Title: Electrolytic Production of Silicon Using Liquid Zinc Alloy in Molten CaCl₂

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Kyoto University
A new electrolytic production process for solar-grade Si has been proposed utilizing liquid Si–Zn alloy cathode in molten CaCl2. To establish this process, the behavior of liquid Zn metal in molten CaCl2 at 1123 K was investigated. Evaporation of Zn metal was largely suppressed by immersion in the molten salt, which enabled the use of a Zn electrode despite its high vapor pressure. Cyclic voltammetry results suggested that the reduction of SiO2 on a Zn cathode proceeded at a more negative than 1.45 V vs. Ca2+/Ca. After potentiostatic electrolysis at 0.9 V, Si particles with sizes of 2–30 μm were precipitated in the solidified Zn matrix by a slow cooling process. The rate-determining step for electrochemical reduction of SiO2 on the Zn cathode was discussed on the basis of a measurement of the alloying rate between solid Si and liquid Zn.

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liquid Si alloy cathode is applied to electrolytic reduction of SiO2 in a molten salt, there are many advantages, such as easy separation of Si from both the molten salt and unreacted SiO2, and easy transfer from the electrolysis cell. Further, because MG-Si can be refined by solidification of liquid Si alloys,37–51 a high separation ability is expected in the precipitation of Si from a liquid alloy, in which impurities are removed from the solid phase.

As alloying elements for Si that give a liquid alloy, Zn, Sn, Pb, and Al are candidates because they have no intermetallic compounds with Si. Their characteristics are summarized in Table I.52–59 Although Al shows promise because of its greater solubility at the electrolysis temperature, it is difficult to remove Al impurities from the Si phase. The minimum impurity level of Al is reported to be approximately 100 ppm for electrolysis of SiO2 on an Al cathode 31 and refining of Al shows promise because of its greater solubility at the electrolysis temperature and composition in the proposed process are indicated in the electrochemical behavior of the liquid Zn electrode, Kipouros and Sharma reported electrolysis of a Ca–Zn liquid alloy in the molten CaCl2–CaO–CaF2 system at 973–1023 K. 61 However, the electrode potential was unclear because a two-electrode system was employed. In this study, the fundamentals of the electrolysis process, namely, evaporation of Zn metal in molten CaCl2, electrochemical reduction of SiO2 on the Zn cathode, and the alloying rate for the Si–Zn system, were investigated at 1123 K. The effect of immersion of Zn metal in molten CaCl2 on its evaporation behavior was analyzed. Regarding the electrochemical behavior of the liquid Zn electrode, Kipouros and Sharma reported electrolysis of a Ca–Zn liquid alloy in the molten CaCl2–CaO–CaF2 system at 973–1023 K.61 However, the electrode potential was unclear because a two-electrode system was employed. In the present study, we investigated the effective potential range for metallic Si is recovered by lowering the temperature.

\[
\text{Si–Zn}(l, \text{ high Si conc.}) \rightarrow \text{Si}(s) + \text{Si–Zn}(l, \text{ low Si conc.}) \quad [3]
\]

When the temperature is lowered to 923 K, the solubility is also lowered to 1 at%-Si; thus, solid Si at 5 at% with reference to Zn is recovered. After the precipitation process, the Si–Zn alloy with a low Si concentration is reused as the cathode in the electrolysis process. The produced Si is then transferred to the refining process. An ingot of SOG-Si is manufactured by directional solidification of the treated Si after leaching and vacuum refining.

This process is expected to have several advantages in terms of productivity and purification ability. In contrast to the Siemens process, the proposed process can be operated semicontinuously, which contributes to high productivity. High purification efficiency is expected because there are two segregation steps: precipitation of solid Si from the Si–Zn liquid alloy in the precipitation process and preparation of solid Si from liquid Si in the refining process. The low distribution coefficients of the impurity elements, which indicate high purification ability, are reported for preparation from both liquids of metallic Si and alloys of Si–Al, Si–Cu, Si–Sn, Si–Fe, Si–Ni, and Si–Na. Furthermore, the remaining Zn can be easily removed to several parts per million even by the evacuation techniques used more than 30 years ago. More complete removal of Zn is possible by using advanced vacuum refining technology.

