





Long-term Evolution of Nonthermal Emission from Type Ia and Core-collapse Supernova Remnants in a Diversified Circumstellar Medium

Ryosuke Kobashi¹, Haruo Yasuda¹ , and Shiu-Hang Lee^{1,2} ¹ Department of Astronomy, Kyoto University, Kitashirakawa, Oiwake-cho, Sakyo-ku, Kyoto 606-8502, Japan; kobashi@kustastro.kyoto-u.ac.jp² Kavli Institute for the Physics and Mathematics of the Universe (WPI), The University of Tokyo, Kashiwa 277-8583, Japan

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Abstract

The contribution of galactic supernova remnants (SNRs) to the origin of cosmic rays (CRs) is an important open question in modern astrophysics. Broadband nonthermal emission is a useful proxy for probing the energy budget and production history of CRs in SNRs. We conduct hydrodynamic simulations to model the long-term SNR evolution from explosion all the way to the radiative phase (or 3×10^5 yr at maximum) and compute the time evolution of the broadband nonthermal spectrum to explore its potential applications on constraining the surrounding environments, as well as the natures and mass-loss histories, of the SNR progenitors. A parametric survey is performed on the ambient environments separated into two main groups, namely, a homogeneous medium with a uniform gas density and one with the presence of a circumstellar structure created by the stellar wind of a massive red supergiant progenitor star. Our results reveal a highly diverse evolution history of the nonthermal emission closely correlated to the environmental characteristics of an SNR. Up to the radiative phase, the roles of CR reacceleration and ion–neutral wave damping on the spectral evolution are investigated. Finally, we make an assessment of the future prospect of SNR observations by the next-generation hard X-ray space observatory FORCE and predict what we can learn from their comparison with our evolution models.

Unified Astronomy Thesaurus concepts: Galactic cosmic rays (567); Non-thermal radiation sources (1119); Circumstellar matter (241); Interstellar medium (847); Supernova remnants (1667)

1. Introduction

Supernova remnants (SNRs) are believed to be an important source of cosmic rays (CRs) in our and other galaxies (e.g., Blandford & Eichler 1987; Ellison & Cassam-Chenaï 2005). To quantify the contribution of SNRs to the production of Galactic CRs, it is necessary to follow the production history of CRs in an SNR throughout its lifetime. Observationally, nonthermal emission across a wide energy range covering the radio, X-rays, and gamma-rays is a powerful tool for the inference of CR production in an SNR. The diverse interstellar medium (ISM) and circumstellar medium (CSM) surrounding the SNRs are known to be one of the most important determining factors for the CR acceleration history and hence the resulting time evolution of the nonthermal emission (e.g., Yasuda et al. 2021, 2022). Comparisons of hydrodynamic models with observational data have been performed for individual SNRs to estimate their CR energy budgets (e.g., Lee et al. 2013; Slane et al. 2014). However, systematic parametric surveys taking into account the rich diversity of the ambient environments and progenitors of various types of SNRs are still lacking.

The CR acceleration efficiency and thus the total amount of CR produced in an SNR strongly depend on the ambient environment, age, and the progenitor system. Therefore, it is important to quantify the effects of environmental parameters such as the ambient gas density and magnetic field profiles using a self-consistent numerical setup. Indeed, according to Yasuda & Lee (2019, hereafter YL19), who performed such a

task up to an SNR age of 5000 yr, a rich variety of nonthermal emission evolution has been found under different parameters for the surrounding environments. Another aspect to be explored is the ability of nonthermal emission observations to constrain the CSM structure and hence the pre-SN mass-loss activities of SN progenitors.

In this study, we extend the work by YL19 to follow the evolution from explosion all the way to an age of a few $\times 10^4$ yr to 3×10^5 yr, as well as the implementation of more realistic CSM environments for a red supergiant (RSG) star by performing a hydrodynamic simulation for the pre-SN wind–ISM interaction. We simulate the shock hydrodynamics and CR acceleration simultaneously until the forward shocks have weakened enough to stop accelerating CRs efficiently up to an age of \sim a few or tens of 10^4 yr depending on the ejecta/CSM model. The resulting grid of SNR/CSM models will provide a broader vision on the long-term evolution of nonthermal emissions from SNRs interacting with different kinds of environments.

One of the novel aspects introduced in this paper is the self-consistent inclusion of the radiative phase of an SNR inside our CR-hydrodynamic simulation framework (a similar approach has been adopted in several previous studies, e.g., Lee et al. 2015; Brose et al. 2020, 2021). Radio and gamma-ray-bright middle-aged SNRs such as W44 and IC 443 (e.g., Ackermann et al. 2013) are usually found to possess radiative shocks. Their bright radio synchrotron emission and GeV gamma-rays from π^0 -decay are suggested to originate from a rapid compression of gas, CRs, and magnetic field in the cold dense shell formed behind the radiative shocks (e.g., Lee et al. 2015). In the radiative phase, it has been suggested that reacceleration of preexisting CRs (e.g., Uchiyama et al. 2010) and the effects of ion–neutral damping of CR-trapping magnetic waves (e.g., Malkov et al. 2011; Bykov et al. 2013) are important to account



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for the observed spectral properties in evolved SNRs. Some numerical studies have taken into account the effects of reacceleration and wave damping at shocks propagating in dense environments such as molecular clouds and becoming radiative so that the CR acceleration efficiency is no longer high (e.g., Lee et al. 2015; Cardillo 2019). An alternative interpretation using a CR escape model (e.g., Gabici et al. 2009; Ohira et al. 2010) has also been proposed, which can explain such characteristic spectra from evolved SNRs by a rapid decrease of the maximum proton energy with age (Celli et al. 2019; Brose et al. 2020). Lee et al. (2015) calculated the hydrodynamics of a fast cloud shock driven into a dense cloud by an SNR and the accompanying nonthermal emission. Likewise, Cardillo (2019) performed a similar calculation but used an analytic approach for the hydrodynamics. Both works did not survey over different SN progenitors or CSM models. They also did not consider the SNR evolution and particle acceleration in the free-expansion and Sedov phase before the shock–cloud interaction begins, which can have a nonnegligible contribution to the nonthermal emission even at old ages. A few other previous theoretical studies have also investigated the evolution of CR energetics as a function of SNR age (e.g., Lee et al. 2012), but these works primarily focused on the younger remnants without any discussion on the later evolution stages. Our study addresses these points using a coherent hydrodynamic simulation to connect the young ones to the old ones. In addition, from the viewpoint of better understanding the connection between the nonthermal emission properties of young and evolved SNRs, it is important to understand the role of reacceleration of preexisting CRs as a function of age under different ambient environment settings. In this study, using our grid of SNR/CSM models from explosion up to the radiative phase, we quantify the importance of CR reacceleration in terms of the total CR energy budget throughout the lifetime of an SNR.

In the last part of the paper, we assess the future prospect of Focusing On Relativistic universe and Cosmic Evolution (FORCE, https://www.cc.miyazaki-u.ac.jp/force/wp-content/uploads/force_proposal.pdf), a next-generation hard X-ray imaging observatory, on constraining particle acceleration parameters using our grid of SNR/CSM models. When it comes to X-rays, observations of various SNRs have been done in the soft X-ray bands using instruments on board satellites such as Chandra, Suzaku, and XMM-Newton, for which there is often much contamination from the thermal emission when one tries to separate out the nonthermal component. For the study of CR (electron) acceleration, hard X-ray data at >10 keV with good statistics are highly desirable. Such observations have been performed for a few examples using the NuSTAR observatory with an arcminute-scale spatial resolution that is close to the angular size of many young SNRs. The power-law index of CR electrons can be constrained from the high-energy edge of the synchrotron tail for some SNRs, e.g., RX J1713.7–3946 (Tsuji et al. 2019) and Tycho’s SNR (Lopez et al. 2015), allowing one to constrain the acceleration efficiency of electrons and magnetic field strengths, as well as the nonthermal bremsstrahlung emission from some SNRs interacting with dense clouds, e.g., W49B (Tanaka et al. 2018) and IC 443 (Zhang et al. 2018), providing information on the subrelativistic accelerated particles and hence the poorly understood electron injection process. Here we expect future observations using the FORCE satellite, which is planned to launch in the later half of the 2020s and will observe SNRs with

a high sensitivity in the 10–40 keV band. With an angular resolution $<15''$, which is $\gtrsim 4$ times better than NuSTAR, FORCE will enable us to realize spatially resolved spectroscopic observations of SNRs in the crucial hard X-ray window.

