ratio of  $Rc0$ . As compaction proceeds due to the pressure solution,

628 contact-area ratio  $Rc$  increases and free-face dissolution/precipitation occurs simultaneously,

629 resulting in porosity modification.

630 Figure 4. Comparison of porosity reduction with time between experimental data [19] and

631 predictions of the model.

632 Figure 5. Comparison of silica concentration in pore fluid between experimental data [19] and

633 predictions of the model.

634 Figure 6. Calculation domain. The calculation domain is a rectangle with vertical and horizontal

635 lengths of 700 and 12.2 m, respectively. The cavity, with a diameter of 2.22 m, is excavated by

636 lateral setting at a depth of 450 m. The EDZ ranges, in the radial direction, from the cavity wall

637 to 0.8 m.

638 Figure 7. Distribution of von Mises stress before and after cavity excavation.

639 Figure 8. Temperature change with time that is used as the boundary condition applied on the

640 periphery of the cavity [38].

641 Figure 9. Change in temperature distribution with time in the range of 100 to 104 years under the  
642 PS condition.

643 Figure 10. Change in Si concentration distribution with time in the range of 100 to 104 years  
644 under the PS condition.

645 Figure 11. Change in normalized permeability with time in the range of 100 to 104 years under  
646 the no-PS condition. No permeability change is confirmed.

647 Figure 12. Change in normalized permeability with time in the range of 100 to 104 years under  
648 the PS condition. The permeability decreases with time. The reduction is especially significant  
649 around the periphery of the cavity.

650 Figure 13. Specific locations where changes in permeability with time are observed.

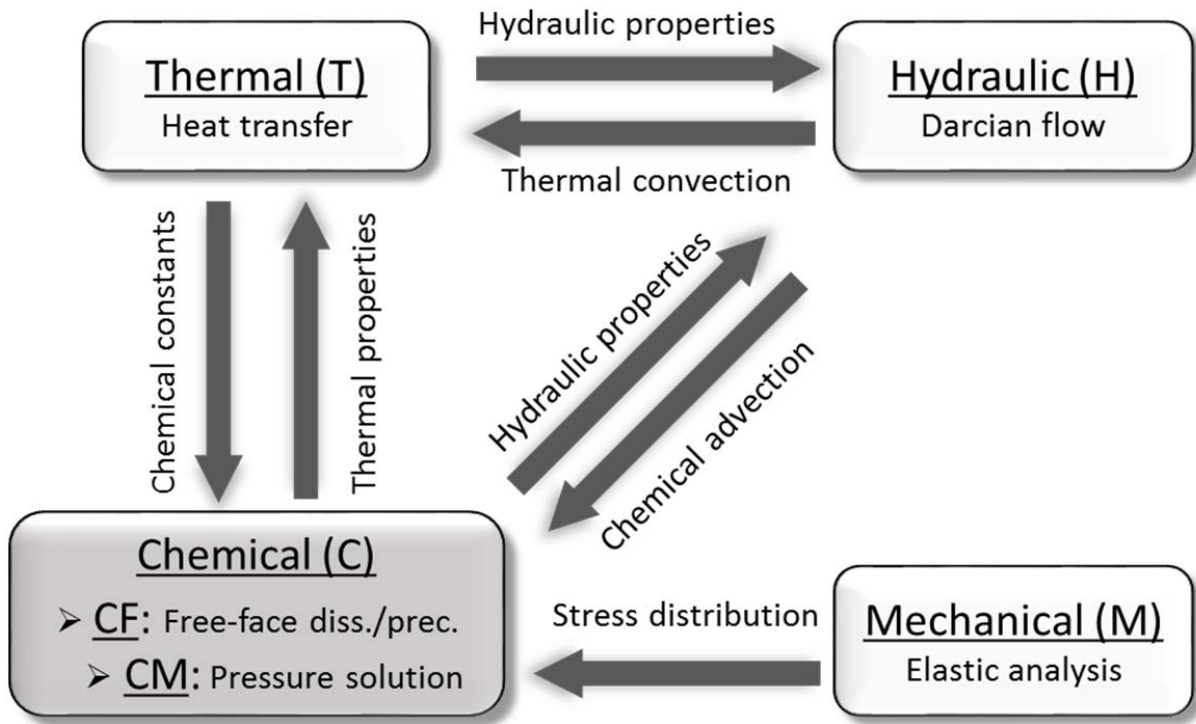
651 Figure 14. The permeability changes with time at specific locations indicated in Figure 13((a) the  
652 no PS condition and (b) the PS condition).

653 Figure 15. The permeability changes with time under the PS condition at No. 1, indicated in  
654 Figure 13((a) initial porosity of 0.40 and (b) 0.45).