In this study, the fundamentals of the electrolysis process, namely, evaporation of Zn metal in molten CaCl2, electrochemical reduction of SiO2 on the Zn cathode, and the alloying rate for the Si–Zn system, were investigated at 1123 K. The effect of immersion of Zn metal in molten CaCl2 on its evaporation behavior was analyzed. Regarding the electrochemical behavior of the liquid Zn electrode, Kipouros and Sharma reported electrolysis of a Ca–Zn liquid alloy in the molten CaCl2–CaO–CaF2 system at 973–1023 K. However, the electrode potential was unclear because a two-electrode system was employed. In the present study, we investigated the effective potential range for

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**Figure 1.** Schematic drawing of SOG-Si production using electrochemical reduction of SiO2 powder on a liquid Si–Zn alloy cathode in molten CaCl2.

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**Table I. Properties of alloying elements for Si.**

<table>
<thead>
<tr>
<th>Metal</th>
<th>(T_{m.p.}/\text{K})</th>
<th>(T_{b.p.}/\text{K})</th>
<th>Solubility of Si at 1123 K / mol%</th>
<th>Distribution coefficient between liquid and solid Si at (T_{m.p.}) (Si)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Zn</td>
<td>69352</td>
<td>118052</td>
<td>6.054</td>
<td>1.0 \times 10^{-554}</td>
</tr>
<tr>
<td>Sn</td>
<td>50553</td>
<td>287553</td>
<td>0.058</td>
<td>1.6 \times 10^{-235}</td>
</tr>
<tr>
<td>Pb</td>
<td>60152</td>
<td>201952</td>
<td>&lt;0.256</td>
<td>2.0 \times 10^{-358}</td>
</tr>
<tr>
<td>Al</td>
<td>93552</td>
<td>279152</td>
<td>32.657</td>
<td>2.0 \times 10^{-359}</td>
</tr>
</tbody>
</table>
the production of Si–Zn alloy by electrolysis of SiO₂ granules on the Zn electrode. Furthermore, the alloying rate was studied to estimate the rate-determining step in the electrochemical reaction on the Zn electrode.

**Experimental**

**Evaporation of Zn.**—The evaporation rate of Zn in Ar atmosphere at 1123 K was measured using the weight change of Zn metal (Kojundo Chemical Laboratory Co., Ltd., 99.9999%, grains, 5.4–5.6 g) placed at the bottom of a silica tube [outer diameter (o.d.) 12.5 mm, inner diameter (i.d.) 10.5 mm] with and without added CaCl₂ (Kojundo Chemical Laboratory Co., Ltd., >99%, 5.4–5.6 g or 8.2–8.4 g). The samples were dried under vacuum at 453 K for 24 h and charged in a silica tube in a glove bag under an Ar atmosphere. Then, a balloon was set on the open end of the tube with a paraffin film to maintain the Ar atmosphere. The tube was inserted into a silica chamber (i.d. 127 mm, height 403 mm) in an electric furnace maintained at 1123 K and was left for a given period of time. The tube was pulled out in 1 min and then cooled at room temperature. The Zn sample was weighed after water washing and drying. If separation of the Zn sample from the silica tube was difficult, its weight was calculated from the values before and after leaching treatment with 1 M HCl solutions. The Zn content in the molten salt was analyzed using inductively coupled plasma atomic emission spectrometry (ICP-AES; Thermo Scientific, iCAP 6200 Duo) of a solution prepared by dissolving 0.1 g of recovered CaCl₂ into a HNO₃ solution.

