

Neutron lifetime measurement with pulsed cold neutrons

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 The neutron lifetime has been measured by comparing the decay rate with the reaction rate of ³He nuclei of a pulsed neutron beam from the spallation neutron source at the Japan Proton Accelerator Research Complex (J-PARC). The decay rate and the reaction rate were determined by simultaneously detecting electrons from the neutron decay and protons from the ³He(n,p)³H reaction using a gas chamber, the working gas of which contains diluted ³He. The measured neutron lifetime was $898 \pm 10_{\text{stat}}^{+15} {}_{-18}^{\text{sys}}$ s.

Subject Index C02, C30, D02, D40

1. Introduction

A neutron decays into a proton, an electron, and an antineutrino through the weak interaction. The decay lifetime is an important parameter for both cosmology and elementary particle physics. The Big Bang Nucleosynthesis (BBN) is considered to create light elements, and the comparison of

the observational data and the theoretical prediction for light element abundances provides a good opportunity to test cosmological models [1–4]. The neutron lifetime determines the number ratio of protons to neutrons at the beginning of the BBN, which affects the BBN yields of light elements, especially ^4He [5].

In the Standard Model of particle physics, the neutron lifetime is described with a matrix element of V_{ud} in the Cabibbo–Kobayashi–Maskawa matrix. The neutron lifetime and the ratio of the weak axial-vector to vector coupling constants make it possible to determine the V_{ud} [1,6–9]. The neutron lifetime is also required in the calculation of the cross section of the antineutrino capture reaction by a proton, which is the inverse reaction of the neutron beta decay [10].

The neutron lifetime has been measured by many groups over the past 50 years [11]. The recent measurements were performed by two different experimental methods. One is a so-called bottle method; the number of the surviving ultra-cold neutrons (UCNs) contained in a storage bottle is measured as a function of the elapsed time, and the lifetime is determined by fitting the data with an exponential decay curve [12–18]. On the other hand, the beam method determines the neutron lifetime from the decay probability of the neutron obtained from the measured ratio of the decay rate to the incident neutron flux [19,20]. The averaged neutron lifetimes are 879.4 ± 0.4 s and 888.0 ± 2.0 s for the bottle method and the beam method, respectively. The central values differ by 8.5 s, corresponding to the deviation of 4.0σ using quoted uncertainties.

The discrepancy is called the “neutron lifetime puzzle”, and it is still unsettled whether it is due to any unconsidered systematic effect or any new physics. As a solution for the neutron lifetime puzzle, several scenarios of exotic decay modes of a neutron have recently been discussed. If a neutron decays into some undetectable particles with a branching ratio of about 1%, e.g., a mirror neutron [21] or dark particles [22], the puzzle can be solved. Note that some models with dark particles were already excluded [23–25] and the characteristics of the dark particles are restricted by the astronomical data on massive neutron stars [26–29].

In the current situation, it is important to verify the puzzle by experiments in which different systematic errors dominate. We performed a new experiment with the beam method; the neutron lifetime was measured by the counting rate of the decay electrons relative to the $^3\text{He}(n,p)^3\text{H}$ reaction rate in a ^3He -diluted gas detector. A great benefit is that this method is free from some systematic uncertainties thanks to the simultaneous measurement of the neutron flux and the neutron decay in the same detector volume, in contrast to the conventional beam methods which counted the decay protons [20,30]. It should be mentioned that our experiment measures the decay electrons but not decay protons; therefore it has a sensitivity to the decay mode with no proton emission which is discussed in Ref. [22].

This method was originally developed by Kossakowski *et al.* [31]. In their experiment, the diffracted neutron beam from a nuclear reactor was chopped into monochromatized bunches in order to separate the γ -ray background induced by neutron capture reactions on transmission through detector windows and the beam catcher. Our experiment was performed with the high-intensity pulsed neutron beam provided at the Japan Proton Accelerator Research Complex (J-PARC), which enables one to deliver such neutron bunches without loss due to monochromatization.

2. Experiment

2.1. Principle

In this experiment, electrons from the neutron decays are counted by observing the ionization tracks induced in the gas of a time projection chamber (TPC), because it is sensitive to electrons but not

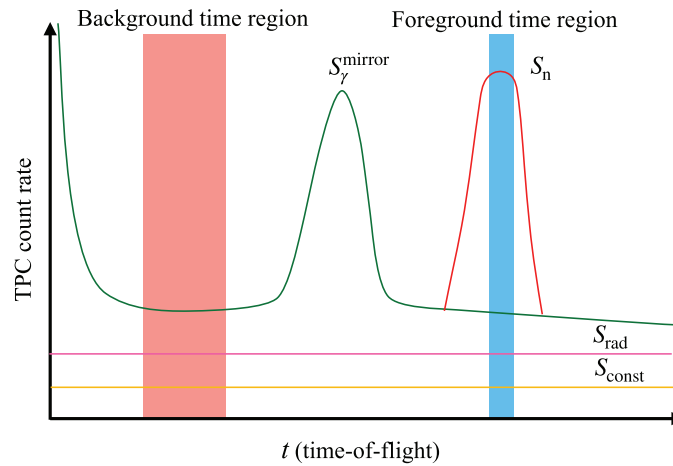


Fig. 1. Schematic illustration of the distribution of charged particles reaching or produced in the sensitive region of the TPC as a function of time-of-flight, in the case of a single bunch per pulse.

to γ -rays. A thin ^3He gas (50–200 mPa) was admixed in the working gas in order to measure the neutron flux by counting protons of 572 keV and tritons of 191 keV from the $^3\text{He}(n,p)^3\text{H}$ reactions simultaneously. The neutron lifetime, τ_n , can be expressed as follows [31]:

$$\tau_n = \frac{1}{\rho\sigma_0v_0} \left(\frac{S_{\text{He}}/\varepsilon_{\text{He}}}{S_{\beta}/\varepsilon_{\beta}} \right), \quad (1)$$

where S_{He} and S_{β} are the numbers of observed events of the $^3\text{He}(n,p)^3\text{H}$ reactions and the decay electrons, respectively; ε_{He} and ε_{β} are the detection efficiency of each reaction; ρ is the number density of the ^3He nuclei in the TPC. Since the neutron absorption cross section is inversely proportional to the neutron velocity at low energies (known as the $1/v$ law), the product of the cross section and the velocity is constant. Therefore, we can represent the reaction rate as σ_0v_0 , where σ_0 is the cross section of the $^3\text{He}(n,p)^3\text{H}$ reaction, known as 5333 ± 7 barn [32] at the thermal neutron velocity of $v_0 = 2200$ m/s. The number density, ρ , is controlled by diluting the ^3He gas at the calibrated conditions of volume, pressure, and temperature. The efficiencies, ε_{He} and ε_{β} in Eq. (1), are evaluated by Monte Carlo simulations which reproduce the responses of the TPC with sufficient accuracy.

The numbers of events, S_{He} and S_{β} , are obtained by analyzing detected events in the TPC. The signal and possible background events in this experiment are schematically shown in Fig. 1. Since events caused by neutrons occur when the neutrons are inside the TPC, they make a peak structure on the time-of-flight, t , and the number of events in the peak is denoted as S_n . The TPC detects background events by cosmic rays or natural radiations. These t -independent backgrounds are denoted as S_{const} . Events caused by neutrons, which are t -dependent, can be extracted by subtracting S_{const} by using the neutron-free region on t . Neutron-capture reactions at the neutron mirrors during the beam transport produce γ -rays. The number of backgrounds caused by the γ -rays is denoted as $S_{\gamma}^{\text{mirror}}$. Because this background is t -dependent, it is evaluated by switching the beam to the TPC on and off using a neutron shutter. The neutron captures also create radioactive isotopes, and we denote the number of backgrounds coming from them as S_{rad} . It depends on the lifetimes of the radioactive isotopes. If their lifetimes are sufficiently longer than the period of the shutter-switching, their events are subtracted as well as S_{const} . Thus the radioactive isotopes with short lives only appear when the shutter is open. Subtraction with/without the beam on t -regions and with the shutter open/closed is applied to derive S_n , which consists of S_{He} , S_{β} and other background events caused by the TPC working gas. Finally,

S_{He} and S_{β} are derived by applying some cuts and corrections to S_n . Note that the S terms are defined as the number of events by each component in the foreground time region with the beam shutter open.

The experimental apparatus and procedure of the measurements are described in the rest of Sect. 2, and the analysis is described in Sect. 3.

2.2. Neutron source and beamline

A spallation neutron source at the Materials and Life Science Experimental Facility (MLF) in the J-PARC produces pulsed neutron beams by using 3-GeV protons with a repetition rate of 25 Hz. The neutron source emits fast neutrons on the injection of the primary proton beam, and the timing is defined as zero on t . The neutrons are cooled down with liquid hydrogen moderators and transported to beamlines at the experimental halls of MLF. This experiment is conducted at the ‘‘Polarized-beam’’ branch of the beamline BL05 (NOP) [33]. A schematic view of the beamline and experimental apparatus is illustrated in Fig. 2 [34]. Neutrons are transported from a moderator to the experimental area through a polarizing neutron bender of 3.5 m filled with He gas, and vacuum guides of 4 m. The time-averaged beam intensity at the exit of the vacuum guide (E in Fig. 2) corresponds to $(4.0 \pm 0.3) \times 10^7 \text{ s}^{-1} \text{ cm}^{-2}$ at 1 MW operation [35,36] with a beam polarization of 97–94% in the wavelength of 0.2–0.9 nm [37]. The coordinate system used in this paper is depicted in the figure; the z -axis is in the beam direction at the TPC, the y -axis is the vertical upward axis, and the x -axis is perpendicular to these so as to form a right-handed frame.

2.3. Devices for the beam transport

The experimental apparatus consists of two sections: the beam shaping section (b)–(e) and the detector section (f)–(m). In this experiment, the neutron beam is shaped to the spin flip chopper (SFC). Because the SFC requires polarized neutrons, the apparatus was installed downstream of the Polarized-beam branch. The SFC can create monochromatic bunches by combining the pulsed neutrons while avoiding γ -rays from upstream by shifting the beam axis. The SFC consists of magnetic super mirrors and neutron spin flippers [38], shown in (b)–(d) in Fig. 2.

The neutron spin is controlled by switching RF current of the flippers. The spin-flipped neutrons pass through the magnetic mirrors and are dumped, while the non-flipped ones are reflected by the mirrors to be transported downstream. The neutron beam is formed into bunches whose lengths are about half (40 cm) of the TPC. Because the bunch intervals were set to 3.3 m to avoid overlapping of signal and background from the SFC or beam catcher, the number of bunches per pulse was adjusted to the allowable maximum of 5. The contrast of the SFC ran into ~ 400 [36].

Then neutron bunches are transported into the TPC (k) in Fig. 2, after passing through a beam monitor [39] (e), a 50- μm -thick Zr window (f), and the neutron switching shutter (g). The shutter is a 5-mm-thick tile which is made of polytetrafluoroethylene (PTFE) containing 95% isotopically enriched ^6LiF with 30 wt%. The neutron transmission of the switching shutter is calculated as 3×10^{-6} . The tiles are used to cover the inside of the beam duct (D) and the TPC, whose cross section is $40 \times 40 \text{ mm}^2$ for the inlet of the TPC, and $60 \times 60 \text{ mm}^2$ for the outlet. A very small portion of the neutrons (10^{-5} – 10^{-6}) make the neutron decays or $^3\text{He}(n,p)^3\text{H}$ in the TPC, and the rest of the beam is dumped at a beam catcher (l), which is a box filled with ^6LiF powder with a 0.5 mm PTFE window.

