Minimal-Disturbance Seismic Rehabilitation of Steel Moment-Resisting Frames 1 using Light-weight Steel Elements 2 3 Masahiro Kurata¹, Miho Sato², Zhang Lei², Oren Lavan³, 4 Tracy Becker⁴, Masayoshi Nakashima¹ 5 6 ¹Disaster Prevention Research Institute, Kyoto University, Kyoto, Japan 7 ² Architecture and Architectural Engineering, Kyoto University, Kyoto, Japan 8 ³Civil and Environmental Engineering, Technion - Israel Institute of Technology, Haifa, 9 Israel 10 ⁴Civil Engineering, McMaster University, Ontario, Canada 11 12 13 14 ABSTRACT 15 This paper presents a rehabilitation technique developed under a design and construction 16 scheme, termed minimal-disturbance seismic rehabilitation. This scheme pursues enhancing 17 the seismic performance of buildings with the intention of improving the continuity of 18 business while minimizing obstruction of the visual and physical space of building users and 19 20 the use of heavy construction equipment and hot work (welding/cutting). The developed rehabilitation technique consists of light-weight steel elements and aims to decrease demands 21 to beam-ends of steel moment-resisting frames. The behavior of the baseline model was 22 23 verified through numerical analysis and proof-of-concept testing. Furthermore, the effectiveness of rehabilitation is studied through retrofitting a four-story steel moment-24 resisting frame originally designed with Japanese design guidelines. 25 26 27 **KEYWORDS**: seismic rehabilitation; minimal-disturbance; steel moment-resisting frames; 28 light-weight elements; tension-only 29 30 **1. INTRODUCTION** 31 A considerable number of existing buildings in earthquake-affected regions are still at risk of 32 poor performance in seismic events. Major earthquakes have shown that older buildings can 33 34 present serious hazards. Such buildings will still be a part of the landscape throughout the world in the foreseeable future [Nakashima et al, 2014]. Retrofitting at-risk buildings would 35 minimize damage to them and thus decrease the initial disruption to normal functionality. As 36 37 a consequence, quick recovery would be facilitated, requiring less effort and resources. 38 Many rehabilitation techniques have been developed and practical applications for the repair 39 and rehabilitation of earthquake-damaged and seismically deficient buildings have been 40 published [e.g., FEMA, 2007; MEXT, 2008, ASCE, 2006]. However, most seismic 41 rehabilitation schemes require significant changes in architectural planning and relocation of 42

occupants during construction. These consequences of retrofitting may be particularly
undesirable for many applications. For cases that require relatively small or partial seismic
upgrading, rapidly deployable rehabilitation devices may be a preferable option for reducing
indirect costs associated with construction. Kurata et al. presented a strategy named rapid
seismic rehabilitation and the benefits of adopting a tension-only approach [Kurata et al.,
2012a and 2012b]. The benefits of the tension-only system include: (1) elimination of

undesirable global and local buckling in supplemental load-carrying elements, enabling the
use of light-weight steel components; (2) rational implementation of a strict capacity design
(over-strength is known or capped); (3) use of simple connections with rapid and adjustable
installation.

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54 Deformation capacity of steel moment-resisting frames, designed to achieve a beam collapse mechanism by providing columns with sufficient reserved strength, is controlled primarily by 55 the failure of beam-column connections. When steel beams are connected to a floor slab in 56 such a way that they act as one element, the contributions of the concrete floor slab to the 57 beam are non-negligible. Experience and laboratory testing indicated the major contributions 58 are an increase in flexural strength when the slab is in compression (i.e., positive bending), an 59 increase in the second-moment of inertia of the beam in the strong axis, and asymmetric 60 cyclic deterioration in strength and stiffness [e.g., Leon et al, 1998; Chen and Chao, 2001; 61 Kim et al, 2004; Nakashima et al, 2005]. A full-scale test of a two-story composite steel 62 building with steel moment-resisting frames [Nakashima et al, 2005] demonstrated that the 63 beam flexural strength increased about 1.5 times in positive bending and 1.2-1.4 times in 64 negative bending compared with that of the bare steel beam. However, large tensile strains at 65 the bottom flanges of composite steel beam with concrete slab initiate fracture near column 66 67 surfaces when subjected to positive bending that puts tension on the lower fibers. In other words, because of composite action, beam-column connections possess reserved deformation 68 capacity to fracture under negative bending relative to positive bending. 69 70

- 71 Several techniques have been proposed to enhance the ductility of beam-column connections in response to the severe damage observed in the 1994 Kobe and 1995 Northridge 72 73 earthquakes [Suita et al., 2000; AISC, 2009]. One straightforward method is to strengthen a beam end near the column surface by welding steel plates to increase the area of the bottom 74 flange, shifting the neutral axis in the critical section closer to the mid-height. Another 75 76 effective method is to intentionally reduce the flange width at the section away from the beam 77 ends (i.e., reduced beam sections) [FEMA, 2008]. However, all these methods require interruption of normal building operations. 78
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This paper presents an innovative rehabilitation technique of steel beam-column connections 80 developed within a design scheme termed minimal-disturbance seismic rehabilitation. The 81 goal of this strategy is improved seismic performance with minimal obstruction of the visual 82 and physical space for building users. The presented rehabilitation technique increases the 83 strength and stiffness of steel beam-column connections and provides stable energy 84 dissipation while reducing the bending-moment demand at beam ends. Contrary to 85 rehabilitation using large structural elements, enhancement by means of the combined 86 multiple seismic measures (e.g., strength, stiffness, added damping and ductility capacity) is 87 expected so as to avoid excessive increase in force demands on the neighboring components 88 and foundations. Disturbance to the original framing is minimized by limiting the location of 89 added elements to the upper part of the frames and thus retaining walking access and 90 sightlines for the building users. First, the design concept and mechanism of the proposed 91 92 rehabilitation technique are introduced. The behavior and performance are then verified through finite element (FE) analyses and quasi-static loading tests. Finally, the effectiveness 93 of the technique is evaluated through the application to a four-story steel moment-resisting 94 95 frame. The responses of the bare and rehabilitated frames to a set of ground motions are 96 compared in terms of plastic rotations at beam-ends as well as roof drifts.