**Electrochemical behavior.**—Figure 3 schematically illustrates the electrochemical apparatus. CaCl₂ (350 g) was charged in an alumina crucible (Nikkato Corp., SSA-S grade, o.d. 87 mm, i.d. 80 mm, height 129 mm) and dried under vacuum at 453 and 773 K for 24 h at each temperature. All the electrochemical experiments were performed in a dry Ar atmosphere at 1123 K. The electrochemical behavior was investigated by cyclic voltammetry and potentiostatic electrolysis using a newly designed liquid Zn electrode. Figure 4 shows a photograph and a schematic illustration of the liquid Zn electrode. Zn grains (Kojundo Chemical Laboratory Co., Ltd., 99.9999%, grains, 3–5 mm, 1.3 g) were set at the bottom of an alumina tube (Nikkato Corp.,

**Figure 2.** Binary phase diagram for the Si–Zn system. (a) Entire composition range and (b) Zn-rich region.

**Figure 3.** Schematic drawing of the electrolysis cell. (a) Ag⁺/Ag reference electrode, (b) graphite counter electrode, (c) liquid Zn electrode with SiO₂ granules, (d) Ca²⁺/Ca dynamic reference electrode on a Mo wire, (e) thermometer, (f) molten CaCl₂, and (g) alumina crucible.

**Figure 4.** (a) Photograph and (b) schematic illustration of the Zn electrode.
SSA-S grade, o.d. 13 mm, i.d. 9 mm) with an open window 10 mm × 20 mm in size on the side. A Mo wire (Nilaco Corp., dia. 1.0 mm, 99.95%) threaded into an alumina insulating tube (Nikkato Corp., SSA-S grade, o.d. 2.0 mm, i.d. 1.0 mm) was used for an electric lead. Purified SiO2 grains (Taiheiyo Cement Corp., dia. < 0.1 mm, 0.30 g) were placed above the Zn grains. The densities of liquid Zn, solid SiO2, and molten CaCl2 are 5.9 g cm⁻³, 2.2 g cm⁻³, and 2.05 g cm⁻³ at 1123 K, respectively. The counter electrode was a graphite rod (Tokai Carbon Co., Ltd., dia. 5.0 mm). An Ag⁺/Ag reference electrode was used. The potential was calibrated using the Ca²⁺/Ca redox potential measured by electrodepositing Ca metal on a Mo wire electrode (Nikkato Corp., dia. 1.0 mm, 99.95%). In the cyclic voltammetry tests, in situ IR compensation using an electrochemical measurement system was performed with a compensation ratio of 95%, which was the highest value in the range that did not cause potential instability. After potentiostatic electrolysis, the sample was recovered from the cell within 1 min and allowed to cool to room temperature by radiative cooling. The samples remaining in the alumina tube were cut into halves and polished with emery paper of descending degrees of roughness, specifically, #240, 400, 600, 1000, and 2000, and finally with a buffing compound (Buehler, Micro Polish II, 0.3 μm). The analysis was conducted using scanning electron microscopy (SEM; Keyence Corp., VE-8800) and energy-dispersive X-ray spectroscopy (EDX; AMETEK, EDAX Genesis APEX2).

**Alloying reaction between solid Si and liquid Zn.**—Zn granules (330 or 660 g, Wako Pure Chemical Industries, Ltd., grains) were charged into 210 g of molten CaCl2 to prepare a Zn pool in a graphite crucible (Toyo Tanso Co., Ltd., IG-110 grade, o.d. 90 mm, i.d. 80 mm, height 120 mm) in a dry Ar atmosphere at 1123 K. Single-crystal Si plates [SUMCO Corp., 6 mm × 35 mm, thickness 0.5 mm, n-type, (100) plane, resistivity 1–10 Ω cm] or Si prismatic rods (Furuuchi Chemical Corp., 4 mm × 4 mm, height 30 mm) attached to a Ni wire (Ryoko Sangyo Co., Ltd., > 99%, dia. 1.0 mm) and mullite tubes (Nikkato Corp., HB-grade, o.d. 6 mm, i.d. 4 mm, length 500 mm) were immersed in the Zn pool for 2–60 s. Round Si rods (Furuuchi Chemical Corp., dia. 6 mm, length 50 mm) affixed to a stainless steel tube (SUS304, o.d. 12.0 mm, i.d. 8.0 mm, length 500 mm) by a ceramic bond were also used for the measurements. For some experiments, Si lumps were added to the liquid Zn pool to prepare Si–Zn alloys. Si samples were immersed in the Zn pool or Si–Zn pool for a fixed duration and then pulled out and cooled at room temperature. After the adhered salt was washed away with water, the thickness or diameter of the Si specimens before and after immersion was measured by a micrometer.

