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<td>石井 晶</td>
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Tests of Mean Vectors in High-Dimension, 
Low-Sample-Size Context

Aki Ishii

Graduate School of Pure and Applied Sciences, University of Tsukuba, Ibaraki, Japan

Abstract: A common feature of high-dimensional data is that the data dimension is high, however, the sample size is relatively low. We call such data HDLSS data. In this paper, we consider a new one-sample test and two-sample test for high-dimensional data under the strongly spiked eigenvalue (SSE) model. We focus on the asymptotic properties of the first principal component to provide new test procedures. We consider HDLSS asymptotic theories as the dimension grows for both the cases when the sample size is fixed and the sample size goes to infinity. We introduce the noise-reduction (NR) methodology and provide asymptotic properties of the largest-eigenvalue estimation. We apply the NR method to the one-sample test and two-sample test. Finally, we give simulation studies and discuss the performance of the new one-sample test procedure.

Keywords: HDLSS; Large p, small n; Noise-reduction methodology; One-sample test; Two-sample test.

1 Introduction

In this paper, we consider the one-sample test and the two-sample test for high-dimensional data. The problem of testing mean vectors has been studied by a lot of papers, however, it is still necessary to study these problems under more suitable conditions for actual high-dimensional data.

Suppose we have two independent \(d \times n_i\) data matrices, \(X_i = [x_{ij}, \ldots, x_{in_i}], i = 1, 2\), where \(x_{ij}, j = 1, \ldots, n_i\), are independent and identically distributed (i.i.d.) as a \(d\)-dimensional distribution with a mean vector \(\mu_i\) and covariance matrix \(\Sigma_i (\geq O)\). We assume \(n_i \geq 3, i = 1, 2\). The eigen-decomposition of \(\Sigma_i\) is given by \(\Sigma_i = \Lambda_i H_i H_i^T\), where \(\Lambda_i = \text{diag}(\lambda_{1(i)}, \ldots, \lambda_{d(i)})\) having \(\lambda_{1(i)} \geq \cdots \geq \lambda_{d(i)}(\geq 0)\) and \(H_i = [h_{1(i)}, \ldots, h_{d(i)}]\) is an orthogonal matrix of the corresponding eigenvectors. Let \(X_i - [\mu_1, \ldots, \mu_d] = H_i \Lambda_i^{1/2} Z_i\) for \(i = 1, 2\). Then, \(Z_i\) is a \(d \times n_i\) spherical data matrix from a distribution with the zero mean and identity covariance matrix. Let \(Z_i = [z_{1(i)}, \ldots, z_{d(i)}]^T\) and \(z_{j(i)} = (z_{j1(i)}, \ldots, z_{jn_i(i)})^T, j = 1, \ldots, d\), for \(i = 1, 2\). Note that \(E(z_{jk(i)}z_{jk'(i)}) = 0 (j \neq j')\) and \(\text{Var}(z_{j(i)}) = I_{n_i}\), where \(I_{n_i}\) is the \(n_i\)-dimensional identity matrix. Let \(z_{o(i)} = z_{j(i)} - (\overline{z}_{j(i)} - \overline{z}_{j(i)})^T, j = 1, \ldots, d; i = 1, 2\), where \(\overline{z}_{j(i)} = n_i^{-1} \sum_{k=1}^{n_i} z_{jk(i)}\). Also, note that if \(X_i\) is Gaussian, \(z_{j(i)}\)s are i.i.d. as the standard normal distribution, \(N(0, 1)\). We assume that \(\lim_{d \to \infty} E(z_{jk(i)}^4) < \infty\) for all \(i, j, k\), and \(P(\lim_{d \to \infty} ||z_{o1(i)}|| \neq 0) = 0\) for \(i = 1, 2\). As necessary, we consider the following assumption for \(z_{1k(i)}, k = 1, \ldots, n_i\):

(A-i) \(z_{1k(i)}, k = 1, \ldots, n_i\), are i.i.d. as \(N(0, 1)\) for \(i = 1, 2\).

