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<td>Jin, Sheng-Ye; Susaki, Junichi</td>
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Kyoto University
A 3-D Topographic Relief Correlated Monte Carlo Radiative Transferring Simulator (TRCMCRTS) for Forest Bidirectional Reflectance Estimation

Abstract—Understanding the physical processes that affect electromagnetic waves within forests is a key to a better analysis of global environmental change. In this letter, we propose a 3-D vector model (TRCMCRTS) for estimating a bidirectional reflectance factor (BRF) for a forest with complex terrain relief. Unlike existing models, this model takes into account rugged terrain conditions by modeling ground surface as bilinear surface interpolated from digital elevation model (DEM). The proposed model is compared with the well-performing Monte Carlo model FLiES for validation, and good agreement is obtained. Forest BRF estimations for six different terrain relief conditions are derived, and these BRFs have reasonable variation according to ground conditions.

Index Terms—Monte Carlo Ray-Tracing, Radiative Transferring, Forest, Topographic Relief, Bidirectional Reflectance.

I. INTRODUCTION

The ongoing issue of global environmental change is having a critical impact on the global ecosystem. Understanding of global terrestrial environmental change can be achieved by remote sensing (RS). For example, optical RS helps in mapping vegetated areas and estimating the biological activity of forests. However, optical RS data have been utilized poorly to date in relation to understanding the physical processes of electromagnetic waves in vegetated areas. This situation would be improved with a physical model of the correspondence between optical electromagnetic waves and landscape parameters, which would allow the calibration of optical RS images and the retrieval of landscape parameters. In general, numerical methods based on a radiative transfer equation (RTE) can be used to express the radiative regime. Difficulties in determining the boundary conditions of the radiative transfer (RT) field make solving the RTE problematic [1]. Although Liang and Strahler ingeniously overcame the boundary condition problem by coupling the atmospheric and canopy RTEs, methods for solving RTEs still have innate drawbacks [2]. In particular, properties of the canopy within the RT field are input with average conditions so that individual leaves cannot be distinguished [3], [4].

One approach to accurately estimating the radiation distribution of a complicated landscape is computer simulation, which can be classified into two branches: radiosity modeling [5], [6] and Monte Carlo radiative transfer (MCRT) modeling [7]. For more precise calculations, both radiosity and MCRT modeling methods could be applied to understand the RT field balance and to validate other models. Radiosity modeling aims to render the initialized landscape by means of computer-graphic algorithms. However, despite being able to analyze the input scene from all observation angles, the radiosity method is limited if the landscape complexity exceeds the available computing power. Alternatively, MCRT can provide a faster solution by averaging the RT field at a particular volume scale rather than defining the canopy comprehensively.

When used for solving complicated heterogeneous RT problems, MCRT models provide accurate and robust results and are computationally inexpensive [8]. In MCRT modeling, photon scattering is determined using a phase function rather than by being calculated explicitly as in radiosity modeling. Myneni et al. have summarized the MC models that simulate RT within vegetated areas. They conclude that, apart from the limitations of computational power, MC simulation is an exceptional method that can either trace photon motion within the canopy or determine photon-mass interaction [9]. Disney et al. have comprehensively reviewed subsequent canopy MCRT models [10]. Kobayashi and Iwabuchi developed a three-dimensional (3D) heterogeneous forest RT simulator (FLiES) [11] that was coupled to a one-dimensional (1D) atmospheric RT model by Iwabuchi [12]. This provides remarkable results for flat terrain, but rugged conditions that affect bidirectional reflection in the RT regime make it necessary to include complex topographic reliefs in RT models [13]. In order to consider the RT budget in mountainous areas, a MC approach was developed to solve RTEs for complex ground conditions [14]. This was followed by an RT model that expressed ground relief using a digital elevation model (DEM), thereby addressing the issue of clouds obscuring the observations and also suggesting a way of dealing with complex topographic conditions [15].