**Results and Discussion**

**Evaporation of Zn.**—Since the vapor pressure of Zn at the electrolysis temperature of 1123 K is rather high (0.54 atm), one may assume that metallic Zn cannot be used as a liquid electrode because of immediate evaporation at temperatures close to its boiling point. On the other hand, the suppression of Zn evaporation in molten salt is well expected by the analogy that the evaporation rate of water in a test tube is significantly suppressed when the surface of water is covered by oil. Thus, the evaporation behavior of Zn in molten CaCl2 was investigated before the electrochemical experiments.

Figure 5 shows photographs of the samples before and after the evaporation experiments at 1123 K for 6 h. When only Zn metal was placed at the bottom of the tube maintained in Ar atmosphere, a considerable quantity of Zn deposits was observed on the upper side of the inner part of the tube, where the temperature was lower than 1100 K (Figure 5a2). These deposits result from evaporation and transport from the liquid Zn through the gas phase. On the other hand, in the presence of a molten CaCl2 layer of 5.4–5.6 g, solidified CaCl2 and Zn layers were observed, and no deposit was formed in the upper part, as shown in Figure 5b2. The stacking sequence of these layers (CaCl2 above Zn) is determined by their densities, and the layer thickness is

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**Table II. Weight of Zn samples after evaporation experiments at 1123 K.**

<table>
<thead>
<tr>
<th>Time, t / h</th>
<th>Thickness of CaCl2 layer, l_{CaCl2} / mm</th>
<th>Surface area, A / cm²</th>
<th>Weight of Zn Before, W_{bef} / g</th>
<th>Weight of Zn After, W_{aft} / g</th>
<th>Loss / g, W_{loss} / cm²</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.25</td>
<td>0</td>
<td>0.866</td>
<td>5.5322</td>
<td>5.2184</td>
<td>0.3132</td>
</tr>
<tr>
<td>0.25</td>
<td>31</td>
<td>0.866</td>
<td>5.5198</td>
<td>5.5026</td>
<td>0.0170</td>
</tr>
<tr>
<td>6</td>
<td>0</td>
<td>0.866</td>
<td>5.4502</td>
<td>4.3979</td>
<td>1.05</td>
</tr>
<tr>
<td>6</td>
<td>31</td>
<td>0.866</td>
<td>5.6016</td>
<td>5.5730</td>
<td>0.28</td>
</tr>
<tr>
<td>6</td>
<td>47</td>
<td>0.866</td>
<td>5.4916</td>
<td>5.4672</td>
<td>0.34</td>
</tr>
<tr>
<td>24</td>
<td>0</td>
<td>0.866</td>
<td>5.5781</td>
<td>1.6440</td>
<td>3.93</td>
</tr>
<tr>
<td>24</td>
<td>31</td>
<td>0.866</td>
<td>5.5310</td>
<td>5.4401</td>
<td>0.99</td>
</tr>
<tr>
<td>24</td>
<td>47</td>
<td>0.866</td>
<td>5.4688</td>
<td>5.4141</td>
<td>0.07</td>
</tr>
</tbody>
</table>

where 

\[ W_{\text{loss}} = W_{\text{bef}} - W_{\text{aft}}. \]

\[ W_{\text{loss}} = \frac{W_{\text{loss}}}{A}. \]
the same as that calculated (Zn: 10 mm, CaCl$_2$: 31 mm). The weight loss of Zn metal in the experiments with and without the presence of molten CaCl$_2$ over liquid Zn is summarized in Table II and plotted in Figure 6a versus the reaction time. The graph clearly shows that evaporation was significantly suppressed by the presence of the molten salt layer above the liquid Zn metal. In both cases, the weight of the Zn metal decreased almost linearly with time. The evaporation rate, defined as the slope of the plot is $1.90 \times 10^{-1}$ gc m$^{-2}$ h$^{-1}$ when the Zn metal was evaporated in the absence of CaCl$_2$. The rate decreases significantly to $4.45 \times 10^{-3}$ gc m$^{-2}$ h$^{-1}$ (0.023 times) in the presence of the molten salt, which corresponds to an evaporation rate of 0.18 mm day$^{-1}$. Thus, the evaporation of Zn metal covered with molten CaCl$_2$ is found to be negligibly small when it is used as a cathode in the electrolysis process, despite the high vapor pressure of Zn.

