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Paper

Transient behavior of redox flow battery connected to circuit based on global phase structure

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Abstract: A Redox Flow Battery (RFB) is one of the promising energy storage systems in power grid. An RFB has many advantages such as a quick response, a large capacity, and a scalability. Due to these advantages, an RFB can operate in mixed time scales. Actually, it has been demonstrated that an RFB can be used for load leveling, compensating sag, and smoothing the output of the renewable sources. An analysis on transient behaviors of an RFB is a key issue for these applications. An RFB is governed by electrical, chemical, and fluid dynamics. The hybrid structure makes the analysis difficult. To analyze transient behaviors of an RFB, the exact model is necessary. In this paper, we focus on a change in a concentration of ions in the electrolyte, and simulate the change with a model which is mainly based on chemical kinetics. The simulation results introduces transient behaviors of an RFB in a response to a load variation. There are found three kinds of typical transient behaviors including oscillations. As results, it is clarified that the complex transient behaviors, due to slow and fast dynamics in the system, arise by the quick response to load.

Key Words: redox flow battery, chemical reaction, slow and fast dynamics, global dynamics

1. Introduction

Power storage is the most important element of power grid to overcome the restriction of simultaneous power balancing. With an increase of installation of the renewable energy sources, power storage should inevitably absorb the fluctuation. Power storage has advantages as a large capacity and a quick response [1]. The large capacity is necessary for applications like load leveling, and the quick response is necessary for applications like compensating sag and smoothing of the output of renewable sources. Among the possible storage systems, a Redox Flow Battery (RFB) has a feature of scalability [2, 3]. The feature is beneficial when installing the RFB in a various capacities of power grid. The feasibility of a Vanadium RFB for the load leveling was studied in Ohio [4]. A Vanadium RFB was applied for the compensating of the momentum voltage sag in a semiconductor factory in Japan [5]. A Vanadium RFB was tested for smoothing the output of the wind farm at Hokkaido, Japan [5, 6].
An analysis on transient behaviors of an RFB is a key issue for the applications. Transient behaviors of the RFB deeply depend on the chemical reaction and the flow of the electrolyte. However, the dynamics of the transient behaviors contain mixed times scale transient dynamics. Moreover, if an RFB is connected to power grid, it will include the electric circuit restriction. And previous analysis of RFB is still far from the practical operation.

An ODE model [7] is one of the more helpful tools to analyze the transient behavior. Researchers have developed several kinds of models such as empirical models, equivalent models, and ODE models to analyze transient behaviors of an RFB [8]. In [7], an ODE model is proposed mainly based on chemical kinetics. This model represents change in a concentration of ions governing transient behaviors of the RFB. This model enables us to consider the chemical reaction, the flow of electrolyte, and the electric circuit restriction. The authors simulate electromotive force (EMF) at charging/discharging operation under constant current. The simulation results were confirmed by comparing to the experimental results in a constant current setting. The result showed that the model was valid.

We use the model suggested in [7] and research transient behaviors of a Vanadium RFB in a response to a load variation, and consider the dynamical mechanism of the transient behaviors. In the research, the transient behaviors shows a non linearity.

2. Current at transient due to load variation

This chapter discusses, transient behaviors of the RFB in a response to a load variation using the model based on chemical kinetics [7]. After introducing the model, the setting of simulation is explained. Here are found three types of transient behaviors in the simulations.

2.1 Model equation

A model of the micro RFB was introduced based on chemical kinetics [7]. The model represents a change in concentration of ions and EMF. Table I shows the nomenclature.

<table>
<thead>
<tr>
<th>Nomenclature</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$c_c$</td>
<td>Concentration of ions (V$^{2+}$) in cell mol L$^{-1}$</td>
</tr>
<tr>
<td>$c_t$</td>
<td>Concentration of ions (V$^{2+}$) in tank mol L$^{-1}$</td>
</tr>
<tr>
<td>$i$</td>
<td>Current A</td>
</tr>
<tr>
<td>$W$</td>
<td>Flow rate L min$^{-1}$</td>
</tr>
<tr>
<td>$\alpha_c$</td>
<td>Volume of cell L</td>
</tr>
<tr>
<td>$\alpha_t$</td>
<td>Volume of tank L</td>
</tr>
<tr>
<td>$F$</td>
<td>Faraday constant C mol$^{-1}$</td>
</tr>
<tr>
<td>$c_{max}$</td>
<td>Maximum of $c_c$ mol L$^{-1}$</td>
</tr>
<tr>
<td>$E_{oc}^{0}$</td>
<td>$E_{oc}$ at $c_c = c_{max}/2$ V</td>
</tr>
</tbody>
</table>