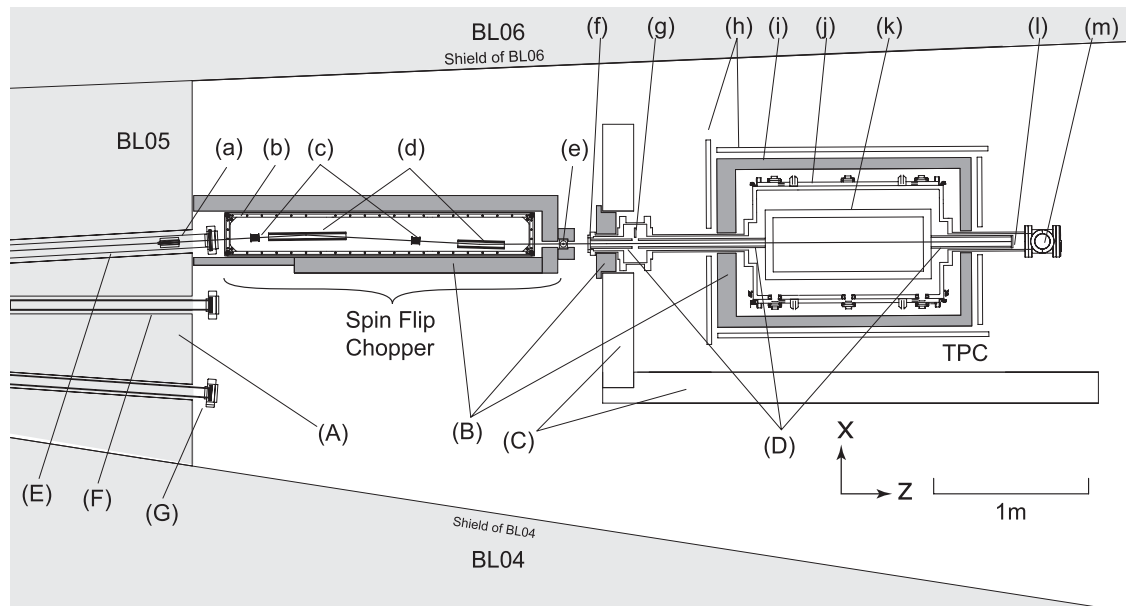


Fig. 2. Schematic top view of experimental apparatus installed at the Polarized neutron beam branch of the NOP beamline: (A) concrete shield, (B) lead shields, (C) iron shield, (D) ^6LiF beam collimator, (E) Polarized-beam branch, (F) Unpolarized-beam branch, (G) Low-divergence branch, (a) short-wavelength pass filter, (b) guide coil, (c) resonance spin flipper coils, (d) magnetic super mirrors, (e) neutron beam monitor, (f) 50- μm -thick Zr window, (g) neutron switching shutter, (h) cosmic-ray veto counters, (i) lead shield, (j) vacuum chamber, (k) TPC, (l) ^6LiF beam catcher, and (m) turbo molecular pump.

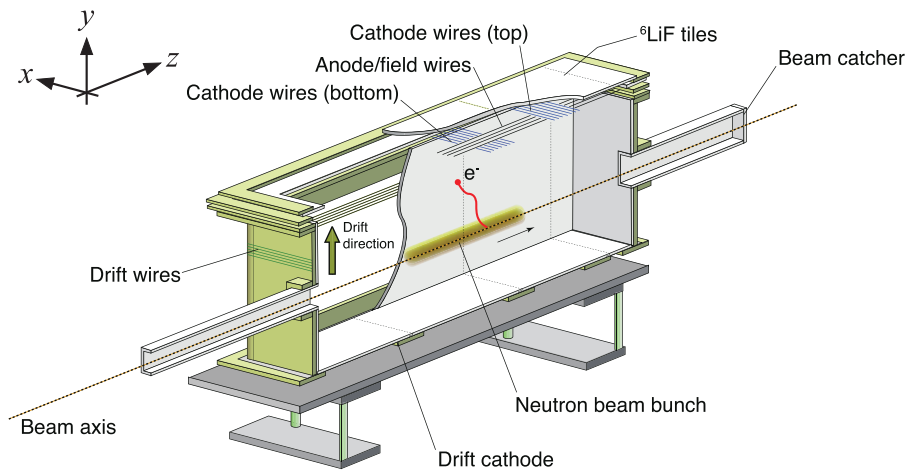


Fig. 3. Schematic view of the TPC [34].

2.4. Detector

The TPC with polyether ether ketone (PEEK) and ^6LiF tiles was developed to detect neutron decays with a low background environment in the long-term operation [34]. The schematic view of the TPC is shown in Fig. 3. Since the count rate for the neutron decay is 1 cps at 200 kW in the beam bunches, that of the natural background (S_{const}) should be kept at the same level or smaller for statistics. The PEEK frame is a substance with small radioactive material contamination. Thanks to this property, the background rate from the TPC support structure is suppressed to 4 cps.

Table 1. Specification of the TPC and operating condition.

Sensitive region	290 mm (x) \times 300 mm (y) \times 960 mm (z)
Anode	24 wires (z -direction), \varnothing 20 μ m AuW
Field	24 wires (z -direction), \varnothing 50 μ m BeCu
Cathode	162 wires \times 2 (x -direction), \varnothing 50 μ m BeCu
Gas mixture	$^4\text{He} : \text{CO}_2 : ^3\text{He} = 85\% : 15\% : 0.5\text{--}2$ ppm
Pressure	100 kPa
Anode voltage	+1720 V
Drift voltage	−9000 V

The inside of the TPC and the beam transport duct are covered with the ^6LiF tiles in order to avoid the background of γ -rays generated by neutrons hitting the wall. This ^6LiF tile can suppress the γ -ray generation against a neutron absorption to 2.3×10^{-4} [40]. The ^6LiF tiles are packed in 100- μm -thick PTFE sheets to prevent the ions emitted by the $^6\text{Li}(n,\alpha)^3\text{H}$ reaction from entering the fiducial volume of the TPC. Almost all the scattered neutrons are absorbed by the ^6LiF tiles; therefore, possible β -nuclei produced in the TPC structure materials, which are the origins of S_{rad} , are only ^8Li (half-life 839.9 ms, Q-value 16004 keV) and ^{20}F (half-life 11.07 s, Q-value 7025 keV) [41]. Because the neutron absorption by the ^6LiF tile creates ^8Li and ^{20}F with probabilities of 2.5×10^{-6} and 3.5×10^{-5} , respectively [34], the difference of S_{rad} between t -foreground and background is estimated to be 2×10^{-3} . These advantages enable us to achieve better statistical uncertainties than that of the previous measurement performed by Kossakowski *et al.*

The TPC is installed in a vacuum chamber which is sealed with fluorocarbon O-rings. A mixture of He and CO_2 of 85 and 15 kPa as the TPC working gas was chosen because both of them have relatively small capture and scattering cross sections of the neutron. A few ppm of ^3He is accurately admixed for the simultaneous measurement of the neutron flux. The working gas is used in the sealed condition during a series of measurements.

The TPC has a drift volume and a multi-wire proportional chamber (MWPC) placed above the drift volume. An aluminized PET film is placed on the ^6LiF tile at the bottom surface of the TPC and a drift voltage of −9000 V is applied. On the surface of the ^6LiF tile at the top, additional aluminized PET films are placed and kept +150 and +100 V to prevent the back-drifting of electrons outside the drift volume. The MWPC consists of an anode plane sandwiched within cathode planes. The anode plane is made of anode and field wires which are stretched alternately in the z -direction with a spacing of 6 mm. Each cathode plane has 162 wires stretched in the x -direction with a spacing of 6 mm. The gaps between the anode and cathode planes are 6 mm. The charge distribution of a particle track is projected on to the anode and cathode planes, and its two-dimensional image is obtained by measuring the signals from the anode/field wires and the cathode wires. Table 1 shows the specification of the TPC and each wire. The details of the TPC are described in Ref. [34]. A ^{55}Fe X-ray source on a rotation stage is equipped at the side of the drift cage, and 5.9-keV X-rays are injected from two slits on the ^6LiF tile at 75 and 225 mm from the MWPC for calibration of the TPC.

The vacuum chamber is surrounded by a lead shield [(i) in Fig. 2] to reduce the environmental background radiation emitted from radioisotopes such as ^{40}K , uranium-series and thorium-series which are contained in the concrete of the building. The thickness of the lead is 5 cm, which shields 98% of environmental γ -rays. Because γ -rays caused by neutron capture at the mirrors of the SFC produce considerable backgrounds, the shield thickness on the upstream side is 10 cm. Besides,

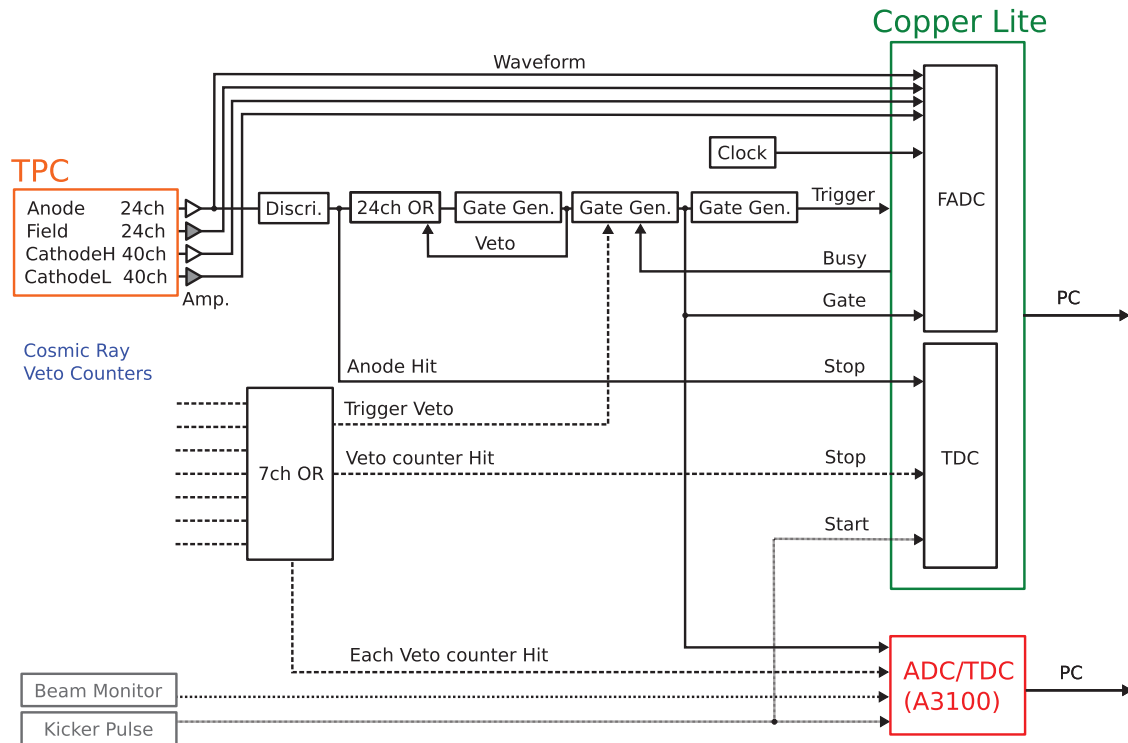


Fig. 4. Diagram of the DAQ.

20-cm-thick iron walls [(C) in Fig. 2] are placed at the front and sides to shield γ -rays from the neighboring beamlines.

A veto system using plastic scintillators [(h) in Fig. 2] is placed on the lead shield. It consists of 7 pairs of 12-mm-thick scintillator layers with wavelength-shifter fibers connected to 14 photomultiplier tubes. The scintillators are arranged to surround all sides of the lead shields, except the bottom side. The coincidence of pairs of scintillators is used as a veto to cosmic-ray events. The veto efficiency is estimated to be 99%. Finally, the whole count rate of S_{const} is suppressed to 8 cps without any cuts [34].

A diagram of the data acquisition system (DAQ) is given in Fig. 4. Signals of wires of the TPC are amplified and converted to voltages by preamplifiers. The preamplifiers with two different gains are used to obtain a wide dynamic range; the anode and the bottom layer of the cathode wires with high gain, and the field and the top layer of the cathode wires with low gain. The conversion factors of the high- and low-gain amplifiers are 1.3 and 0.23 V pC⁻¹, respectively. While each anode or field wire is connected to a readout channel, the four adjacent cathode wires are bundled into one readout channel. A trigger for the DAQ is generated when at least one of the anode wire signals exceeds the threshold voltage of 20 mV. The waveforms are recorded using a flash analog-to-digital converter (FADC) as data of 100 μ s length with 100-ns resolution. The waveforms of 70 μ s after the trigger were treated as an event. Note that the number of triggers was recognized as the number of events. The measured time from the primary proton beam pulse (kicker pulse in Fig. 4), which is referred to as t , is recorded by a time-to-digital converter (TDC). The set of the FADC and TDC data is sent to a PC through the COPPER-Lite board, developed in KEK [42]. The information of the beam monitor, hit-timings of anode wires, cosmic-veto counters, and proton beam pulses is recorded in parallel by an ADC/TDC system (Nikiglass A3100).