We define \(\overline{x}_{in_i} = \sum_{j=1}^{n_i} x_{ij} / n_i\) and \(S_{in_i} = \sum_{j=1}^{n_i} (x_{ij} - \overline{x}_{in_i})(x_{ij} - \overline{x}_{in_i})^T / (n_i - 1)\) for \(i = 1, 2\). Let us write the eigen-decomposition of \(S_{in_i}\) as \(S_{in_i} = \sum_{j=1}^{d} \lambda_j(i) h_j(i) h_j(i)^T\), where \(h_j(i)\) denotes a unit eigenvector corresponding to \(\lambda_j(i)\).
A famous method to test for mean vectors is Hotelling's $T^2$ test, however, one cannot use the test statistic in the HDLSS context such as $n_{i}d ightarrow 0$, $i = 1, 2$. In order to overcome such situations, Dempster [7, 8] and Srivastava [12] considered the two-sample test when the populations $\pi_{1}$ and $\pi_{2}$ are Gaussian. When $\pi_{1}$ and $\pi_{2}$ are non-Gaussian, Bai and Saranadasa [4] and Cai et al. [5] considered the test under the homosedasticity, $\Sigma_{1} = \Sigma_{2}$, and Chen and Qin [6] and Aoshima and Yata [1, 2] considered the test under the heteroscedasticity, $\Sigma_{1} \neq \Sigma_{2}$. We note that those two-sample tests were constructed under the eigenvalue condition as follows:

$$\frac{\lambda^{2}_{1(i)}}{\text{tr}(\Sigma_{1}^{2})} \rightarrow 0 \text{ as } d \rightarrow \infty \text{ for } i = 1, 2. \quad (1.1)$$

Aoshima and Yata [3] called (1.1) the "non-strongly spiked eigenvalue (NSSE) model". On the other hand, Aoshima and Yata [3] considered the "strongly spiked eigenvalue (SSE) model" as follows:

$$\liminf_{d \rightarrow \infty} \left\{ \frac{\lambda^{2}_{1(i)}}{\text{tr}(\Sigma_{1}^{2})} \right\} > 0 \text{ for } i = 1 \text{ or } 2. \quad (1.2)$$

For the SSE model, Katayama et al. [10] considered a one-sample test when $x_{ij}$s are Gaussian. Ishii et al. [9] considered the one-sample test for non-Gaussian cases. Ma et al. [11] considered a two-sample test for the factor model. Aoshima and Yata [3] gave two-sample tests by considering eigenstructures when $d \rightarrow \infty$ and $n_{i} \rightarrow \infty$, $i = 1, 2$. In this paper, we discuss a one-sample test and a two-sample test for the SSE model when $d \rightarrow \infty$ while $n_{i}$s are fixed.

In Section 2, we introduce the noise-reduction (NR) methodology and provide asymptotic distribution of the largest-eigenvalue estimation in the HDLSS context. Then, we apply the NR method to the one-sample test for the SSE model in Section 3. In Section 4, we consider the two-sample test for the SSE model and give a new test procedure in the HDLSS context. In Section 5, we give simulation studies and discuss the performance of the new test procedure.

## 2 Asymptotic Properties of the Largest Eigenvalue

In this section, we provide asymptotic properties of the largest eigenvalue. We introduce a method for eigenvalue estimation called the noise-reduction (NR) methodology that was proposed by Yata and Aoshima [14]. See Sections 2 and 3 in Yata and Aoshima [14] for the details. When we apply the NR methodology, the NR estimator of $\lambda_{j(i)}$ is given by

$$\tilde{\lambda}_{j(i)} = \hat{\lambda}_{j(i)} - \frac{\text{tr}(S_{in_{i}}) - \sum_{k=1}^{j} \hat{\lambda}_{k(i)}}{n_{i} - 1 - j} \quad (j = 1, \ldots, n_{i} - 2).$$