Electrochemical behavior.—Figure 7 shows the cyclic voltammograms of a liquid Zn electrode with and without SiO$_2$ granules. The solid curve for Zn metal without an addition of SiO$_2$ granules indicates a negative current around 50 mA cm$^{-2}$ from the rest potential (1.48 V vs. Ca$^{2+}$/Ca) and a sharp current increase at 0.9 V. Because Ca and Zn form a liquid phase over the entire composition range at 1123 K, this current is attributed to the formation of liquid Ca–Zn alloy. The potential of 0.9 V vs Ca$^{2+}$/Ca corresponds to the Ca mole fraction of $1.6 \times 10^{-6}$ in liquid Ca–Zn alloy calculated from Henry’s law and the reported activity coefficient of Ca at 1073 K ($2.15 \times 10^{-3}$). To confirm the reaction, the Zn electrode was galvanostatically electrolyzed at $-1.06$ A cm$^{-2}$ for 30 min. The open-circuit potential immediately after electrolysis was 0.35 V. When the sample was analyzed by EDX, the composition of the surface zone was determined to be 90 at%Zn–10 at%Ca. These values agree with those calculated from the reported activity coefficient of Ca. Incidentally, the Ca content was below the detection limit of EDX in the samples obtained by potentiostatic electrolysis at 0.90 V, which is explained by the fact that less electricity is used compared to the case of galvanostatic electrolysis. From the above results, the reduction current observed at values more negative than 0.9 V is attributed to the formation of liquid Ca–Zn alloys.

Zn ($l$) + $y$ Ca$^{2+}$ + $2y$ e$^{-}$ → ZnCa$_y$ ($l$) \[4\]

The broken curve in Figure 7 shows the voltammogram for the Zn electrode after the addition of SiO$_2$. Although the rest potential is almost identical to that before the addition of SiO$_2$, larger cathodic currents of 100 mA cm$^{-2}$ are observed during the scan in the negative direction. Thus, the increased current suggests the reduction of SiO$_2$ into the molten salt and then evaporate at the interface between the gas and the molten salt after transport in the melt. To investigate the effect of diffusion distance of the dissolved Zn in molten CaCl$_2$ on the evaporation rate, experiments were carried out with different thicknesses of molten salt layer. Figure 6b compares the evaporation behavior at different thicknesses of the molten CaCl$_2$ layer. The evaporation rates for thicknesses of 31 and 47 mm are $4.45 \times 10^{-3}$ and $2.75 \times 10^{-3}$ gc m$^{-2}$ h$^{-1}$, respectively. Obviously, the rate of weight loss varies inversely with the thickness of the CaCl$_2$ layer. Thus, diffusion in the molten salt is likely the rate-determining step.

![Figure 6. Weight loss of Zn per area at 1123 K. (a) Plots with and without immersion of Zn sample in molten CaCl$_2$. (b) Weight loss versus time for CaCl$_2$ layer thicknesses of 31 and 47 mm.](image-url)
to form liquid Si–Zn alloy between 0.9 and 1.45 V.

\[
\text{SiO}_2 (s) + \text{Zn} (l) + 4e^- \rightarrow \text{Si} - \text{Zn} (l) + 2\text{O}^{2-} \quad [5]
\]

To proceed a direct electrolytic reduction of insulating solid SiO$_2$, the use of a current collector is necessary for electron supply. Here, the onset potential of SiO$_2$ reduction on the liquid Zn cathode (1.45 V) is more positive than that on a solid current collector such as a Mo electrode (1.25 V),\textsuperscript{17} which is explained by the lower activity of Si in the Zn–Si alloy.