This paper is structured as follows. In Section 2 we first explain our numerical methods, which enable us to calculate SNR evolution until a few or tens of 10^4 yr, and then introduce our models for the surrounding environments in this paper, i.e., models with a uniform ambient medium and those with a CSM created by the pre-SN stellar wind. In Sections 3.1 and 3.2, we present our results from both classes of models sequentially and discuss their various implications. Section 3.3 is dedicated to the analyses of a few physical effects especially relevant to the nonthermal emission in the radiative phase, followed by a brief discussion on the future prospect of FORCE in hard X-ray studies of young and old SNRs in Section 3.4. Section 4 provides a summary of our results and concluding remarks.

2. Methods

2.1. Included Physics

We use the CR-Hydro code developed by YL19 with adaptations to fit the purposes of this work. The CR-Hydro code performs 1D spherically symmetric hydro simulations on a Lagrangian grid VH-1 (e.g., Blondin & Ellison 2001) coupled with a semianalytic nonlinear diffusive shock acceleration (NLDSA) calculation (e.g., Blasi 2004; Caprioli et al. 2010a, 2010b) similar to the framework introduced in, e.g., Lee et al. (2012). To account for the feedback of the accelerated particles and magnetic fields on the hydrodynamics, the code uses an effective ratio of specific heats γ_{eff} that is updated in real time at each Lagrangian cell as follows (Blondin & Ellison 2001):

$$\frac{\gamma_{\text{eff}}}{\gamma_{\text{eff}} - 1} P_{\text{tot}} = \frac{\gamma_g}{\gamma_g - 1} P_g + \frac{\gamma_{\text{CR}}}{\gamma_{\text{CR}} - 1} P_{\text{CR}} + \frac{\gamma_B}{\gamma_B - 1} P_B, \quad (1)$$

where $\gamma_g = 5/3$, $\gamma_{\text{CR}} = 4/3$, and $\gamma_B = 2$ are the ratios of specific heats for ideal gas, CR, and magnetic field, respectively; $P_{\text{tot}} = P_g + P_{\text{CR}} + P_B$ is the total pressure; and P_g , P_{CR} , and P_B are gas, CR, and magnetic pressures, respectively.

For radiative cooling, we adopt the nonequilibrium (NEQ) cooling function from Sutherland & Dopita (1993) coupled to the exact time integration method of Townsend (2009). In accordance with Blondin et al. (1998), we introduce the timescale t_{tr} for the transition to the radiative phase,³ which will be used as a basic time unit for our results throughout the paper, i.e.,

$$t_{\text{tr}} \approx 2.9 \times 10^4 (E_{\text{SN}}/1.0 \times 10^{51} \text{ erg})^{4/17} n_0^{-9/17} \text{ yr}, \quad (2)$$

where E_{SN} is the SN explosion energy and n_0 is the number density of the ambient gas in cm^{-3} .

To obtain the phase-space distribution function of the accelerated protons $f(x, p)$, we solve the diffusion–convection equation in the shock rest frame (e.g., Blasi 2004; Caprioli et al. 2010a, 2010b; Lee et al. 2012). From the formulation of the solution $f(x, p)$ (Lee et al. 2012, Equation (13)), we can decompose it into two components depending on the type of

³ By “radiative phase” we refer to the age when the post-shock radiative cooling effect becomes important on the shock dynamics. It is duly noted that this is different from the conventional definition of the radiative phase, which is when $R_{\text{sk}} \sim r^{2/7}$ holds after the shock oscillation has subsided, as in Petruk et al. (2021).

seed particles being accelerated from:

$$f(x, p) \propto \left[\frac{\eta m_0}{4\pi p_{\text{inj}}^3} \exp\left(-\int_{p_{\text{inj}}}^p \frac{dp'}{p'} \frac{3S_{\text{tot}}U(p')}{S_{\text{tot}}U(p')-1}\right) \right] + \int_{p_{\text{inj}}}^p \frac{dp''}{p''} f_{\text{pre},p}(p'') \left[\exp\left(-\int_{p''}^p \frac{dp'}{p'} \frac{3S_{\text{tot}}U(p')}{S_{\text{tot}}U(p')-1}\right) \right], \quad (3)$$

where S_{tot} is the effective total compression ratio of the shock, $U(p)$ is the dimensionless gas flow velocity, and $f_{\text{pre},p}$ is the distribution function of any preexisting CR protons. Using the parameterization for the injection efficiency in the language of the so-called ‘‘thermal leakage’’ model, the fraction of downstream thermal particles being injected into the DSA process is $\eta = \{4/(3\sqrt{\pi})\}(S_{\text{sub}} - 1)\chi_{\text{inj}}^3 e^{-\chi_{\text{inj}}^2}$ with $S_{\text{tot}} = (u_0 - v_{A,0})/(u_2 + v_{A,2})$, $S_{\text{sub}} = (u_1 - v_{A,1})/(u_2 + v_{A,2})$ based on the so-called ‘‘Alfvénic drift’’ model (see Section 3.5 for a discussion on a few caveats along this line), where u_i is the gas velocity and $v_{A,i}$ is the Alfvén speed, for which the subscript i indicates values far upstream (0), immediately upstream (1), and immediately downstream (2) of the shock, respectively. The dimensionless quantity $\chi_{\text{inj}} = 3.8$ is chosen to reflect the typical values inferred from emission modeling of a few young SNRs (Lee et al. 2012, 2013; Slane et al. 2014).⁴ To obtain the electron distribution function, we assume an electron-to-proton number ratio at relativistic energies $K_{\text{ep}} = 10^{-2}$ (see model B in YL19). We calculate the maximum energy of the accelerated particles as the minimum of the age-limited, loss-limited (mainly for electrons), and escape-limited maximum energies at each time epoch. The same approach has been adopted in, e.g., Lee et al. (2012), Slane et al. (2014), Yasuda & Lee (2019), and Yasuda et al. (2021, 2022).

It has been suggested that reacceleration of preexisting CRs plays a pivotal role in the production of nonthermal emission in older SNRs (Uchiyama et al. 2010; Lee et al. 2015). We will further elaborate in Section 3.3.1 on the mechanism in detail. Following Uchiyama et al. (2010) and Lee et al. (2015), we assume that such preexisting CRs have phase-space distributions $f_{\text{pre},p/e}$ of the Galactic CR protons and electrons+positrons,

$$4\pi p^2 f_{\text{pre},p} = 4\pi J_p \beta^{1.5} p_0^{-2.76} \\ 4\pi p^2 f_{\text{pre},e} = 4\pi J_e p_0^{-2} (1 + p_0^2)^{-0.55}, \quad (4)$$

where $J_p = 1.9 \text{ cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1} \text{ GeV}^{-1}$, $J_e = 0.02 \text{ cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1} \text{ GeV}^{-1}$, β is the proton velocity in units of c , and p_0 is the particle momentum in GeV/c . For simplicity, we assume equipartition with the magnetic pressure for the total number densities of the preexisting CRs (e.g., Boulares & Cox 1990; Cox 2005; Noutsos 2012), although the CR density and heavy ion abundance in the ISM can be enhanced in regions where a higher concentration of core-collapse (CC) SNRs has happened in the past, e.g., OB associations, superbubbles, and so on, which is beyond the scope of this work.

Ion–neutral damping effects are effective when the shock has decelerated to a point when photoionization of the pre-shock medium by the downstream emission becomes partial.

⁴ We note that the actual DSA injection mechanism at the shock is not necessarily a ‘‘thermal leakage’’ process, but we are using the parameterization scheme for numerical convenience.

The typical shock speed when this happens is $\sim 120 \text{ km s}^{-1}$, at which the post-shock temperature has decreased to a few $\times 10^5 \text{ K}$ (e.g., Hollenbach & McKee 1989). Depending on the upstream ionization degree x_{ion} , a spectral break in the accelerated CR spectrum occurs owing to the evanescence of the trapping magnetic waves and an enhancement of CR escape above the break momentum. We first calculate the pre-shock ionization fraction (Hollenbach & McKee 1989) at any given time, which is then used to calculate the local spatial diffusion coefficient and the break momentum in the same way as in Uchiyama et al. (2010), Malkov et al. (2011), and Lee et al. (2015). The momentum break is then applied to the phase-space distribution of the accelerated particles accordingly. The corresponding equations are

$$p_{\text{br}}/m_p c = 10B_{-6}^2 T_4^{-0.4} n^{-1.5}/(1 - x_{\text{ion}}^{0.5})x_{\text{ion}}^{-0.5}, \\ D(x, p) \propto \frac{vpc}{3eB(x)} \left(1 + \frac{p}{p_{\text{br}}}\right), \\ f(x, p > p_{\text{br}}) = f_0(x, p) \cdot (p_{\text{br}}/p). \quad (5)$$

Figure 12 illustrates a result with this feature (see Section 3.3.2 for details). The existence of such a momentum break has been suggested recently by gamma-ray observations of older SNRs such as W44 (Malkov et al. 2011).