Note that $\tilde{\lambda}_{j(i)} \geq 0$ for $j = 1, \ldots, n_{i} - 2$. Yata and Aoshima [14, 15] showed that $\tilde{\lambda}_{j(i)}$ has several consistency properties when $d \rightarrow \infty$ and $n_{i} \rightarrow \infty$. In this paper, we focus on the largest eigenvalue, $\tilde{\lambda}_{1(i)}$, that has the most important information in data analyses. We assume the following conditions for the largest eigenvalue:

\[(A-i)\] \[\frac{\text{tr}(\Sigma_{1}^{2}) - \lambda_{1(i)}^{2}}{\lambda_{1(i)}^{2}} = \frac{\sum_{j=2}^{d} \lambda_{j(i)}^{2}}{\lambda_{1(i)}^{2}} = o(1) \text{ as } d \rightarrow \infty \text{ for } i = 1, 2;\]

\[(A-ii)\] \[\sum_{n_{i} \geq 2} \lambda_{n(i)} \lambda_{n(i)} E\{ (z^{2}_{rk(i)} - 1)(z^{2}_{sk(i)} - 1) \} = o(1) \text{ as } d \rightarrow \infty \text{ for } i = 1, 2.\]
Note that (A-ii) is one of the SSE model (1.2). We also note that (A-ii) implies the condition that \( \lambda_{2(i)}/\lambda_{1(i)} \rightarrow 0 \) as \( d \rightarrow \infty \). Note that (A-iii) is naturally satisfied when \( X_i \) is Gaussian and (A-ii) is met.

**Remark 2.1.** For a spiked model such as

\[
\lambda_{j(i)} = a_{ij} d^{\alpha_{ij}} \quad (j = 1, \ldots, m_i) \quad \text{and} \quad \lambda_{j(i)} = c_{ij} \quad (j = m_i + 1, \ldots, d)
\]

with positive and fixed constants, \( a_{ij} \), \( c_{ij} \), and \( \alpha_{ij} \), and a positive and fixed integer \( m_i \), (A-ii) holds under the conditions that \( \alpha_{i1} > 1/2 \) and \( \alpha_{i1} > \alpha_{i2} \). See Yata and Aoshima [14] for the details.

**Remark 2.2.** For several statistical inferences of high-dimensional data, Bai and Saranadasa [4], Chen and Qin [6] and Aoshima and Yata [2] assumed a general factor model as follows:

\[
x_{ij} = \Gamma_i w_{ij} + \mu_i
\]

for \( j = 1, \ldots, n_i \), where \( \Gamma_i \) is a \( d \times r_i \) matrix for some \( r_i > 0 \) such that \( \Gamma_i \Gamma_i^T = \Sigma_i \), and \( w_{ij}, \ j = 1, \ldots, n_i \), are i.i.d. random vectors having \( E(w_{ij}) = 0 \) and \( \text{Var}(w_{ij}) = I_{r_i} \). As for \( w_{ij} = (w_{ij(1)}, \ldots, w_{ij(r)}^T) \), assume that \( E(w_{ijq(i)}^2) = 1 \) and \( E(w_{ijq(i)}w_{ijq(i)}^T) = 0 \) for all \( q \neq s, t, u \). From Lemma 1 in Yata and Aoshima [15], one can claim that (A-iii) holds under (A-ii) in the factor model. Also, we note that the factor model naturally holds when \( X_i \) is Gaussian.

Then, Ishii et al. [9] gave the following theorem.

**Theorem 2.1 ([9]).** Under (A-ii) and (A-iii), it holds that as \( d \rightarrow \infty \)

\[
\frac{\lambda_{1(i)}}{\lambda_{1(i)} - 1} \rightarrow \chi_{n-i}^2
\]

for \( i = 1, 2 \). Under (A-i) to (A-iii), it holds that as \( d \rightarrow \infty \) when \( n_i \) is fixed

\[
(n_i - 1) \frac{\lambda_{1(i)}}{\lambda_{1(i)} - 1} \Rightarrow \chi_{n-1}^2 \quad \text{for} \ i = 1, 2.
\]

### 3 One-Sample Test for SSE Model

In this section, we consider the one-sample test in the high-dimensional context. We consider the following test:

\[
H_0 : \mu_i = 0 \quad \text{vs.} \quad H_1 : \mu_i \neq 0,
\]

(3.1)

Bai and Saranadasa [4] proposed a test statistic:

\[
T_{BS} = n_i ||\overline{x}_{in_i}||^2 - \text{tr}(S_{in_i}):
\]