A change in concentration of ions is modeled by considering the reduction-oxidation reaction and the electrolyte flow. Figure 1 illustrates the scheme of the Vanadium RFB. The RFB mainly consists of a cell unit and a tank [3]. In the cell, the chemical energy is converted to electrical energy by reduction-oxidation reaction. The reaction is represented as following Eqs. (1a) and (1b) [9].
\[
\begin{align*}
\text{VO}_2^+ + 2\text{H}^+ + e^- &\rightleftharpoons \text{VO}^{2+} + \text{H}_2\text{O} \quad (1a) \\
\text{V}^{2+} &\rightleftharpoons \text{V}^{3+} + e^- \quad (1b)
\end{align*}
\]

The concentration of \(\text{VO}_2^+\) or \(\text{V}^{2+}\) at the cell governs the reaction. In the tank, the chemical energy is stored as a form of ion substantial. The electrolyte circulates between the cell and the tanks by pumps. The circulation makes a flow in the cell to supply the concentration of ions for the continuous reaction described by Eqs. (1a) and (1b). The phenomena in the RFB make it difficult to describe the change in the concentration of ions and the voltages. Then, assumptions are needed to simplify the phenomena. Here we set following assumptions,

- Chemical kinetics is restricted by the current in the external circuit.
- The electrolyte keeps the consistency of ions.
- The time delay of circulation of electrolyte is negligible.
- The concentration of ions (\(\text{V}^{2+}\)) in the negative half cell is equal to the concentration of ions (\(\text{VO}_2^+\)) in the positive half cell.

The change in the concentration of ions in the RFB is described based on these assumptions as following Eqs. (2) and (3) [7].

\[
\begin{align*}
\frac{d^2c}{dt^2} &= -W \left( \frac{1}{\alpha_c} + \frac{1}{\alpha_t} \right) \frac{dc}{dt} - \frac{Wi}{\alpha_c\alpha_t F} - \frac{1}{\alpha_c F} \frac{di}{dt} \quad (2) \\
\frac{dc}{dt} &= -\frac{\alpha_c}{\alpha_t} \frac{dc}{dt} - \frac{i}{\alpha_t F} \quad (3)
\end{align*}
\]

When the RFB is charging/discharging, \(i\) is negative/positive respectively.

The model of the EMF is derived based on Nersnst’s equation [10]. Nersnst’s equation gives the equilibrium potential of the battery. And from experiments in [11], the change in the concentration of \(\text{H}^+\) is also small enough to be ignored. Then, the model of the EMF is derived as following.

\[
E_{ec} = E_{ec}^0 + \frac{2RT}{F} \ln \frac{c_c}{c_{max} - c_c} \quad (4)
\]

### 2.2 Simulation setting

Here explains the setting of the simulation. Figure 2 shows the target system of the simulation. At \(t = 0\) s, the switch turns on and the load is forced to a step change. The setting enables us to study the response of the RFB to the load variation. From KVL, following equation is obtained.

\[
\frac{di}{dt} = -\frac{1}{L} \left\{ (r_1 + r_2)i - \left( E_{ec}^0 + \frac{2RT}{F} \ln \frac{c_c}{c_{max} - c_c} \right) \right\} \quad (5)
\]

By using Eqs. (2) and (5), the following equation is derived.

\[
\frac{d^2c}{dt^2} = -W \left( \frac{1}{\alpha_c} + \frac{1}{\alpha_t} \right) \frac{dc}{dt} + \left( \frac{r_1 + r_2}{L} - \frac{W}{\alpha_t} \right) \frac{i}{\alpha_c F} - \frac{1}{\alpha_c F L} \left( E_{ec}^0 + \frac{2RT}{F} \ln \frac{c_c}{c_{max} - c_c} \right) \quad (6)
\]

![Fig. 2. Target system of simulation which include RFB. The load of RFB has changed in a step at \(t = 0\) s.](image-url)
Table II. Parameters of RFB connected to circuit (Ref. [7]).