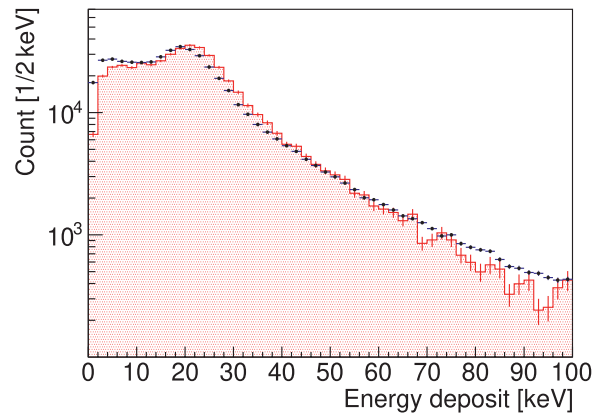


Fig. 5. Energy deposit distribution of the cosmic-ray data (black dots) and simulation which was normalized by the total number of the measured histogram (red hatch).

2.5. Detector simulation

A Monte Carlo code GEANT4 release 4.9.6.04 [43] is used for this experiment. The physics lists of FTFP_BERT_PEN and QGSP_BIC_HP were employed to take into account the interaction of the low-energy particles and the neutron capture reactions, respectively. The TPC, vacuum chamber, lead and iron shields, and cosmic-veto counters were included in the geometric condition of the simulation. The waveforms of the signals obtained from the anode, field, and cathode wires were simulated by calculating the drift motion of the ionized electrons which were liberated along the trajectories of the charged particles. Here, the number of ionized electrons was obtained from the local energy deposit and the W value (40.9 eV) for the gas mixture of 85% He and 15% CO₂. The non-linearity of the pulse heights due to the space charge effect in the electron avalanche process was taken into account using the saturation model [34,44]. The calculated event data were recorded and analyzed with the same procedure as the real experimental data.

The conversion between the signal amplitude and the energy deposit was validated by comparing the measured and simulated spectra of cosmic muons. The cosmic-ray veto signal from the coincidence of a pair of scintillators was occasionally inverted so that clear cosmic-ray events were acquired for monitoring the operating condition of the TPC by comparing the observed and simulated energy spectra of cosmic-rays as shown in Fig. 5. The energy was calibrated by the ⁵⁵Fe X-ray source, described in Sect. 2.7. The discrepancy of the energy calibration in all of the measurement series was estimated to be 5–9%, which is used to evaluate systematic uncertainties in cut energies of the event selection.

2.6. Gas handling and ³He number density

Commercially available high purity He of 99.99995% (G1He) and CO₂ of 99.999% are used as the TPC working gas. The neutron flux is measured by counting the ³He(n,p)³H reactions with ³He gas diluted in the working gas. As shown in Eq. (1), since the measured neutron lifetime is a function of the number density of ³He, ρ , it should be determined with high accuracy. The partial pressure of ³He was adjusted to 50–200 mPa in order to obtain sufficient statistical accuracy in the neutron flux measurement through the detection of the ³He(n,p)³H reaction events. The maximum pressure of 200 mPa was determined by the pileup of the ³He(n,p)³H, which was estimated as $\sim 0.4\%$ with 200 kW. Because it is not easy to measure such a small pressure directly with accuracy, isotopically pure ³He gas ($> 99.95\%$) was injected into a smaller container with high pressure (~ 3 kPa), and

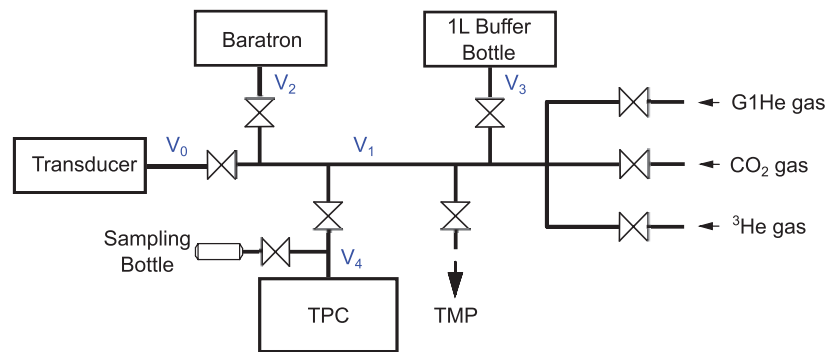


Fig. 6. Schematic view of the gas-handling system [45,46].

then released into the vacuum chamber of the TPC. The gas-handling system for the procedure is shown in Fig. 6, and the details are described in Ref. [45,46].¹ Here, the volume ratio of the vacuum chamber for the TPC to the small container was determined as $(1.497 \pm 0.028) \times 10^4$ by measuring the pressure change when G1He gas was released from the container to the vacuum chamber. Corrections to the ideal gas law using the second virial coefficient and thermal transpiration effect on the transducer were taken into account. The uncertainty of the ratio was evaluated based on the measurements of the pressure and the temperature, isotopic and chemical purity of ^3He .

Since ρ in the working gas is a sum of the admixed ^3He , ρ_{ad} and ^3He in the G1He gas, ρ_{G1} , we denote ρ_{VE} as

$$\rho_{\text{VE}} = \rho_{\text{ad}} + \rho_{\text{G1}}. \quad (2)$$

We determined ρ_{G1} by the ratio of $^3\text{He}/^4\text{He}$ measured by a mass spectrometer [47] with accuracies of 1.5–3.0% for all bottles used in this work. The working gases after the operation were sampled and their $^3\text{He}/^4\text{He}$ ratios were measured by the mass spectrometer to confirm whether the ρ terms were properly controlled. Putting the number density of ^3He measured with the mass spectrometer as ρ_{MS} , the relation between ρ_{VE} and ρ_{MS} is shown in Fig. 7 for 8 independent gas fillings. The values of ρ_{VE} and ρ_{MS} are consistent with an accuracy of 0.4%. Because ρ_{VE} has better accuracy than ρ_{MS} , we employ the ρ_{VE} as ρ .

The determined value of ρ_{VE} needs small corrections to be converted into ρ during the operation. The vessel deformation due to the pressure and the temperature change was evaluated from the mechanical strengths and thermal expansion coefficients of structure materials of the chamber: stainless steel and aluminum. We budgeted the correction as half of the maximum deformations with the symmetric uncertainty. Another correction is for temperature non-uniformity. A temperature gradient due to local heating around the preamplifiers at the top of the TPC was observed. It decreased the gas density of the high-temperature region and increased the others. The increased amount of the ^3He number density at the beam axis of the TPC was approximately 0.02% [48]. The number density ρ was evaluated for each gas filling and applied for the analysis, and that of a typical gas filling is shown in Table 2. As a result, the uncertainty of ρ in the table was derived to be 0.42%.

¹ These works have been done as an application of this experimental apparatus.

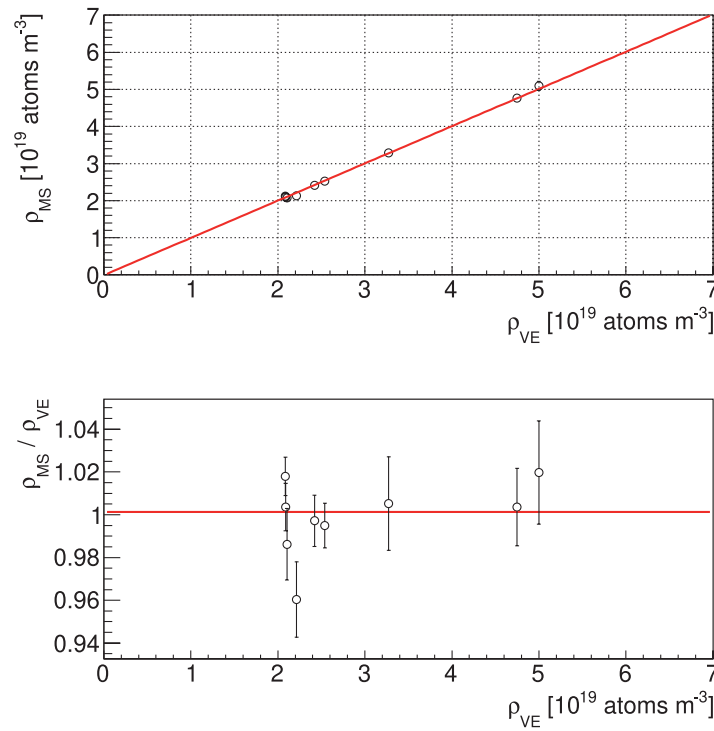


Fig. 7. The ^3He number densities of ρ_{VE} (x -axis) and ρ_{MS} (y -axis) (top panel), and the ratio of the two methods (bottom panel).

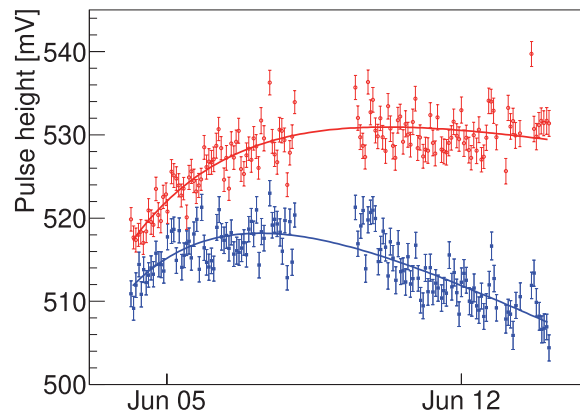


Fig. 8. Pulse heights of the X-rays from the ^{55}Fe source over time with fitting curves. The red circles and blue squares correspond to the source at 75 and 225 mm from the MWPC, respectively.

2.7. Measurement

Six series of measurements were performed during the years of 2014 and 2016. At the beginning of every series, the TPC was refilled with fresh gas. In each series, the measurements with the beam shutter open and closed were repeated alternately. The period of each measurement was 1000 s. The total measurement times are summarized in Table 3. Note that ρ values of Series 4 and 5 were intentionally changed to double and half, respectively, to check the systematic effect due to the ρ values.

The fluctuation of the TPC gain was checked by the calibration runs with the ^{55}Fe source placed at two positions on the y -axis to measure attenuation in the y -direction. Figure 8 shows the peak heights

Table 2. Value, correction, and uncertainty budgets of ρ (Series 6).

Term	^3He number density (10^{16} m^{-3})	Correction (%)	Uncertainty (%)
ρ_{ad}	2089 ± 7		0.3
ρ_{G1}	202 ± 6		3.0
ρ_{VE}	2291 ± 9		0.4
Vessel deformation (pressure)		-0.15	0.15
Vessel deformation (temperature)		-0.02	0.02
Temperature uniformity			0.02
ρ	2287 ± 10		0.42

Table 3. Summary of the measurement series.

Year	Series	Beam power (kW)	Measurement time open/closed (hour)	^3He number density (ρ) (10^{16} m^{-3})
2014	1	300	35/33	2417 ± 12
2015	2	500	16/16	2084 ± 7
	3	200	18/18	2348 ± 8
2016	4	200	73/69	4176 ± 13
	5	200	69/63	1194 ± 8
	6	200	71/71	2287 ± 10

of the 5.9 keV X-rays as a function of the elapsed date from the beginning of a measurement series. It is expected that the fluctuation of the gain was caused by that of the temperature of the TPC. The drift velocity of the TPC was monitored by measuring the tracks of the cosmic-rays traversing from the top to the bottom of the TPC, which was stable at 0.3% in a measurement series. The time differences of the earliest and latest signals in such events correspond to the maximum drift length, and the drift velocity averaged over the whole drift length was obtained as $1.0 \text{ cm}/\mu\text{s}$ with 4% accuracy.

3. Analysis

3.1. Procedure

In this section, we describe the procedure to obtain the ratio of S_β , S_{He} , ε_β , and ε_{He} in Eq. (1). The numbers of events, S_β and S_{He} , are derived from the experimental data, schematically shown in Fig. 1, by using the time-of-flight, the open/closed state of the neutron shutter, the signal amplitude distribution, and the track geometry together with the simulation of the detector response. The efficiencies, ε_{He} and ε_β , which are dependent on the cut conditions, are calculated by the simulation.