The nonthermal emission components calculated in this study include inverse Compton (IC) scatterings, synchrotron radiation, nonthermal bremsstrahlung emission, and π^0 -decay (YL19, and references therein). We do not consider the contribution from secondary particles produced through π^\pm decays in this work, which can be important for very dense environments such as giant molecular clouds (see, e.g., Lee et al. 2015) but is beyond the scope of this paper. We also focus on the nonthermal emission from particle acceleration at the forward shock and ignore any possible contribution from the reverse shock.

2.2. Models for the Circumstellar Environments and SN Ejecta

We have prepared models in two categories, i.e., Group A (A1–A3) and Group B (B1–B5), for the circumstellar environments surrounding the SNR. The respective model parameters are summarized in Table 1. For the models in Group A, we assume a uniform ambient medium with a constant gas density. This density n_{ISM} is varied from 10^{-3} to 10 cm^{-3} . In Group B, we consider the structure created by the progenitor stellar wind with a constant mass-loss rate blowing into a uniform medium. A wind bubble/shell is formed around the ejecta surrounded by a uniform ISM-like gas. The CSM structure is obtained by hydrodynamic simulations using the VH-1 code (e.g., Blondin & Ellison 2001) with radiative loss taken into account (Sutherland & Dopita 1993). The pre-SN CSM density profiles are plotted in Figure 1. The density of the wind deviates from a pure power-law r^{-2} near the interface with the outer ISM whose structure depends on the mass-loss rate. While the ejecta (progenitor) mass and the pre-SN mass-loss history are related to each other from stellar evolution models, we fix the ejecta mass in this study within each group and vary the mass-loss rates $\dot{M} = 10^{-6} - 10^{-4} M_\odot \text{ yr}^{-1}$ to study the effect of the latter on the SNR evolution. In the free-expanding wind, $\rho(r) = \dot{M}/(4\pi r^2 v_w)$, with the wind velocity assumed to be $v_w = 20 \text{ km s}^{-1}$ for an RSG star. The density of the outer uniform medium is fixed at $n_{\text{ISM}} = 0.1 \text{ cm}^{-3}$. We

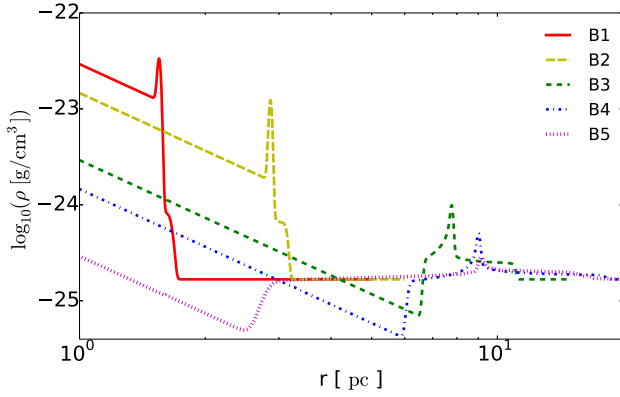


Figure 1. Radial density profiles of the ambient environments in the models of Group B. The red solid, yellow long-dashed, green dashed, blue dashed-dotted, and magenta dotted lines are associated with models B1, B2, B3, B4, and B5, of which the mass-loss rates of the progenitor are $\dot{M} = 10^{-4}$, 5.0×10^{-5} , 10^{-5} , 5.0×10^{-6} , $10^{-6} M_{\odot} \text{ yr}^{-1}$, respectively. The total mass loss is $8 M_{\odot}$ for each model, and the gas density in the outer region is fixed at $n_{\text{ISM}} = 0.1 \text{ cm}^{-3}$.

Table 1
Model Parameter

Model	M_{ej} (M_{\odot})	E_{SN} (10^{51} erg)	n_{ISM} (cm^{-3})	B_{ISM} (μG)	\dot{M} ($M_{\odot} \text{ yr}^{-1}$)	v_w (km s^{-1})
A1 ^a	1.4	1.18	10	10
A2	1.4	1.18	0.1	1.0
A3	1.4	1.18	10^{-3}	0.1
B1 ^b	12.2	1.21	0.1	1.0	1.0×10^{-4}	20
B2	12.2	1.21	0.1	1.0	5.0×10^{-5}	20
B3	12.2	1.21	0.1	1.0	1.0×10^{-5}	20
B4	12.2	1.21	0.1	1.0	5.0×10^{-6}	20
B5	12.2	1.21	0.1	1.0	1.0×10^{-6}	20

Notes.

^a All models in group A use an exponential profile for the ejecta, $T_0 = 10^4 \text{ K}$, $d_{\text{SNR}} = 1.0 \text{ kpc}$, and $\chi_{\text{inj}} = 3.8$.

^b All models in Group B use a power-law profile for the ejecta with $n_{\text{pl}} = 12$, $T_0 = 10^4 \text{ K}$, $\sigma_w = 0.01$, $d_{\text{SNR}} = 1.0 \text{ kpc}$, and $\chi_{\text{inj}} = 3.8$.

assume that the CSM is composed of an RSG wind and ignore any mass loss from the main-sequence (MS) and other possible mass-loss phases. We recognize that the MS stellar wind prior to the RSG phase can impose a large influence on the SNR evolution, which can alter the light curves/spectral evolution in a nonnegligible way, as shown by a number of previous works that investigated models taking into account the mass loss in the MS phase and their interactions with the subsequent RSG wind and in some cases (e.g., for a Type Ib/c progenitor) Wolf-Rayet wind and binary mass transfer as well (e.g., Yasuda et al. 2021, 2022; Das et al. 2022, and references therein). We are ignoring the MS wind bubble and for that matter episodic mass loss for simplicity here to focus on the systematic effect of \dot{M} on the long-term emission evolution and leave the discussion on the MS wind effect to a future work.

The initial magnetic field strength profiles are plotted in Figure 2. There are ‘‘jumps’’ in the magnetic field strength at the interface between the wind and the ISM in our models, which are also featured in Sushch et al. (2022). Stemming from this jump, we have confirmed a ‘‘double-bump’’ feature in the gamma-ray spectral energy distribution (SED; via IC and

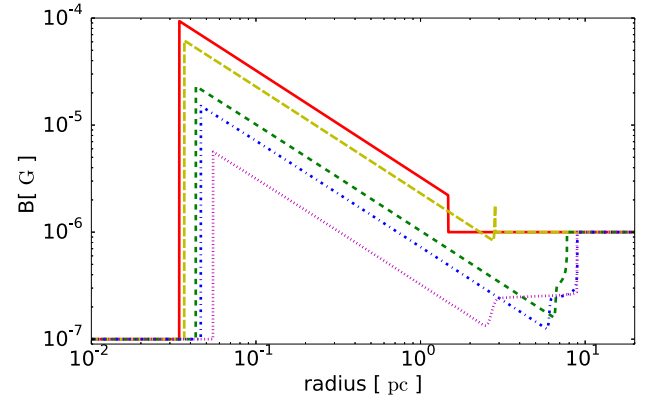


Figure 2. Radial profiles of the magnetic field strength in the ambient environments of the models in Group B. The line formats are the same as in Figure 1.

bremsstrahlung) when the shock propagates through the interface (see Section 3.2), which is also observed in Yasuda et al. (2021, 2022) and Sushch et al. (2022). The magnetic field strength in the wind is determined by the magnetization parameter $\sigma_w \equiv (B^2/8\pi)/(\rho v_w^2/2) = 10^{-2}$ (e.g., Lee et al. 2012, 2013). The magnetic field strength in the ISM-like ambient medium for models in both Groups A and B is, on the other hand, determined by a scaling proportional to $\sqrt{n_{\text{ISM}}}$ assuming magnetic flux freezing under isothermal conditions (e.g., Crutcher 1999; Uchiyama et al. 2010). For $n_{\text{ISM}} = 0.1 \text{ cm}^{-3}$ and $T_{\text{ISM}} = 10^4 \text{ K}$, we assume $B_{\text{ISM}} = 1 \mu\text{G}$.