On the basis of the voltammetric results, potentiostatic electrolysis was conducted for a liquid Zn electrode after SiO$_2$ granules with a diameter of 0.1 mm were added at 0.90 V for 60 min in molten CaCl$_2$ at 1123 K. The sample was observed after cross-sectioning in the vertical direction. Figures 8a and 8b show cross-sectional optical and SEM images, respectively, of the sample after electrolysis. The precipitated grains are observed only on the upper part of the Zn electrode. According to EDX analysis for the particles shown in the magnified SEM image in Figure 8c, Si is detected to be 100 wt% and other elements are below their detection limits. Thus, the deposition of Si particles with sizes of 2–30 μm in the Zn matrix is confirmed. According to the Si–Zn phase diagram,\textsuperscript{54} the solubility of Si in liquid Zn metal is 6.0 at% at 1123 K, and it becomes negligibly small in solid Zn at room temperature. Thus, it is reasonable to conclude that SiO$_2$ was electrochemically reduced to form liquid Si–Zn alloy [Reaction 5] and that Si particles were precipitated during the cooling process. The precipitated Si particles are observed only in the upper part because they floated and aggregated in the liquid phase owing to their lower density.

The anodic reaction is an evolution of CO$_2$ gas because consumption of the graphite rod counter electrode was observed after the experiment. Since the amount of recovered Si was small, which is mainly due to the recovery loss during the HCl leaching, the current efficiency is not discussed in this study. In the case of direct electrolytic reduction of solid SiO$_2$ to solid Si in molten CaCl$_2$, the current efficiencies were already reported to be 90% for SiO$_2$ plates\textsuperscript{17} and 70.3–78.5% for SiO$_2$ granules.\textsuperscript{24} Current efficiency for the production of liquid Si–Zn alloy might be also influenced by the side reaction of liquid Ca–Zn alloy formation.

**Alloying reaction between solid Si and liquid Zn.**—Figure 9 shows photographs taken before and after the alloying experiments at 1123 K for different immersion times. After the experiments, Zn was not found on the surface of the recovered Si plate by either visual observation or EDX analysis. The liquid alloy formed at high temperature was probably removed as the sample was pulled out through the molten CaCl$_2$ layer. The photographs in Figure 9 clearly show a decrease in the plate thickness due to dissolution of Si, even for the sample immersed in Zn for 2 s. For the Si plate reacted for 60 s, the immersed part of the Si plate disappeared completely. Because the alloying reaction proceeds on both sides of the Si plate, the decrease in thickness was evaluated as the value for one side; the results are listed in Table III. As shown in Figure 10, the thickness of the plate decreases linearly with increasing immersion time, and the alloying rate is determined to be 4.56 μm s$^{-1}$ from the slope of the plots.

Similar measurements were made for Si–Zn alloy pools with different Si concentrations, and the results are summarized in Table III and Figure 10. The alloy formation rate decreases with increasing Si concentration in the liquid alloy. The alloy formation rate ($v_{\text{alloy}}$) is plotted in Figure 11 against the Si concentration ($c_{\text{Si}}$) in the alloy. A
Table III. Thickness of Si plate or diameter of Si rod and alloy formation rate in Zn pool at each Si concentration at 1123 K.

<table>
<thead>
<tr>
<th>Si conc. in Zn pool, ( c_{Si} ) / at%</th>
<th>Immersion time, ( t_{im} ) / s</th>
<th>Before immersion, ( L_{bef} ) / ( \mu )m</th>
<th>After immersion, ( L_{aft} ) / ( \mu )m</th>
<th>Reduced value for one side, ( L_{reduced} ) / ( \mu )m</th>
<th>Alloy formation rate ( v_{alloy} ) / ( \mu )m s(^{-1})</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
<td>–</td>
<td>–</td>
<td>0</td>
<td>4.56c</td>
</tr>
<tr>
<td>1.10</td>
<td>120</td>
<td>4021</td>
<td>3171</td>
<td>425</td>
<td>3.54</td>
</tr>
<tr>
<td>2.40</td>
<td>120</td>
<td>5992</td>
<td>5332</td>
<td>330</td>
<td>2.75</td>
</tr>
<tr>
<td>4.87</td>
<td>60</td>
<td>530</td>
<td>428</td>
<td>51</td>
<td>0.85</td>
</tr>
</tbody>
</table>

\( L_{reduced} = L_{bef} - L_{aft} \)

\( v_{alloy} = \frac{L_{reduced}}{t_{im}} \)

\( c_{Si} \) calculated from the slope of the plots in Fig. 10.