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2. DESIGN CONCEPT

100 2.1. Minimal Disturbance Seismic Rehabilitation for Steel Moment-Resisting Frames

In steel moment-resisting frames, bottom flanges of composite beam near column surfaces are 102 103 the location where fracture initiates because of large bending and composite action. The section's neutral axis under positive bending is located at a higher position than that under 104 negative bending because of the large compressive force in the concrete slab. Thus, the 105 fracture normally initiates from the beam bottom flanges rather than from the top flanges, and 106 the deformation capacity before fracture is larger in negative bending than in positive bending. 107 This is true if proper lateral bracing is provided to prevent global buckling after the onset of 108 local buckling at the beam flanges. 109

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Reducing the positive bending moment at the beam ends can enhance the deformation 111 capacity of beam-column connections and eventually that of the overall frame. Such 112 rehabilitation can be achieved by adding supplemental load-resisting components to create 113 alternative load paths in the original frames as shown in Figure 1. This rehabilitation 114 technique, named the Minimal-Disturbance Arm Damper (MDAD), is specifically designed to 115 116 minimize the disturbance to the existing frame. The use of light steel members enables the installation of the damper without welding or using heavy construction equipment, and the 117 configuration only uses the corner part of the opening, retaining visibility. MDAD connects 118 119 the mid-span of the beam with the upper part of the column using two identical tension-only rods. Energy dissipation is hysteretic, composed of yielding in steel bending plates at the 120 column-MDAD interface. The plates are attached to the column by post-tension rods. By 121 yielding, the steel plates limit the load exerted on the existing frame under severe earthquakes 122 and dissipate seismic energy in a stable manner without the pinching behavior described in 123 the next section. 124

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The bending plates are connected to the column as shown in Figure 1(b). Bending plates are placed on either side of the column with supported by two spacer plates at their ends. The spacer plates are firmly attached to the column surface by tightening the post-tension rods to cause a large friction force between the plates and the column, preventing the entire MDAD from sliding against the column during loading. These spacer plates ensure that the bending plates do not touch the column, which would stop bending plate deformation, limiting the

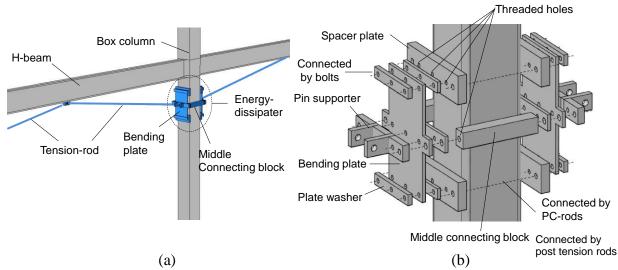


Figure 1. Schematic of rehabilitation system: (a) overall shape; (b) exploded view of MDAD.

energy dissipation. The bending plates are fixed to the spacer plates by several bolts. The two rigid rectangular bars named "middle-connecting blocks" connect the two bending plates, so they displace as one. The pin-connection for the tension-rod is bolted to the middle of the bending plate. The other end of the tension-rod is connected to the beam by high-strength bolts which require drilling holes in the beam flanges; there exists a room for future development for this part.

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139 2.2. Basic Mechanism

For the MDAD a tension-only load-resisting mechanism was adopted. Figure 2 shows the 141 hysteretic behavior of the MDAD. When the lateral load is applied to a beam-column 142 connection, as shown in Figure 2(a), one side of the beam-column connection opens and the 143 other side closes. Accordingly, the tension-rod in the opening side pulls on the bending plate 144 it is attached to. As the two steel plates are connected at their mid-section, they deform 145 together and yield (point b in Figure 2). The deformation of the steel plates prevents 146 compression of the tension-rod in the closing side. When loading is reversed (Figure 2(b)), at 147 point d in the hysteresis loop, the tension-rod on the left side starts to sustain tension force, 148 while the tension-rod on the right side loses tension force. Eventually, once the force is great 149 enough on the left tension-rod, the bending plates will yield in the opposite direction. The rod 150 in the compression side does not contract or buckle because of the unique deformation of the 151 pair of bending plates moving together, which results in the generation of a fat loop from 152 153 point d to e (Figure 2(c)). This mechanism enables the MDAD to dissipate energy with a stable bilinear relationship. 154

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The benefit of reducing the positive bending moment at beam ends, and thus postponing yielding, is illustrated in Figure 3. The tension-rod applies vertical and lateral forces to the beam at mid-span, as well as a bending moment, because of the vertical distance between the

159 point of application of the forces and the beam centroid. These forces and bending moment

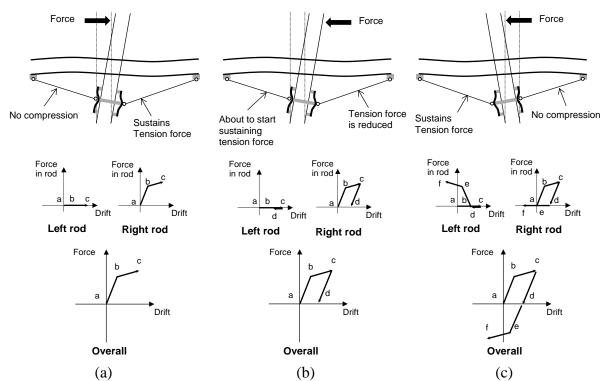


Figure 2. Mechanism of MDAD: (a) at loading; (b) at unloading; and (c) at reversed loading.

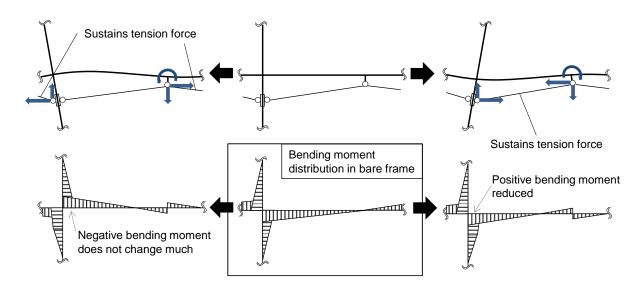


Figure 3. Reduction in demand to beam ends.

generate additive negative bending moment at the beam end that was originally subjected to a 160 positive bending moment. The other beam end that was originally subjected to a negative 161 bending moment sustains little change. For a static pushover loading, the MDAD does not 162 have specific contributions in reducing joint rotation after the yielding of the beam ends. 163 However, the reduction in bending moment while the beam ends remain elastic delays the 164 vielding of the beam ends, and the plastic rotation starts accumulating at a later stage. Thus, 165 166 even after yielding, for the same drift the plastic rotation is smaller with the MDAD. For earthquake loadings, the MDAD repeatedly delays the yielding of the beam end under 167 positive bending while decreasing story drift by dissipating energy and increasing story 168 stiffness and strength. The MDAD restrains the local deformations of a critical section and 169 enhances the deformation capacity of entire frame in a comprehensive manner. 170

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Similar load-resisting systems using the tension-only approach have been proposed in the past [Pall, 1983; Anagnostides et al., 1989; Mualla and Bellev, 2002; Kurata et al., 2012a; Kang and Tagawa, 2013]. Nevertheless, all of them occupy large spaces because they are configured in X- or V-bracing. In addition, in the proposed system the size of the energy dissipating part is reduced as much as possible by the positive use of the existing column.