More recently, models have been proposed that emphasize the polarization of reflectance by vegetation cover. These assume two types of canopy leaf scattering: Lambertian reflectance and transmittance, or specular reflection [16], [17].

In this letter, we describe a 3D vector MCRT model for estimating the bidirectional reflectance factor (BRF) of a forest area with complicated ground relief. We refer to this model as the Topographic-relief-correlated Monte Carlo Radiative-transfer Simulator (TRCMCRTS). In particular, a solution is developed for retrieving the ground normal vector during ray tracing, which is the key step in determining the scattering direction when a photon hits the ground. In order to evaluate the effects of terrain relief during the simulation, the contribution of single scattering from the ground is estimated. To assess the validity of TRCMCRTS, we compare its estimations of the red and infrared BRFs with those of the FLiES model. Assumed topographic conditions are used to show the extent to which TRCMCRTS is sensitive to different terrain reliefs.
II. MODEL DELINEATION

The forest in this model is composed of individual trees distributed heterogeneously in an area with relief topography. In relation to RS observations, the canopy consists of leaves that are particles and branches that are formed as regular geometrical volumes. To take account of topographic effects, the forest scene is divided into a cubic matrix according to the DEM grid of the area. Each cube contains trees and ground objects. Tree objects comprise canopy (leaf), branch (stem), and trunk objects. Ground objects comprise the understory (grass) turbid layer and the soil. The ground is assumed to be a bilinear surface of the photon. The ground is assumed to be a bilinear surface determined by the parametric line equation

\[ r = r_0 + tn_x, \]

where \( r_0 \in \mathbb{R}^3 \) is the initial photon position, \( n_x \in [0, 1]^3 \) is the directional vector, and \( t (t \geq 0) \) is the traveling distance of the photon. The ground is assumed to be a bilinear surface \( B(u, v) \) interpolated from the DEM grid:

\[ B(u, v) = uva + vbc + d, \quad (u, v) \in [0, 1]^2; \]

where \( a = p_{11} - p_{01} + p_{00}, b = p_{10} - p_{00}, c = p_{01} - p_{00}, \) and \( d = p_{00}; p_{ij} \) for DEM grid point coordinates \( p_{ij} \) with \( i, j \in \{0, 1\} \). The ray-bilinear interpolation algorithm was formed by substituting Eq. (1) into Eq. (2) [18]. The local surface normal \( n_x \) of the ground, which is important for determining the scattering direction of the photon, at the point \( p_g = (p_{gx}, p_{gy}, p_{gz}) \) is

\[ n_g = n_x \times n_y. \]

Here, \( n_x = p_x - p_g \) and \( n_y = p_y - p_g \), where

\[ p_x = [p_{gx} + \xi \cdot p_{gy}, p_{xz}]^T, \]
\[ p_y = [p_{gy} + \xi \cdot p_{gx}, p_{yz}]^T \]

are two neighboring points of \( p_g \) on \( B(u, v) \) in the positive \( x \) and \( y \) directions, respectively, at a constant distance \( \xi (\xi > 0) \). Terms \( p_{xz} \) and \( p_{yz} \) are the retrieved \( z \) coordinates of \( p_x \) and \( p_y \), respectively.

B. PHOTON TRAJECTORIES

Photon tracing in the forest scene is implemented within the cubic matrix (Fig. 1). Each cube contains objects such as trees, understory, and soil. The ray-tracing algorithm was designed according to the following scheme:

(i) Initialize new photon.
(ii) Trace photon in cube.
(a) Determine whether photon interacts with materials (canopy, soil).
(b) Apply single-leaf or soil scattering.
(c) Russian roulette to determine whether photon dies.
(iii) Update photon position (Eq. 1).
(iv) If photon passes through reference plane, go to (i).
(v) Else run into next cube and go to (ii).