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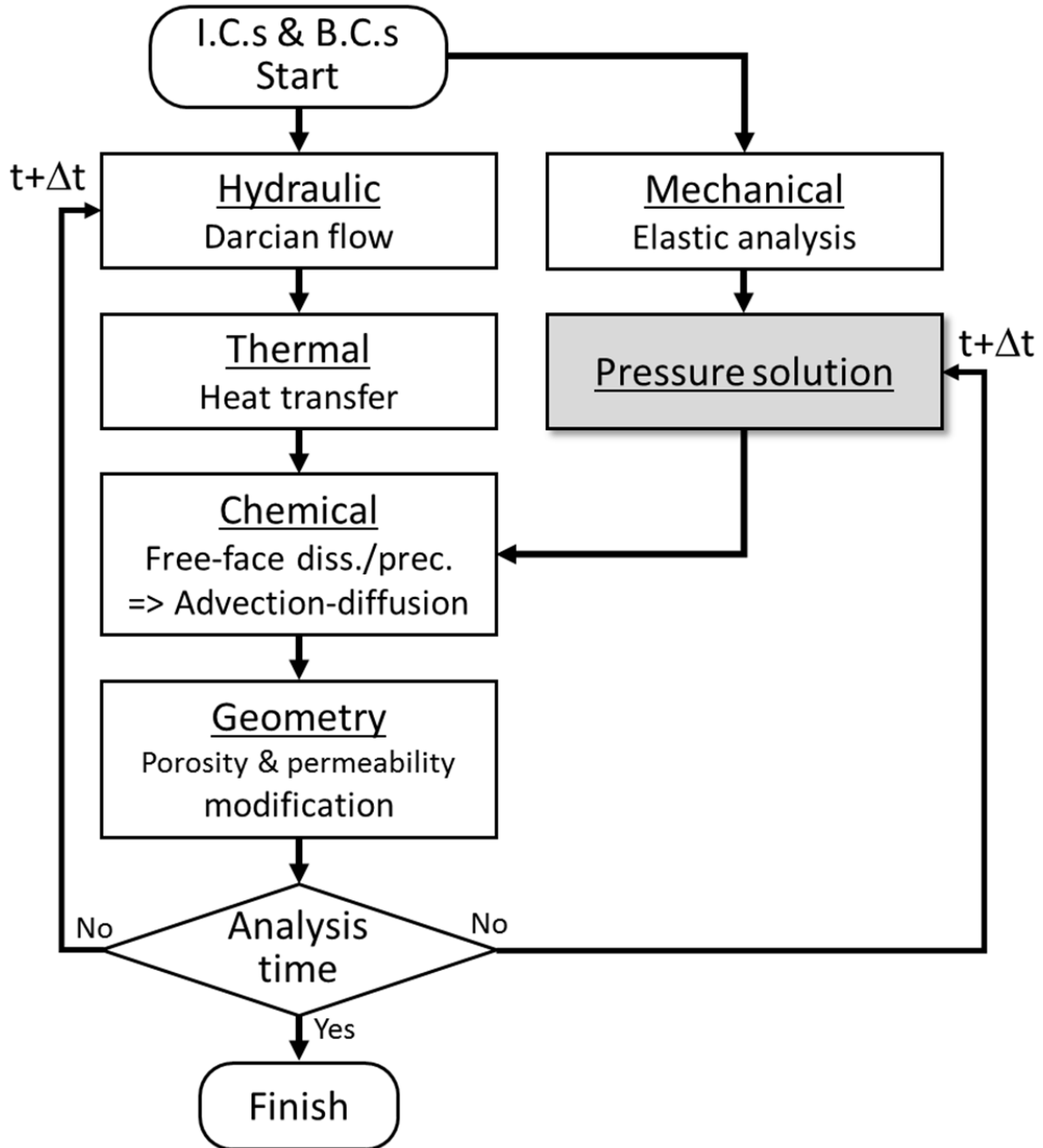


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658 Figure 1. THMC interactions considered in the developed numerical model.

659

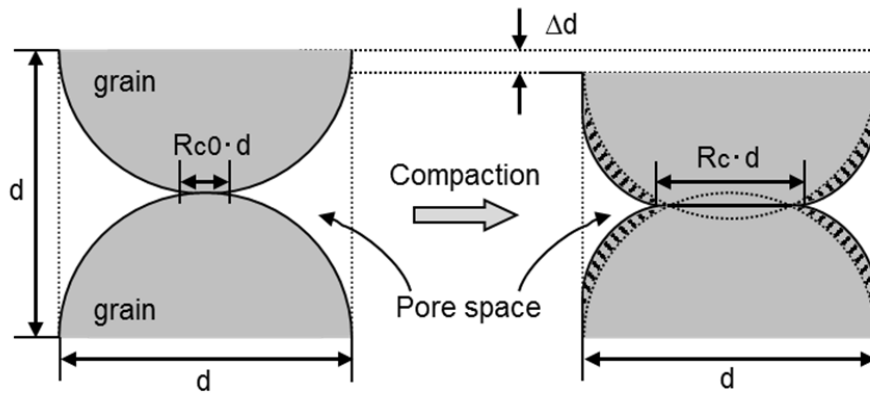
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661

662 Figure 2. Sequential procedure to conduct consistent calculations of porosity change with time.

663



664

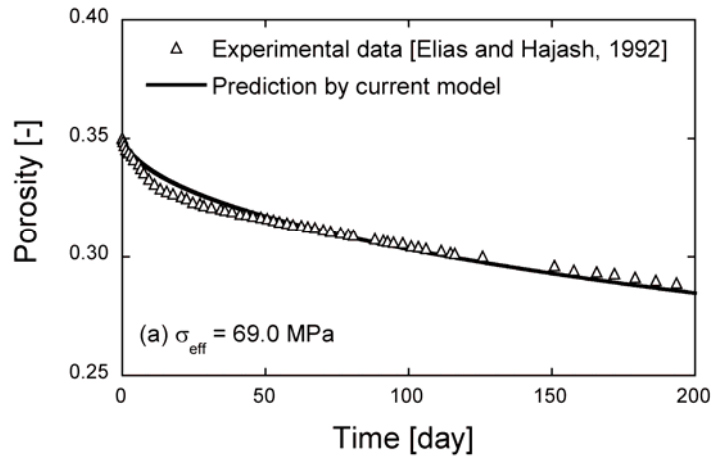
665 Figure 3. Geometrical model of grain-to-grain contact. Initially, two grains contact each other

666 with an initial contact-area ratio of  $R_{c0}$ . As compaction proceeds due to the pressure solution,

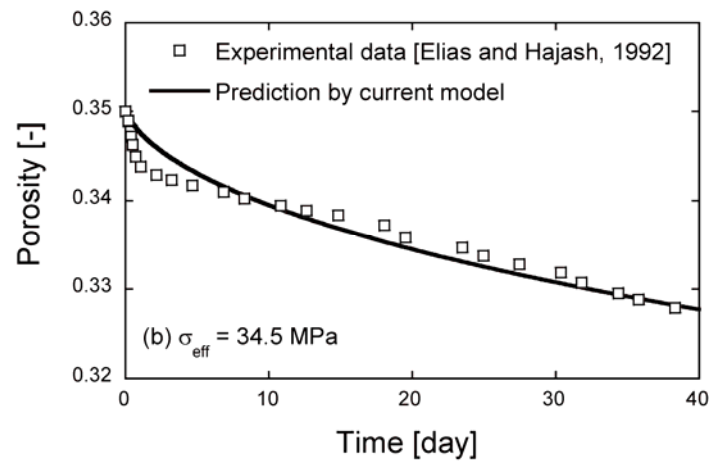
667 contact-area ratio  $R_c$  increases and free-face dissolution/precipitation occurs simultaneously,

668 resulting in porosity modification.