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3. NUMERICAL ANALYSIS

A baseline model of the MDAD designed for rehabilitating a steel beam-column connection
 in a low-rise steel moment-resisting frame was numerically analyzed using general-purpose
 FE analysis code. The load-resisting and energy-dissipating mechanism of the MDAD was
 verified and the design details of the baseline model were examined.

- 184185 *3.1. Baseline model*
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The baseline model of the MDAD was designed for a frame with a 7.2 m span and 3.6 m story height, representative of typical low-rise steel moment-resisting frames in Japan. The beam and column sections were selected as H-400×200×9×16 (Z_{px} =1.56×10⁶ mm³) and HSS-350×350×19 (Z_p =2.97×10⁶ mm³) from Japanese standard sections. The design yield strength of the MDAD in terms of lateral-resisting force was tentatively set at around 10% of the shear strength of the column. The stiffness of the MDAD was selected to yield at a story drift of

1.0%. The design yield strength of the MDAD in terms of lateral-resisting force was 193 tentatively set at around 10% of the shear strength of the column. The stiffness of the MDAD 194 was selected to yield at a story drift of 1.0%. The MDAD was located at three quarters of the 195 story height, considering the balance between the minimal disturbance to the users' eyesight 196 and the effectiveness of MDAD. With this configuration, the strength and stiffness of the 197 198 MDAD can be easily controlled by adjusting the dimension of bending plates. The aforementioned designed requirements were achieved with a reasonable dimension of bending 199 plates (length \times width \times thickness = 450 mm \times 350 mm \times 19 mm) and tension rods with a 200 diameter of 45 mm. 201

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203 *3.2. Behaviors in Finite Element Simulations*

205 The basic behavior of the baseline MDAD model was examined using a simplified model as illustrated in Figure 4(a). This model is built to a half scale to estimate the responses of 206 following experimental tests conducted in a half scale. In this model, only the MDAD resisted 207 the lateral-force that was applied at the bottom of the column, and the flexibility of columns 208 and beams was not included. As the MDAD only adds axial force less than 10% to the 209 yielding axial force of beams, undesirable deformation at beam-column connections or 210 211 reduction in bending moment capacity due to the added axial force is not expected. The fundamental behavior of this model was examined using FE analysis code, Abaqus [Dassault 212 Systems, 2010]. The model consisted of a pin-supported column and the MDAD as shown in 213 Figure 4(b). The column was modeled as being elastic using shell elements (4-node 214 quadrilateral shell element with reduced integration). The energy-dissipating part of the 215 MDAD, consisting of steel bending plates, spacers and a middle connecting block (see 216 Figure 1 for details), was modeled using solid elements (3D 8-node linear isoparametric 217 element with reduced integration). The spacers were rigidly attached to the column surface 218 and thus no slippage at the surface was allowed. The tension-rods were modeled using a beam 219 element (B31) with moment release at both ends. The steel bending plates had a bilinear 220 221 stress-strain relationship with a yielding stress of 300 MPa and strain hardening of 0.5%. To trace the plasticity in the plates accurately, they were finely meshed with six elements along 222 the thickness. Figure 4(c) shows a close-up of the energy dissipater of the MDAD during 223 cyclic loading. Two bending plates pulled by the tension-rod deformed together as intended in 224 the design. The space between the bending plates and the column flange was sized based on a 225 preliminary finite element analysis, and thus the touching between the plates and column does 226 not occur even under very large deformations. 227

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Figure 4(d) shows the force-deformation relationship of the baseline MDAD model under 229 incremental cyclic loading. The loading was controlled with beam-column rotation that was 230 computed using the displacement of the column at the mid-location of the energy dissipater. 231 The loading was repeated for two cycles at amplitudes of 1%, 2%, and 3%. The resulting 232 hysteresis behavior was a stable and "fat" loop. The steel bending plates yielded at a beam-233 column rotation of 0.8% and a lateral force of 15 kN. The lateral force reached 23 kN by the 234 end of the loading. Figure 4(e) shows the force history of the tension-rods in terms of the 235 beam-column rotation. Over the entire loading, one of the tension rods always carried a force 236 while a slight gap appeared at zero force during a transfer of force from one tension-rod to the 237 other. The rod force was 52 kN at the yielding of the steel bending plates and 105 kN at the 238 end of loading. These values were below the yield strength of the tension-rods, which was 239 240 132 kN.

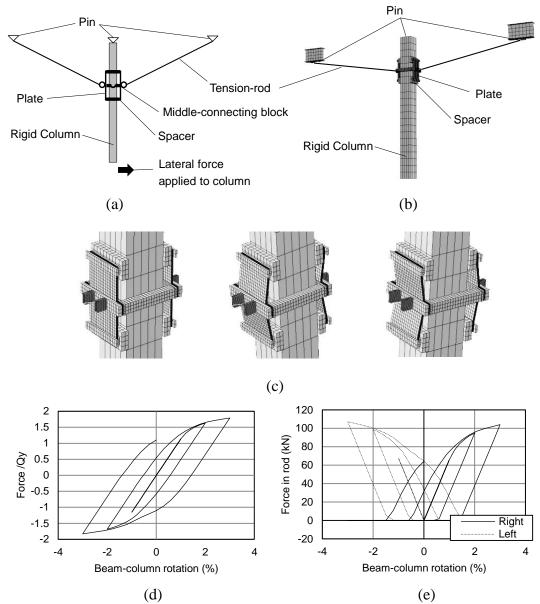


Figure 4. Numerical simulation of baseline model: (a) explanation of simplified model; (b) FE model; (c) behavior of bending plates in FE analysis; (d) relationship between lateral force and beam-column rotation; (e) force history in tension-rod.

The FE model was also used to compute the necessary force in the post-tension rods used to 242 connect the bending plates to the column. The force must be great enough to restrict the 243 vertical movement of the bending plates resulting from slippage between the spacers and 244 column surface. The static friction coefficient between the spacers and the column surface 245 was assumed as 0.1 with the adoption of a large safety factor considering the surface 246 unevenness of cold-formed HSSs explained in Section 5.1. The required force in the 247 connecting post-tension rods to be applied during installation (see Figure 1) was computed as 248 249 35 kN based on the vertical force components transferred from the tension-rods. A possible failure mechanism of the MDAD at very large deformations is the yielding of the tension-rods. 250 This would significantly reduce the stiffness of the MDAD and caps the force input to the 251 bending plates. 252

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4. EXPERIMENTAL PROGRAM

The basic behavior of the baseline model was first examined using a setup examining only the behavior of the MDAD, without considering the flexibility of the steel beam-column connection to be rehabilitated. Afterwards, a steel beam-column connection rehabilitated with the MDAD was tested.