If the photon dies at step (c), which is determined by the Russian roulette method [11], a new photon is generated. The free path within the canopy is determined by a random number according to Beer’s Law. Lambertian scattering is assumed on the material surface. The contribution of photons from the scattering direction to the observation direction is calculated using the local estimation method, and the scattering direction \( \Omega_s(\theta_s, \phi_s) \) is determined randomly using the rejection method [19]. The following steps were designed to determine \( \theta_s, \phi_s \):

1. Generate two random numbers \( \rho_1 \) and \( \rho_2 \) in (0, 1).
2. If \( \rho_1 < \rho_2 \), go to (1).
3. Otherwise, \( \cos \theta_s = \rho_1, \sin \theta_s = \sqrt{1 - \rho_1^2} \).

The azimuth \( \phi_s \) is set as follows:
(A) Generate two random numbers \( \rho_3 \) and \( \rho_4 \) in (0, 1).
(B) \( f_1 = 1 - 2\rho_3, f_2 = 1 - 2\rho_4 \).
(C) \( \delta = f_1^2 + f_2^2; \) if \( \delta > 1 \), go to (A).
(D) Otherwise, \( \cos \phi_s = f_1 f_3, \sin \phi_s = f_2 f_3 \).

Therefore, the scattering vector is

\[ n_s = [\sin \theta_s \cos \phi_s, \sin \theta_s \sin \phi_s, \cos \theta_s]^T. \]

Single-leaf scattering is achieved by assuming the leaves to be bi-Lambertian scattering surfaces [20], and the leaf-scattering phase function is created from look-up tables. Lambertian scattering from the soil is achieved by setting the local normal \( n_g \) as the nadir, which means \( n_g \) should be updated by coordinate rotation.

III. RESULTS AND DISCUSSION

A. COMPARISON WITH FLiES

To validate TRCMCRTS, we compare it with FLiES for a 100 × 100 m² area. The 3D scene was defined according to the RAdiation transfer Model Intercomparison (RAMI) Online Model Checker (ROMC) standard [21]. The canopy was formed from spheres whose center height varied from 11.0 m to 19.0 m above ground. Figure 2 shows the comparison between TRCMCRTS and FLiES with 3×10⁵ photons for the same input parameters (Table I) in the red (650 nm) and infrared (800 nm) bands with solar zeniths at 20° and 50°.

Figure 2(a-c) shows that the BRF results are highly correlated (correlation coefficients of greater than 0.99) between the two models. The root-mean-square deviations for...
the observation directions are on a plane that is perpendicular to the observation plane of condition (a). Condition (c) is a topography that slopes from the bottom-left to top-right corners of the figure, with two depressions in the top-left and bottom-middle locations. Condition (d) is the same as (c) but rotated clockwise by 180°. In contrast to the relative azimuth relationship between conditions (a) and (b), the solar settings of condition (c) are the opposite to those of (d). Condition (e) is a ridge that runs between top middle and bottom middle, and is lower on the left than on the right. Condition (f) is the same as (e) but rotated clockwise by 90°. The relative azimuth relationship between conditions (e) and (f) is the same as that between conditions (a) and (b). The other parameters are given in Table I.

First two-row figures of Fig. 4 show the total BRFs of four bands (450, 550, 650, and 800 nm) estimated for the six different topographic conditions shown in Fig. 3. The BRF peak due to the hot-spot effect is the same for all six conditions. The dotted line (g) is for flat ground; all the lines (a–g) correspond to the same parameter settings of conditions except the ground conditions. The bottom row figures of Fig. 4 show the single scattering contributions from the canopy. With the same tree parameters (conditions (a–f)), the contributions from the canopy are reasonably stable. The contribution from canopy single scattering remains stable for conditions (a–g) in each band; hence, the total BRF is affected mostly by the ground contributions. Compared with condition (g) (flat ground), the BRFs from conditions (a–g) are enhanced differently. This type of enhancement is found at observation azimuth angles other than just the principal plane (Fig. 5). Conditions (c), (d), and (f) show considerable changes in response because of the altered topography.