We can further categorize the initial CSM profiles into two types: B1–B2 and B3–B5. Models B1 and B2 have relatively large mass-loss rates, which result in a dense wind shell whose spatial scale is mainly dictated by the mass-loss duration prior to explosion. Models B3–B5, on the other hand, form a wind ‘‘bubble’’ surrounded by a dense shell whose dynamics is determined by mechanical (pressure) balance instead. B5 in particular has a relatively small cavity-like structure owing to the low mass-loss rate and hence gas ram pressure. The total mass loss is fixed at $8 M_{\odot}$ for all models in Group B (see below). These differences in the CSM profiles will reflect strongly in the resulting light curves in the SNR phase.

We assume an ejecta with energetics typical of a Type Ia SN for Group A and an ejecta from the CC explosion of an RSG star for Group B. We use the *DDT12* model (Martínez-Rodríguez et al. 2018, and references therein) for the Type Ia ejecta, which is representative of a ‘‘normal’’ thermonuclear explosion of a near-Chandrasekhar-mass white dwarf star, i.e., $M_{\text{ej}} = 1.4 M_{\odot}$, $E_{\text{SN}} = 1.18 \times 10^{51} \text{ erg}$, with an exponential profile (Dwarkadas & Chevalier 1998). An RSG model *s25D* (Patnaude et al. 2015; Heger & Woosley 2010) is used for the CC SNRs in Group B with an original zero-age MS mass of $25 M_{\odot}$, for which $M_{\text{ej}} = 12.2 M_{\odot}$, $E_{\text{SN}} = 1.21 \times 10^{51} \text{ erg}$, with a power-law envelope model (Truelove & McKee 1999) whose index is $n_{\text{pl}} = 12$ (Matzner & McKee 1999) for the ejecta density profile. This model involves a total mass loss of $8 M_{\odot}$ through stellar wind prior to CC.

3. Results and Discussion

3.1. Models with a Uniform Medium

In this section, we first elaborate on the results from the models in Group A with a uniform ambient medium, which will also serve as a reference for the discussion of the models in

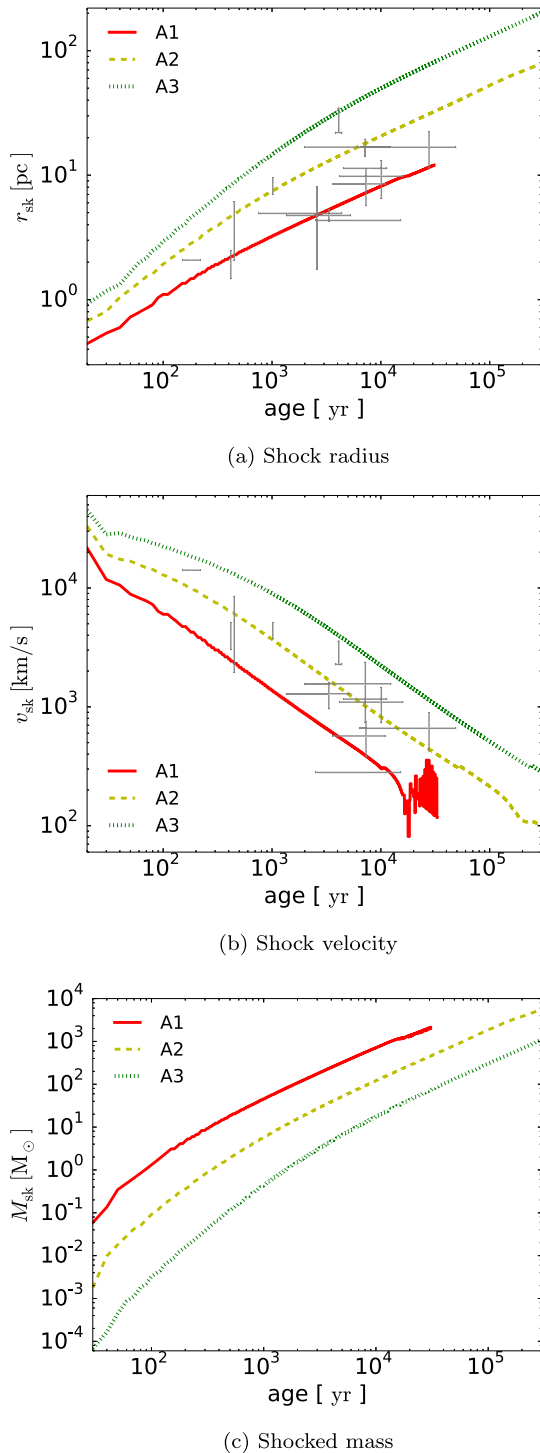


Figure 3. (a) Shock radius, (b) velocity, and (c) shocked gas mass as a function of age for Group A compared with the observation data of Type Ia SNRs shown by the data points. The red solid, yellow dashed, and green dotted lines show the model results for models A1, A2, and A3, of which the ISM densities are $n_{\text{ISM}} = 10$, 0.1, and $10^{-3} M_{\odot} \text{ yr}^{-1}$, respectively.

Group B in which more complicated CSM environments are involved. Figure 3 shows the time evolution of the shock radius r_{sk} , velocity v_{sk} , and shocked mass M_{sk} . With the same explosion energetics of a typical Type Ia SN for the three models, a lower-density ISM leads naturally to a larger remnant and a faster blast wave at any given age. A higher ISM density such as in model A1 also results in an earlier transition to the

radiative phase as the shock speed has decreased to $\sim 100 \text{ km s}^{-1}$. This can be witnessed from the oscillation of the shock speed after the transition commences, which comes from the interaction of the newly formed post-shock cold dense shell with the fast expanding gas in the interior (see, e.g., Lee et al. 2015) and is more prominent for a higher n_{ISM} , where the denser radiative shell formed behind the shock imposes a larger influence on the bulk hydrodynamic evolution. This oscillation, however, is known to be exaggerated by 1D treatments and is expected to be much milder in multidimensional simulations in which the spherical symmetry is broken (Petruk et al. 2021). For a sanity check, data points are compiled from measurements of known Type Ia SNRs for reference listed in Table 2, which show a general agreement with the range of results yielded by our models.

Figure 4 shows the broadband SED evolution for the nonthermal emission. We first confirm that the results before an age of 5000 yr are in broad agreement with those reported in YL19. For example, we see a similar dependence of the hadronic versus leptonic origin of the gamma-rays on the ISM density, as well as its variation with the SNR age. The subsequent SED evolution beyond the Sedov phase is first explored in this work. At $t = 3t_{\text{tr}}$, the remnants in models A1 and A2 have already entered the radiative phase. We can see a significant softening of the spectra across the entire frequency band. This can be attributed to the now-decelerated shock with a velocity $\sim 100\text{--}200 \text{ km s}^{-1}$, at which the velocity of the magnetic scattering centers in the upstream can no longer be neglected. Both the maximum attainable energy and the effective compression ratio felt by the accelerating CRs decrease, resulting in a soft CR spectrum. The spectral shapes of the synchrotron and IC components are remarkably different between A1 and A2 (i.e., a stronger radio and weaker IC contributions and a lower-energy cutoff in model A1), which can be explained by the higher averaged magnetic field strength in the shocked plasma in model A1 with a higher ISM density and hence a faster synchrotron loss for the electrons. The dense cold shell formed behind the shock in model A1 in the radiative phase also contributes to an amplification of the magnetic field and gas density due to the fast compression during the formation of the shell. The GeV emission from pion decay and the bremsstrahlung contribution in the hard X-ray and MeV energy range (whose luminosities are proportional to n_{ISM}^2) are also much more prominent in A1, resulting in an interesting distinction in spectral shape with model A2. Model A3, on the other hand, shows a relatively monotonic evolution in comparison, which is mainly dominated by the fast adiabatic expansion of the SNR in a tenuous medium. Over the course of 3×10^5 yr, radiative cooling never plays an important role for such a low ISM density.

One of the novel features our models have discovered is that we cannot confirm the emergence of a clear spectral break in a radiative SNR (models A1 and A2), which is expected from the effect of ion–neutral damping of the magnetic waves in a partially ionized shock precursor.⁵ In contrast to, e.g., Lee et al. (2015), who only considered the local emission from a cloud shock, the difference comes from the fact that we initialize our simulations from the SN explosion so that the contribution from all CRs accelerated by the SNR shock before the SNR becomes radiative cannot be neglected. As a result, the

⁵ In Brose et al. (2020), this break feature is explained by a fast CR escape instead.