The neutrons arrived at the TPC generate the neutron decay and $^3\text{He}(n,p)^3\text{H}$ events. The CO_2 in the TPC working gas and nitrogen contamination in it cause $^{12}\text{C}(n,\gamma)^{13}\text{C}$, $^{17}\text{O}(n,\alpha)^{14}\text{C}$ and $^{14}\text{N}(n,p)^{14}\text{C}$ events, and we denote them as S_{C} , S_{O} and S_{N} , respectively. Neutrons scattered by the working gas or at the surface of the ^6LiF tile downstream of the switching shutter additionally induce γ -rays by neutron captures of the structure materials. We define the number of these events as $S_{n\gamma}$. These events appear accompanying the neutron bunches. Finally, the number of the neutron-induced events in the TPC, S_{n} , is given as

$$S_{\text{n}} = S_\beta + S_{\text{He}} + S_{\text{C}} + S_{\text{O}} + S_{\text{N}} + S_{n\gamma}. \quad (3)$$

The numbers of events observed in the foreground/background time region with the switching shutter open/closed are denoted as $S_{\text{FG-OPEN}}$, $S_{\text{FG-CLOSE}}$, $S_{\text{BG-OPEN}}$, and $S_{\text{BG-CLOSE}}$, respectively, which are normalized with the dead-time corrected time-windows and the incident neutron intensity measured with the beam monitor to match $S_{\text{FG-OPEN}}$. The contents of the S terms for these measurement modes are related to individual S components via

$$\begin{bmatrix} S_{\text{FG-OPEN}} \\ S_{\text{BG-OPEN}} \\ S_{\text{FG-CLOSE}} \\ S_{\text{BG-CLOSE}} \end{bmatrix} = \begin{bmatrix} 1 \\ \eta_n^{\text{SFC}} \\ \eta_n^{\text{shutter}} \\ \eta_n^{\text{SFC}} \eta_n^{\text{shutter}} \end{bmatrix} S_n + \begin{bmatrix} 1 \\ \eta_\gamma^{\text{SFC}} \\ \eta_\gamma^{\text{shutter}} \\ \eta_\gamma^{\text{SFC}} \eta_\gamma^{\text{shutter}} \end{bmatrix} S_\gamma^{\text{mirror}} + \begin{bmatrix} 1 \\ \eta_{\text{rad}}^{\text{short}} \\ \eta_{\text{rad}}^{\text{long}} \\ \eta_{\text{rad}}^{\text{long}} \\ \eta_{\text{rad}} \end{bmatrix} S_{\text{rad}} + \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \end{bmatrix} S_{\text{const}}, \quad (4)$$

where the η terms are ratios for each component to $S_{\text{FG-OPEN}}$; η_n^{SFC} is the ratio of incident neutrons in the background to the foreground time region, and η_γ^{SFC} is the same one for neutron-induced γ -rays. The ratios η_n^{shutter} and $\eta_\gamma^{\text{shutter}}$ are the transmission of the switching shutter for the neutrons and γ -rays, respectively. The ratios η_{short} and η_{long} represent the residual radioactive isotopes; η_{short} for the background to foreground time region, η_{long} long for the shutter closed to open, respectively.

In this analysis, the following subtraction is performed to obtain S_n :

$$\begin{aligned} S_{\text{subt}} &= (S_{\text{FG-OPEN}} - S_{\text{BG-OPEN}}) - (S_{\text{FG-CLOSE}} - S_{\text{BG-CLOSE}}) \\ &= (1 - \eta_n^{\text{SFC}})(1 - \eta_n^{\text{shutter}})S_n + (1 - \eta_\gamma^{\text{SFC}})(1 - \eta_\gamma^{\text{shutter}})S_\gamma^{\text{mirror}} + (1 - \eta_{\text{rad}}^{\text{short}})S_{\text{rad}}. \end{aligned} \quad (5)$$

Here, η_n^{shutter} is negligibly small, as described in Sect. 2.3; in contrast, $\eta_\gamma^{\text{shutter}}$ is ~ 0.95 . We can reasonably assume $\eta_n^{\text{SFC}} \simeq \eta_\gamma^{\text{SFC}}$, and η_n^{SFC} is less than 5×10^{-3} (see Fig. 13); thus, we neglect them in this analysis. According to the discussion in Sect. 2.4, $(1 - \eta_{\text{rad}}^{\text{short}})$ is estimated to be 2×10^{-3} , then $(1 - \eta_{\text{rad}}^{\text{short}})S_{\text{rad}}$ can be negligible because S_{rad} is $\sim 1/10$ of S_β (see Fig. 13 and later discussion). Consequently, Eq. (5) can be written as

$$S_{\text{subt}} \simeq S_n + (1 - \eta_\gamma^{\text{shutter}})S_\gamma^{\text{mirror}}. \quad (6)$$

Here, the term with $\eta_\gamma^{\text{shutter}}$ will be corrected by using simulations of the γ -rays from the neutron mirrors in the neutron transport in further analysis described in Sect. 3.4.

A schematic diagram for the analysis procedures with cuts and corrections is shown in Fig. 9. The procedures are as follows:

- (1) First, the events are classified as high-energy group (E^+) and low-energy group (E^-) by using maximum pulse heights. The group E^+ mainly consists of the ${}^3\text{He}(n,p){}^3\text{H}$ events, and E^- contains the neutron decay events, described in procedure (A) in Sect. 3.3.
- (2) Individual cuts are applied to E^+ and E^- to extract the ${}^3\text{He}(n,p){}^3\text{H}$ and the neutron decay events with higher purities, described as procedure (B^+) and (B^-) in Sect. 3.4, respectively.
- (3) The subtractions of FG-OPEN, FG-CLOSE, BG-OPEN, and BG-CLOSE in Eq. 5 are performed for E^+ and E^- with the cuts to obtain S^+ and S^- .
- (4) Corrections to exclude S_N and S_O are applied to S^+ in order to extract S_{He} , described as procedure (C) in Sect. 3.5.

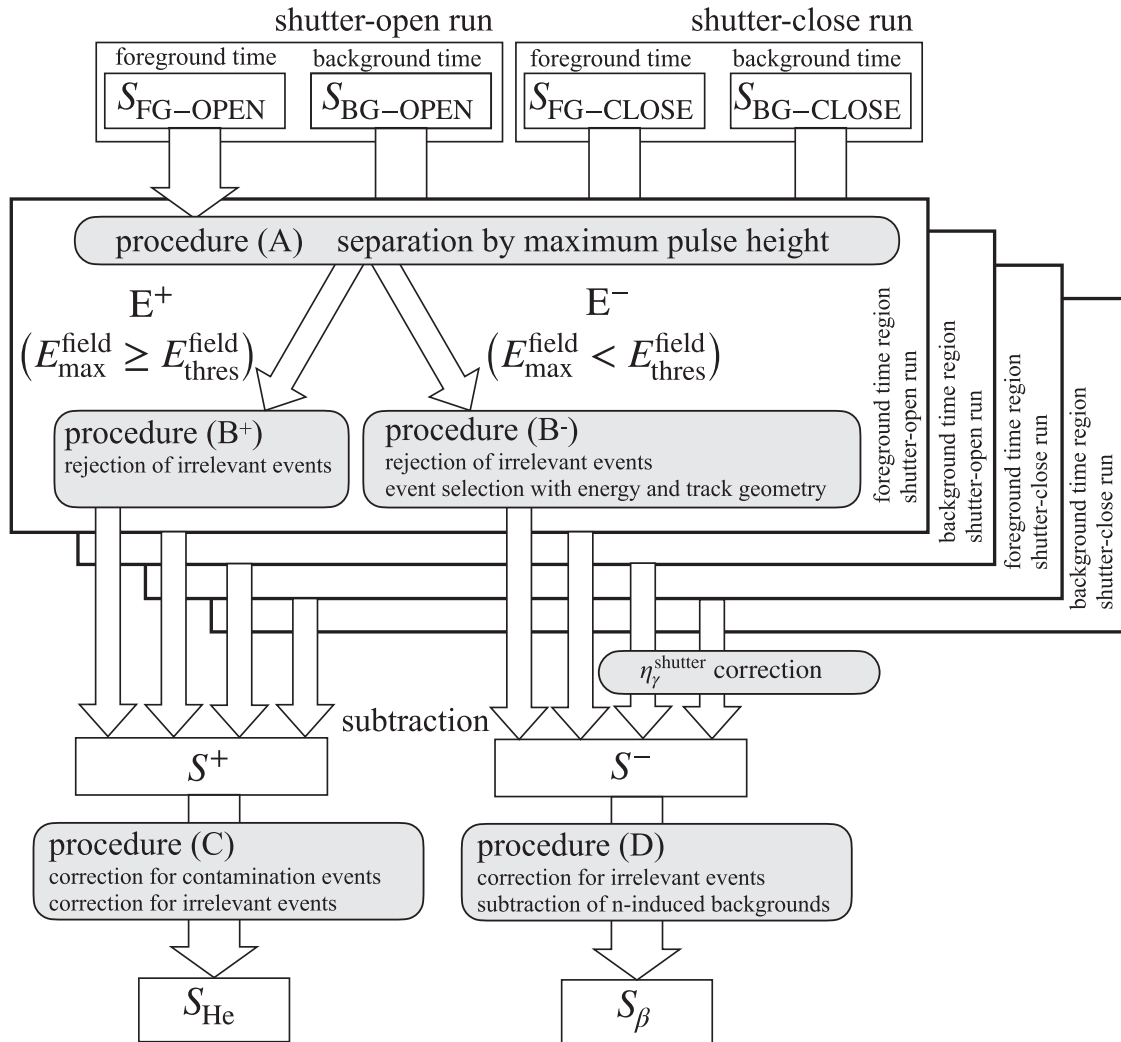


Fig. 9. Flowchart of the analysis procedure. Grey boxes represent analysis procedures and white boxes represent the event data.

- (5) A correction to exclude $S_{n\gamma}$ is applied to S^- in order to extract S_β , described as procedure (D) in Sect. 3.6.

The detail of each procedure will be described below.

3.2. Region of the time-of-flight

Since the tracks of the ${}^3\text{He}(n,p){}^3\text{H}$ events are observed clearly in the TPC, the event distribution observed with the low-gain amplifier outputs reflects the neutron distribution in the TPC. Here, we define the weighted z -position as

$$\bar{z} = \frac{\sum_i Q_i Z_i}{\sum_i Q_i}, \tag{7}$$

where i is the channel number of a cathode wire, Z_i is the z -coordinate of the i th cathode channel, and Q_i is the charge on the low-gain amplifier of the i th cathode channel. Figure 10 shows the distribution of experimentally observed events on the $\bar{z}t$ -plane. The propagation of the 5 neutron