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261 4.1. Test Specimens

To examine the behavior of the rehabilitation technique in detail, four parameters were 263 considered: the rigidity of the middle connection block, the location of the bending plates, the 264 force in the post-tension rods, and the steel yield strength. Table 1 shows a summary of the 265 specimens. Specimen 1 was regarded as the baseline model that was analyzed at half scale in 266 Section 3.2. Specimen 2 used relatively flexible elements for the middle connecting block, i.e., 267 4.3 times less in axial stiffness, and thus the two bending plates attached to the column were 268 expected to deform differently. In Specimen 3, the effect of the inclined angle of the tension 269 rods on the behavior was examined by attaching the bending plates slightly farther from the 270 beam-column joint node, i.e., at 600 mm in Specimen 3 instead of 400 mm in Specimen 1. In 271 Specimen 4, the force in the post-tension rods was increased from 30 kN to 50 kN to prevent 272 273 the slippage of the bending plate on the surface of the column. In Specimen 5, low-yield-point (LYP) steel that is characterized by low yielding stress and significant isotropic strain 274 hardening was used for the bending plates to achieve yielding and energy dissipation at small 275 276 levels of deformation. In Specimen 6, two plates made of high-strength steel (HS) and LYP were stacked and jointed by bolts at the middle and both ends. This configuration was 277 intended to achieve early yielding while maintaining a large secondary stiffness. Finally, 278 279 Specimen 1 was applied to a beam-column connection.

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The shape of the bending plates in the various specimens differed slightly [Figure 5]. Specimens 1, 3, 4 and 5 used bending plates with wings in the middle, and the stiffness in the connecting region to the middle connecting blocks was increased. Specimen 2 used the bending plates without wings and thus had relatively small out-of-plane flexibility at the connections to the middle connecting blocks. Specimen 6 used the bending plates made of HS and LYP with different plate widths.

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- 288 *4.2. Test Setup*

The performance of the proposed system was evaluated through a series of quasi-static cyclic 289 loading tests. Figure 6(a) shows the loading system for the component tests. The test setup for 290 the component level test consisted of an elastic column and two short beams that represented 291 the mid-part of the beams. The column bottom was pin-connected so that only the 292 rehabilitation system resisted the lateral force applied at the top of column by a hydraulic jack. 293 The column was 1913 mm long and the distance between the centers of the two short beams 294 was 3600 mm. The typical assembly of the proposed system was as follows: 1) steel bending 295 plates were firmly attached to the surfaces of column over spacers using post-tension rods 296 297 with a force of 40 kN; 2) the mid-sections of two steel bending plates placed at the two sides of the column were connected to each other using a rigid steel block; 3) the mid-span of 298 beams and the mid-sections of the steel bending plates were connected with tension-rods and 299 300 tightened with turnbuckles.

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Figure 6(b) shows the test setup for an application test, in which a beam-column connection with a story height of 1800 mm and beam span of 3600 mm was rehabilitated with the proposed system. The column base was pin-connected and the beam ends were roller-

Sp.	Steel type	Plate location [mm]	Plate width [mm]	Thickness [mm]	Force in post-tension rod [kN]	Connector between plates
1	SS400	400	175	9	35	Block
2	SS400	400	175	9	35	Post-tension
						rod
3	SS400	600	175	9	35	Block
4	SS400	400	175	9	50	Block
5	LYP	400	175	9	35	Block
6	HS/LYP	400	100/150	6/9	35	Block

Table 1. Test specimens for component tests

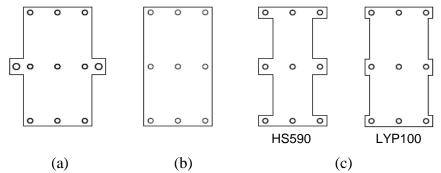


Figure 5. Shape of bending plates: (a) Specimen 1 and 3-5; (b) Specimen 2; (c) Specimen 6.

supported. The top of column was connected to a hydraulic jack. The sizes of the main components were: (a) a HSS column with a \Box -175×175×12 cross-section; (b) beams with a H-200×100×5.5×8 cross-section; (c) M22 tension rods.

- 308 *4.3. Measurement system*
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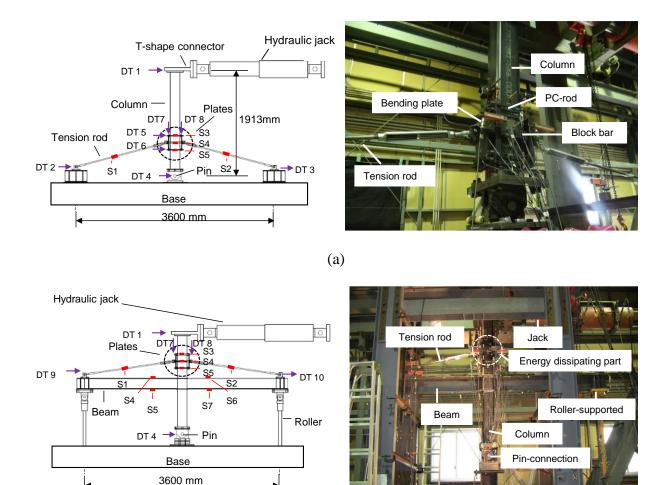
The locations of the displacement transducers (DT) and strain gauges (S) are shown in Figure 6(a) and (c). In both tests, the displacement of the loading point was recorded using DT1. In the component tests, the column displacement for computing the beam rotation angle was measured as the average displacement from DT5 and DT6. DT2 and DT3 monitored the horizontal deformation of the pins. In the application test, the horizontal displacement of the beam-ends was measured using DT9 and DT10. In both tests, DT7 and DT8 monitored the vertical slippage of steel bending plates against the column.

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The axial forces in the tension-rods were monitored using S1 and S2 attached to the turnbuckles, which were the part of the tension-rod. S3 and S5 were used to monitor the force in the post-tension rods. S4 was used to monitor the axial force in the middle connecting block. When the beam was added to the setup (Figure 6(c)), S6 to S9 were used to estimate the bending moments in the beam.

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- 324 *4.4. Loading protocol*

The loading protocols used in the tests are shown in Figure 7. Loading was repeated three times at displacements under 1% drift and twice for larger amplitudes. For the component test, the loading protocol was applied as a beam-column rotation that was computed using the displacement of the column at the mid-location of the energy dissipater. The amplitude of the rotation angle was increased from 0.25% to 3%. In Specimens 3 and 4 with steel bending



(b)

Figure 6. Loading system and measurement plan: (a) component test; (b) photo of component test setup; (c) application test; (d) photograph of application test setup.