(3.2)

Srivastava and Du [13] proposed a test statistic:

\[
T_S = n_i \overline{x}_{in_i}^T D_i^{-1} \overline{x}_{in_i},
\]

(3.3)

where \( D_i = \text{diag}(s_{11(i)}, \ldots, s_{dd(i)}) \) and \( s_{jj(i)}, \ j = 1, \ldots, d \) are the diagonal elements of \( S_{in_i} \). They gave the asymptotic normality of \( T_{BS} \) or \( T_S \) under \( H_0 \) in (3.1) for the NSSE model (1.1). On the other hand, Katayama et al. [10] gave the asymptotic distribution of \( T_{BS} \) and \( T_S \) for the SSE model (1.2) when \( X_i \) is Gaussian.

Now, we consider a new one-sample test for the SSE model by using the asymptotic properties of the largest eigenvalue. By considering \( T_{BS} \) in (3.2) under (A-ii), we have the following result.
Lemma 3.1. Under (A-ii), it holds as \(d \to \infty\) that
\[
\frac{||\bar{x}_{in_{i}} - \mu_{i}||^{2} - \text{tr}(S_{in_{i}})/n_{i}}{\lambda_{1(i)}} = \frac{z_{1(i)}^{2}}{n_{i}} - \frac{||z_{01(i)}/\sqrt{n_{i}-1}||^{2}}{n_{i}} + o_{p}(n_{i}^{-1}),
\]
either when \(n_{i}\) is fixed or \(n_{i} \to \infty\).

By using the NR method, we consider the following test statistic:
\[
F_{1} = \frac{n_{i}||\bar{x}_{in_{i}}||^{2} - \text{tr}(S_{in_{i}})}{\tilde{\lambda}_{1(i)}} + 1.
\]
Note that \(E(\tilde{\lambda}_{1(i)}(F_{1} - 1)/n_{i}) = ||\mu_{i}||^{2}\). Then, by combining Theorem 2.1 and Lemma 3.1, Ishii et al. [9] gave the following result.

Theorem 3.1 ([9]). Under (A-i) to (A-iii), it holds as \(d \to \infty\) that
\[
F_{1} \Rightarrow \begin{cases} 
F_{1,n_{i}-1} & \text{when } n_{i} \text{ is fixed,} \\
\chi_{1}^{2} & \text{when } n_{i} \to \infty,
\end{cases}
\]
under \(H_{0}\) in (3.1), where \(F_{\nu_{1},\nu_{2}}\) denotes a random variable distributed as \(F\) distribution with degrees of freedom, \(\nu_{1}\) and \(\nu_{2}\); and \(\chi_{1}^{2}\) denotes a random variable distributed as \(\chi^{2}\) distribution with \(\nu\) degrees of freedom.

For a given \(\alpha \in (0, 1/2)\) we test (3.1) by
\[
\text{rejecting } H_{0} \iff F_{1} > F_{1,n_{i}-1}(\alpha),
\]
where \(F_{\nu_{1},\nu_{2}}(\alpha)\) denotes the upper \(\alpha\) point of \(F\) distribution with degrees of freedom, \(\nu_{1}\) and \(\nu_{2}\). Note that \(F_{1,n_{i}-1}(\alpha) \to \chi_{1}^{2}(\alpha)\) as \(n_{i} \to \infty\), where \(\chi_{1}^{2}(\alpha)\) denotes the upper \(\alpha\) point of \(\chi^{2}\) distribution with \(\nu\) degrees of freedom. Then, under (A-i) to (A-iii), it holds as \(d \to \infty\) that
\[
\text{size } = \alpha + o(1)
\]
either when \(n_{i}\) is fixed or \(n_{i} \to \infty\).