Table 2
Observation Data

SNR	Common Name	Type ^a	Age (yr)	Distance (kpc)	r_{sk} (deg)	v_{sk} (arcsec yr ⁻¹)	F_1 GHz (Jy)	$F_{1-100 \text{ GeV}}^{\text{b}}$ (10 ⁻⁹ cm ⁻² s ⁻¹)	$F_{1-10 \text{ TeV}}^{\text{c}}$ (10 ⁻¹³ cm ⁻² s ⁻¹)	Ref
G1.9+0.3		Ia	150–220	8.5	0.014	0.35	0.6	0.27	0.81	[15,23]
G4.5+6.8	Kepler, SN1604	Ia	418	2.9–4.9	0.029	0.22 ± 0.009	19	0.32 ± 0.09	0.69 ± 0.17	[1,14,24]
G6.4–0.1	W28	CC	33,000–36,000	1.6–2.2	0.6	0.0033 ± 0.0003	310	72.19 ± 2.84	2.9 ± 0.1	[2,16,25]
G7.7–3.7		CC	500–2200	3.2–6	0.15	...	11	0.89	6.1	[26]
G15.9+0.2		CC	1000–3000	8.5	0.043 ± 0.001	0.021 ± 0.0007	5.0	4.09 ± 0.57	2.6	[3,27]
G18.1–0.1		CC	5100–9000	5.6–6.6	0.092 ± 0.004	0.025 ± 0.003	4.6	3.5	9.46 ± 0.65	[17,28]
G21.8–0.6		CC	8800–9200	5.4–5.8	0.145	0.049	65	2.4	...	[29]
G23.3–0.3	W41	CC	60,000–200,000	4.6–5	0.55	...	70	8.11 ± 0.86	24.09 ± 2.15	[2,18,30]
G33.6+0.1	Kes 79	CC	4400–6700	3.5–7.1	0.083	0.015 ± 0.001	20	5.15 ± 0.34	...	[4,31]
G34.7–0.4	W44	CC	7900–8900	2.1–3.3	0.52 ± 0.07	0.010 ± 0.0002	240	154.41 ± 13.61	11.2	[2,32]
G41.1–0.3	3C397	Ia	1350–5300	8–9	0.032 ± 0.003	0.032 ± 0.008	25	7.7	...	[33]
G43.3–0.2	W49B	CC	2900–6000	10.9–11.7	0.033	0.021	38	18.79 ± 1.45	1.46 ± 0.21	[5,34]
G49.2–0.7	W51C	CC	16,400–18,000	4.8–6	0.057	0.0034 ± 0.0002	160	36.08 ± 2.80	...	[2,33]
G53.6–2.2		CC	15,000–50,700	2.3–6.7	0.25 ± 0.02	0.020 ± 0.006	8	64.37 ± 1.49	5.3	[6,35]
G57.2+0.8		CC	16,000–95,000	5.9–7.3	0.092	...	1.8	0.59	5.5	[36]
G65.1+0.6		CC	40,000–140,000	9–9.6	0.58 ± 0.16	...	5.5	2.8	19.4	[37]
G67.7+1.8		CC	1500–13,000	7–17	0.08	0.018 ± 0.005	1.0	0.43	15.3	[38]
G73.9+0.9		CC	11,000–12,000	0.5–4	0.23	0.0047	9	1.46 ± 0.74	...	[7,39]
G74.0–8.5	Cygnus Loop, W78	CC	10,000–20,000	0.576–1	1.6 ± 0.2	0.077 ± 0.047	210	10.60 ± 0.60	...	[40]
G82.2+5.3		CC	14,100–20,900	1.3–3.2	1.2 ± 0.6	0.069 ± 0.002	120	1.3	...	[41]
G84.2–0.8		CC	8400–11,700	4.8–6.2	0.15 ± 0.02	0.027 ± 0.001	11	0.34	...	[42]
G85.4+0.7		CC	3500–55,000	2.5–5.2	0.3	0.11 ± 0.02	...	2.2	...	[43]
G85.9–0.6		Ia	6400–49,000	3.2–6.4	0.2	0.029 ± 0.004	...	2.1	...	[43]
G89.0+4.7		CC	4800–18,000	0.8–2.1	1.0	< 0.026	220	8.37 ± 0.66	...	[44]
G111.7–2.1	Cas A	CC	316–352	3.3–3.7	0.043 ± 0.003	0.47	2300	6.25 ± 0.42	5.8 ± 1.2	[45]
G116.5+1.1		CC	15,000–50,000	1.6	0.59	0.026	10	1.8	...	[46,47]
G116.9+0.2		CC	7500–18,100	1.6–3.5	0.30	0.0023 ± 0.0004	8	1.5	...	[46,48]
G120.1+1.4	Tycho, SN1572	Ia	450	1.7–5	0.07	0.30 ± 0.06	50	0.91 ± 0.16	1.1 ± 0.4	[8,49]
G127.1+0.5		CC	20,000–30,000	1.15	0.44	...	12	2.1	...	[50]
G132.7+1.3		CC	25,000–33,000	2–2.2	0.67	0.034 ± 0.005	45	6.3	...	[51]
G156.2+5.7		CC	7000–36,600	1.7–3	0.9	0.035	5	2.0	...	[52]
G160.9+2.6		CC	2600–9200	0.3–1.2	1.0	...	110	2.8	...	[53]
G166.0+4.3		CC	9000–20,100	1–4.5	0.38	0.015 ± 0.010	7	1.7	...	[54]
G182.4+4.3		Ia	3800–4400	≥3	0.42	0.16	0.5	0.82	...	[55]
G189.1+3.0	IC 443, Jellyfish Nebula	CC	3000–30,000	0.7–2	0.38	0.012	165	83.09 ± 4.18	...	[2,39,56]
G205.5+0.5		CC	30,000–150,000	0.9–1.98	1.88	0.0059	140	2.38 ± 0.41	4.16 ± 0.51	[9,19,57]
G260.4–3.4	Puppis A	CC	2200–5400	1.3–2.2	0.6	0.12	130	16.53 ± 1.43	...	[2,58]
G266.2–1.2	Vela Jr., RX J0852.0–4622	CC	2400–5100	0.5–1	0.86 ± 0.17	0.42 ± 0.10	50	11.53 ± 0.76	274.62 ± 14.04	[2,20,59]
G272.2–3.2		Ia	3600–11,000	2.5–5	0.13	0.032	0.4	1.2	5.6	[60]
G290.1–0.8		CC	10,000–20,000	3.5–11	0.25	...	42	0.46	5.8	[61]
G296.1–0.5		CC	2800–28,000	2	0.26 ± 0.05	0.022	8	2.0	3.6	[62]
G296.5+10.0		CC	7000–10,000	1.3–3.9	0.65 ± 0.10	0.11 ± 0.04	48	0.94 ± 0.16	...	[10,63]
G296.8–0.3		CC	2000–11,000	9	0.099	...	9	1.4	5.7	[64]
G299.2–2.9		Ia	4500–11,400	5	0.13	0.049	0.5	0.76	71.8	[65]
G304.6+0.1		CC	2000–64,000	≥9.7	0.067	0.20 ± 0.18	14	3.6	...	[66]

Table 2
(Continued)

