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AUTHOR(S):

Morinari, Takao

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Relationship between Magnetic Anisotropy Below Pseudogap Temperature and Short-Range Antiferromagnetic Order in High-Temperature Cuprate Superconductor

Takao Morinari

Graduate School of Human and Environmental Studies, Kyoto University, Kyoto 606-8501, Japan

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The central issue in high-temperature cuprate superconductors is the pseudogap state appearing below the pseudogap temperature T^* , which is well above the superconducting transition temperature. In this study, we theoretically investigate the rapid increase of the magnetic anisotropy below the pseudogap temperature detected by the recent torque-magnetometry measurements on $\text{YBa}_2\text{Cu}_3\text{O}_y$ [Y. Sato *et al.*, Nat. Phys., 13, 1074 (2017)]. Applying the spin Green's function formalism including the Dzyaloshinskii–Moriya interaction arising from the buckling of the CuO_2 plane, we obtain results that are in good agreement with the experiment and find a scaling relationship. Our analysis suggests that the characteristic temperature associated with the magnetic anisotropy, which coincides with T^* , is not a phase transition temperature but a crossover temperature associated with the short-range antiferromagnetic order.

The central issue in high-temperature cuprate superconductors[1] is the nature and origin of the normal state pseudogap. Below the pseudogap temperature, T^* , which is higher than the superconducting transition temperature, T_c , a partial gap is observed in various experiments.[2, 3] The key question about the pseudogap is whether T^* is a phase transition temperature or a crossover temperature. For instance, resonant ultrasound spectroscopy measurements exhibited a discontinuous change in the temperature dependence of frequency supporting that T^* is the phase transition temperature.[4] The measurement of the second-harmonic response, which detected the inversion symmetry breaking below T^* , also supported the phase transition picture.[5] Meanwhile, a phenomenological theory describing a crossover scenario was proposed,[6, 7] and spectroscopic and thermodynamic experiments were discussed using a model Green's function with doping-dependent parameters. On the other hand, recent nuclear magnetic resonance[8, 9] and x-ray scattering[10–12] studies reported a symmetry-breaking phase of the charge-density wave order in the pseudogap phase. Although the role of this order is unclear, it seems to compete with superconductivity[13] and it appears at a temperature between T^* and T_c . It has also been proposed that these orders are intertwined.[14]

In this Letter, we focus on the recent torque-magnetometry measurements on $\text{YBa}_2\text{Cu}_3\text{O}_y$ (YBCO) reporting a rapid increase in anisotropic spin susceptibility within the $a - b$ plane below T^* . [15] A magnetic torque is induced if the magnetization $\mathbf{M}$ of the sample is not parallel to the applied magnetic field $\mathbf{H}$. When the magnetic field is rotated in the $x - y$ ($a - b$) plane by an azimuthal angle ϕ , the magnetic torque is given by

$$\begin{aligned}\tau_\phi &= \mu_0 V (\mathbf{M} \times \mathbf{H})_z \\ &= \frac{1}{2} \mu_0 V H^2 [(\chi_{xx} - \chi_{yy}) \sin 2\phi - 2\chi_{xy} \cos 2\phi].\end{aligned}\quad (1)$$

Here, μ_0 is the permeability of vacuum and V is the sample volume. The spin susceptibility is denoted by $\chi_{\alpha\beta} = \partial M_\alpha / \partial (\mu_0 H_\beta)$, with $\alpha, \beta = x, y$. For the CuO_2

plane with fourfold rotational symmetry, C_4 , we see that $\tau_\phi = 0$. In YBCO, τ_ϕ exhibits sinusoidal oscillation with $\chi_{xx} > \chi_{yy}$ and $\chi_{xy} = 0$. [15] A rapid increase in the amplitude is observed below the characteristic temperature T_τ that coincides with the T^* value determined by other experiments. [15] The authors in Ref. 15 conclude that T_τ corresponds to a nematic phase transition temperature and thus T^* is also a phase transition temperature.

We propose a theory to explain this magnetic torque experiment. The theory is based on a localized spin model with anisotropic magnetic interaction. For this, we assume the Dzyaloshinskii–Moriya (DM) interaction [16–18] arising from the buckling of the CuO_2 plane. Usually, one may neglect this DM interaction owing to its energy scale. However, it breaks the C_4 symmetry and can play an important role for the physical quantities that do not vanish when the C_4 symmetry is broken. Applying second-order perturbation theory, we show that τ_ϕ is proportional to cube of the spin susceptibility, and there is a scaling relationship. The analysis suggests that T_τ is the onset of a short-range antiferromagnetic (AF) order.