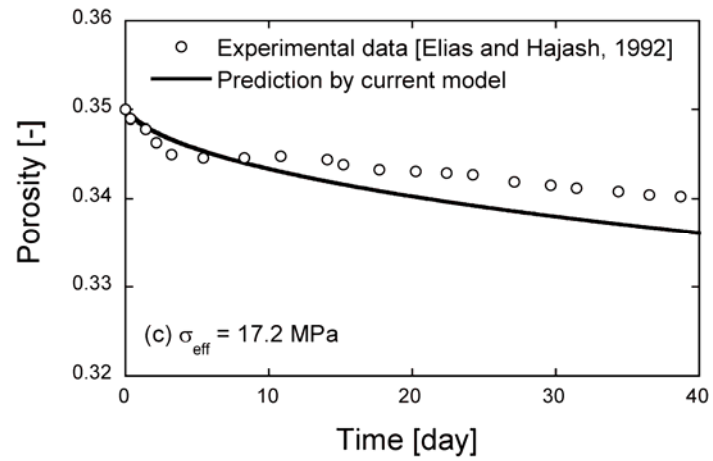
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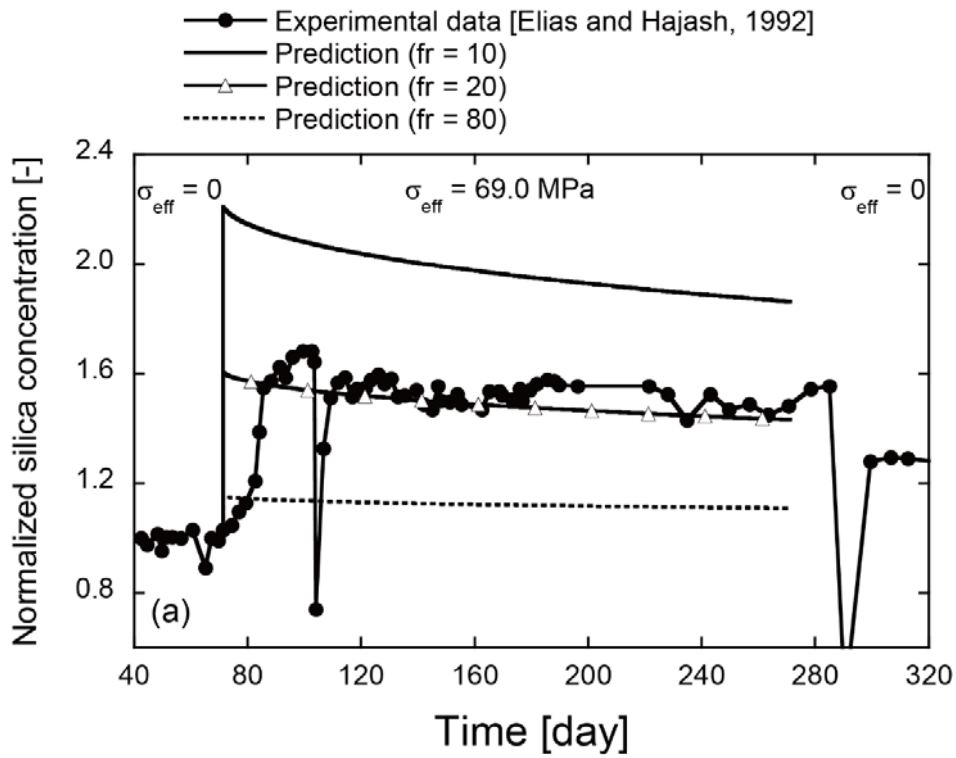
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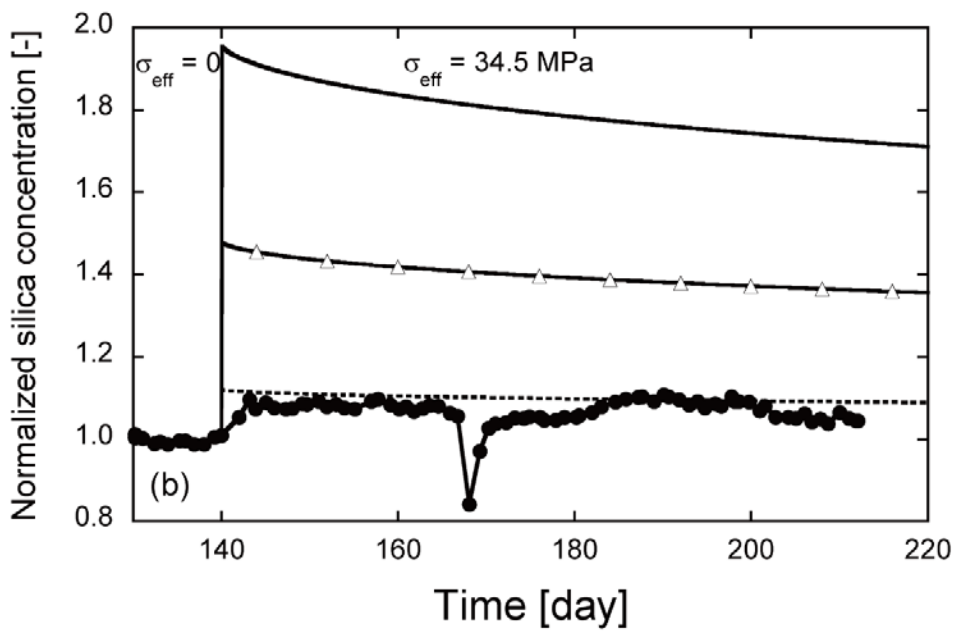
672

673 Figure 4. Comparison of porosity reduction with time between experimental data [19] and  
 674 predictions of the model.