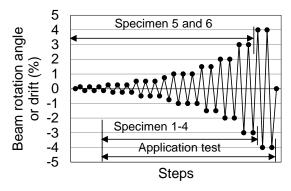


Figure 7. Loading protocol.

plates made of LY100, three cycles of 0.125% loading were added to examine the early yielding of the bending plates. For the application test, the loading protocol was applied as story drift that was calculated as the column top displacement divided by the story height. The loading continued until 4%, taking into account the extra deformation resulting from the flexibility in the beam-column connection.

335 4.5. Material properties

Material	Steel plates			Beam flange	Beam web	Tension-rod
properties	SS400	LY100	HS590	SS400	SS400	SS400
Yield stress σ_y (N/mm ²)	290	58	550	326	335	350
Maximum stress σ_u (N/mm ²)	440	239	655	448	455	548

Table 2 Material properties

Three different steel materials, conventional mild steel (SS400), LY100 and high strength steel (HS590) were used in the tests. Their material properties obtained from coupon tests are shown in Table 2. For the application test, the material properties of the beam flange and web were also obtained.

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5. TEST RESULTS

The results for the component tests and the application test are summarized and compared with the results of the preliminary analysis in Figures 8 to 11. In the plots, the solid and the dotted lines correspond to the test and analysis results, respectively.

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346 5.1 Baseline Model

348 Figure 8(a) shows the overall behavior of the baseline specimen. The tests behaved well with 349 stable energy dissipation up to large deformations. The initial stiffness matched well between the test and analysis, with a discrepancy less than 10%. The drift at yielding was 0.95% in the 350 test and 1.15% in the analysis. The strength at the yielding of the bending plates was 16.0 kN 351 352 in the test and 17.0 kN in the analysis. The maximum strength at a 3% beam-column rotation was 23.4 kN in the test and 23.3 kN in the analysis. As intended in the design, the two 353 bending plates connected by the rigid middle-connection block deformed together, i.e., when 354 one went towards the column, the other moved away from the column (Figure 9). Thus, the 355 tension rods only sustained tension forces (Figure 8(b)) and no contraction or buckling was 356 observed as a result of the innovative geometric configuration. The maximum force in the 357 358 tension rods was 102 kN, sufficiently below their yielding strength. However, a pinching behavior, defined as the shift of beam-column rotation over 0.1% near the zero force in the 359 hysteresis loop, became obvious at the second cycle of 1.5% drift. The shift of beam-column 360 rotation due to the pinching was 0.15% in this cycle. This was caused by the vertical slippage 361 of the bending plates against the surface of the column. When the bending plates slipped, the 362 distance between the two ends of the tension-rod was shortened, generating the pinching seen 363 in the relationship between the force and beam-column rotation. This phenomenon was also 364 seen in Figure 8(b) as gaps in the deformation at the transition of force from one tension-rod 365 to the other. The slipping of the bending plates was caused by uneven contact between the 366 spacers and the column because of the shape of the box-column section where the mid-367 surfaces were slightly recessed at the corners. This caused the friction force at the spacer-368 column interface to be lower than anticipated. Measures to overcome such slippage through 369 enhanced friction force were later developed. 370

The horizontal dotted line in the figure corresponds to the design strength of the basic model. The design strength was defined as the yielding of the full plate section and computed using the following equation:

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$$Q_y = \frac{4b_p t_p^2}{l_p} \sigma_{yp} \times \frac{d}{L_c} \tag{1}$$

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376 Q_{y} indicates the force at the bottom of the column at the yielding strength of the plates, b_{p} the width of the plates, t_p thickness of the plates, l_p vertical length of the plates, σ_{vp} yielding 377 stress of the plates, d the distance between the beam-column connection and the bending 378 plates, and L_c the length of the column. The ultimate strength of the MDAD Q_u is 379 approximately $1.5Q_y$ for plate bending. For instance, the maximum strength of the baseline 380 specimen calculated as Eq. 1 multiplied by 1.5 was about 23 kN, which was consistent with 381 the test results. Note that the proposed equation is not applicable to the MDAD with LYP 382 plates of large strain hardening. 383

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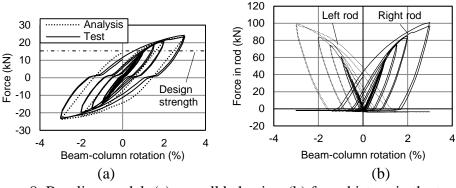
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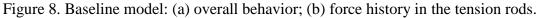
385 5.2 Alternate configurations

The hysteresis behavior of Specimens 2–6 are shown in Figure 10. Lateral forces in the plots for Specimens 1–4 are normalized according to their design strength computed using Eq. 1. In Specimen 2, the two plates were connected by the flexible bars at their middle. The elongation of the middle-connecting bar was 10 times greater than that in Specimen 1 where the plates were connected by the stiff blocks. The deformation of each plate was allowed to be independent, which caused considerable pinching behavior as seen in Figure 10(a). This result implies that the middle-connecting block must be designed to be sufficiently rigid.

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In Specimen 3, the bending plates were located farther from the beam-column joint node; the





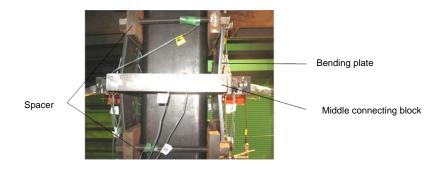


Figure 9. Deformed shape of the bending plates in the baseline model.

distance was increased from 400 mm to 600 mm. Because of the larger inclined angle of the 396 tension-rods, the force in the tension-rods increased by 1.5 times from the baseline specimen 397 when compared at the same beam-column rotation. Accordingly, the beam-column rotation at 398 the yielding of the bending plates became less than that in the baseline specimen 399 (Figure 10(b)). Moreover, as the point of the rod force moved farther from the beam-column 400 401 joint node, the initial stiffness and the yield strength increased by 1.5 times and 2.2 times from the baseline specimen. However, this configuration increased the disturbance to the 402 403 occupied building area and the pinching behavior increased because of greater slippage 404 caused by increased vertical forces at the column interface.