In describing the localized spins in the parent compound of the cuprate, the renormalization group analysis of the nonlinear σ model was successful. [19] Mean field theories such as Schwinger bosons [20] and modified spin wave theory [21] also gave a good description of the system. However, these approaches are useful only in the low-temperature regime. At high temperatures around T^* , we need to take a different approach. Here, we take the spin Green's function approach. [22–27]

For the calculation of τ_ϕ , we need to compute the following correlation functions:

$$\langle S_i^x S_j^x \rangle - \langle S_i^y S_j^y \rangle = \text{Re} \langle S_i^+ S_j^+ \rangle, \quad (2)$$

$$\langle S_i^x S_j^y \rangle + \langle S_i^y S_j^x \rangle = \text{Im} \langle S_i^+ S_j^+ \rangle. \quad (3)$$

Here, S_j^α ($\alpha = x, y$) denotes the α component of the spin moment at site j . Note that these correlation functions depend on $i - j$ because of the translational invariance in the pseudogap phase. In the absence of any magnetically anisotropic term, the right-hand sides of these equa-

tions vanish. The Hamiltonian for the localized $S = 1/2$ moments, on inclusion of the DM interaction mentioned above, is given by

$$\mathcal{H} = J_p \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j + \sum_{\langle i,j \rangle} \mathbf{D}_{ij} \cdot (\mathbf{S}_i \times \mathbf{S}_j). \quad (4)$$

Here, J_p is the exchange interaction between nearest-neighbor spins, which is assumed to depend on the doped hole concentration, p . The three-dimensional vector $\mathbf{D}_{ij} = \mathbf{D}_{i-j}$ is the DM vector on the bond connecting sites i and j . For the case of $D_{i-j}^z = 0$, the DM interaction term is rewritten as

$$\mathcal{H}_{\text{DM}} = \sum_i \sum_{\delta=\hat{a},\hat{b}} (g_\delta S_i^- S_{i+\delta}^z + H.c.). \quad (5)$$

Here, $\hat{a}$ and $\hat{b}$ are the displacement vectors along the a and b axes, respectively, and $g_\delta = (iD_\delta^x - D_\delta^y)/2$, with D_δ^α being the α component of the DM vector. It is obvious from Eq. (5), that its first-order contribution to $\langle S_i^+ S_j^+ \rangle$ vanishes, but the second-order contribution does not.

Now, we define the following Matsubara Green's function:

$$G_{i-j}(\tau) = -\langle T_\tau S_i^+(\tau) S_j^-(0) \rangle, \quad (6)$$

with τ being the imaginary time. Taking the derivative of $G_{i-j}(\tau)$ with respect to τ twice, and then applying the Tyablikov approximation and the Fourier transform, we obtain[23, 24]

$$G_{\mathbf{k}}(i\omega_n) = \frac{4J_p c_1 (1 - \gamma_{\mathbf{k}})}{(i\omega_n)^2 - \omega_{\mathbf{k}}^2}, \quad (7)$$

with ω_n denoting the Matsubara frequency and

$$c_{i-j} = 4 \langle S_i^z S_j^z \rangle = 2 \langle S_i^+ S_j^- \rangle = 2 \langle S_i^- S_j^+ \rangle. \quad (8)$$

(Hereafter, we set $\hbar = 1$ and the lattice constant is set to unity.) The spin excitation energy $\omega_{\mathbf{k}}$ is given by

$$\omega_{\mathbf{k}} = \sqrt{8\alpha |c_1| J_p \sqrt{(1 - \gamma_{\mathbf{k}})(1 + \Delta + \gamma_{\mathbf{k}})}}, \quad (9)$$

with $\gamma_{\mathbf{k}} = (\cos k_x + \cos k_y)/2$ and $\Delta = (1 - \alpha c_1 + 3\alpha c_2)/(4\alpha |c_1|) - 1$. The parameter α is introduced while applying the Tyablikov approximation,[23] which is interpreted as a vertex correction.[24] The parameter c_2 is defined by $c_2 = \sum_{\delta'(\neq -\delta)} c_{\delta+\delta'}/3$. The

parameters c_1 , α , and c_2 are determined by solving the following self-consistent equations[24]:

$$1 = -\frac{4J_p c_1}{N} \sum_{\mathbf{k}} \frac{1 - \gamma_{\mathbf{k}}}{\omega_{\mathbf{k}}} \coth\left(\frac{\omega_{\mathbf{k}}}{2k_B T}\right), \quad (10)$$

$$c_1 = -\frac{4J_p c_1}{N} \sum_{\mathbf{k}} \frac{\gamma_{\mathbf{k}}(1 - \gamma_{\mathbf{k}})}{\omega_{\mathbf{k}}} \coth\left(\frac{\omega_{\mathbf{k}}}{2k_B T}\right), \quad (11)$$

$$\frac{3c_2' + 1}{4} = -\frac{4J_p c_1}{N} \sum_{\mathbf{k}} \frac{\gamma_{\mathbf{k}}^2 (1 - \gamma_{\mathbf{k}})}{\omega_{\mathbf{k}}} \coth\left(\frac{\omega_{\mathbf{k}}}{2k_B T}\right). \quad (12)$$

Here, N is the number of the lattice sites, and k_B is the Boltzmann constant.