The correlation coefficient between standard ground (condition (g)) and the other conditions of the total BRF can reflect the aforementioned differences between BRF distributions. A lower value of correlation coefficient means that the BRF distribution is affected more by the topography, and vice versa. The values of the correlation coefficient ($\rho_{(g,a)}$) between conditions (a) and (g) for the four bands are 0.987, 0.989, 0.989, and 0.985, respectively. Comparing conditions (b) and (g), we have $\rho_{(g,b)} = 0.982$, 0.984, 0.980, and 0.983, respectively. Conditions (a) and (b), which correspond to a bowl-shaped area located symmetrically around the east-west line, show symmetrical responses at viewing angles around ±60°. Conditions (c) and (d), which correspond to symmetrical slopes about the north-south line, present symmetrical responses with variation in observation angle. Condition (c) holds obvious phenomenon in comparison with condition (g): we have $\rho_{(g,c)} = 0.961$, 0.971, 0.962, and 0.973, respectively.

**TABLE I**

<table>
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<th>800 nm</th>
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<td>canopy leaf transmittance</td>
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Fig. 2(a-d) are 0.0014, 0.0012, 0.0086, and 0.0116, respectively. In general, the TRCMCRTS results fit better with the FLiES results under backward-scattering conditions than under forward-scattering conditions; however, the opposite is true in Fig. 2(d). With the same parameter settings for the two MC models, the deviations are mainly due to the particular random-number series that were used. These types of shift could be mitigated crudely by averaging multiple calculation results from TRCMCRTS. However, TRCMCRTS is currently not equipped to remove these variations as this would require further numerical optimization. In order to describe ground reliefs accurately according to the local DEM, TRCMCRTS does not discretize the 3D scene into voxels as does FLiES. Therefore, computational speed is sacrificed at present.

**B. Topographic Relief**

To demonstrate the effect of topography on BRF estimation, six different ground reliefs were assumed (see Fig. 3). In each case, the solar beam was incident from the west ($\theta_0 = 20°$, $\phi_0 = 180°$), and the topographic relief was limited to 0–1.5 m above the ground in order to test the sensitivity of TRCMCRTS in response to the topography. As shown in Fig. 3, Condition (a) is a valley that runs between the top-left and bottom-right corners of the figure. Condition (b) is the same as (a) but rotated counterclockwise by 90°. Another way to consider the differences between conditions (a) and (b) is to set (a) as the standard. Then condition (b) becomes the solar conditions ($\theta_0 = 20°$, $\phi_0 = 90°$), and
The most affected condition is \((d)\); we have \(\rho_{(g,d)} = 0.928, 0.936, 0.924,\) and 0.971, respectively. Condition \((e)\) shows only a small effect because the ground relief has a symmetrical appearance when lit from the front or the back. Condition \((f)\), which is \((e)\) rotated clockwise by 90°, produces a strong contribution to the backlit condition: for the four bands, we have \(\rho_{(g,e)} = 0.947, 0.960, 0.949,\) and 0.972, respectively, and \(\rho_{(g,f)} = 0.962, 0.971, 0.962,\) and 0.968, respectively. The results for the infrared band (800 nm) are more stable to topographic changes than are the other three bands. In addition, slope conditions \((c)\) and \((d)\) affect the BRF value more than do the other pairings.

![Total BRF (a)-(d)](image)