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\alpha_c$</td>
<td>0.100</td>
<td>L</td>
</tr>
<tr>
<td>$\alpha_t$</td>
<td>0.900</td>
<td>L</td>
</tr>
<tr>
<td>$T$</td>
<td>307</td>
<td>K</td>
</tr>
<tr>
<td>$c_{\text{max}}$</td>
<td>1.70</td>
<td>mol L$^{-1}$</td>
</tr>
</tbody>
</table>

Equations (4)–(6) enable to simulate the transient behaviors of the RFB in this setting. Table II shows the parameters of the RFB. The initial condition of the simulation is determined by putting assumptions as followings.

- $\frac{di}{dt} = 0 \ (t \to -0)$.
- $c_c = c_t \ (t \to -0)$.

In this simulation, fourth-order Runge-Kutta method [12] is adopted to solve the ODE. The step size is fixed at $h = 0.001$ s.

2.3 Result of simulation

In this section, first, the results of the simulation is explained and the transient behaviors are grouped into three types. Second, the consumption of the ions in the tank is examined in rate with comparing the transient behaviors of current.

The simulation reveals that the current depends on the flow rate and behaves by different mechanics. Figure 3 shows the result of the simulation. The initial value of the concentration of ions in the cell $c_{c0}$ is fixed at 0.125 mol L$^{-1}$. And the flow rate is set at $W = 0.050 \text{ L min}^{-1}$, 0.100 L min$^{-1}$, and 0.200 L min$^{-1}$. As Figs. 3(a) and 3(b) show, at $W = 0.050 \text{ L min}^{-1}$, the current and the EMF show sharp drops and the discharging simultaneously stops at the drops. We call the mode Case1. On the other hand, at $W = 0.200 \text{ L min}^{-1}$, the current and the EMF show gradual decreases and discharges slowly. The discharging times are long. We call the mode Case2. At $W = 0.100 \text{ L min}^{-1}$, the current and the EMF show an oscillation. It is called Case3. The transient behaviors due to other initial conditions are also categorized to the Case1, 2, and 3. There seems to be critical states in Fig. 3.

![Simulated results of transient behaviors of RFB due to load variation](image)

**Fig. 3.** Simulated results of transient behaviors of RFB due to load variation. The initial value of the concentration of ions in the cell ($c_{c0}$) is fixed at 0.125 mol L$^{-1}$. The flow rate is set at $W = 0.050 \text{ L min}^{-1}$, 0.100 L min$^{-1}$, and 0.200 L min$^{-1}$. The transient behaviors are categorized into three types (Case1–3).

The difference of the transient behaviors among the cases is corresponds to the consumption rate of ions in the tank. As showed in Fig. 3(c), almost all the ions in the tank are not consumed at $W = 0.050 \text{ L min}^{-1}$. It suggests that the transient behaviors are allocated to the consumption rate of the ion in the tank.
In order to confirm the assumption, the consumption rate of the ions in the tank is calculated for $W = 0.001 \text{ L min}^{-1}–0.200 \text{ L min}^{-1}$ and $c_{t0} = 0.01 \text{ mol L}^{-1}–1.00 \text{ mol L}^{-1}$. The consumption rate is defined as following.

$$\varepsilon_t = \frac{c_{t0} - c_{tf}}{c_{t0}} \quad (7)$$

Here, $c_{tf}$ denotes the concentration of ions in the tank at the time when the discharging has finished. The results are shown in Fig. 4(a). As showed in the figure, a line divides the graph into two regions. The region above the line represents the complete consumption of ions in the tank, and the below represents the remaining of ions until the end of discharging. Transient behaviors of current are simulated under conditions A1–4 as showed in Fig. 4(b). When the conditions are set at A1 and A4, the current behaves as classified in Case2. When the conditions are set at A2 and A3, the current behaves as classified in Case1. Transient behaviors of current are also simulated under conditions L1–12 as showed in Fig. 4(c). When the conditions are set at L1–12, the current behaves as classified in Case3. Figure 4 shows that the transient behaviors are actually correspond to the consumption of the ions in the tank.