SNR	Common Name	Type ^a	Age (yr)	Distance (kpc)	r_{sk} (deg)	v_{sk} (arcsec yr ⁻¹)	$F_{1 \text{ GHz}}$ (Jy)	$F_{1-100 \text{ GeV}}^{\text{b}}$ (10 ⁻⁹ cm ⁻² s ⁻¹)	$F_{1-10 \text{ TeV}}^{\text{c}}$ (10 ⁻¹³ cm ⁻² s ⁻¹)	Ref
G306.3-0.9		Ia	2500-15,300	8	0.031	0.0074	0.16	0.93 ± 0.17	1.1	[11,67]
G308.4-1.4		CC	2400-7500	9.1-10.7	0.070	0.016 ± 0.004	0.4	0.58	3.5	[68]
G309.2-0.6		CC	700-4000	2-6	0.11 ± 0.01	...	7	0.96	3.8	[69]
G315.4-2.3	RCW 86	Ia	2000-12,400	2.3-3.2	0.35	0.12 ± 0.06	49	1.37 ± 0.17	18.2 ± 9.4	[2,61,70]
G327.4+0.4	Kes 27	CC	2400-23,000	4.3-6.5	0.17	0.028	30	3.4	5.1	[71]
G327.6+14.6	SN 1006	Ia	1016	1.6-2.2	0.25	0.49	19	0.088 ± 0.041	3.7 ± 0.8	[12,63]
G330.0+15.0		CC	15,000-52,200	0.15-0.5	2.5 ± 0.3	0.20 ± 0.03	350	0.48	...	[72]
G330.2+1.0		CC	1000-15,000	≥5	0.083	0.38	5	0.64	8.2	[15,73]
G332.4+0.1		CC	3000-8600	7.5-11	0.13	0.14	26	0.89	76.08 ± 5.24	[18,74]
G337.2-0.7		Ia	750-4400	2-9.3	0.05	...	1.5	1.1	...	[69]
G337.8-0.1		CC	1700-16,000	12.3	0.063 ± 0.013	0.0042 ± 0.0002	15	5.21 ± 0.44	...	[13,75]
G344.7-0.1		CC	3000-6000	6.3-14	0.083	0.037	2.5	4.5	40.88 ± 3.31	[18,76]
G346.6-0.2		Ia	4200-16,000	5.5-11	0.068 ± 0.004	0.028	8	1.7	...	[77]
G347.3-0.5	RX J1713.7-3946	CC	1629	1	0.46 ± 0.04	0.82 ± 0.06	30	8.20 ± 0.64	145.71 ± 5.77	[2,21,78]
G348.5+0.1		CC	6000-30,000	6.3-12.5	0.125	...	72	15.61 ± 1.75	2.04 ± 0.29	[2,18,39]
G348.7+0.3		CC	650-16,800	9.8-13.2	0.085	0.020 ± 0.002	26	15.61 ± 1.75	5.11 ± 0.69	[2,18,79]
G349.7+0.2		CC	1800-3100	11.5-12	0.033	0.013	20	4.00 ± 0.76	1.23 ± 0.21	[22,80]
G355.6-0.0		CC	7300-20,000	13	0.083 ± 0.016	...	3	3.3	2.7	[81]

Notes. For radio flux we use data from Green (2019), GeV flux data from Acero et al. (2016), TeV flux and distance data from H.E.S.S. Collaboration et al. (2018b) and references therein, other data from *SNRcat* (<http://www.physics.umanitoba.ca/snr/SNRcat>; Ferrand & Safi-Harb 2012), and the others can be found in References note. **References.** Fermi:–[1] Xiang & Jiang (2021)[2] Ackermann et al. (2017)[3] Xiang et al. (2021)[4] He et al. (2022)[5] H.E.S.S. Collaboration et al. (2018c) [6] Ergin et al. (2017)[7] Zdziarski et al. (2016)[8] Archambault et al. (2017)[9] Li et al. (2017)[10] Ackermann et al. (2018)[11] Sezer et al. (2017)[12] Condon et al. (2017)[13] Supan et al. (2018), H.E.S.S.:–[14] H.E.S.S. Collaboration et al. (2022)[15] H.E.S.S. Collaboration et al. (2014)[16] Spengler (2020)[17] H.E.S.S. Collaboration et al. (2020)[18] H.E.S.S. Collaboration et al. (2018a)[19] Aliu et al. (2014)[20] H.E.S.S. Collaboration et al. (2018e)[21] H.E.S.S. Collaboration et al. (2018d)[22] H.E.S.S. Collaboration et al. (2015), $r_{\text{sk}}, v_{\text{sk}}$: [23] Carlton et al. (2011)[24] Vink (2008)[25] Velázquez et al. (2002)[26] Zhou et al. (2018)[27] Sasaki et al. (2018)[28] Leahy et al. (2014)[29] Zhou et al. (2009)[30] Tian et al. (2007)[31] Kuriki et al. (2018)[32] Park et al. (2013)[33] Leahy & Ranasinghe (2016) [34] Zhu et al. (2014); Keohane et al. (2007) [35] Dubner et al. (1994); Agrawal et al. (1983) [36] Zhou et al. (2020)[37] Tian & Leahy (2006)[38] Hui & Becker (2009)[39] Green (2019)[40] Fesen et al. (2018)[41] Rosado & Gonzalez (1981)[42] Leahy & Green (2012)[43] Jackson et al. (2008)[44] Mavromatakis et al. (2007)[45] Gotthelf et al. (2001); Patnaude & Fesen (2009)[46] Yar-Uyaniker et al. (2004)[47] Reich & Braunsfurth (1981) [48] Lozinskaia (1980)[49] Hayato et al. (2010); Katsuda et al. (2010)[50] Joncas et al. (1989)[51] Lazendic & Slane (2006)[52] Pfeffermann et al. (1991); Katsuda et al. (2009)[53] Leahy & Tian (2007)[54] Milne (1970); Lozinskaia (1979)[55] Kothes et al. (1998)[56] Ambrocio-Cruz et al. (2017)[57] Graham et al. (1982); Odegard (1986)[58] Reynoso et al. (2017)[59] Allen et al. (2015)[60] Kamitsukasa et al. (2016)[61] Rosado et al. (1996)[62] Gök & Sezer (2012a)[63] Roger et al. (1988)[64] Sánchez-Ayaso et al. (2012)[65] Park et al. (2007); Slane et al. (1996)[66] Gök & Sezer (2012b); Gelfand et al. (2013)[67] Sawada et al. (2019)[68] Prinz & Becker (2012)[69] Rakowski et al. (2001)[70] Helder et al. (2013)[71] Chen et al. (2008)[72] Toor (1980)[73] Borkowski et al. (2018)[74] Vink (2004)[75] Combi et al. (2008)[76] Whiteoak & Green (1996); Giacani et al. (2011)[77] Auchettl et al. (2017)[78] Tsuji & Uchiyama (2016)[79] Blumer et al. (2019)[80] Yasumi et al. (2014)[81] Minami et al. (2013).

^a For SN explosion type, “Ia” indicates Type Ia explosion, and “CC” includes core-collapse explosion and explosion with inadequate information on the explosion type.

^b We use 1–100 GeV flux from Fermi-LAT and for nondetected SNRs 99% upper limits assuming spectral index $\Gamma = 2.5$.

^c We use 1–10 TeV flux from H.E.S.S. and for nondetected SNRs 99% upper limits assuming spectral index $\Gamma = 2.3$.

^d For converting the observed photon number flux into the luminosity we use the same formula as Equation (12) in YL19.