675



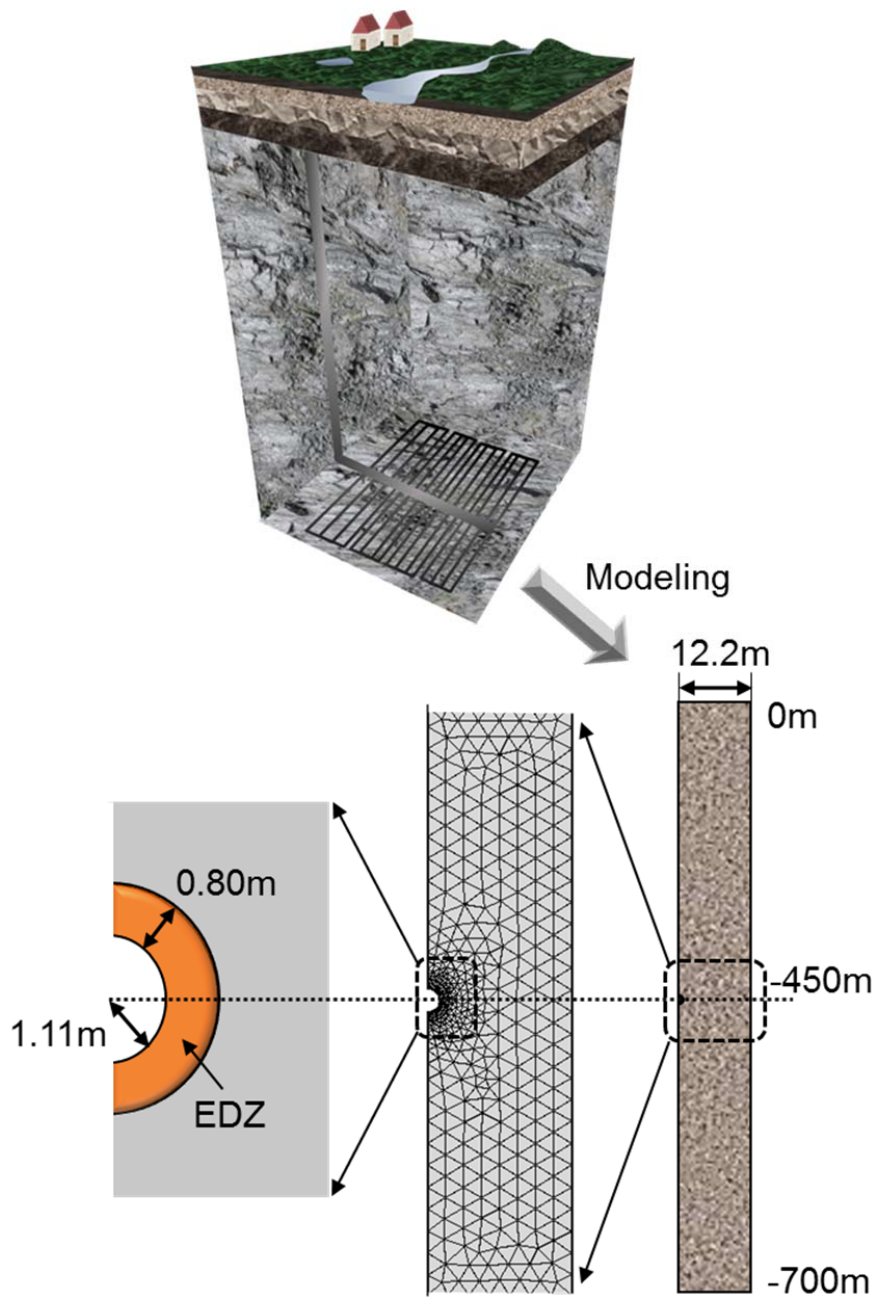
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677

678 Figure 5. Comparison of silica concentration in pore fluid between experimental data [19] and  
 679 predictions of the model.





681

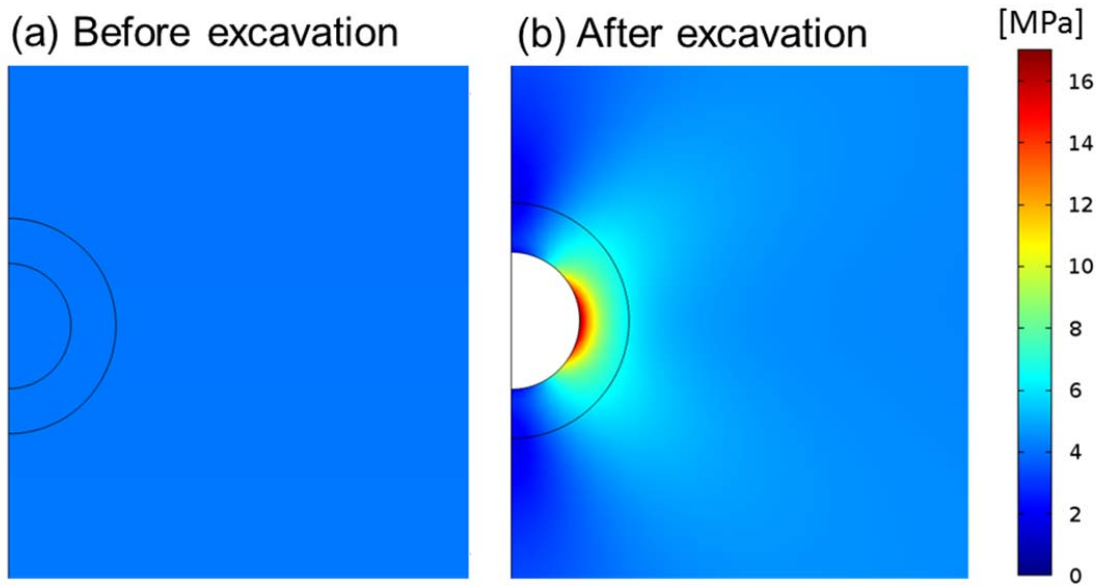
682 Figure 6. Calculation domain. The calculation domain is a rectangle with vertical and horizontal

683 lengths of 700 and 12.2 m, respectively. The cavity, with a diameter of 2.22 m, is excavated by

684 lateral setting at a depth of 450 m. The EDZ ranges, in the radial direction, from the cavity wall to

685 0.8 m.