### 3. Dynamical mechanism of transient behaviors

There seems to exist a mechanism which governs the transient behaviors to lead them into three types. In this chapter, we are going to focus on a dynamical mechanism of the transient behaviors. A dynamical mechanism of the three types of the transient behaviors is discussed with a dimensionless model in this chapter. The following discussions are from the viewpoint of local dynamics around fixed point and global phase structures.

#### 3.1 Analysis around a fixed point

The behavior of the system is described by the evolution of the variables $c_c$, $dc_c/d\tau$, and $i$. The evolution is modeled by Eqs. (5) and (6). The target system is modeled by following Eqs. (8a)–(8c) from Eqs. (5) and (6).
Eigenvalue of $\delta x_3/\delta t = -x_3 + 1 + \varepsilon \ln \frac{x_1}{1 - x_1}$ (8c)

Where $x_1$, $x_2$, and $x_3$ are the dimensionless variables corresponding to $c_c$, $dc_c/dt$, and $i$ with the constants $\hat{c}$, $\hat{i}$, and $\hat{t}$. The variables $c_c$, $dc_c/dt$, and $i$ have the different dimension. Then these variables must be dimensionless. in order to discuss the dynamical mechanism of the transient behavior. The constants $\hat{c}$, $\hat{i}$, and $\hat{t}$ are given by Eq. (9).

$$\hat{c} = c_{\text{max}}, \hat{i} = \sqrt{\frac{\alpha_c F L c_{\text{max}}}{E_0}}, \hat{t} = \frac{E_0}{r_1 + r_2}$$ (9)

Where the parameters $\beta$, $\gamma$, $\delta$, and $\varepsilon$ are given by Eq. (10).

$$\beta = W \left( \frac{1}{\alpha_c} + \frac{1}{\alpha_i} \right), \gamma = \frac{W L}{\alpha_t (r_1 + r_2)}, \delta = \frac{\hat{t}}{\hat{t}}, \varepsilon = \frac{2RT}{FE_0}$$ (10)

From $dx/d\tau = 0 \ (x = [x_1 \ x_2 \ x_3]^T)$, the system has only one fixed point $x^* = [3.51 \times 10^{-12} \ 0 \ 0]^T$. The fixed point corresponds to the state in which the EMF is 0 V, the rate of change in the concentration of ions in the cell $dc_c/dt$ is zero, and the current $i$ is 0 A.

The local stability is analyzed with eigenvalues of a linearized model of Eqs. (8a)–(8c) [13]. The linearization around $x^*$ is described by Eq. (11).

$$\Delta x = A \Delta x$$ (11)

Here, $\Delta x$ is $x - x^*$. The matrix associated with the linearized model is given as following Eq. (12).

$$A = \begin{bmatrix} 0 & 1 & 0 \\ -f(x^*) & -\beta & 1 - \gamma \\ f(x^*)/\delta & 0 & -1/\delta \end{bmatrix}$$ (12)

Where $f(x)$ is given by Eq. (13).

$$f(x) = \frac{\varepsilon}{x_1(1 - x_1)}$$ (13)

Table III shows eigenvalues of $A$ for $W = 0.050 \text{ L min}^{-1}$, $0.100 \text{ L min}^{-1}$, and $0.200 \text{ L min}^{-1}$. For these three parameters, the real part of eigenvalues are negative. Then, the fixed point $x^*$ is locally

<table>
<thead>
<tr>
<th>$W$(L min$^{-1}$)</th>
<th>Eigen value of $A$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.050</td>
<td>$-8.70 + 1.49 \times 10^5 j$</td>
</tr>
<tr>
<td></td>
<td>$-8.70 - 1.49 \times 10^5 j$</td>
</tr>
<tr>
<td></td>
<td>$-3.17 \times 10^{-2}$</td>
</tr>
<tr>
<td>0.100</td>
<td>$-8.84 + 1.49 \times 10^5 j$</td>
</tr>
<tr>
<td></td>
<td>$-8.84 - 1.49 \times 10^5 j$</td>
</tr>
<tr>
<td></td>
<td>$-6.34 \times 10^{-2}$</td>
</tr>
<tr>
<td>0.200</td>
<td>$-9.13 + 1.49 \times 10^5 j$</td>
</tr>
<tr>
<td></td>
<td>$-9.13 - 1.49 \times 10^5 j$</td>
</tr>
<tr>
<td></td>
<td>$-12.7 \times 10^{-2}$</td>
</tr>
</tbody>
</table>
stable, for these $W$. The stability implies the convergence of the solutions in the neighborhoods of the fixed point. Moreover while the solutions are approaching the fixed point, the solution oscillates around the fixed point [13]. That is, the original values also can oscillate around the fixed point.