To assess the topographic effects in detail, Fig. 5 shows the single-scattering contribution from the soil for the six ground conditions and without topography input (condition \((g)\)). The model parameters are the same as those for Fig. 4. The topographic conditions enhance the single scattering globally compared with flat ground (condition \((g)\)) for azimuth angles of 0°–360°. From the results for the four bands, we see growing linear variations from 450 to 800 nm for each ground condition. The BRFs of conditions \((a)\) and \((b)\) are similar for 450 and 550 nm. The BRF contributions from condition \((b)\) are stretched more in the forward-scattering domain at 650 nm compared to condition \((a)\). The contour lines show obvious shifts toward being circular around 45°, 120°, and 45°, 240°. Asymmetrical distributions of BRF are seen for conditions \((c)\) and \((d)\). The BRF distributions of the two conditions shows contrary tendencies: the BRF of condition \((c)\) is inclined in the 315° direction, whereas that of condition \((d)\) tends to 135°. Condition \((d)\) also provides a powerful forward-scattering effect. The ridge condition \((e)\) supports forward scattering better than does condition \((f)\), which indicates that the angle between the principle plane and the ridge plane also has an impact on the magnitude of the ground scattering. The ridge plane of condition \((e)\) is along the middle vertical line perpendicular to the image plane, and that of condition \((f)\) is along the middle horizontal line perpendicular to the image plane.

The micro-topographic effect in our model is expressed by estimating the local normal of the point at which light intersects the bilinear surface. This means the scattered photon weight is larger when the relative angle \(\Theta_{topography}\) (the angle between the observation direction and the local ground normal) is smaller than \(\Theta_{flat}\) (the angle between the observation direction and the flat ground normal). According to the Lambertian scattering law, a smaller relative angle gives a higher reflected radiance. This also means that the photon can survive longer after scattering and can contribute more to the BRF estimation.

The ground conditions were selected for the purpose of checking the sensitivity of the model. Hence, the difference between the minimum and maximum elevations is not extreme. Enhancement is shown clearly for ground conditions \((c)\), \((d)\), and \((e)\). According to the geometry of solar incidence, \((c)\) is stronger for backward scattering and \((d)\) is stronger for forward scattering because \((c)\) and \((d)\) correspond to sloping ground. Condition \((c)\) is also affected by the hot-spot effect, so the enhanced BRF is less obvious than it is for \((d)\). Conditions \((a)\) and \((b)\) show the same symmetrical aspect distribution according to the solar direction, so the enhancements are almost the same. Condition \((e)\) contributes to both forward and backward BRFs because the ridge slopes both forward and backward, whereas \((f)\) shows less enhancement.

Despite the above evidence for systematic enhancement, we cannot conclude that an enhanced BRF estimation would be found for any ground situation. We believe that for some extreme relief conditions like steep hills with a steep gradient on the back side will not be observed. Of course, we must emphasize the important point that the forest must be relatively open so that the reflectance of the bare ground contributes sufficiently to the BRF. The proposed TRCMCRTS contributes micro-topographic effects to the BRF estimation, especially for open forests with bare ground. This type of ground-level local-normal estimation for determining the ground-reflectance contribution accurately can be applied to the local DEM or digital terrain model. Because it calculates the exact interaction between photons and the ground, our model cannot run as fast as can other voxel-optimized models. To accelerate the present model, it may be necessary to implement it in a parallel computing environment.

IV. CONCLUSION AND FUTURE WORK

A 3D vector Monte Carlo radiative-transfer model known as TRCMCRTS has been developed to assess the bidirectional reflectance of forests with complex topographic relief. Preliminary results indicate that the model provides similar results for the bidirectional reflectance factor in the red and infrared bands to those of the FLiES model. The present model could be improved by including atmospheric effects in both the physical radiative-transfer modeling of the open forest area and the retrieval of landscape parameters from remotely sensed
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Fig. 5. BRF polar plots of soil single scattering (450, 550, 650, and 800 nm) with Fig. 3 defined topographic conditions from (a) to (f), and flat condition (g). Solar zenith is 20°. Observation zenith varies from 0° to 80°; azimuth are from 0° to 360° with 30° span. Scale bar shows the linear variation from 0.0 to 0.15.

data. However, the present ability to estimate the response according to the topographic relief is more than adequate. Estimations of the ground contribution showed that, for open forest areas, the ground could have an appreciable impact on the BRF distribution, especially if the topographic conditions were considered. Further validation of the TRCMCRTS in the field is planned so that the model can be adjusted to fit with measurements.