4 Two-Sample Test for SSE Model

In this section, we consider the two-sample test in the high-dimensional context. Now, we consider the following test:
\[
H_{0} : \mu_{1} = \mu_{2} \quad \text{vs.} \quad H_{1} : \mu_{1} \neq \mu_{2}.
\]
(4.1)

We assume the following assumption:
\[
(A-\text{iv}) \quad \frac{\lambda_{1(1)}}{\lambda_{1(2)}} = 1 + o(1) \text{ and } h_{1(1)}^{T} h_{1(2)} = 1 + o(1) \text{ as } d \to \infty.
\]

Remark 4.1. Note that (A-iv) is not a general condition for high-dimensional data, so that it is necessary to check. See Lemma 4.1 in Ishii et al. [9] for checking the condition in actual data analyses.
Let
\[ T_n = ||\overline{x}_{1n1} - \overline{x}_{2n2}||^2 - \sum_{i=1}^{2} \text{tr}(S_{in_i})/n_i. \]
Note that \( E(T_n) = ||\mu_1 - \mu_2||^2 \) and
\[ \text{Var}(T_n) = \sum_{i=1}^{2} \frac{\text{tr}(\Sigma_i^2)}{n_i(n_i-1)} + 4 \sum_{i=1}^{2} \frac{(\mu_1 - \mu_2)^T \Sigma_i (\mu_1 - \mu_2)}{n_i}. \]
By using Theorem 1 in Chen and Qin [6] or Theorem 4 in Aoshima and Yata [2], we can claim that as \( d \to \infty \) and \( n_i \to \infty \), \( i = 1, 2 \)
\[ \frac{T_n}{\text{Var}(T_n)^{1/2}} \Rightarrow N(0,1) \]
under \( H_0 \) in (4.1), (1.1) and some regularity conditions.

We consider an asymptotic distribution of \( T_n \) under the SSE models. We have the following results.

**Lemma 4.1.** Under (A-ii) and (A-iv), it holds that
\[ \frac{T_n}{\lambda_{1(1)}} = (\overline{z}_{1(1)} - \overline{z}_{1(2)})^2 - \sum_{i=1}^{2} \frac{||z_{o1(i)}/\sqrt{n_i-1}||^2}{n_i} + o_p(1) \text{ under } H_0 \text{ in (4.1)} \]
as \( d \to \infty \) either when \( n_i \)s are fixed or \( n_i \to \infty \).

Let \( \nu = n_1 + n_2 - 2 \). From Theorem 2.1, we have the following result.

**Lemma 4.2.** Under (A-i) to (A-iv), it holds as \( d \to \infty \) when \( n_i \)s are fixed that
\[ \frac{\sum_{i=1}^{2} (n_i-1)\tilde{\lambda}_{1(i)}}{\lambda_{1(1)}} \Rightarrow \chi_{\nu}^2. \]
Under (A-ii) to (A-iv), it holds as \( d \to \infty \) and \( \nu \to \infty \) that
\[ \frac{\sum_{i=1}^{2} (n_i-1)\tilde{\lambda}_{1(i)}}{\nu \lambda_{1(1)}} = 1 + o_p(1). \]

Let
\[ F_2 = u_n \frac{T_n + \sum_{i=1}^{2} \tilde{\lambda}_{1(i)}/n_i}{\sum_{i=1}^{2} (n_i-1)\tilde{\lambda}_{1(i)}}, \]
where \( u_n = \nu(1/n_1 + 1/n_2)^{-1} \). Then, by combining Lemmas 4.1 with 4.2, we have the following theorem.

**Theorem 4.1.** Under (A-i) to (A-iv), it holds as \( d \to \infty \) that
\[ F_2 \Rightarrow \begin{cases} F_{1,\nu} & \text{when } \nu \text{ is fixed}, \\ \chi^2_1 & \text{when } \nu \to \infty \end{cases} \]
under \( H_0 \) in (4.1).
For a given $\alpha \in (0, 1/2)$ we test (4.1) by
\[ \text{rejecting } H_0 \iff F_2 > F_{1, \nu}(\alpha), \] (4.2)
Then, under (A-i) to (A-iv), it holds that
\[ \text{size} = \alpha + o(1) \]
as $d \to \infty$ either when $\nu$ is fixed or $\nu \to \infty$.