686



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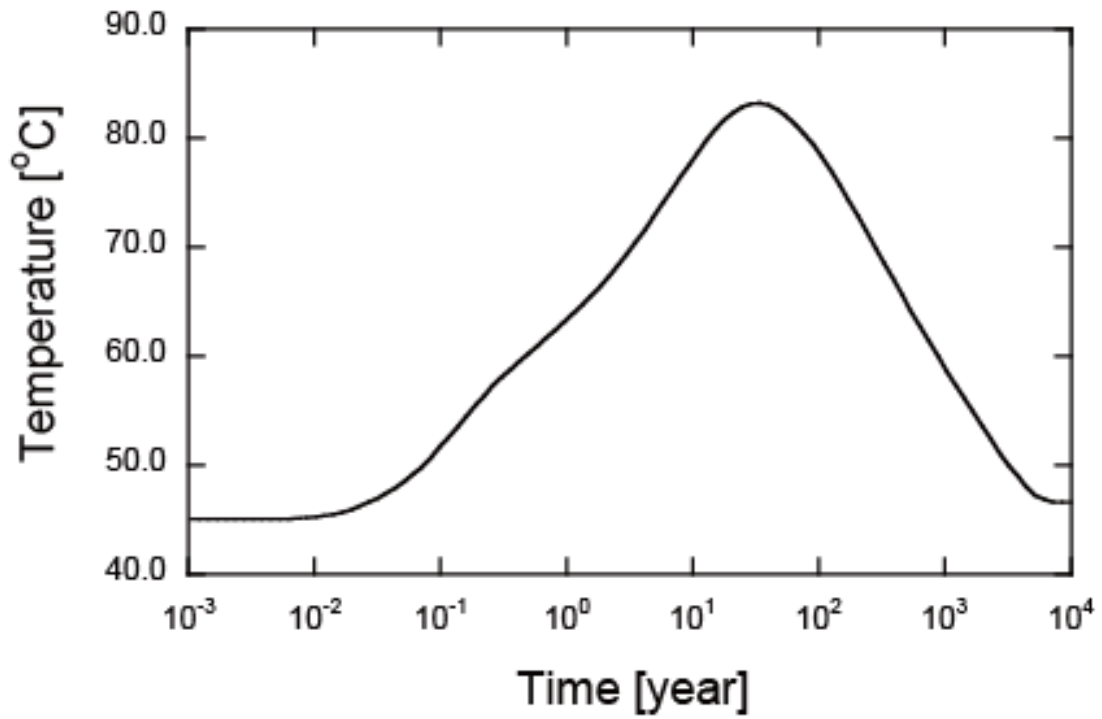
688 Figure 7. Distribution of von Mises stress before and after cavity excavation.

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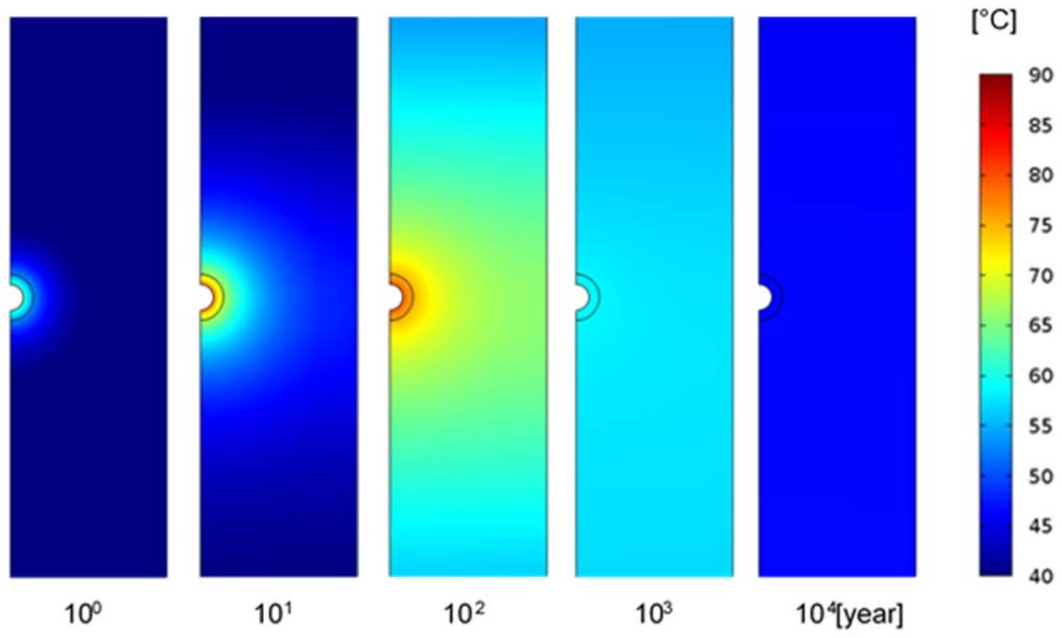
693 Figure 8. Temperature change with time that is used as the boundary condition applied on the

694 periphery of the cavity [38].