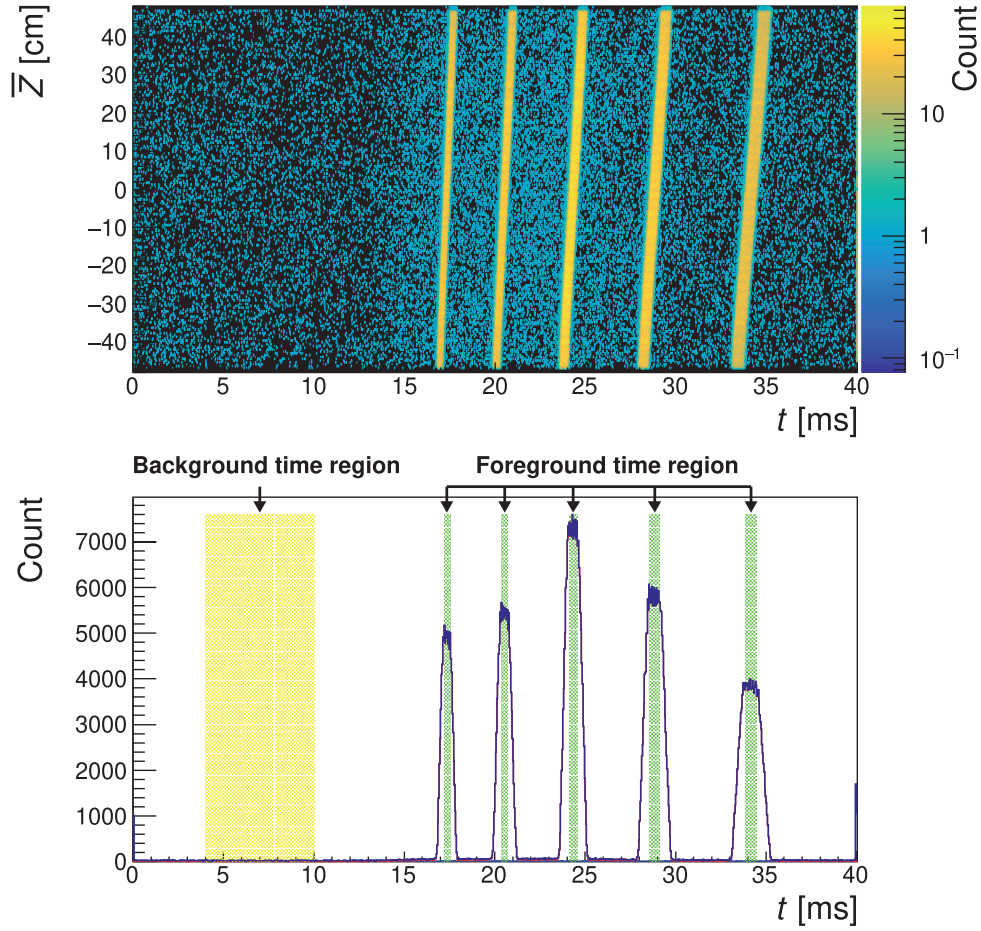


Fig. 10. Event distribution on the $\bar{Z}t$ -plane (top) and its projection on to t -axis (bottom). The foreground and background time regions are shown by green and yellow hatching, respectively.

bunches is clearly visualized as 5 bands. The slope on the $\bar{Z}t$ -plane, which corresponds to the neutron velocity, decreased with t . Also, the time interval between bunches increased with t since the bunches were made to be equally spaced, as described in Sect. 2.3.

We defined the region of $-34 \text{ cm} \leq \bar{Z} \leq 34 \text{ cm}$ as the foreground region, which corresponded to the t -regions centered at 17.4, 20.5, 24.3, 28.8, and 34.2 ms. The total foreground time width was 2.3 ms. We defined the background region as $4 \text{ ms} \leq t \leq 10 \text{ ms}$ to minimize $S_{\gamma}^{\text{mirror}}$.

3.3. Procedure (A): Separation by maximum pulse height

In further analysis, S_{subt} in Eq. (6) is divided into two groups; ion-emission events and the others, defined as E^+ and E^- classes, respectively. In the derivation process, some cuts are applied to remove the background and increase the purity of the signal, which are discussed in Sect. 3.4. Here,

$$S'_{\text{subt}} = S^+ + S^- \quad (8)$$

is defined, where S^+ and S^- are the numbers of events in E^+ and E^- after the cuts, respectively.

Since the ion events have relatively higher energy deposits than electrons, each event is classified according to the maximum energy deposit among all the field wires, $E_{\text{max}}^{\text{field}}$. Figure 11 shows the $E_{\text{max}}^{\text{field}}$ distribution of S'_{subt} together with the simulated distributions of S_{He} and S_{β} . The results of simulations show that the physical processes responsible for each event can be roughly classified

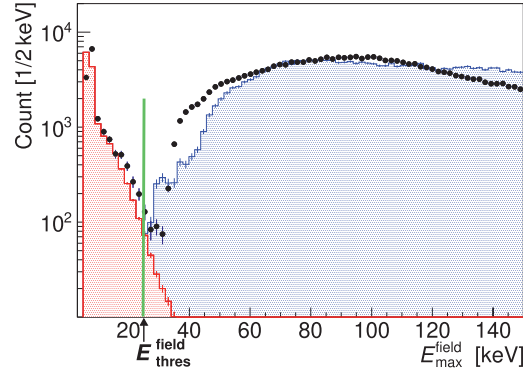


Fig. 11. Distribution of the maximum energy deposit among all field wires (E_{\max}^{field}) with that of the simulation of the neutron decay (left-hand red hatching) and the ${}^3\text{He}(n,p){}^3\text{H}$ reaction events occurring (right-hand blue hatching). The cut threshold (25 keV) is also shown, as a green vertical line.

and are mixed in the vicinity of their boundaries. We set a threshold $E_{\text{thres}}^{\text{field}} = 25$ keV to minimize the admixtures between the two kinds of events as shown in Fig. 11. Because of the ambiguity of the ${}^3\text{He}(n,p){}^3\text{H}$ simulation, the cut threshold was set lower than the valley of the measured spectrum. The events with $E_{\max}^{\text{field}} \geq E_{\text{thres}}^{\text{field}}$ ($E_{\max}^{\text{field}} < E_{\text{thres}}^{\text{field}}$) were classified as E^+ (E^-).

For the sake of simplicity, here we consider S_{He} and S_{β} only, and they are described as

$$\begin{bmatrix} S^+ \\ S^- \end{bmatrix} = \begin{bmatrix} 1 - \xi_{\text{sep}}^{\text{He}} & \xi_{\text{sep}}^{\beta} \\ \xi_{\text{sep}}^{\text{He}} & 1 - \xi_{\text{sep}}^{\beta} \end{bmatrix} \begin{bmatrix} S_{\text{He}} \\ S_{\beta} \end{bmatrix}, \quad (9)$$

where the ξ terms are the fraction of unfavored classification; $\xi_{\text{sep}}^{\text{He}}$ is the fraction of S_{He} mixed into S^- and ξ_{sep}^{β} is the fraction of S_{β} mixed into S^+ . Note that the effects of them were less than 0.6% for all measurements in this work.

3.4. Procedure (B^+) and (B^-): Event selections for E^+ and E^- classes

Respective cuts were applied to E^+ and E^- classes as shown in Fig. 9. Thanks to the low radioactive TPC, the event rate caused by backgrounds other than the neutron bunch ones in E^+ was suppressed to 0.15 cps, which is 3×10^{-3} of S^+ . Therefore only a cut for electric noise was applied to E^+ , where the effect was negligibly small.

Three cuts were applied to E^- , as follows. The first cut is to remove the event by recoil nuclei from the ${}^{12}\text{C}(n,\gamma){}^{13}\text{C}$ reaction occurring in the TPC working gas which has kinetic energy of 1.0 keV. We set a cut on the energy deposit with threshold level $E_{\text{thres}}^{\text{anode}} = 5$ keV to eliminate S_C from E^- . The distribution of the energy deposit on the anode wires for E^- is shown in Fig. 12 together with the simulated spectrum of the neutron decay. The ratio of the residual of S_C after the energy cut to S^- , denoted as ξ_C , was estimated to be less than 0.3% by the Monte Carlo simulation.

The other two cuts were applied for statistical advantage by reducing S_{const} and S_{rad} components. Since the neutron decay events occur in the neutron beam region which is the center of the TPC, their spatial distribution in the TPC is different from that of the background events. Thus, we can select the neutron decay events among various spatially distributed tracks using the waveform and/or distribution over the anode wires. For y -direction, we required that the drift length is less than 190 mm, which corresponds to the sum of the half-length of the TPC and the beam size, for removing charged particles generated outside of the beam region. For another background, β -decays of the

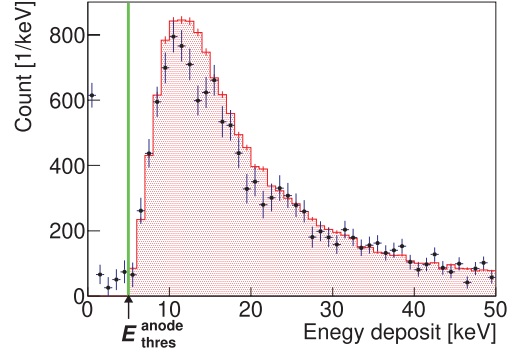


Fig. 12. Energy distribution of S^- of Series 6 (black circle) and that of the simulation of the neutron decay events normalized by the total events (red hatching). The green vertical line shows the cut threshold of 5 keV.

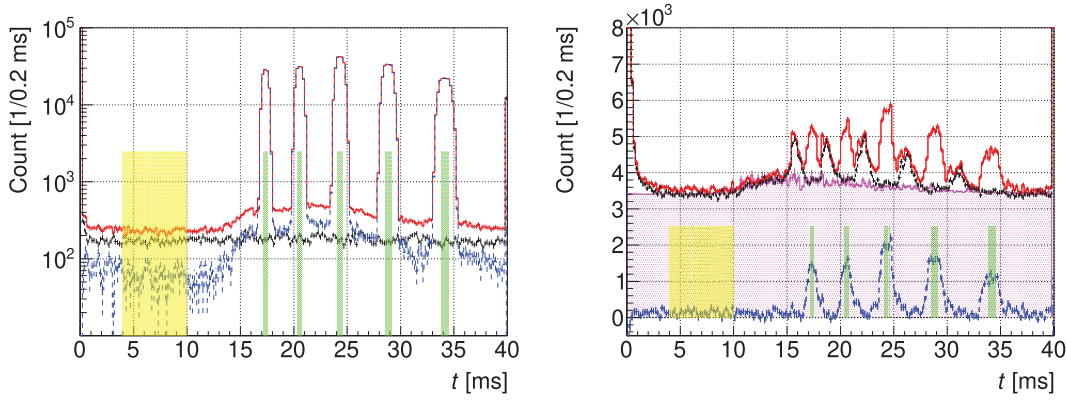


Fig. 13. Time-of-flight spectra of the experimental data for S^+ (left) and S^- (right). The red solid and black dotted lines represent the shutter open and closed data, respectively, and the blue dashed line shows the difference between them. The hatched regions in green and yellow show the foreground and background time regions, respectively. The pink hatched histogram is S_γ^{mirror} calculated by the simulations.

tritiums (half-life 12.33 years, Q-value 18.6 keV) [41] were observed, which had been produced by the ${}^6\text{Li}(n,\alpha){}^3\text{H}$ reactions in the TPC, and accumulated after a gas filling. Since those decay electrons have short tracks and low energies, they have peak-like shapes in their waveforms. Therefore, they can be identified by taking the ratio of the energy deposit around the highest peak to the full integration of the waveform. Events which had 80% of the energy deposit in the peak region were rejected.

The t -spectra of S^+ and S^- after applying the cuts are shown in Fig. 13. A simulation spectrum is plotted together with S^- . In the simulation, the γ -rays produced from the neutron mirrors in the beam transport were calculated by PHITS 2.88 [49] and the interactions of the γ -rays were simulated by GEANT4. The time-independent component was added to match the simulated γ -ray and BG-CLOSED. The shielding effect of γ -rays by the neutron shutter, $(1 - \eta_\gamma^{\text{shutter}})S_\gamma^{\text{mirror}}$ in Eq. (6), was compensated here by using the simulation. The difference between experimental data of FG-CLOSE and the simulation was budgeted as the uncertainty of the correction. The correction, denoted as $\xi_\gamma^{\text{shutter}}$, was calculated to be $(0.3 \pm 0.3)\%$.

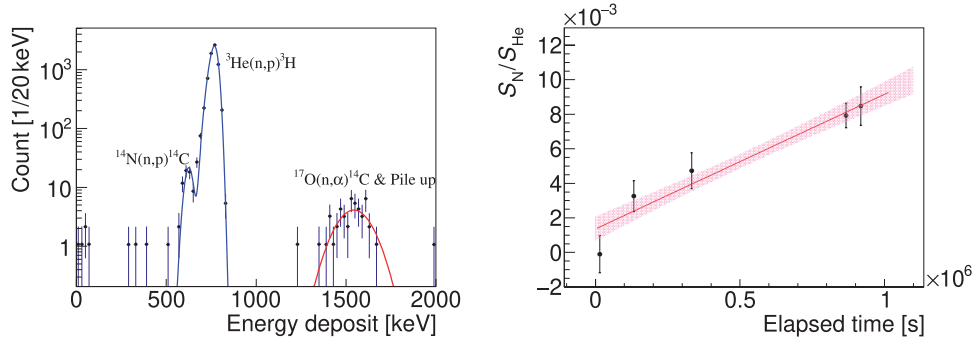


Fig. 14. Pulse height spectrum of a low-gain operation (left) and ratio of event rates of the $^{14}\text{N}(n,p)^{14}\text{C}$ to those of the $^3\text{He}(n,p)^3\text{H}$ versus the elapsed time after gas filling (right). The red line and the hatched region show the fitted curve and its error, respectively.

