

# Change of Plumb Line referred to the Axis of the Earth as found from the Results of the International Latitude Observations

(the second paper<sup>1</sup>)

By Eiiti Nisimura

(Received July 30, 1937)

In continuation of the first study on the subject of this title by Prof. T. Shida and Prof. M. Matsuyama,<sup>2</sup> we analysed the data given in "Ergebnisse des Internationalen Breitendienstes von 1912.0 bis 1922.7 (von B. Wanach und H. Mahnkopf)." The Report contains the results of the six observing stations of north parallels ( $\varphi = +39^{\circ}8'$ ).

|                            |                             |                       |
|----------------------------|-----------------------------|-----------------------|
| Mizusawa, Japan            | $\lambda = -141^{\circ} 8'$ | period, 1912.0-1922.7 |
| Tschardjui, Central Asia   | - 63 35                     | 1912.0-1919.4         |
| Carloforte, Italy          | - 8 19                      | 1912.0-1922.7         |
| Gaithersburg, East America | + 77 12                     | 1912.0-1915.0         |
| Cincinnati, Middle America | + 84 25                     | 1912.0-1916.0         |
| Ukiah, West America        | + 123 13                    | 1912.0-1922.7         |

And the present study was made of the results of the three stations— Mizusawa, Carloforte, and Ukiah, because of their continuous observations during the whole period.

The daily corrections read from the most probable curve of latitude at each station given in the Report, were applied to each observed value of each star-pair to eliminate the proper variation of latitude. The residuals thus obtained for each star-pair were divided into six sets (each containing two groups of stars), and in each set were arranged according to the hour-angle of the true moon at the time of observation of each star-pair. The mean of these six means shows the correlation of the moon's hour-angle and the latitude. The number of star-pairs used and mean hourly values obtained for three stations are shown in Tables I, II, III and Figs. 1, 2, 3. Analysing harmonically, multiplying by the augmenting factor and reducing to the

1. This paper was read at the Annual Meeting of the Physico-Mathematical Society of Japan, Osaka, 1935 April.

2. Mem. Coll. Sci. and Eng., Kyoto Imperial Univ., 4 (1912) 277-284.

mean inclination of the moon's orbit to the equator, the numerical values give the following expressions;

1912.0-1922.7

$$\begin{aligned} \text{Mizusawa} &\dots\dots\dots 0.^{\prime\prime}0032 \cos(2t - 260^\circ) \pm 0.^{\prime\prime}0014 \\ \text{Carloforte} &\dots\dots\dots 0.^{\prime\prime}0118 \cos(2t - 334^\circ) \pm 0.^{\prime\prime}0008 \\ \text{Ukiah} &\dots\dots\dots 0.^{\prime\prime}0105 \cos(2t - 11^\circ) \pm 0.^{\prime\prime}0013 \end{aligned}$$

where  $t$  is the hour-angle of the true moon.

The slight difference between the present result and that formerly obtained in the first paper for Carloforte ( $0.^{\prime\prime}00878 \cos(2t - 356^\circ)$ ) is considered to be attributable partly to the point that in the present analysis the hour-angle of the true moon was used instead of the mean moon in the first study. The results obtained are certainly influenced by the secondary effect of the ocean tide, and for two stations—Carloforte and Ukiah—the roughly estimated values of these effects may account for the inconsistency of the results. For Mizusawa, the secondary effect alone can not serve as the quantitative interpretation of its peculiar result and the problem remains unexplained. We intend to obtain in the near future more accurate values by covering the longer period of observation with the same analysing method and eliminating the secondary effect of the ocean tide in more detailed points.

In conclusion the writer wishes to express his cordial appreciation to the late Prof. T. Shida, by whose kind suggestion and encouragement the present analysis was commenced and carried out. The writer's cordial thanks are also due to Messrs. K. Itô, T. Kawahara, and H. Hayasi for their kind help provided in the present computation.

Mizusawa

Table I.