695

696

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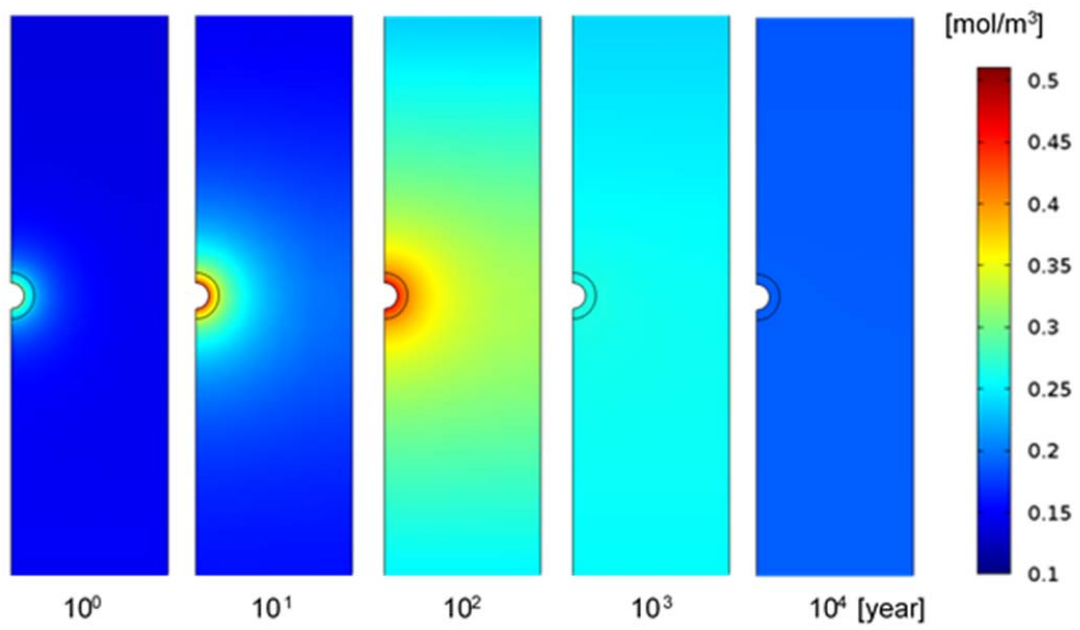


698

699 Figure 9. Change in temperature distribution with time in the range of  $10^0$  to  $10^4$  years under the

700 PS condition.

701

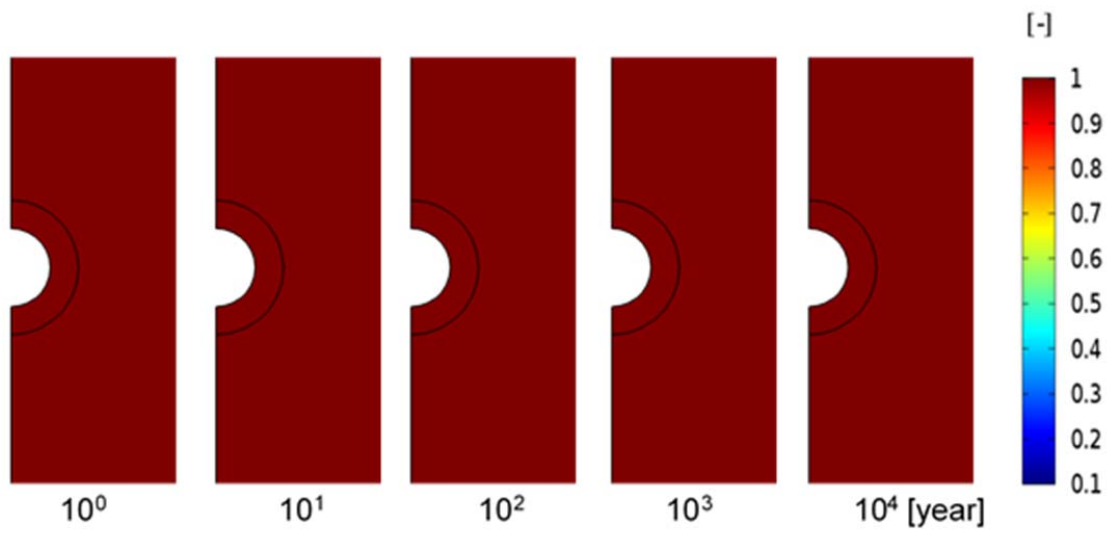


702

703 Figure 10. Change in Si concentration distribution with time in the range of  $10^0$  to  $10^4$  years under  
704 the PS condition.

705

706

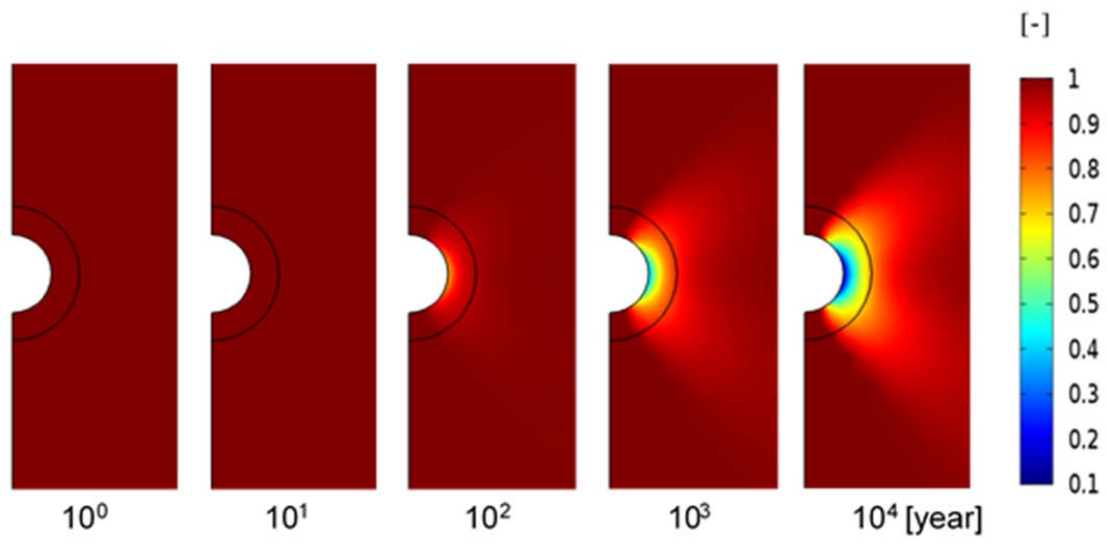


707

708 Figure 11. Change in normalized permeability with time in the range of  $10^0$  to  $10^4$  years under the

709 no-PS condition. No permeability change is confirmed.