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406 In Specimen 4, a force 1.6 times that of the baseline model was applied to the post-tension rods that fixed the plates to the column (Figure 10(c)). At 1.5% beam-column rotation, quite 407 408 small vertical slippage was observed but no pinching behavior appeared in the hysteresis loop until 3%. At 3%, the vertical slippage reached 2 mm and the pinching behavior at 0.15% was 409 seen in the hysteresis loop. According to this result, it was revealed that the vertical slippage 410 411 within 2 mm did not affect the overall behavior. It was also found that the pinching behavior in the hysteresis loop in Specimens 1 and 3 was caused by this vertical slippage, which 412 reached 5 mm in these specimens. 413

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In Specimen 5, low yielding steel was used for the bending plates instead of conventional steel (Figure 10(d)). The plates yielded at 0.12% beam-column rotation. The hysteresis curve showed the stable energy-dissipation capacity with isotropic strain hardening. However, the maximum strength was much less than the baseline specimen because the dimensions of the plates were the same.

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In Specimen 6, low-yielding point and high strength steel plates were combined. They were designed to have equal initial stiffness to the baseline specimen (Figure 10(e)). The lowyielding-point steel plates yielded in beam-column rotations as small as 0.17%, meaning that energy dissipation was initiated earlier as in Specimen 5. However, the high strength steel plates remained elastic until 1.5%, so the maximum strength was higher than Specimen 5 and relatively high secondary stiffness was achieved.

- 428 Figure 10(f) shows the energy dissipation capacity calculated according to the definition of the equivalent viscous damping coefficient, h_{eq} [Chopra, 2001]. In Specimen 1, h_{eq} was small 429 in the earlier stages of loading but increased gradually after 1% beam-column rotation when 430 the plates yielded. In Specimen 2, which showed the pinching behavior, h_{eq} was relatively 431 small at 0.1 even in large beam-column rotation such as 2% to 3%. In Specimen 5, the low 432 yielding steel started to dissipate energy from 0.12%; consequently, h_{eq} was four times greater 433 compared with the baseline specimen at 1% drift, and finally achieved 0.3. Also in 434 Specimen 6, the low yielding steel resulted in larger h_{eq} , but not as large as Specimen 5 435 because of the reduced dimension of the low-yielding-point steel plates in Specimen 6 436 compared with Specimen 5. 437
- 438

439 The initial stiffness, yielding strength and maximum strength for the component tests are 440 summarized in Table 3. The results of numerical simulation by FE analysis and the calculated 441 design strengths are also shown in the table. In the test results, yielding strength was defined 442 as the point where the stiffness started to decrease significantly.

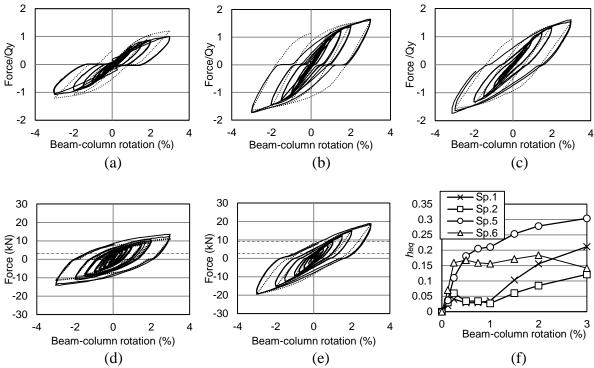


Figure 10. Component tests: (a) Specimen 2; (b) Specimen 3; (c) Specimen 4; (d) Specimen 5; (e) Specimen 6; (f) energy dissipation capacity.

	$k [\times 10^2 \text{ kN/rad}]$		Q_y [kN]			Q_u [kN]		
Sp.	. Initial stiffness		Yielding strength			Maximum strength		
	FE analysis	Test	Design	FE analysis	Test	Design	FE analysis	Test
1	14.8	16.8	15.3	17.0	16.0	23.0	23.3	23.4
2	11.3	10.6	15.3	12.0	10.5	23.0	18.4	15.1
3	30.8	28.0	22.9	24.0	24.5	34.4	36.9	38.0
4	11.7	14.1	15.3	17.0	16.0	23.0	23.3	24.6
5	14.8	14.2	3.2	2.5	3.0	4.8	11.5	13.4
6	14.1	13.0	2.7	3.5	3.5	4.1	18.7	18.9

Table 3. Component tests

444 5.3 Application to Beam-Column Connection Assemblage

445

446 In the application test, the MDAD, which had the same dimensions and material properties as Specimen 1 in the component test, was installed in a beam-column connection. Although in 447 the real application this system was attached below the beams, in the test the specimen was 448 placed upside down for easier installation. Figure 11(a) shows the overall behavior of the 449 rehabilitated frame, and Figure 11(b) shows the comparison between the bare and 450 rehabilitated frames. The lower horizontal line in Figure 11(b) corresponds to the design force 451 when the bending moment at the beam ends of bare frame reaches the plastic moment (F_p) 452 and the upper line corresponds to F_p plus the yield strength of the MDAD calculated by Eq. 1. 453 The results of the test showed that: (1) the MDAD behaved as expected during the 454 deformation of the beam and column; and (2) the initial stiffness and strength at 4% drift 455 456 increased by 26.1% and 27.4% compared with the non-rehabilitated beam-column connection.

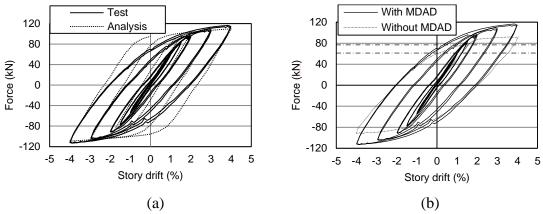


Figure 11. Application test: (a) force-story drift plot; (b) with and without MDAD.

457 For reference information, attaching the MDAD at a half scale took only 1.5 hours with two458 workers, and all was implemented by hand without any welding.

- 459
- 460 461

6. FOUR-STORY STEEL MOMENT-RESISTING FRAME

462 *6.1. Description of the Bare Frame*

A case study of a four-story building designed in accordance with the requirements for 463 Japanese seismic design was used to investigate the overall effect of the MDAD on the 464 behavior of a frame. The building was a four- by two-bay frame structure (Figure 12(a)). The 465 steel was SS400 with a modulus of elasticity of 205,000 MPa and a yield strength of 235 MPa. 466 The dimensions of the beam and column are given in the figure. The floor mass taken by this 467 frame was 302,400 kg, and its fundamental period was 0.78 s. The base shear coefficient of 468 469 the elastic stage was 0.27. Considering the composite effect with the concrete floor slab, the moment of inertia of beams was increased by 1.8 times in positive bending where the concrete 470 slab sustained a compression force. 471