3.5. Procedure (C): Event selection and corrections for S^+

Contaminations of S_N and S_O are included in S^+ . Here, we define S_{Hecand} as

$$S_{\text{Hecand}} = S_{\text{He}} + S_N + S_O = (1 + \xi_N + \xi_O)S_{\text{He}} \quad (10)$$

with $\xi_N = S_N/S_{\text{He}}$ and $\xi_O = S_O/S_{\text{He}}$. Because lowering the gain of the TPC was necessary to avoid the saturation of the pulse heights due to the space charge effect, measurements with a reduced gain were performed every other day to monitor the influence of $^{14}\text{N}(n,p)^{14}\text{C}$. Figure 14 shows the pulse height spectrum of a low-gain operation and the ratio of the event rates of $^{14}\text{N}(n,p)^{14}\text{C}$ to $^3\text{He}(n,p)^3\text{H}$ as a function of the elapsed time. Because the outgas rate was roughly constant, the accumulated N_2 in the working gas proportionally increased over time. Using the data for the time dependence of the $^{14}\text{N}(n,p)^{14}\text{C}$ event rate, ξ_N was estimated as $(0.50 \pm 0.05)\%$. This contamination level was consistent with a value expected from the N_2 concentration in the working gas which had been measured by gas chromatography.

Since the $^{17}\text{O}(n,\alpha)^{14}\text{C}$ reaction occurs with ^{17}O nuclei contained in CO_2 , which is the quenching gas of the TPC, its event rate can be estimated using the existing data of the isotopic abundance of ^{17}O [50] and the $^{17}\text{O}(n,\alpha)^{14}\text{C}$ reaction cross section [32]. The event rate ratio of $^{17}\text{O}(n,\alpha)^{14}\text{C}$ to $^3\text{He}(n,p)^3\text{H}$ was evaluated as $(0.51 \pm 0.03)\%$.

The incident neutrons were partially scattered ($\sim 1\%$) by the working gas or the entrance window of the vessel. The scattered neutrons are captured by the ^6LiF tiles on the inner surface of the TPC or ^3He , or decay in the path. Here, we define the average x -position of each event weighted by the energy deposit as

$$\bar{X} = \frac{\sum_i E_i^{\text{field}} X_i}{\sum_i E_i^{\text{field}}}, \quad (11)$$

where X_i is x -position of the i th field wire with respect to the beam center. The \bar{X} distribution is shown in Fig. 15 and compared with the simulation of the $^3\text{He}(n,p)^3\text{H}$ events using the beam profile. The shape of the neutron beam was defined by the SFC geometry and collimators. The incident neutrons went into the beam catcher and were distributed in the $4\text{ cm} \times 4\text{ cm}$ at $z = -34\text{ cm}$ and $6\text{ cm} \times 6\text{ cm}$ at $z = 34\text{ cm}$. The blue hatched area shows the simulation of the scattered neutrons, where the scattering distribution was calculated with the semi-classical model [51,52]. Both simulations were scaled to the experimental data; the simulation for the scattered neutrons was

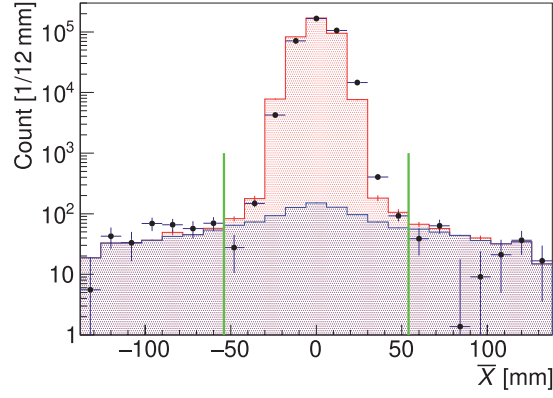


Fig. 15. Experimental data of \bar{X} distribution (black dots) and simulations of incident neutrons (top red hatching) and scattered neutrons (bottom blue hatching). The green vertical lines show the boundaries of the incident and scattered neutrons.

normalized in the region of $|\bar{X}| > 54$ mm, and the simulation for the incident neutrons was scaled so as to reproduce the experimental data together with the contribution of the scattered neutrons in the region of $|\bar{X}| \leq 54$ mm. The ratio of the scattered neutrons to the incident neutrons, $\xi_{\text{scat}}^{\text{He}}$, was $0.39 \pm 0.04\%$, the uncertainty of which is statistical error. We selected the events of the inside region of $|\bar{X}| \leq 54$ mm for the further analysis.

A pileup event is defined as two or more events detected in the same time window ($70 \mu\text{s}$). In this analysis, we classify an event as an occurrence which caused the trigger, and the effect of the pileup is corrected so that the event number represents the trigger rate. For the pileup correction of S_{He} , there are three combinations of events; E^+ to E^+ , E^+ to E^- , and E^- to E^+ . We classified these combinations as E^+ events because of their large energy deposit. The first two events do not affect the result, because the event classification is correct. The last requires a small negative correction, $\xi_{\text{pileup}}^{\text{He}}$. For conservative analysis, the magnitude and the uncertainty of it were set to be 0.08% , which corresponds to the E^- to E^+ pileup event rate.

Finally, S_{He} after the corrections described above is given as

$$S_{\text{He}} = \frac{S_{\text{He cand}}}{(1 + \xi_{\text{N}} + \xi_{\text{O}})} = \frac{(1 + \xi_{\text{pileup}}^{\text{He}})(S^+ - \xi_{\text{sep}}^{\beta} S_{\beta})}{(1 + \xi_{\text{N}} + \xi_{\text{O}})(1 + \xi_{\text{scat}}^{\text{He}})} \quad (12)$$

$$\simeq \left(1 - \xi_{\text{sep}}^{\beta} \frac{S_{\beta}}{S^+} - \xi_{\text{N}} - \xi_{\text{O}} - \xi_{\text{scat}}^{\text{He}} + \xi_{\text{pileup}}^{\text{He}} \right) S^+.$$

Corrections and uncertainties for S_{He} in Series 6 are summarized in Table 4. Note that $\xi_{\text{sep}}^{\text{He}}$ is not included because it is budgeted in ε_{He} .

3.6. Procedure (D): Background estimation and correction for S^-

Here, we define the event candidates of the neutron decay in S^- , $S_{\beta \text{cand}}$ as

$$S_{\beta \text{cand}} = S_{\beta} + S_{\beta \text{scat}} + S_{n\gamma}, \quad (13)$$

where $S_{\beta \text{scat}}$ is the number of neutron decay events caused by the scattered neutrons, which can be estimated by $\xi_{\text{scat}}^{\text{He}}$ obtained in Sect. 3.5. The neutron-induced γ -ray background, $S_{n\gamma}$, is estimated by applying an analysis of track geometry and subtracted from the neutron decay candidate events.

Table 4. Correction and uncertainty budgets of S_{He} (Series 6).

Term	Correction (%)	Uncertainty (%)
Statistics of S^+		$\pm 0.18_{\text{stat}}$
Misclassified neutron decay ($-\xi_{\text{sep}}^\beta S_\beta / S^+$)	-0.05	$+0.05$ -0.00
Contamination of ^{14}N ($-\xi_N$)	-0.50	0.05
Contamination of ^{17}O ($-\xi_O$)	-0.51	0.03
Scattered neutron ($-\xi_{\text{scat}}^{\text{He}}$)	-0.39	0.04
Pileup ($\xi_{\text{pileup}}^{\text{He}}$)	-0.08	$+0.08$ -0.00
S_{He}		$0.18_{\text{stat}} \begin{matrix} +0.11 \\ -0.06 \end{matrix} \text{sys}$

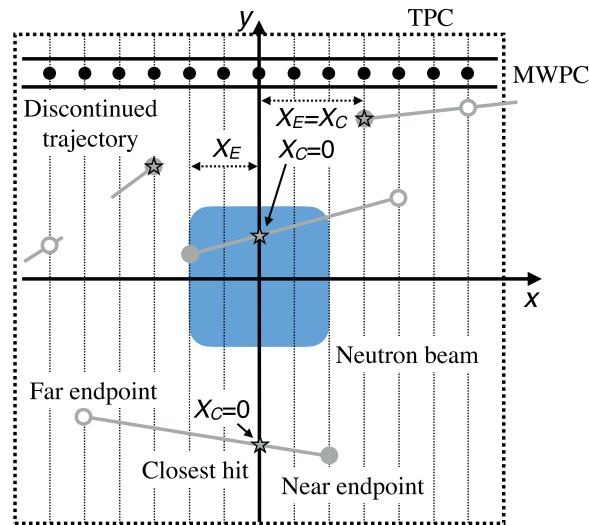


Fig. 16. Schematic figure of tracks and anode hit positions to illustrate the variables X_C and X_E . The outermost dotted square region, inner blue-colored region, and upper black circles indicate the TPC, neutron beam region, and anode wires, respectively. The closed and open circles correspond to near and far endpoints from the central wire, and the star shows the nearest hit position for each track. The number of wires and the geometric scale are not the same as those of the experiment. X_C is the distance along the x -axis between the origin and the nearest hit anode wire, and X_E is that between the origin and the nearer endpoint of the track.

Variables for the x -position of the anode wires, X_C and X_E , are introduced for this analysis. A schematic figure for them is shown in Fig. 16, where X_C is the distance along the x -axis between the origin and the nearest hit anode wire, and X_E is that between the origin and the near endpoint of a track. The continuity of each track is not required in the analysis. The distributions of X_C and X_E of S^- are shown in Fig. 17 with scaled simulations of the neutron decay without scattering, the decay of the scattered neutron, and the neutron-induced γ -ray background. Since the number of the anode wires is odd, the space for the 0th channel is half that for the other channels.

Using these variables, we classified the tracks as the central ($X_E \leq w$), the peripheral ($X_C > w$), and the remaining ($X_E > w$ and $X_C \leq w$) components. The relation $X_C \leq X_E$ is always satisfied by definition. Because tracks of the neutron decays in the beam have a hit within the neutron beam width, the neutron decay events without scattering are mainly classified in the central, and few ($< 0.02\%$) exist in the peripheral. We can estimate $S_{n\gamma}$ from the peripheral component with $S_{\beta_{\text{scat}}}$ determined by $\xi_{\text{scat}}^{\text{He}}$. Ignoring the neutron decay without scattering in the peripheral, the central and peripheral

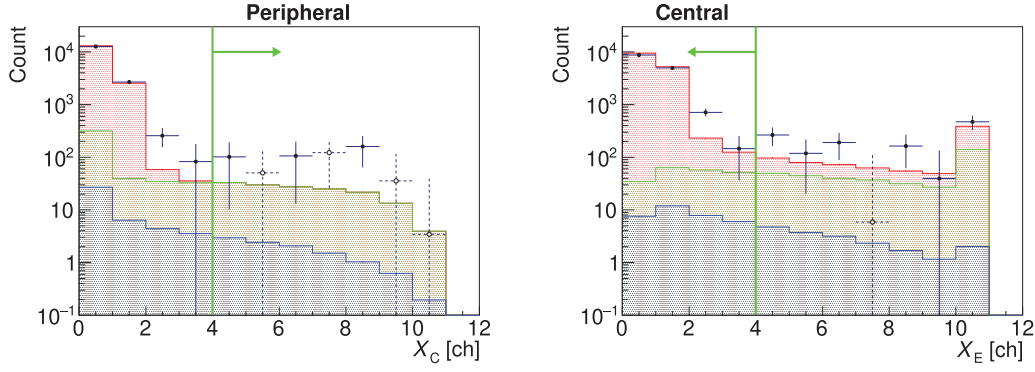


Fig. 17. Distribution of X_C (left) and X_E (right) of S^- (Series 6). Black circles with error bars show the experimental data, where the negative data points were turned up to show in the log plot as open circles with dotted error bars. The green vertical lines show the cut position and the green arrows indicate the central and peripheral components mentioned in the text. Simulated spectra of the neutron decays without scattering (red upper hatching), neutron-induced background (green middle hatching), and decay events of scattered neutrons (blue lower hatching) are plotted together.