On the other hand, the dynamics apart from the fixed point is governed by the vector flow of global phase structure. Figure 5 illustrates the trajectory solutions categorized Case1–3. Figures 5(a)–(d) show trajectories of the solutions categorized into Case1. The trajectories will not converge to the fixed point. Figures 5(e)–(h) show the trajectories of the solutions categorized into Case3. They will not oscillate around the fixed point. The obtained solutions show the features of the global phase structure which is governed by the non linearity.

3.2 Global phase structure

This section discusses a part of the global phase structure of the solutions and the vector field. The global phase structure is magnified at small scale for visualizing the vector field. The approach is based on the knowledge of fast-slow system [14, 15].

Figure 6(a) shows a part of the solutions for $W=0.100 \text{ L min}^{-1}$. In this figure, the oscillations are found in a small scale which is $x \sim 10^{-4}$. $x_1$ corresponds to $i$. Then, oscillations occur at low concentration of ions at the cell. On the other hand, the scale of changes in $x_3$, corresponding to $i$, is much bigger than both $x_1$ and $x_2$. This implies the current is sensitive to the change in concentration of ions. The scale reveals the magnification characteristics in the battery from ion density to the current.

The vector field is showed in Figs. 6(b)–(j). Figures 6(b)–(d) show the vector field and the trajectories of the solutions on the planes $x_2=-2.0 \times 10^{-3}, 0$, and $2.0 \times 10^{-3}$. In the figures, the trajectories converge to the nullcline $dx_3/d\tau=0$. When $dx_3/d\tau=0$ is established, the RFB is limited by circuit condition. Fast flows appear along $x_3$, due to the value of $\delta$ in Eqs. (8a)–(8c). The value of $\delta$ implies the ratio of time scale of current to that of change in concentration of ions. Figures 6(e)–(g) show the vector field and the trajectories of the solutions on the planes $x_3=0.60, 0.66$, and 0.70. As the figures show, the trajectories converge to the nullcline $dx_1/d\tau = 0$. Figures 6(h)–(j) show the vector field and the trajectories of the solutions on the planes $x_1=0.50 \times 10^{-4}, 1.0 \times 10^{-4}$, and $2.0 \times 10^{-4}$. As the figures show, the trajectories converge to the nullcline $dx_1/d\tau = 0$. From the vector field, it is found that the system is fast-slow system. But the system can not be divided into slow-subsystem.
Fig. 6. Global phase structure of solutions and vector field at \(W = 0.100 \text{L.min}^{-1}\). The area where the oscillation occur is focused on. In this area, the concentration of ions \((x_1)\) is low and the current \((x_3)\) changes largely compared to other two variables. (b)–(j) Vector field and nullcline is showed. Fast flow transverses to the nullcline \(d x_3 / d \tau = 0\).

The mechanism of the oscillations can be discussed by linearization with taking a plane perpendicular to a slow variable, \(x_1\) is one of the slow variables. The values of \(x_1\) are swapped in \(f(x)\) from \(x_1 = 0.0000010\) to \(x_1 = 0.005\). And the eigen values on each planes are shown in Figs. 7(a) and 7(b). In the figures, all of the eigen values are located on complex plane with \(\text{Re}[\lambda] < 0\) \(i = 1, 2, 3\). Then, a bifurcation appears at \(x_1 = 5.72 \times 10^{-4}\). As shown in \(x_1 > 5.72 \times 10^{-4}\), the eigen values become real. It implies that there does not appear any oscillatory transient behaviors in \(x_1 > 5.72 \times 10^{-4}\). And \(\lambda_1\) and \(\lambda_2\) come close to each other as \(x_1\) decreases. At \(x_1 = 5.72 \times 10^{-4}\) they conjoint. After the conjoint by \(x_1\) decreasing, for \(x_1 < 5.72 \times 10^{-4}\), the values increase as \(x_1\) decreases. This clearly shows the appearance of oscillation in \(x_1 < 5.72 \times 10^{-4}\). Figure 7(c) shows the phase lags of \(\lambda_i\) \(i = 1, 2, 3\). \(x_1 \rightarrow 0\), the lags converge to 90°, 90°, and 180°. Then, the phase lags of the oscillations are also expected to converge 90°, 90°, and 180°. Actually, in Figs. 5(b)–(j), the oscillation in \(x_1\) has about 90° phase lag to \(x_2\) and \(x_3\), and the oscillation in \(x_2\) has about 180° phase lag to \(x_3\). The eigen values in Fig. 7 certainly shows the mechanism of the oscillation.