472

For the purpose of analysis, a model of the frame was built and analyzed in OpenSees 473 (Mazzoni, 2009). Concentrated plasticity was assumed for both the beam and column 474 elements, while shear deformations were ignored. The effect of the concrete slab on the 475 composite beam stiffness was determined by adopting an elastic fiber model along the span of 476 the beams while adopting a no tension material model for the concrete slabs. This led to a 477 moment of inertia in positive bending that was 1.8 times that of the bare steel beam. No 478 deterioration in the composite action is considered in the model. Zero length elements with an 479 effectively rigid-plastic moment rotation relationship were adopted to model the plastic hinge 480 behavior at the beam and column ends. The positive and negative yield moments of the 481 composite beam section were taken as 1.3 and 1.0 times the yield moment of the steel beam 482 section, respectively. The value of its post-yielding stiffness was computed such that a 483 secondary stiffness of 0.01 was achieved at the beam level. The chord rotation of composite 484 beams at fracture ranges from 0.02 rad to 0.036 rad according to the references [7]-[11]. In 485 this paper that the chord rotations at fracture were defined as 0.02 rad and 0.03 rad for 486 positive and negative bending, respectively. Accordingly, the plastic hinge rotations at 487 488 fracture, without elastic beam deflections, were set as 0.015 rad and 0.022 rad for positive and negative bending. 489

490

As shown in the next sections, the performance of the bare frame (without the addition of any
retrofit method) was not satisfactory. The main performance issue was excessive positive
plastic hinge rotations, and thus, application of the MDAD was deemed appropriate. The next

494 section describes the MDAD allocation layout and properties. Section 6.3 will then present
495 the pushover curves of the bare and retrofitted frames while Section 6.4 presents their
496 behavior in nonlinear time history analysis under a suite of ground motions.

- 497498 6.2. Damper Allocation Layout and Properties
- 499

During pushover analysis of the bare frame, the first two stories exhibited large positive 500 plastic rotations compared with the top stories (not shown). Therefore, the retrofitting scheme 501 employed MDADs with similar properties in the first two stories (see Figure 12(b)). The 502 MDADs are also installed on exterior columns with the intention of reducing the positive 503 bending moments at the beam ends. The MDADs applied to the exterior columns have a 504 typical ratcheting behavior rather than a hysteretic behavior, characterized by stable "fat" 505 506 loops. Nonetheless, the forces they produce at a maximum drift assist in reducing the positive bending moments and delay yielding and fracture. 507

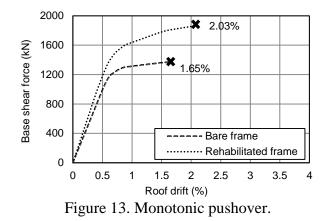
508

509 The MDADs were designed to yield at a force of 330 kN and a drift of 0.36%. The force was 510 designed as MDADs reduced the positive bending moment at the beam end to 60% or the 511 original value examined at the yielding drift of the bare frame. The stiffness of MDADs was

adjusted to achieve 35% earlier yielding of the bending plates compared with the beam ends

Z, 1st-story and 2nd-story: 3rd-story and 4th-story: Beam : H section-450*200*8*12 Beam : H section-400*200*7*11 Column: Box section-350*350*16 Column: Box section-350*350*12 Beam-column strength ratio: 1.81 Beam-column strength ratio: 1.79 Unit: mm 3300 Tension 3300 rod 0.018 0.016 0.016 0.009 0.009 0.016 3300 0.011 0.009 0.020 0.018 0.018 0.018 0.010 0.010 3300 0.011 0.010 ~ 20 Spring assuming 6000 6000 6000 6000 bending plates (a) (b) 30 20 **Rigid elements** Force (kN) 10 Beam 0 Column -10 Tension only -20 Test elements Zerolength elements Rigid link -- OpenSees -30 -4 -3 -2 -1 0 1 2 3 4 Beam-column rotation (%) (c) (d)

Figure 12. Building and MDAD model used in OpenSees analysis: (a) front view of four-story bare frame; (b) location of MDADs; (c) details of MDAD model; (d) comparison between OpenSees MDAD model and test result.



of the existing frame. This was attained using plate dimensions 360 mm long, 350 mm wide and 20.6 mm thick with SS400 grade steel. The secondary stiffness slope ratio of the plates' assembly was assumed to be 0.3, as observed in the experiments (see Section 5.1.1). The cross section area of the tension rods was 3847 mm² with SS400 grade steel.

518 The modeling of the MDAD is presented in Figure 12(c). It used zero length spring elements with a nonlinear material behavior (steel01 in OpenSees) to model the plate's behavior, and 519 truss elements with tension only behavior for the rods (a combination of ENT material with 520 521 negative stiffness and an elastic material with positive stiffness in OpenSees). The end joints of the two truss elements used to model the plates were connected with rigid links to ensure 522 the same horizontal displacements, in effect modeling the middle connecting block. Rigid 523 elements were used to account for the eccentricity between the connections of the rods and the 524 centerline of the beam. The hysteresis from the OpenSees MDAD model and experimental 525 results (baseline specimen) are compared in Fig. 12(d). The results compare component level 526 behavior without including the flexibility of other components such as beams and columns. 527 The initial stiffness and yielding strength of two hysteresis matched very well. 528

529

530 6.3. Monotonic Pushover

531

532 The models of the bare and retrofitted frames were first evaluated using pushover analysis, with an inverted triangle lateral load distribution. Figure 12(a) and (b) show the beam plastic 533 rotations at the left end in radians when the roof drift was 2%. The MDADs effectively 534 reduced the local deformation by 45%. Figure 13 shows the pushover curves attained. The 535 analyses were run until any of the plastic hinges first reached its fracture plastic rotation (i.e., 536 pre-defined as 0.015rad or 0.022 rad in the positive or the negative directions). In the bare 537 frame, pushover analysis ended at 2.03% when the plastic rotation at the most left beam end 538 in the second floor reached 0.015 rad. In the rehabilitated frame, pushover analysis ended at 539 540 2.40% when the plastic rotation at the most left beam end in the fourth floor reached 0.015 rad. By incorporating the MDAD, the stiffness and the strength of the frame yielding first 541 increased by 22% and 43%, respectively. This is expected to reduce the displacement 542 543 demanded under earthquakes. Furthermore, the displacement capacity of the frame increased by 23%. This is a very important contribution as many other retrofitting schemes concentrate 544 only on reducing displacement demands. The results also showed that additional stresses 545 induced from the MDAD would not cause undesirable damage modes to the column or beam. 546 The effects of the MDAD significantly enhance structural performance, as will be seen from 547 the nonlinear time history analysis results in the following section. 548