components of $S_{\beta\text{cand}}$ are described as

$$\begin{aligned} S_{\beta\text{cand}}^{\text{cent}} &= S_{\beta} + S_{\beta\text{scat}}^{\text{cent}} + S_{n\gamma}^{\text{cent}}, \\ S_{\beta\text{cand}}^{\text{per}} &= S_{\beta\text{scat}}^{\text{per}} + S_{n\gamma}^{\text{per}}, \end{aligned} \quad (14)$$

where $S_{\beta\text{scat}}^{\text{cent}}$, $S_{\beta\text{scat}}^{\text{per}}$, $S_{n\gamma}^{\text{cent}}$ and $S_{n\gamma}^{\text{per}}$ are the central and peripheral components of $S_{\beta\text{scat}}$ and $S_{n\gamma}$, respectively. Note that S_{β} represents the neutron decay without scattering. Though a small part of the S_{β} was truncated by selections, the effects are compensated by the ε_{β} , discussed in Sect. 3.7. In this analysis, $S_{n\gamma}^{\text{cent}}$ is estimated by the simulation of $S_{n\gamma}$ which is scaled so that $S_{\beta\text{scat}}^{\text{per}} + S_{n\gamma}^{\text{per}}$ matches the peripheral component of S^- . Here, we define κ as

$$S_{n\gamma}^{\text{cent}} = \kappa S_{n\gamma}^{\text{per}}, \quad (15)$$

where $\kappa = 1.29$ by the simulation; $S_{\beta\text{cand}}^{\text{cent}}$ can then be described as

$$S_{\beta\text{cand}}^{\text{cent}} = S_{\beta} + S_{\beta\text{scat}}^{\text{cent}} + \kappa S_{n\gamma}^{\text{per}} = S_{\beta} + (\xi_{\text{scat}}^{\beta} + \xi_{n\gamma}) S_{\beta\text{cand}}^{\text{cent}}, \quad (16)$$

where $\xi_{\text{scat}}^{\beta} = S_{\beta\text{scat}}^{\text{cent}}/S_{\beta\text{cand}}^{\text{cent}}$ and $\xi_{n\gamma} = \kappa S_{n\gamma}^{\text{per}}/S_{\beta\text{cand}}^{\text{cent}}$. The statistics of the peripheral component of S^- and the systematics of κ were budgeted as an uncertainty of $\xi_{n\gamma}$.

As the average of all measurement series, $\xi_{n\gamma}$ was $4.1 \pm 0.8\%$, which is 3.2 times the value expected by the originally simulated (n, γ) reactions. The origin of the difference is unknown but may be caused by extra neutron captures outside the neutron shield of ${}^6\text{LiF}$. The unknown γ -rays which account for $(1 - 1/3.2) = 0.69$ of $S_{n\gamma}$ may obey different energy and position distributions from the simulation and result in a different κ . Therefore, we used further track information in the peripheral component to estimate the systematic deviation of κ . In this estimation, we used the two sets of the simulations of γ -rays: one is the energy contrast distribution with the monochromatic energy $E_{\gamma} = 0.1, 0.2, 0.4, 0.8, 1.6, \dots, 12.8$ MeV and the same position distribution as the original simulation; the other is the position contrast distribution which has the same energy distribution as the original simulation and the initial position is the point from where the TPC center moved on to the lead shield surface in the direction along one of the axes x_{\pm}, y_{\pm} , or z_{\pm} , selected to be the most biased position inside the shielding.

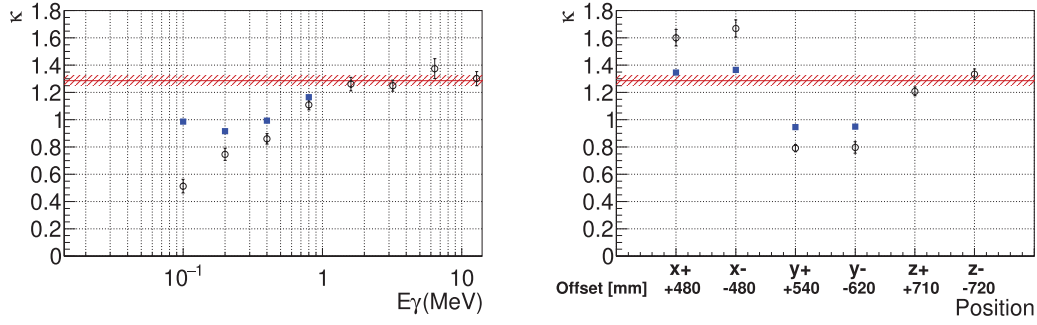


Fig. 18. Comparison of κ of the original and energy contrast simulations (left) and position contrast ones with offset lengths of the source positions (right). The red line indicates κ of the original simulation of $1.29 \pm 0.04_{\text{stat}}$ and black circles shows that of the contrast simulations. Blue squares correspond to the possible 1σ deviations from the original κ calculated by the minimum χ^2 estimation. The resulting uncertainty on κ is calculated using the maximum distance between the blue squares and the red line.

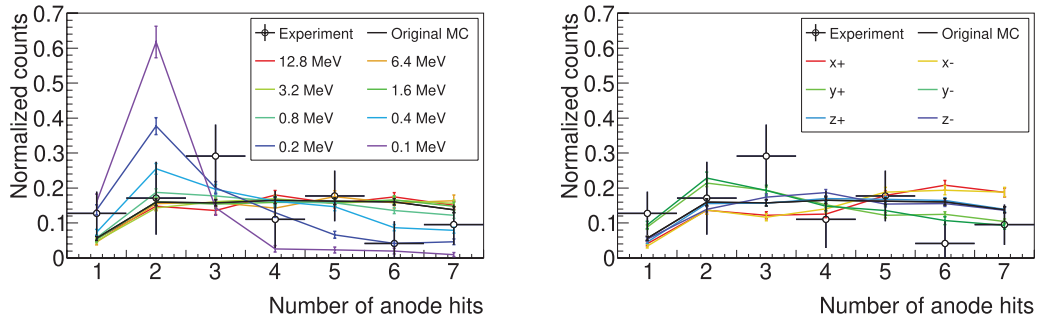


Fig. 19. Distributions of the number of anode hits of the experiment, the original, and energy contrast simulations (left) and position contrast ones (right) of the peripheral tracks. Black circles correspond to the distribution of the experiment. Black lines indicate that of the original simulation and other colored lines do that of contrast ones.

The κ values calculated by the simulations shown in Fig. 18, and the anode wire hits distribution in the peripheral components shown in Fig. 19, are used to estimate the possible deviation of κ from the original simulation. In the case of $E_\gamma = 0.1$ MeV, κ is 0.51 ± 0.05 , but the spectrum of the anode distribution is unlikely from the experimental data, as shown in the energy contrast simulation of Fig. 19. Hence, the contamination fraction of the γ -rays with that energy is constrained with the statistical range from the experimental data. The maximum possible value in 1σ error of the contamination fraction, varied in the range of from 0 to 0.69, was calculated by the minimum χ^2 estimation. The results of the possible κ values are shown in Fig. 18 as the blue squares. Since the energy contrast simulations of $E_\gamma \geq 1.6$ MeV and the position ones of $z+$ and $z-$ have almost the same κ as that of the original one, we ignored them. By taking the worst cases, the 1σ deviation of κ was obtained as

$$\begin{aligned} \kappa &= 1.29 \pm 0.04_{\text{stat}} \begin{matrix} +0.00 \\ -0.37 \end{matrix}_{\text{energy}} \begin{matrix} +0.08 \\ -0.34 \end{matrix}_{\text{position}} \\ &= 1.29_{-0.51}^{+0.09}, \end{aligned} \quad (17)$$

where statistical and systematic errors were summed in quadrature.

The pileup for S_β was corrected in the same manner as described in Sect. 3.5. If the neutron decay and the ${}^3\text{He}(n,p){}^3\text{H}$ events were detected in the same time window, the events are possibly

Table 5. Correction and uncertainty budgets of S_β (Series 6).

Term	Correction(%)	Uncertainty (%)
Statistic of S^-		1.7 _{stat}
Misclassified ion events ($-\xi_{\text{sep}}^{\text{He}} S_{\text{Hecand}}/S^-$)	0.0	+0.0 -0.3
Contamination of $^{12}\text{C}(n,\gamma)^{13}\text{C}$ ($-\xi_{\text{C}}$)	0.0	+0.0 -0.3
γ -ray shielding by neutron shutter ($\xi_{\gamma}^{\text{shutter}}$)	-0.3	0.3
Scattered neutron ($-\xi_{\text{scat}}^{\beta}$)	-0.2	0.02
Neutron-induced γ -ray ($-\xi_{n\gamma}$)	-1.3	2.0 _{stat} +0.5 -0.1 sys
Pileup ($\xi_{\text{pileup}}^{\beta}$)	+0.2	+0.4 -1.2
S_β		2.6 _{stat} +0.6 -1.3 sys

Table 6. Efficiency (ε_{He}) uncertainty budgets (Series 6).

Cut name	Efficiency (%)	Uncertainty (%)
$E_{\text{max}}^{\text{field}}$ cut ($\xi_{\text{sep}}^{\text{He}}$)	-0.01	+0.01 -0.00
ε_{He}	99.99	+0.01 -0.00

recognized as the $^3\text{He}(n,p)^3\text{H}$ events, and this reduces the number of neutron decay events. The probability calculated by the event rates was corrected. We also evaluated the pileups of events of E^- to E^- , which might change the classification of the neutron decay events, or the other classes to the neutron decay events by changing its energy deposit and/or event topology. Thus, we budgeted the pileup probability of E^- to E^- as the systematic uncertainty. We denote this pileup correction as $\xi_{\text{pileup}}^{\beta}$.

Finally, S_β after the corrections described above is given as

$$\begin{aligned}
 S_\beta &= (1 - \xi_{\text{scat}}^{\beta} - \xi_{n\gamma}) S_{\beta\text{cand}}^{\text{cent}} \\
 &= (1 - \xi_{\text{scat}}^{\beta} - \xi_{n\gamma}) \frac{(1 + \xi_{\gamma}^{\text{shutter}})(1 + \xi_{\text{pileup}}^{\beta})(S^- - \xi_{\text{sep}}^{\text{He}} S_{\text{He}})}{(1 + \xi_{\text{C}})} \\
 &\simeq \left(1 - \xi_{\text{sep}}^{\text{He}} \frac{S_{\text{He}}}{S^-} - \xi_{\text{C}} + \xi_{\gamma}^{\text{shutter}} - \xi_{\text{scat}}^{\beta} - \xi_{n\gamma} + \xi_{\text{pileup}}^{\beta}\right) S^-.
 \end{aligned} \tag{18}$$

Corrections and uncertainties for S_β in Series 6 are summarized in Table 5. Note that ξ_{sep}^{β} is budgeted in ε_β .

3.7. Efficiency ε_{He} and ε_β

The detection efficiencies, ε_{He} and ε_β in Eq. (1), were calculated by the simulation. Since the trigger inefficiencies for the neutron decay and $^3\text{He}(n,p)^3\text{H}$ without scattering were estimated to be small enough from the simulation ($< 10^{-3}$ and $< 10^{-4}$, respectively), the systematic uncertainties of the efficiencies were evaluated for the event selections described in the former subsections. We summarized the results of the cut efficiencies and uncertainties of ε_{He} and ε_β in Tables 6 and 7. The value in the efficiency column for each cut represents the ratio of the neutron decay which was rejected when only the corresponding cut was applied.

The uncertainties of the cut efficiencies were estimated by taking into account possible deviations of the cut thresholds. For instance, the discrepancy between the measurement and the simulation

Table 7. Efficiency (ε_β) uncertainty budgets (Series 6).