The second-order perturbative calculation with respect to H_{DM} gives

$$\begin{aligned} \langle S_i^+ S_j^+ \rangle &= \frac{k_B T}{2N} \sum_{\mathbf{k}} \sum_{\delta, \delta'} g_\delta g_{\delta'} e^{i\mathbf{k} \cdot (\delta - \delta')} \sum_{i\omega_n} e^{i\mathbf{k} \cdot (\mathbf{R}_i - \mathbf{R}_j)} \\ &\quad \times G_{\mathbf{k}}(i\omega_n) G_{-\mathbf{k}}(-i\omega_n) G_{-\mathbf{k}}(i\omega_n), \end{aligned} \quad (13)$$

where $\mathbf{R}_i$ denotes the position of site i . The summation over i shows that we need only the $\mathbf{k} = 0$ term. The terms with $\omega_n \neq 0$ vanish if we set $\mathbf{k} = 0$. Therefore, we may set $\omega_n = 0$, and then $\mathbf{k} = 0$. The result is

$$\frac{1}{N} \sum_i \langle S_i^+ S_j^+ \rangle = \frac{k_B T}{16J_p^3 \alpha^3 (2 + \Delta)^3} \Gamma, \quad (14)$$

with $\Gamma = (g_{\hat{a}} + g_{\hat{b}})^2$. By using this result, we obtain

$$\Delta\chi \equiv \frac{\tau_\phi}{\mu_0 V H^2/2} = \frac{\mu_0 \mu_B^2}{2v_c} \frac{\Gamma_{\parallel} \sin 2\phi - \Gamma_{\perp} \cos 2\phi}{J_p^3 \alpha^3 (2 + \Delta)^3}, \quad (15)$$

where v_c is the unit cell volume per CuO_2 plane, and $\Gamma_{\parallel} = \text{Re}\Gamma$ and $\Gamma_{\perp} = \text{Im}\Gamma$. $\Delta\chi$ oscillates with two components: one is proportional to $\sin 2\phi$, and the other is proportional to $\cos 2\phi$. We note that[24]

$$\frac{1}{N} \sum_i \langle S_i^+ S_j^- \rangle = \frac{1}{2J_p \alpha (2 + \Delta)}. \quad (16)$$

Therefore, the right-hand side of Eq. (15) is proportional to the cube of the spin susceptibility.

Now we apply the theory to the experiment.[15] For YBCO, $D_a^y \neq 0$, $D_b^x \neq 0$, and the other components are negligible.[28] Thus, $\Gamma_{\parallel} \neq 0$ and $\Gamma_{\perp} = -[D_a^{(x)} D_a^{(y)} + D_b^{(x)} D_b^{(y)}]/2 = 0$. Therefore, we find $\tau_\phi \propto \sin 2\phi$, which is the oscillation pattern observed in the experiment.[15] Hereafter, we consider the case $\Gamma_{\perp} = 0$, and denote $\Delta\chi$ as $\Delta\chi_{\parallel}$. The theoretical formula (15) is compared with the experiment[15] with the fitting parameters J_p and $\Gamma_{\parallel}$ by including a constant term consisting of a temperature-independent paramagnetic component. The results shown in Fig. 1 demonstrate that the theory is in good agreement with the experiment. From the fitting, we found $J_{0.11} = 241$ K, $J_{0.13} = 183$ K, and $J_{0.15} = 170$ K as the values of J_p for $p = 0.11, 0.13$, and 0.15 respectively. The value of J_p decreases as p is increased. This monotonic change in J_p as a function of p was also suggested from an analysis of the spin susceptibility and a scaling was found in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_{4-y}$. [29, 30] For $p = 0.11$, there is a discrepancy between theory and the experiment at low temperatures. This is because the spin Green's function approach is not reliable at low temperatures.[24] We note

FIG. 1. (color online) Comparisons between the formula (15) and the experiments[15] for hole concentrations (a) $p = 0.11$, (b) $p = 0.13$, and (c) $p = 0.15$. The solid lines represent the theory based on the spin Green's function.

that this discrepancy starts from $0.40J_p$ below the minimum of $\Delta\chi_{||}$. The data for $p = 0.13$ and $p = 0.15$ are well above this value.