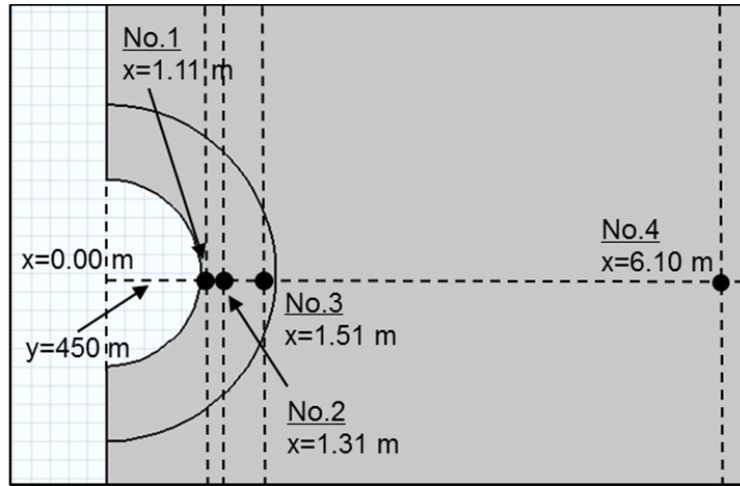
710



711  
 712 Figure 12. Change in normalized permeability with time in the range of  $10^0$  to  $10^4$  years under the  
 713 PS condition. The permeability decreases with time. The reduction is especially significant around  
 714 the periphery of the cavity.

715

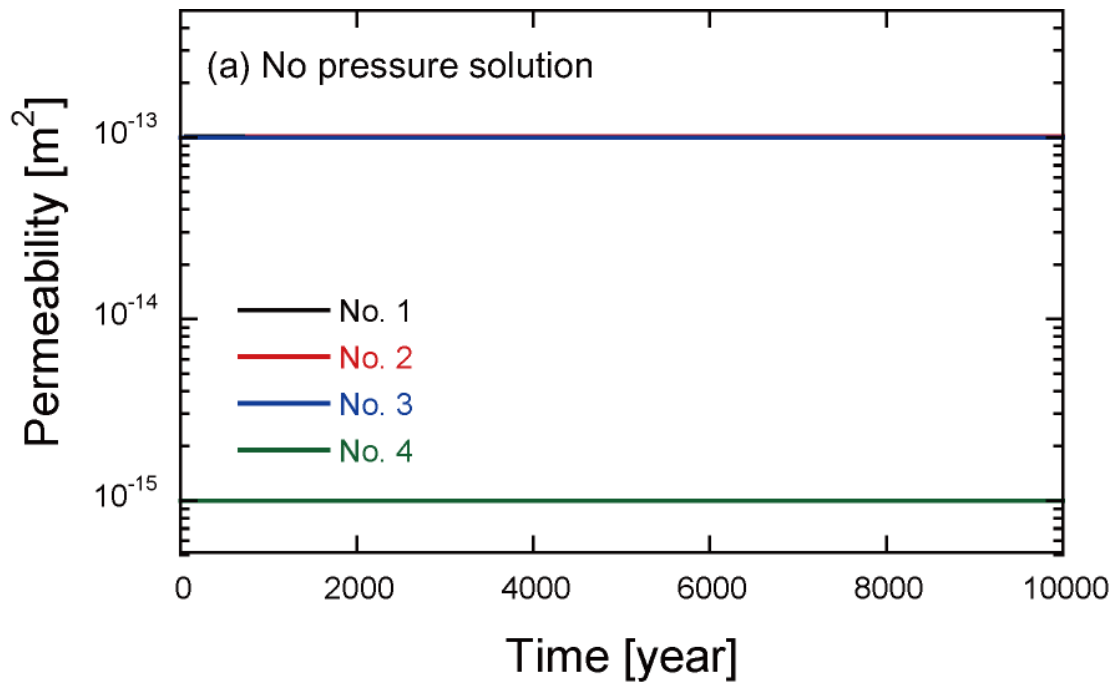
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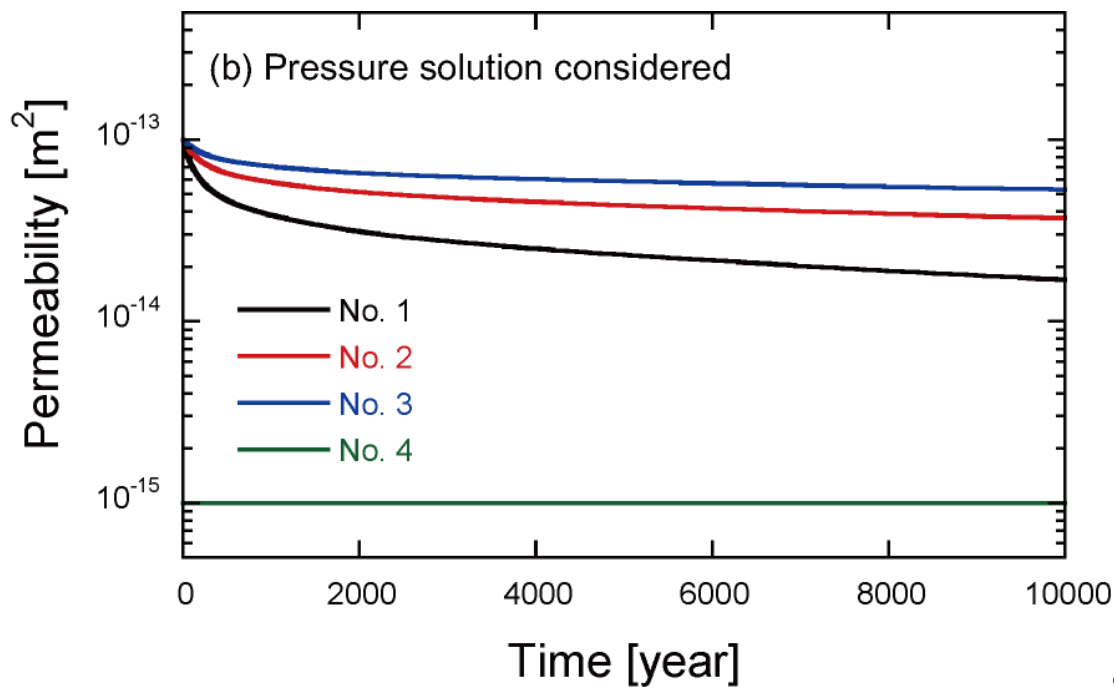
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718 Figure 13. Specific locations where changes in permeability with time are observed.