3.3 Behavior in the original variables

The analysis in Sec. 3.1, and 3.2 explains the behavior of the system. The validity is given by Fig. 8. This figure shows the evolution of the variables in the original scale.

Figure 5 denies the effect of the fixed point to the phenomena denoted in Chap. 2. At the fixed point, \(c_c = 5.97 \text{mol.L}^{-1}\), \(d c_c / d t = 0 \text{mol.L}^{-1.s}^{-1}\), and \(i = 0\text{A}\), and the variables do not change. Figures 8(a)–(c) show that the fixed point also does not secure the convergence of a part of the solutions in the original scale same as Figs. 5(a)–(d). As explained in Chap. 2, for this case, the discharging is forcibly stopped due to the rapid consumption of the ions in the cell despite the existance of the ions in the tank. The conditions of the oscillation also implies that fixed point does not decide the behavior of the system. For Case2, as Figs. 5(e) and 5(h) show, the solution
Fig. 7. (a)(b) Eigen values of Jacobin matrix $A$. A bifurcation appears at $x_1 = 5.72 \times 10^{-4}$. In $x_1 < 5.72 \times 10^{-4}$, appearance of oscillations is showed by imaginary part of eigen values. (c) Phase lags of eigen values $\lambda_i$ ($i = 1, 2, 3$). Phase lags of oscillations are expected to converge to $90^\circ$, $90^\circ$, and $180^\circ$.

oscillates apart from the fixed point. For original scale, as Fig. 8 shows, the oscillation occurs for $c_c \sim 10^{-5} - 10^{-4}$ mol L$^{-1}$ and $i \sim 10A$.

Figure 6 shows that this system is a slow-fast system. Due to $\delta$, $x_3$ behaves as a fast variable. As showed in Fig. 8(d) Then $di/dt = 0$ A s$^{-1}$ is satisfied in most of the period. And when the $i$ is oscillating, the value of $di/dt$ is larger than that of $dc_c/dt$.

Fig. 8. Behavior of solutions in original scale. The behavior verifies the discussion in the phase space. $c_c$, $dc_c/dt$, and $i$ are correspond to $x_1$, $x_2$, and $x_3$. Some solutions classified as Case 1 do not approach the fixed point. Solutions oscillates for $c_c \sim 10^{-5} - 10^{-4}$ mol L$^{-1}$. This area is apart from the fixed point. $i$ is a fast variable and $di/dt = 0$ A s$^{-1}$ is satisfied for most of the period.
4. Conclusion

We discussed the transient behaviors of the RFB in a response to a load variation, and we found the dynamical mechanism of the transient behaviors. Results are summarized as followings.

1. Three types of transient behaviors appear and one of them causes oscillations. The transient behaviors depend on the value of flow rate and the initial value of the concentration of ions.

2. The global phase structure determines the transient behaviors. From the global phase structure, it is clarified that the behaviors are limited by electrical circuit restriction due to the value of a parameter which corresponds to the time scale ratio of current to the changing ratio in concentration of ions. It is also clarified that a necessary condition for occurrence of the oscillations are governed by the low concentration of ions.

The results show that several kinds of phenomena appear in transient behaviors of single RFB, when the RFB is connected to power grid. According to flow rates or initial values of concentration of ions, the discharging of the RFB stops before it consumes all of the ions. On the other hand, there are conditions which arise oscillations. In the worst case, it may cause resonances with external systems. To avoid these anomalous phenomena, a control method of multi layer must be developed with considering chemical, fluid dynamics, and electrical circuit restriction.

The transient behaviors in the wide range are based on the global dynamics, so that the control method must pay attention to the mechanism. However, the whole dynamical structure has not been figured out through the simulations. This paper brought us an interesting dynamical behavior with a difficulty of a mixed time scales system because of the global phase structure along the slowest variable.

References