A linear relationship between \( v_{alloy} \) and \( c_{Si} \) is clearly observed.

\[
\begin{align*}
\nu_{alloy} &= -0.747c_{Si} + 4.49 \\
&= 0.747(6.0 - c_{Si})
\end{align*}
\]

Extrapolation indicates that the alloy formation rate becomes zero at 6.0 at%\( c_{Si} \), which is consistent with the solubility in liquid Si–Zn alloy.54 This fact suggests that the alloying reaction is controlled by diffusion of Si atoms in the diffusion layer between solid Si and liquid Zn.

The linearity of the plots for 0 at%-\( c_{Si} \) in Figure 10a is attributed to rapid diffusion of Si in liquid Zn, which is expected to be on the order of \( 10^{-4} \) \( \text{cm}^2 \text{s}^{-1} \) from the reported diffusion coefficients of Fe \( [1-5] \times 10^{-4} \) \( \text{cm}^2 \text{s}^{-1} \) and Al \( [1.1 \times 10^{-3} \text{cm}^2 \text{s}^{-1}] \) in liquid Zn at 1123 K. The parabolic growth of the diffusion layer thickness is complete at only 1.05 s, as calculated from the alloy formation rate of 4.56 \( \mu \)m s\(^{-1} \) and the estimated diffusion coefficient of 1 \( \times 10^{-4} \) \( \text{cm}^2 \text{s}^{-1} \). This behavior results in the positive deviation of the plot for reaction for 2 s.

To estimate the rate-determining step of electrochemical reduction of SiO\(_2\) using a liquid Zn electrode, the alloying rate is compared with the reaction rate in the other steps involved in the reaction. According to our previous studies, the electrochemical reduction rates are estimated from the results at a reaction time of 300 s in molten CaCl\(_2\) at 1123 K as 2.1 \( \mu \)m s\(^{-1}\) and 0.27 \( \mu \)m s\(^{-1}\) for the surface and inner directions of solid SiO\(_2\), respectively. Furthermore, the reaction for the inner direction becomes slower with increasing electrolysis time because the diffusion length for the \( \text{O}^2^- \) ions in the porous Si layer becomes longer. These rates are schematically compared in Figure 12. Obviously, the alloy formation rate is higher than the reduction rates. This comparison suggests rapid removal of the porous Si layer formed at the outermost surface of the SiO\(_2\), in the same analogy with the removal of Nd–Fe liquid alloy from the surface of an iron cathode in rare earth electrometallurgy.66 The removal of the surface layer retarding the diffusion of \( \text{O}^2^- \) ions would lead to continuation of the fast reaction, which was confirmed to be equivalent to 0.7 A cm\(^{-2}\) in the Hall–Héroult process using molten salt electrolysis.21,22

**Conclusions**

An electrolytic production process for SOG-Si using liquid Si–Zn alloy in molten CaCl\(_2\) was proposed. The presence of the molten salt above a liquid Zn layer significantly suppressed evaporation of Zn. The evaporation rate at 1123 K was 0.18 mm day\(^{-1}\), which is slow enough that a liquid Zn cathode can be used. The reduction of SiO\(_2\)
granules on the Zn cathode to form liquid Si–Zn alloy was suggested to proceed from 1.45 V vs. Ca2+/Ca and confirmed at 0.9 V. The alloy formation rate of solid Si and liquid Zn was measured to be 4.56 μm s⁻¹ at 1123 K, which indicates the potential of rapid reduction of SiO₂.

Acknowledgments

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