719



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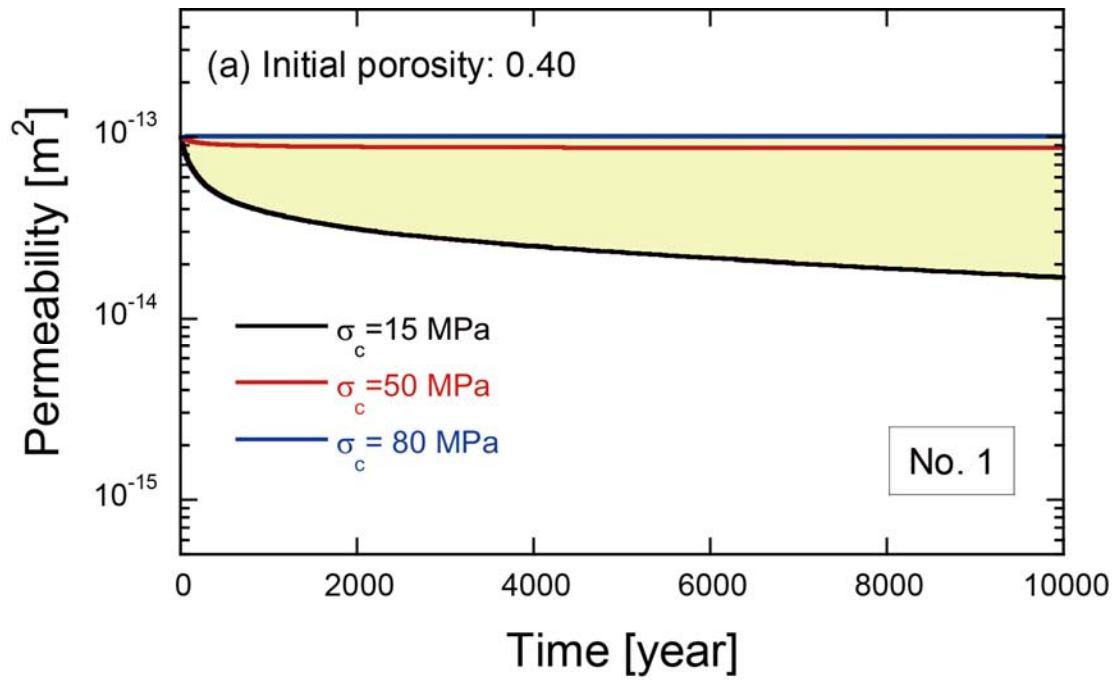


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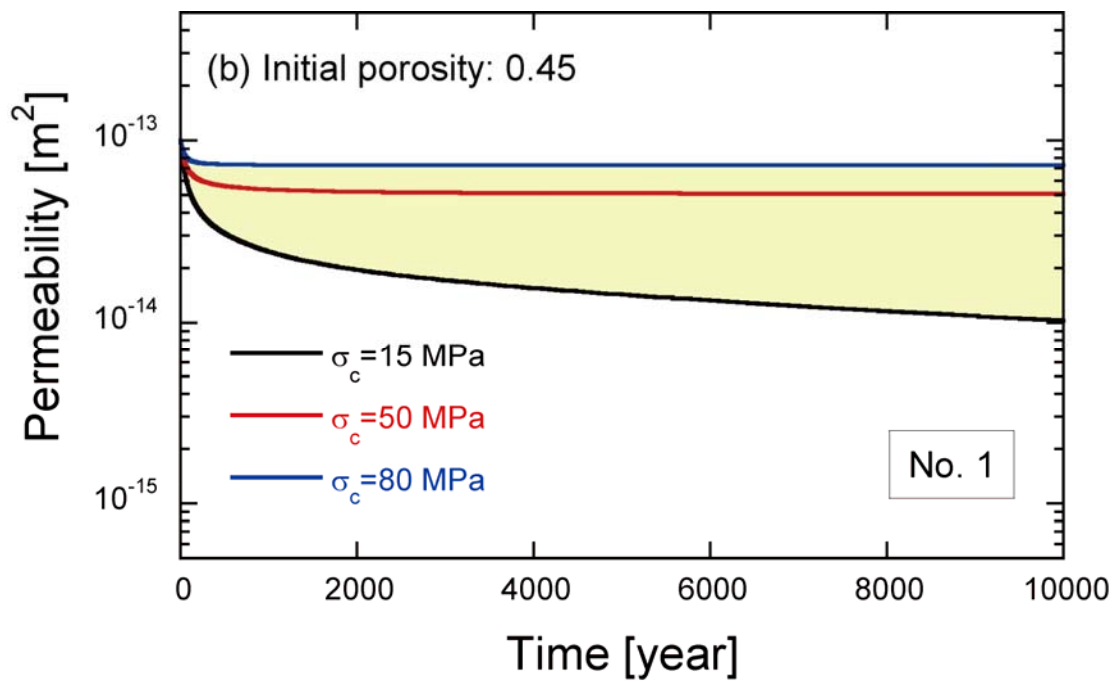
9

722 Figure 14. The permeability changes with time at specific locations indicated in Figure 13((a) the  
 723 no PS condition and (b) the PS condition).

724



725



726

727 Figure 15. The permeability changes with time under the PS condition at No. 1, indicated in

728 Figure 13((a) initial porosity of 0.40 and (b) 0.45).

729