5 Simulation Studies

In order to compare the performances of the one-sample test procedures, we used computer simulations. We consider the test (3.1). In this simulation, we compared the test procedure (3.4) to $T_{BS}$ in (3.2) and the test procedures given by Katayama et al. [10]. We set $\alpha = 0.05$ and $\Sigma = (I_d + d^{-1}1_d1_d^T)/2$, where $1_d = (1, \ldots, 1)^T$. For such a situation, Katayama et al. [10] gave the following test procedures:
\[ \text{rejecting } H_0 \iff \frac{T_{BS}}{\sqrt{\text{tr}(\Sigma^2)}} + 1 > \chi^2(\alpha), \] (5.1)
\[ \text{rejecting } H_0 \iff \frac{T_S - d(n_i - 1)/(n_i - 3)}{\sqrt{\text{tr}(R^2)}} + 1 > \chi^2(\alpha), \] (5.2)
where $\text{tr}(\Sigma^2)$ and $\text{tr}(R^2)$ are the consistent estimators of $\text{tr}(\Sigma^2)$ and $\text{tr}(R^2)$, $R$ is the population correlation matrix, given in Katayama et al. [10]. We considered the case $X_i$ is Gaussian. Note that (A-i) to (A-iii) hold. We considered two cases (I) $d = 2^k (k = 3, \ldots, 11)$ and $n_i = 10$; and (II) $d = 2^k (k = 4, \ldots, 11)$ and $n_i = \lceil d^{1/2} \rceil$, where $\lceil x \rceil$ denotes the smallest integer $\geq x$. In order to check the size, we set (a) $\mu_i = 0$ for each case. As for the power, we set (b) $\mu_i = (1, 1, 0, \ldots, 0)$ whose first $d/2$ elements are 1 for (I); and first $[3.8d/n_i]$ elements are 1 for (II).

The findings were obtained by averaging the outcomes from 2000 $(= R, \text{say})$ replications. We defined $P_r = 1$ (or 0) when $H_0$ in (3.1) was falsely rejected (or not) for $r = 1, \ldots, 2000$ in (a) and defined $\bar{\alpha} = \sum_{r=1}^{R} P_r/R$ to estimate the size. We also defined $P_r = 1$ (or 0) when $H_1$ in (3.1) was falsely rejected (or not) for $r = 1, \ldots, 2000$ in (b) and defined $1 - \bar{\beta} = 1 - \sum_{r=1}^{R} P_r/R$ to estimate the power. Note that their standard deviations are less than 0.011. In Fig. 1, we plotted $\bar{\alpha}$ in the left panels and $1 - \bar{\beta}$ in the right panels for (I) and (II).

Throughout, the original test procedure $T_{BS}$ in (3.2) does not give a good performance in terms of the size. It is probably because $T_{BS}$ does not hold the asymptotic normality when (1.1) is not met. On the other hand, the tests (5.1) and (5.2) do not give good performances in terms of the size when $n_i$ is small. We observed that the power of (3.2), (5.1) and (5.2) gave better performances compared to that of (3.4) in (I). This is because (3.2), (5.1) and (5.2) cannot control the size. In the case of (II), the size of (5.1) and (5.2) become close to $\alpha$ slowly as both the $d$ and $n_i$ are large. Contrary to that, (3.4) showed a quite good performance in terms of the size even when $n_i$ is small. It should be noted that high-dimensional data often have SSE model and the sample size is quite small. Thus, we conclude that if one can assume (A-ii), we recommend to use the new test procedure (3.4).
(I) \( d = 2^k (k = 3, \ldots 11) \) and \( n_i = 10 \).

(II) \( d = 2^k (k = 4, \ldots 11) \) and \( n_i = \lceil d^{1/2} \rceil \), where \( \lceil x \rceil \) denotes the smallest integer \( \geq x \).

**Figure 1.** We compared the test procedure (3.4) to (3.2), (5.1) and (5.2). We set \( \alpha = 0.05 \) and \( X_i \) is Gaussian. The values of \( \bar{\alpha} \) are denoted by the dashed lines in the left panels and \( 1 - \bar{\beta} \) are denoted by the dashed lines in the right panels.

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**References**


Graduate School of Pure and Applied Sciences, University of Tsukuba, Ibaraki 305-8571, Japan
E-mail address: ishii-akitk@math.tsukuba.ac.jp