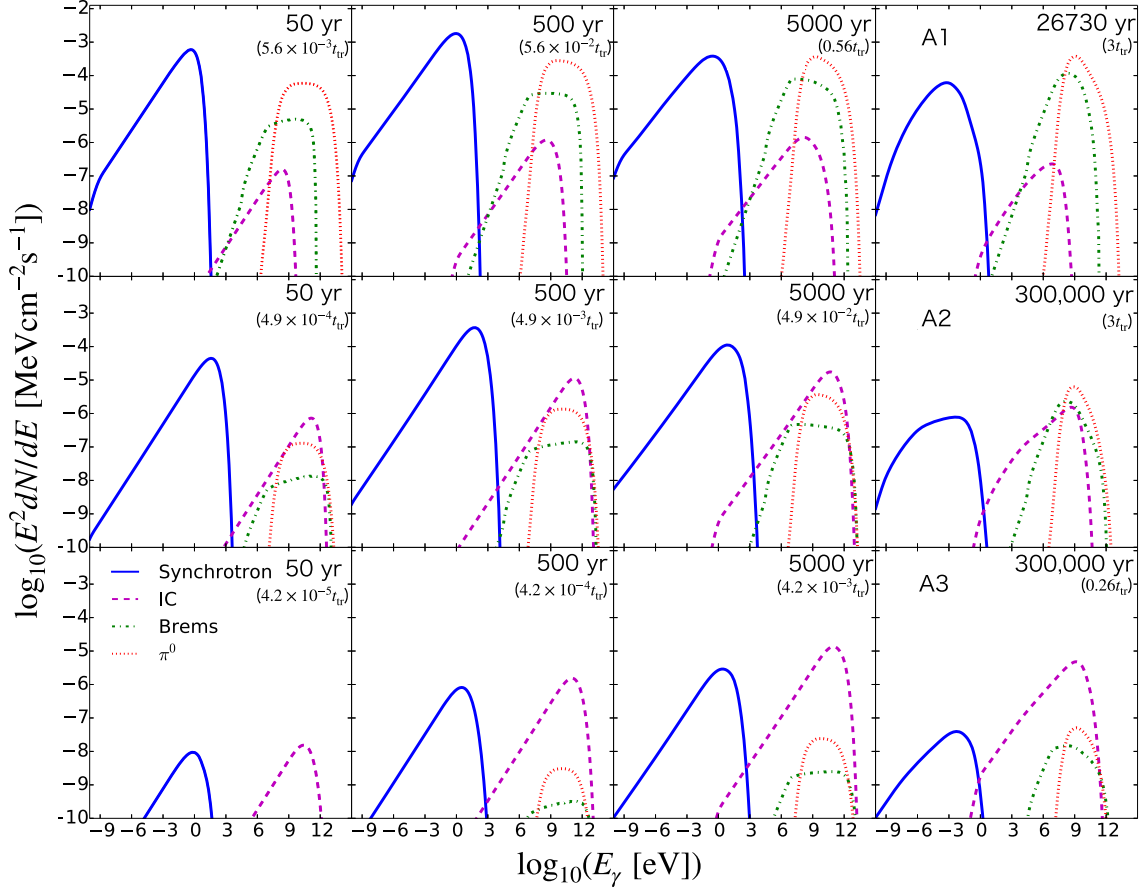


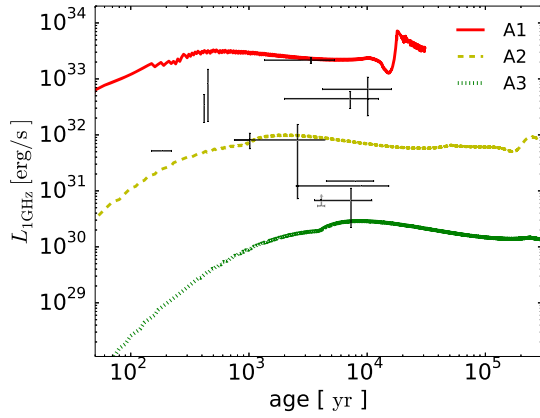
Figure 4. Time evolution of the broadband nonthermal spectra from models in Group A for each emission component until the radiative phase. Snapshots at $t = 50$ yr, 500 yr, 5000 yr, and $3t_{\text{tr}}$ (or 3×10^5 yr for model A3) are shown from left to right, and models A1, A2, and A3 ($n_{\text{ISM}} = 10, 0.1, \text{ and } 10^{-3} \text{ cm}^{-3}$, respectively) from top to bottom. The emission components include synchrotron (blue solid), nonthermal bremsstrahlung (green dashed–dotted), inverse Compton (magenta dashed), and π^0 -decay (red dotted).

contribution from the CRs accelerated in the radiative phase is only partial to the overall volume-integrated SED, making the break feature much less visible. However, we note that a momentum break does indeed appear in the local CR spectra immediately behind the radiative shock (see Section 3.3.2 for details).

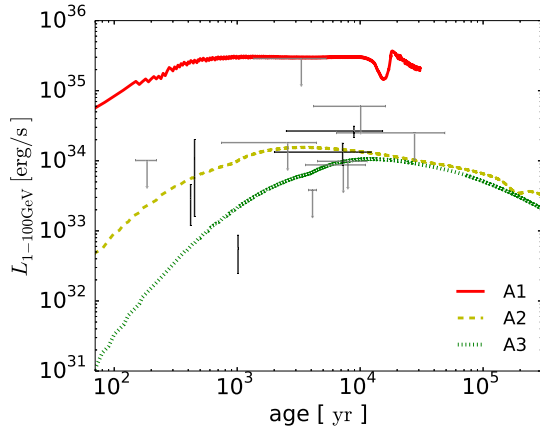
Figure 5 shows the light curves predicted by our models in three energy bands: 1 GHz in panel (a), gamma-ray integrated over the range of 1–100 GeV in panel (b), and over the range of 1–10 TeV in panel (c). The time variation of the radio (synchrotron) emission can be explained by the balance between the contribution from the newly injected CRs in accumulating shocked ISM and the decrease in density of the CRs accelerated in the past and advected downstream. The latter suffer from adiabatic cooling, and the magnetic field density also declines along with the expansion of the SNR. In model A1 with a high ambient density, the luminosity increases rapidly in the first few tens of years as the shocked ISM mass quickly accumulates. After around several $\times 10^2$ yr, the luminosity saturates and begins to decline owing to adiabatic cooling. We can see a luminosity boost after 10^4 yr by a factor of ~ 4 , which comes from the contribution from the formation of a thin cold dense shell behind the radiative shock and the resulting compression of the CR, gas, and magnetic field densities. Models A2 and A3 show similar behaviors to model A1 despite that the luminosities saturate and decrease at later ages, i.e., $\sim 10^3$ yr (A2) and $\sim 10^4$ yr (A3) proportional to their

Sedov ages, reflecting the differences in their evolution (i.e., shock velocity and total mass of shocked gas). The luminosity boost in model A2 is much milder than what is observed in model A1 since the radiative gas shell is much less prominent. We also overlay observation data from Table 2 onto the light curves for comparison. Our results are found to be consistent with the observed Type Ia SNRs for an ambient density ranging from 10^{-3} to 10 cm^{-3} . To this end, further constraints on parameters for the individual observed remnants such as their magnetic field strengths can be obtained from detailed spectral modeling for each object, including the X-rays and gamma-rays, but are beyond the scope of this work.

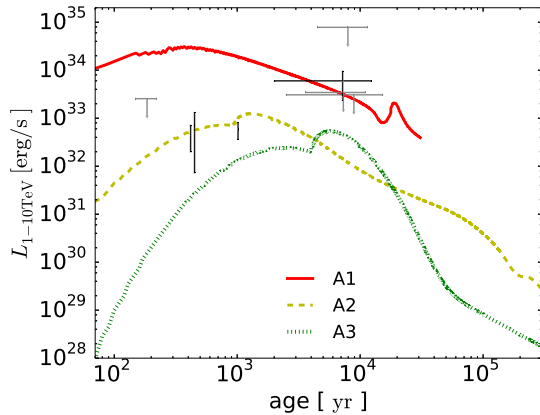
While the overall trends are found to be qualitatively similar between the gamma-rays and radio emission, our results predict similar luminosities for models A2 and A3 in the gamma-rays after $\sim 10^4$ yr despite the different ambient densities and total mass in the shocked gas involved. The SNRs in both A2 and A3 emit gamma-rays mainly through the IC channel up to 10^4 yr of evolution (albeit with a more appreciable mix from π^0 -decay in A2 for obvious reasons). The shocked masses at that point should then roughly differ between the two by a factor of $(n_{0,A2}/n_{0,A3})^{2/5} \sim 6$ from the standard Sedov solution, which can be confirmed in Figure 3(c). From that, the additional effect of a stronger spectral steepening experienced by the CRs in A2 then compensates for this factor of a few and brings the luminosities of A2 and A3 close to each other. Indeed, at an age $\sim 10^4$ yr, the shock in model A2 has



(a) 1 GHz luminosity



(b) 1–100 GeV luminosity



(c) 1–10 TeV luminosity

Figure 5. Time evolution of the luminosities in three energy bands for models in Group A compared to the observation data of Type Ia SNRs (data points). The line formats are the same as in Figure 3. Shown are the luminosities (a) at 1 GHz, (b) from 1 to 100 GeV, and (c) from 1 to 10 TeV.

decelerated to a point such that the Alfvénic Mach number M_A has decreased to a few, resulting in a steeper CR spectrum than in model A3. The hadronic emission does suffer from spectral steepening as well for the same reason as above, but the slower SNR expansion in the denser medium and the long energy-loss timescale from pion production for the protons ensure that the hadronic gamma-rays do not decline rapidly with time. The extra multiplicative factor of ρ in the normalization scaling of

the π^0 -decay emission is also responsible for the boost of the gamma-ray luminosity in the hadronic-dominated model A1 against A2.