From the formula (15), we see that $J_p^3\Delta\chi_{||}$ is independent of J_p . In order to remove constant components coming from doped holes, we subtract its minimum value from $\Delta\chi_{||}$, and then plot it as a function of the normal-

ized temperature in Fig. 2. All the experimental data fall on a single curve. From this analysis, we may conclude that $T_\tau \simeq 1.1J_p$. This characteristic temperature has a simple interpretation. The AF correlation length of the AF Heisenberg model with the exchange interaction J_p is given by[21]

$$\xi_{AF}/a \simeq \frac{0.819}{T/J_p} \exp\left(\frac{1.10}{T/J_p}\right), \quad (17)$$

where a is the lattice constant. From this formula, we find $\xi_{AF} \simeq 2a$ at $T = T_\tau$. In Fig. 2 we also plot the values computed using quantum Monte Carlo (QMC) results for the uniform spin susceptibility χ on the square lattice AF Heisenberg model.[31] These values are in good agreement with the data of $p = 0.11$ at low temperatures. However, the point computed from the QMC data around $T/J_p = 1.3$ does not agree with the experiment and the Green's function result. We note that we find $\Gamma_{||} < 0$ from the fact that the magnitude of the DM vector is proportional to the difference in the lattice constants in the orthorhombic phase of YBCO. This is consistent with the experiment because the maximum of χ corresponds to the minimum of $\Delta\chi_{||}$. We also note that the experimental data seem to be convex upward for $T > T_\tau$ at $p = 0.13$ and $p = 0.15$. However, a similar behavior is not discernible for $p = 0.11$. It might be related to the effect of doped holes and/or CuO chains.

FIG. 2. (color online) Scaling relationship suggested from the formula (15). $\Delta\chi_{||}^{\min}$ is the minimum of $\Delta\chi_{||}$ in Fig. 1. The unit of the vertical axis is K^3 . For the values of J_p , we take $J_{0.11} = 241$ K, $J_{0.13} = 183$ K, and $J_{0.15} = 170$ K for the experimental data. The values computed by using QMC result[31] are also shown.

Now we discuss the value of $\Gamma_{||}$. From the analysis shown in Fig. 2, we find $\sqrt{|\Gamma_{||}|} \simeq 100$ K. This apparently is too large if $\Gamma_{||}$ is associated with the buckling of the CuO₂ plane. Here, we need to include the effect of the doped holes. The exchange coupling between doped hole spins and the localized spins is described by $\mathcal{H}_K = J_K \sum_j \mathbf{S}_j \cdot (c_j^\dagger \boldsymbol{\sigma} c_j)$, where $J_K =$

$t_{dp}^2/(U_d - \Delta) + t_{dp}^2/(U_p + \Delta)$, where t_{dp} is the nearest-neighbor Cu-O hopping and U_d (U_p) is the Cu(O)-site Coulomb repulsion.[32–34] Δ is the energy difference between the O-site energy and the Cu-site energy. The two-component operator $c_j^\dagger$ (c_j) is the creation (annihilation) operator of the doped hole at site j , and σ is the three component vector of the Pauli matrices. The easiest way to include $\mathcal{H}_K$ is the coherent state path integral. By integrating out the doped hole fields, we find that the spin susceptibility χ is enhanced as $\chi/(1 - \eta\chi)$ with $\eta = 3J_K^2\chi_0^h$. Here, χ_0^h is the uniform spin susceptibility of the doped holes. Unfortunately no reliable theoretical formula for χ_0^h is available. Therefore, we use the formula for the non-interacting system, which is proportional to the density of states, and approximate it as $\chi_0^h \sim 1/t$ where $t \sim t_{dp}^2/\Delta$ is the effective hopping parameter of the doped holes.[32–34] Using the parameter values evaluated for the CuO₂ plane,[33–36] we find that $\eta/J_p \sim 10$. With this value of η/J_p , $\sqrt{|\Gamma_{||}|} \sim 2$ K. For $\eta/J_p = 9$, $\sqrt{|\Gamma_{||}|} \sim 15$ K. Although this is an approximate estimate, these values appear to be reasonable from

the fact that $\Gamma_{||}$ is proportional to the difference between the lattice constants along the a and b axes and also the buckling angle.

To conclude, we have shown that the result of the theory based on the spin Green's function with the DM interaction is in good agreement with the recent torque-magnetometry measurements of YBCO.[15] There is a clear scaling relationship as shown in Fig. 2. Our analysis shows that the magnetic anisotropy increases rapidly below $T_\tau \simeq 1.1J_p$ at which $\xi_{AF} \simeq 2a$. Therefore, T_τ is a crossover temperature associated with the short-range AF order, in contrast to the claim in Ref. 15 where T_τ is interpreted as an onset of a nematic phase transition. Given the experimental fact that T_τ coincides with the onset temperature of the pseudogap, the pseudogap may also be a crossover phenomenon.

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