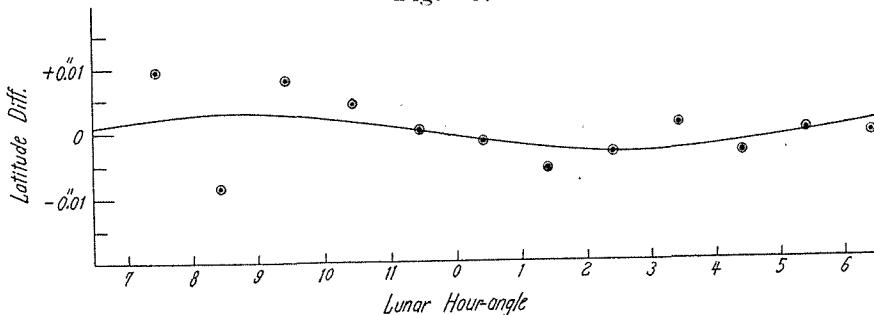
Number of Star-pairs

| Hour-angle<br>Group \ Group | 0 <sup>h</sup> | I    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | 10   | 11   |
|-----------------------------|----------------|------|------|------|------|------|------|------|------|------|------|------|
| IV, V                       | 204            | 228  | 251  | 242  | 247  | 239  | 241  | 259  | 293  | 290  | 286  | 273  |
| VI, VII                     | 264            | 263  | 299  | 323  | 315  | 298  | 286  | 243  | 236  | 239  | 283  | 270  |
| VIII, IX                    | 275            | 290  | 299  | 325  | 327  | 307  | 317  | 275  | 289  | 323  | 305  | 296  |
| X, XI                       | 310            | 316  | 308  | 280  | 306  | 299  | 318  | 290  | 326  | 349  | 337  | 308  |
| XII, I                      | 324            | 323  | 390  | 386  | 343  | 327  | 291  | 283  | 313  | 317  | 377  | 349  |
| II, III                     | 279            | 262  | 264  | 275  | 294  | 281  | 283  | 222  | 219  | 275  | 259  | 269  |
| Sum                         | 1656           | 1682 | 1811 | 1831 | 1832 | 1751 | 1736 | 1572 | 1676 | 1793 | 1847 | 1765 |

Mean Hourly Values

| Hour-angle<br>Group \ Group | 0 <sup>h</sup> | I    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | 10   | 11   |
|-----------------------------|----------------|------|------|------|------|------|------|------|------|------|------|------|
| IV, V                       | 0.6823         | 6868 | 6905 | 6639 | 6741 | 6836 | 6675 | 7029 | 6271 | 6819 | 7002 | 6909 |
| VI, VII                     | 6564           | 6389 | 6445 | 6486 | 6529 | 6345 | 6339 | 6252 | 5969 | 6286 | 6264 | 6237 |
| VIII, IX                    | 5204           | 5320 | 5402 | 5765 | 5487 | 5659 | 5493 | 5434 | 5263 | 5393 | 5177 | 5150 |
| X, XI                       | 6008           | 6096 | 6169 | 6313 | 6161 | 6334 | 6454 | 6637 | 6739 | 6579 | 6332 | 6325 |
| XII, I                      | 6736           | 6517 | 6568 | 6617 | 6585 | 6566 | 6760 | 6663 | 6742 | 6905 | 6915 | 6884 |
| II, III                     | 6759           | 6648 | 6505 | 6424 | 6479 | 6448 | 6417 | 6761 | 6705 | 6687 | 6763 | 6712 |
| Mean                        | 0.6349         | 6306 | 6332 | 6374 | 6330 | 6364 | 6356 | 6463 | 6281 | 6445 | 6409 | 6369 |
|                             | -15            | -58  | -32  | +10  | -34  | 0    | -8   | +99  | -83  | +81  | +45  | +5   |

Fig. I.



*Carloforte*

Table II.

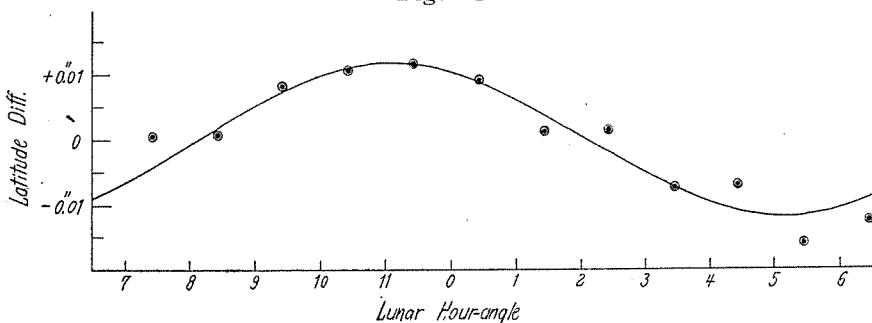
Number of Star-pairs

| Hour-angle<br>Group | 0 <sup>h</sup> | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | 10   | 11   |
|---------------------|----------------|------|------|------|------|------|------|------|------|------|------|------|
| IV, V               | 227            | 203  | 215  | 208  | 226  | 262  | 305  | 294  | 239  | 226  | 238  | 225  |
| VI, VII             | 277            | 294  | 288  | 292  | 307  | 287  | 285  | 257  | 257  | 250  | 259  | 239  |
| VIII, IX            | 402            | 385  | 381  | 413  | 429  | 456  | 438  | 418  | 417  | 392  | 344  | 365  |
| X, XI               | 621            | 586  | 593  | 601  | 656  | 719  | 720  | 756  | 757  | 745  | 704  | 659  |
| XII, I              | 452            | 441  | 429  | 422  | 433  | 416  | 429  | 433  | 438  | 460  | 484  | 484  |
| II, III             | 232            | 222  | 197  | 202  | 211  | 235  | 245  | 208  | 212  | 206  | 199  | 222  |
| Sum                 | 2211           | 2131 | 2103 | 2138 | 2262 | 2375 | 2422 | 2366 | 2320 | 2279 | 2228 | 2194 |