550 6.4. Time History Analysis

551

Nonlinear time history analysis was conducted using the LA 10% in an assembly of 50 years 552 of ground motions from the SAC Project [Somerville et al., 1997]. For the dynamic analysis, 553 a Rayleigh damping matrix with 2% damping in the first and second modes was assumed. 554 555 Table 4 presents the mean plus one standard deviation of important peak responses, including the peak roof drift (roof displacement normalized by the height of the frame), the peak first 556 story drift, the peak first and second story drifts (inter-story drifts normalized by the 557 corresponding height), and the maximum positive and negative plastic rotations over all beam 558 plastic hinges. 559

560

Table 4 shows the 84th percentile response quantities under LA10-50 motions for both the 561 bare and rehabilitated frames. As can be seen in Table 4, the bare frame experienced positive 562 plastic rotations as high as 0.022 rad, which was larger than the predefined plastic rotation at 563 fracture of 0.015 rad. This indicates a need for retrofitting. Implementation of the MDAD 564 reduced these rotations by up to 43%. The addition of the MDAD did not affect drifts as 565 dramatically; however, they decreased on the order of 10%. Thus, the effectiveness of the 566 MDAD is a function of both factors: the increase in strength and stiffness at the structure and 567 568 story levels, which leads to smaller inter-story drifts, and the reduction in positive plastic rotations even for the same inter-story drift. While the contribution of each factor separately 569 may not be very large, these contributions combine to a considerable improvement in the 570 571 integrity of the structure. It should also be noted that the negative plastic rotations did not increase, and even decreased somewhat, as a result of using the MDAD. The demand 572 increases in the 1st story columns in terms of forces and bending moments by the attachment 573 574 of the MDADs are summarized in Table 5 using the 84th percentile responses. The increases in base shear were 29%, which were judged as sufficiently small. The bending moment of the 575 1st story columns became twice at the location of the MDADs while the top of columns 576 sustained similar bending moments. The columns remained elastic at these locations thanks to 577 578 an existing reserved strength. The bottom of columns yielded for the both cases and sustained similar bending moments. 579

580

Figure 14 presents the roof drift and plastic hinge rotation (the left end I_1 of the leftmost beam in the first story, as shown in Figure 12(b)) as a function of time for the bare and retrofitted frames as a response to the LA15 ground motion. With the MDAD, the plastic hinge rotations and global plastic deformations of the frame were efficiently reduced, and fracture at the beam ends was avoided. Furthermore, the residual roof drift was considerable reduced. This is very important because large residual deformations may prevent the ability to restore the structure to its original position after a seismic event, increasing the likelihood of demolition.

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590

7. CONCLUSIONS

This paper presents a seismic rehabilitation technique developed under the scheme of 591 minimal-disturbance seismic rehabilitation, which allows the continuous usage of buildings, 592 593 keeps existing openings and sightlines, and results in minimal increases in force demand to the original framing. To rehabilitate the bottom flanges near the beam-column connections 594 with minimal disturbance, a rehabilitation technique that connected the mid-span of the beam 595 596 and the upper part of the column with two tension-only rods and energy dissipating steel 597 plates, was developed; the rod-plate connector was termed a minimal-disturbance arm damper (MDAD). The MDAD only uses light steel elements and bolted connections to enable 598 599 continuity of business during rehabilitation. All elements were placed above three quarters of

	Peak roof drift [%]	Peak 1 st story drift [%]	Peak 1 st + 2 nd story drift [%]	Peak hinge positive plastic rot [rad]	Peak hinge negative plastic rot [rad]
Bare frame	1.99	2.53	2.58	0.021	-0.022
Rehabilitated	1.84	2.20	2.12	0.012	-0.020

Table 4. Eighty-fourth percentile response quantities under LA10-50 motions.

Table 5. Force demands in first story columns (84th percentile values).

	Base shear [kN]	Column moment at MDAD in first story [kN·m]	Column bottom moment in first story [kN·m]
Bare frame	1.60×10^{3}	220.1	658.2
Rehabilitated frame	2.07×10^{3}	457.7	657.3

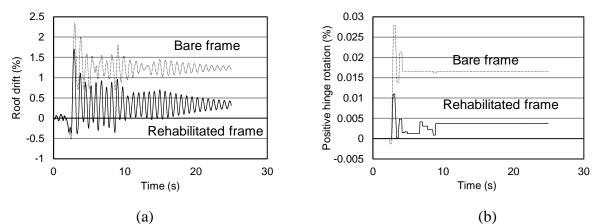


Figure 14. Time history analysis with and without damper for LA15: (a) roof drift versus time; (b) positive hinge rotation versus time at first story.

the story height to minimize the disturbance to the walking access and sightlines of users ofthe building.

602

A baseline model was designed to rehabilitate a beam-column connection in low- to mid-rise steel moment-resisting frames. FE analysis was used to verify the basic load-resisting and energy-dissipating mechanisms intended in the design. The FE analysis was verified with half scale component tests of the MDAD, followed by tests of a full joint connection. After model verification, the response of a four-story building with and without the MDAD was investigated. The major findings are summarized as follows:

609

(1) In the component level tests, the baseline specimen successfully presented bilinear 610 restoring force characteristics. It was found that the flexibility of connecting blocks 611 induced severe pinching behavior in the force-drift relationship, and this should be 612 avoided in the design. When low yield point steel was used for the energy dissipating 613 bending plates, the system had four times greater energy dissipation than the baseline 614 specimen with conventional steel at 1% drift. Both the initial stiffness and strength of the 615 rehabilitation system increased when the plates were located farther from the beam-616 column connection. 617

- (2) When applied to rehabilitate a steel beam-column connection of low-rise steel frames,
 the rehabilitation technique increased the initial stiffness and the maximum strength by
 25% and 32%, respectively. The bending plates in the energy dissipater yielded at 1.0%
 prior to beam yielding at 1.5%.
- (3) The full building analysis verified that the effectiveness of the MDAD results from two 622 623 major factors: the increase in strength and stiffness at the structure and story levels, which leads to smaller inter-story drifts, and the reduction in positive plastic rotations 624 even at the same inter-story drift. It was shown that while the contribution of each factor 625 separately may not be very great, these contributions sum up to a considerable 626 improvement in the integrity of the structure. The 84th percentile maximum peak plastic 627 rotation, under the excitation with a set of ground motions selected from the LA 10% in 628 50 years ensemble, reduced by 43%. 629
- (4) For future study, a generalized design procedure will be developed to use MDAD in
 rehabilitating steel moment-resisting frames with an explicit consideration to reduce
 positive plastic rotation at the beam ends. Furthermore, it is desirable to develop more
 effective connecting methods for the attachment of bending plates to the column surface
 and tension-rod clevises to the beam mid-span.

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