Cut name	Efficiency (%)	Uncertainty (%)
E_{\max}^{field} cut (ξ_{sep}^β)	-1.3	+0.5 -0.7
Low energy cut at $E_{\text{thresh}}^{\text{anode}}$	-0.3	+0.1 -0.2
Tritium decay rejection	-0.6	0.06
Track geometry (y -direction)	-1.3	0.2
Track geometry (X_E)	-3.2	0.03
Neutron polarization		0.13
W value for decay proton		0.35
ε_β	93.9	+0.6 -0.8

in the energy spectra of the cosmic-rays for all measurement series was 5–9%, as shown in Fig. 5. Hence we accounted for a change when the cut threshold in energy was shifted by the discrepant value as a cut uncertainty. The uncertainties for the E_{\max}^{field} cut and the low-energy cut at $E_{\text{thresh}}^{\text{anode}}$ were obtained in this way. For the track geometry (y -direction), the non-uniformity of 9.5% of the drift velocity was considered. The uncertainty for the tritium cut was estimated by the standard deviation of the peak/full-integration ratio distribution of the 5.9 keV X-ray waveforms. The uncertainty of the threshold of X_E could be caused by the misalignment of the beam position, which was estimated to be less than 2 mm. We budgeted 12 mm, which corresponds to 1 wire width, as a conservative estimation.

Some other systematic effects on ε_β are discussed here. The electrons emitted from the neutron decay have an angle distribution around the neutron polarization. The angular distribution, $W(\theta)$, can be described as

$$W(\theta) = 1 + \frac{v}{c}PA \cos(\theta), \quad (19)$$

where θ is an angle between the direction of the electron and neutron polarization, v is the velocity of the electron, c is the speed of light, P is the polarization of the neutron and A is the asymmetry parameter for the neutron decay, $A = -0.1184 \pm 0.0010$ [1]. The polarized neutron beam at BL05 was used for this experiment to produce bunches by the SFC. Although we used the polarized neutron from the SFC, there was no magnetic field to keep the polarization. Thus, the polarization direction of the neutron is unknown and the detection efficiency of electrons in the TPC may change due to the unexpected bias of the momentum direction of the electron. We compared the detection efficiencies when neutrons were completely polarized along the x -, y - or z -axis, as well as when they were unpolarized using the simulation. The maximum deviation was +0.13% when neutrons were polarized in the $-y$ direction, which goes to the bottom of the drift direction. The value was budgeted as an uncertainty.

It is known that W increases for low-energy charged particles [53], although this effect was not implemented in the current simulation. This may be significant for protons from the neutron decay (the kinetic energy is below 1 keV), leading to a decrease in the detection efficiency. The upper limit of this effect can be estimated by forcibly setting the proton kinetic energy as zero in the simulation, i.e., assuming an infinite W value for the proton. The loss of efficiency was consistent with zero, $(0.06 \pm 0.35)\%$ for the neutron lifetime with an uncertainty originating from the statistical error of the simulation.

Table 8. Values and uncertainty budgets (Series 6).

Term	Value	Unit	Relative uncertainty(%)
S_{He}	$(3.581 \pm 0.006_{\text{stat}}^{+0.004} {}_{-0.002}^{\text{sys}}) \times 10^5$	Events	$0.18_{\text{stat}}^{+0.11} {}_{-0.06}^{\text{sys}}$
S_{β}	$(1.441 \pm 0.039_{\text{stat}}^{+0.011} {}_{-0.018}^{\text{sys}}) \times 10^4$	Events	$2.7_{\text{stat}}^{+0.8} {}_{-1.3}^{\text{sys}}$
ε_{He}	$99.99_{-0.00}^{+0.01} {}_{\text{sys}}$	%	$+0.01_{-0.00}^{\text{sys}}$
ε_{β}	$93.9_{-0.8}^{+0.6} {}_{\text{sys}}$	%	$+0.7_{-0.9}^{\text{sys}}$
ρ	$2287 \pm 10_{\text{sys}}$	$10^{16} \text{ atoms m}^{-3}$	0.4_{sys}
σ_0	$5333 \pm 7_{\text{sys}}$	10^{28} m^2	0.13_{sys}
ν_0	2200	m s^{-1}	exact
τ_n	$869 \pm 24_{\text{stat}}^{+13} {}_{-11}^{\text{sys}}$	s	$2.6_{\text{stat}}^{+1.5} {}_{-1.1}^{\text{sys}}$

A portion of the neutron decays emit not only an electron and a proton but also a γ -ray. The probability of the radiative decay is $(9.2 \pm 0.7) \times 10^{-3}$ for γ -rays with energy of more than 0.4 keV [54]. This reaction is expected to have less of an effect because the TPC is insensitive to γ -rays and an electron is produced as well, though its energy is reduced. The effect of the energy reduction was calculated using the theoretical formulation in Ref. [55]. The probability that the electron energy becomes less than the cut-off energy (5 keV) due to the radiative decay is expected to be 6.5×10^{-7} , therefore we ignored this effect.

4. Result and discussion

From the results and discussions in the former sections, the number of events of the ${}^3\text{He}(n,p){}^3\text{H}$ (S_{He}) and neutron decay (S_{β}), the extraction efficiencies of the ${}^3\text{He}(n,p){}^3\text{H}$ reactions (ε_{He}) and neutron decay (ε_{β}), and the number density of ${}^3\text{He}$ in the TPC (ρ), were obtained with uncertainties and are provided in Tables 2, 4, 5, 6, and 7 for a typical measurement series (Series 6), respectively. The neutron lifetime derived by Eq. (1) is listed in Table 8 with all values and uncertainties.

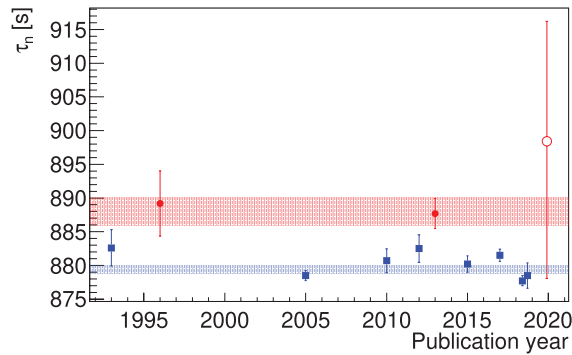
Note that some uncertainties are not independent; S_{β} and S_{He} , ε_{β} and ε_{He} have negative correlations through the $E_{\text{max}}^{\text{field}}$ cut, which introduces an underestimation of the uncertainty of τ_n . However, the effects were negligible ($<0.1\%$) because the uncertainties of $\xi_{\text{sep}}^{\text{He}}$ and ε_{He} were small enough. The uncertainties of $\xi_{\text{pileup}}^{\beta}$ and $\xi_{\text{pileup}}^{\text{He}}$, which describe how the pileup events were identified, also have a negative correlation; this effect is also less than 0.1% and is therefore negligible. There are more parameters which have correlations; $\xi_{\text{scat}}^{\beta}$ was determined by $\xi_{\text{scat}}^{\text{He}}$, and the uncertainty of both of the energy cuts, $E_{\text{thres}}^{\text{field}}$ and $E_{\text{thres}}^{\text{anode}}$, were determined by the discrepancy between the measurement and the simulation of the cosmic-ray. A part of these uncertainties cancel each other out in the estimation of the neutron lifetime. We adopt the quadratic sum of them in Table 8 for a conservative and simple estimation.

For each series of the measurement, a value of the neutron lifetime with uncertainties was derived in the same manner. The results are shown in Table 9. We observed no systematic effects due to the ρ values described in Sect. 2.7 in the present sensitivity. The average was calculated by fitting only with statistical uncertainties, where $\chi^2/\text{ndf} = 5.8/5$. The systematic uncertainties of the complete measurement series were expected to correlate with each other. Thus, we treated them as being fully correlated as a conservative estimation; the upper and lower systematic uncertainties were determined by taking averages of the data points shifted to 1σ . By combining all measurement series, we obtained a neutron lifetime of

$$\tau_n = 898 \pm 10_{\text{stat}}^{+15} {}_{-18}^{\text{sys}} \text{ s}. \quad (20)$$

Table 9. Neutron lifetimes for each measurement series and those combined.

Series	τ_n (s)
1	951 ± 27 stat $_{-34}^{+22}$ sys
2	906 ± 20 stat $_{-12}^{+13}$ sys
3	908 ± 49 stat $_{-34}^{+13}$ sys
4	890 ± 24 stat $_{-15}^{+16}$ sys
5	882 ± 25 stat $_{-19}^{+12}$ sys
6	869 ± 23 stat $_{-11}^{+13}$ sys
Combined	898 ± 10 stat $_{-18}^{+15}$ sys

**Fig. 20.** Data of neutron lifetime obtained with the bottle method (blue squares) [12–18] and the beam method (red circles) [19,20]. The blue and red bands show the global average and error of each method. The result of this work is shown by the open circle.

By simply summing the statistic and systematic uncertainties in quadratic, it gave us $\tau_n = 898^{+18}_{-20}$ s, which is shown in Fig. 20 for comparison with previously published results obtained with the bottle method [12–18] and the beam method [19,20]. Both sets of previously published results are within the uncertainty of our measurement. Because the uncertainty of this work is still larger than the difference between the two methods, further improvements are required to resolve the neutron lifetime puzzle through our experiment.

Improvements in the experimental accuracy are in progress for the statistics and the major systematic uncertainties mentioned below. The beam transport with larger acceptance, which is expected to increase the neutron intensity 8-fold, will be installed to improve the present statistical error of 10 s. The systematic uncertainty in this work was dominated by $\xi_{n\gamma}$, which corresponds to $+2/-14$ s in τ_n . Reduction or identification of the unknown background that simultaneously occurs with the neutron decay, discussed in Sect. 3.6, reduces the systematic uncertainty. Higher statistics by the new beam transport will help the identification because the present statistical error in the peripheral region was dominated by the environmental backgrounds, and the increase of the beam intensity improves the signal-to-noise ratio. Additional measurements with lower-pressure gas would enable us to reduce $\xi_{n\gamma}$; for instance, a 50-kPa operation, which is reasonably performed, makes it half of the present value.

The pileup correction $\xi_{\text{pileup}}^\beta$ on S_β shown in Table 5 is another dominant systematic uncertainty, which corresponds to $+11/-4$ s. This is mostly due to the cosmic-rays coming after the triggers. It can be rejected by implementing a software veto using the signals of the cosmic-ray veto counter recorded in the TDC, and it will reduce the uncertainty to $+4/-0.5$ s. The uncertainty of ε_β was

mainly caused by the E_{\max}^{field} cut as shown in Table 7, which corresponds to $+4/-6$ s. The separation of the neutron decay and ${}^3\text{He}(n,p){}^3\text{H}$ is currently performed by only one parameter (E_{\max}^{field}) but it is possible to reduce the uncertainty by using another parameter of the particle trajectories, e.g. the full-waveform integration. A cut with the two parameters is expected to reduce the uncertainty to 1 s.

The uncertainty of ρ corresponds to 4 s in this work as shown in Table 2. The main source of the uncertainty in ρ_{ad} was caused by the volume-ratio measurement of the vacuum chamber because the ratio was so large that it was measured in 3 steps. Employing a pressure gauge with a larger dynamic range will suppress the uncertainty of ρ_{ad} to $1/3$ (~ 1 s). The uncertainty of ρ_{G1} was limited by the accuracy of the mass spectroscopy. Measurements with nitrogen gas proposed in Ref. [46] can reduce it to $1/10$ of the current value (~ 0.4 s) in principle. With those improvements, the uncertainty of ρ is expected to be reduced to ~ 1 s.

5. Summary

The neutron lifetime puzzle, the discrepancy of 8.5 s (4.0σ) between the experimental data obtained with the bottle and beam methods, is still unsolved. We have launched a new experiment using the pulsed cold neutron beam at J-PARC. In this experiment, the neutron beam was formed into bunches of 40 cm using a spin-flip chopper, and was injected to the TPC of 1-m length. The TPC simultaneously counted the events of the neutron β -decay and the (n,p) reaction on ${}^3\text{He}$, the number density of which was accurately controlled. The neutron lifetime was derived from the ratio of those counting rates. This experiment is classified as a beam method but dominated by the different systematic uncertainties from the previous experiments. As the first result of this experiment, we obtained the neutron lifetime of $898 \pm 10_{\text{stat}}^{+15}_{-18} \text{ s}_{\text{sys}}$. The present value of the neutron lifetime does not contradict the other recent results within the range of its uncertainty. Further improvements in the statistical and systematic uncertainties are underway.

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