Mean Hourly Values

| Hour-angle<br>Group | 0 <sup>h</sup> | 1       | 2       | 3       | 4     | 5     | 6     | 7       | 8       | 9       | 10      | 11      |      |
|---------------------|----------------|---------|---------|---------|-------|-------|-------|---------|---------|---------|---------|---------|------|
| IV, V               | .1.0436        | .1.0059 | .1.0191 | .1.0060 | .9918 | .9737 | .9798 | .9789   | .9825   | .1.0219 | .1.0227 | .1.0356 |      |
| VI, VII             | .9850          | .9856   | .9899   | .9828   | .9833 | .9804 | .9595 | .9582   | .9664   | .9611   | .9615   | .9690   |      |
| VIII, IX            | .8791          | .8746   | .8782   | .8852   | .9042 | .8920 | .8941 | .9010   | .8834   | .8774   | .8684   | .8761   |      |
| X, XI               | .9708          | .9780   | .9581   | .9607   | .9683 | .9714 | .9791 | .9951   | .9962   | .9991   | .9952   | .9761   |      |
| XII, I              | .1.0174        | .1.0064 | .1.0014 | .9927   | .9867 | .9845 | .9966 | .1.0149 | .1.0256 | .1.0243 | .1.0328 | .1.0358 |      |
| II, III             | .1.0145        | .1.0121 | .1.0175 | .9819   | .9794 | .9573 | .9734 | .1.0094 | .1.0068 | .1.0221 | .1.0380 | .1.0312 |      |
| Mean                | "              | 0.9851  | 9771    | 9774    | 9682  | 9689  | 9599  | 9637    | 9762    | 9768    | 9843    | 9864    | 9873 |
|                     |                | +92     | +12     | +15     | -77   | -70   | -160  | -122    | +3      | +9      | +84     | +105    | +114 |

Fig. 2



Ukiah

Table III.

Number of Star-pairs

| Hour-angle<br>Group \ Group | 0 <sup>h</sup> | I    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | 10   | 11   |
|-----------------------------|----------------|------|------|------|------|------|------|------|------|------|------|------|
| IV, V                       | 166            | 176  | 171  | 183  | 193  | 167  | 173  | 190  | 189  | 181  | 154  | 144  |
| VI, VII                     | 167            | 158  | 150  | 187  | 209  | 230  | 208  | 188  | 193  | 204  | 234  | 200  |
| VIII, IX                    | 223            | 201  | 234  | 251  | 277  | 259  | 254  | 244  | 269  | 270  | 235  | 235  |
| X, XI                       | 357            | 342  | 376  | 383  | 366  | 390  | 426  | 458  | 413  | 405  | 389  | 375  |
| XII, I                      | 339            | 352  | 366  | 370  | 376  | 369  | 348  | 361  | 348  | 336  | 345  | 363  |
| II, III                     | 170            | 164  | 190  | 206  | 224  | 221  | 211  | 205  | 206  | 190  | 191  | 186  |
| Sum                         | 1422           | 1393 | 1496 | 1580 | 1645 | 1636 | 1620 | 1646 | 1618 | 1586 | 1548 | 1503 |

Mean Hourly Values

| Hour-angle<br>Group \ Group | 0 <sup>h</sup> | I      | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | 10   | 11   |
|-----------------------------|----------------|--------|------|------|------|------|------|------|------|------|------|------|
| IV, V                       | 0.2648         | 2397   | 2022 | 2338 | 1955 | 2057 | 1602 | 1797 | 1811 | 2085 | 1926 | 2649 |
| VI, VII                     | 1519           | 1589   | 1718 | 1561 | 1515 | 1532 | 1375 | 1209 | 1456 | 1425 | 1191 | 1733 |
| VIII, IX                    | 449            | 482    | 507  | 331  | 464  | 460  | 465  | 523  | 645  | 443  | 748  | 337  |
| X, XI                       | 1088           | 1061   | 1044 | 1202 | 1276 | 1153 | 1234 | 1196 | 1452 | 1252 | 1451 | 1128 |
| XII, I                      | 1825           | 1870   | 1589 | 1615 | 1588 | 1526 | 1706 | 1764 | 1695 | 1852 | 1879 | 2275 |
| II, III                     | 2062           | 1998   | 2051 | 2444 | 2014 | 1838 | 1719 | 1857 | 2089 | 1830 | 1994 | 1920 |
| Mean                        |                | 0.1598 | 1566 | 1489 | 1585 | 1469 | 1428 | 1350 | 1391 | 1525 | 1481 | 1531 |
|                             |                | +91    | +59  | -18  | +78  | -38  | -78  | -157 | -116 | +18  | -26  | +24  |
|                             |                |        |      |      |      |      |      |      |      |      |      | +167 |

Fig. 3