The light curve in the TeV band is additionally affected by the evolution of the maximum CR momenta, which in turn determine the gamma-ray spectral cutoff energies. An abrupt increase in the luminosity can be observed at certain ages, especially in the TeV band for models A2 and A3. This comes from the nonlinear DSA effects kicking in as the SNR enters the Sedov phase and the shock velocity decreases to a few $\times 10^3 \text{ km s}^{-1}$, which results in a nonlinear increase in the DSA efficiency and an accompanying amplification of the magnetic field and increase of the maximum energy of the CRs. The TeV luminosity boost in model A3 is especially strong owing to the smaller downstream magnetic field and hence less influence from synchrotron loss on the gamma-ray (mainly from IC here) cutoff energy compared to other models. As the shock velocity decreases further, the nonlinear DSA effects subside, and the luminosity levels converge back to those expected in the test-particle DSA limit. Meanwhile, the shock compression ratios in our models are generally suppressed compared to those usually expected from an efficient NLDSA. One reason is from the inclusion of the magnetic dynamical feedback effect as described in Caprioli et al. (2009), which makes the fluid less compressible. Moreover, the Alfvénic drift model has an effect of spectral steepening (softening) on the accelerated CRs, such that the pressure from the counterstreaming CR on the inflowing gas is further reduced in the shock precursor. These two factors combined lead to a reduction in the shock compression ratio and prevent a strong shock modification due to the nonlinear CR feedback as seen in some other works. Compared to the gamma-ray observation data (with upper limits) from Table 2, our simulation results are also found to be in bulk agreement. The comparison suggests that most observed Type Ia SNRs are interacting with an ambient medium with densities $\lesssim 0.1 \text{ cm}^{-3}$. SN 1006 (1016 yr old) at a high Galactic latitude is known to be interacting with a tenuous ISM, which is indeed suggested to be the case by our models as well. The apparent discrepancy for the object RCW 86 (2000–12,400 yr old), which is known to interact with a dense molecular cloud (Sano et al. 2017), can be possibly due to a deviation from a simple uniform ISM-like environment encountered by the SNR.

3.2. Models with Stellar Winds

In this section, we switch focus to Group B, which involves wind-blown structures in the CSM for a massive-star progenitor. We compare the results in five models (B1 to B5) in which different mass-loss rates prior to SN are assumed. Figure 6 shows the hydrodynamic information from the models in analogy to Figure 3. We have also overlaid the results from models in Group A for reference.

The first thing one can immediately notice is that the results are differing from each other mainly in the first 10^3 yr or so, after which all models share a very similar dynamical evolution trend. The reason behind this behavior can be explained as follows. Initially, the ejecta expands into the wind structure as shown in Figure 1, whose typical densities differ according to the mass-loss rates assumed, which explains the difference among the models at young ages before a few $\times 10^2$ yr old. The initial expansion is also found to be slower in general compared to model A2, which has the same density for the

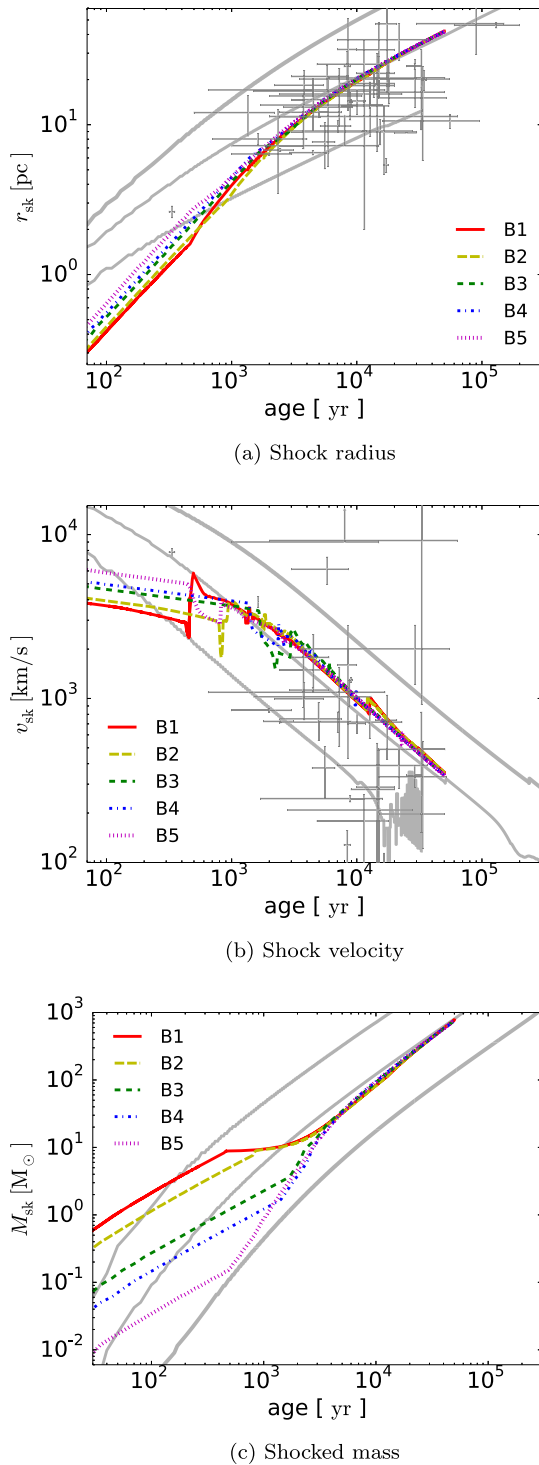


Figure 6. Same as Figure 3, but for Group B, overlaid with the results from models in Group A in gray lines and CC SNR observation data for reference. The line formats are the same as in Figure 1.

outer uniform medium, due to the much higher gas density immediately outside the ejecta than 0.1 cm^{-3} . As the shock propagates inside the wind with an r^{-2} density profile, the shock decelerates at a slower pace compared to model A2 and the SNRs expand rapidly. For models B1 and B2, the shock experiences a “break-out” from a dense wind region into the outer ambient ISM, resulting in an abrupt acceleration of the shock. In the other models, the shock sweeps past the wind

bubble until it hits a dense wind shell at a radius determined by pressure balance and experiences a deceleration until it breaks out from the shell into the outer uniform ISM. In either case (B1–B5) after the “break-out,” the total swept-up mass behind the shock eventually becomes larger than the ejecta mass, which is $12.2 M_{\odot}$ for our progenitor model; the SNR begins to enter the Sedov phase; and the dynamics converges among the models regardless of the different mass-loss history and inner CSM structure. We can see that the later evolution of the models is also similar to that predicted by model A2 for the same reason. We note, however, that there is a possibility that the late-time dynamical evolution can also be highly affected by the mass-loss history of the progenitor if the ejecta mass is smaller than the total mass loss. For example, the various types of stripped envelope SNe can experience an enhanced mass loss from binary interactions and so on. In such cases, the SNR should enter the Sedov phase inside the wind instead, which can result in a very different dynamical behavior even after the shock has propagated into the outer ISM region.

Likewise for Group B, we have overlaid the observation data from a selection of CC SNRs (from Table 2) on the plots and see a broad range of SNR radii and shock velocities from the population. This is not a surprise because we expect a rich diversity in the CC progenitor types and their associated mass-loss histories and hence CSM environments that cannot be encompassed by the parameter space in our models here. Many are also known to be interacting with giant molecular clouds, especially for the middle-aged remnants. With this in mind, despite the existence of a few outliers, the observed evolutionary trend is not inconsistent with our model predictions.

Figure 7 shows the broadband SED for models B1, B3, and B5. Following the convention in Yasuda et al. (2021, 2022), we plot the SEDs at four ages corresponding to the different phases of environment encountered by the forward shock in each model, i.e., the “ r^{-2} wind phase,” the beginning of “wind–shell interaction phase,” the “ISM phase,” and at the end of the simulation. Interestingly, at 5×10^4 yr old the SEDs are similar to each other and to model A2 for the same reason explained above for the dynamical evolution. A slight difference with model A2 exists, which is due to the different assumed energetics in the ejecta.

Differences among the models are mainly observed in the wind phase and shortly after the shock has broken into the outer ISM region. The hadronic versus leptonic origin of the gamma-rays is in line with the mass-loss rates assumed in the models. For model B1 (and B2, not shown here), we can see a double-bump feature in the synchrotron and IC components in the ISM phase. As mentioned above, the shocks in these models experience a “break-out” from a dense wind region as it enters the outer ISM. The sudden expansion of the SNR and acceleration of the shock result in a boost in the maximum momenta of the freshly accelerated CRs at the shock in the ISM and a fast adiabatic energy loss for the CRs accelerated in the past from the shocked wind (e.g., Itoh & Fabian 1984; Itoh & Masai 1989). Meanwhile, the smaller magnetic field strength in the ISM compared to that in the dense wind weakens the effect of synchrotron loss on the electrons. Overall, these lead to the appearance of a small bump in the SED at the higher photon energies, which can also be seen in Yasuda et al. (2021, 2022) and Sushch et al. (2022). The difference in the normalization

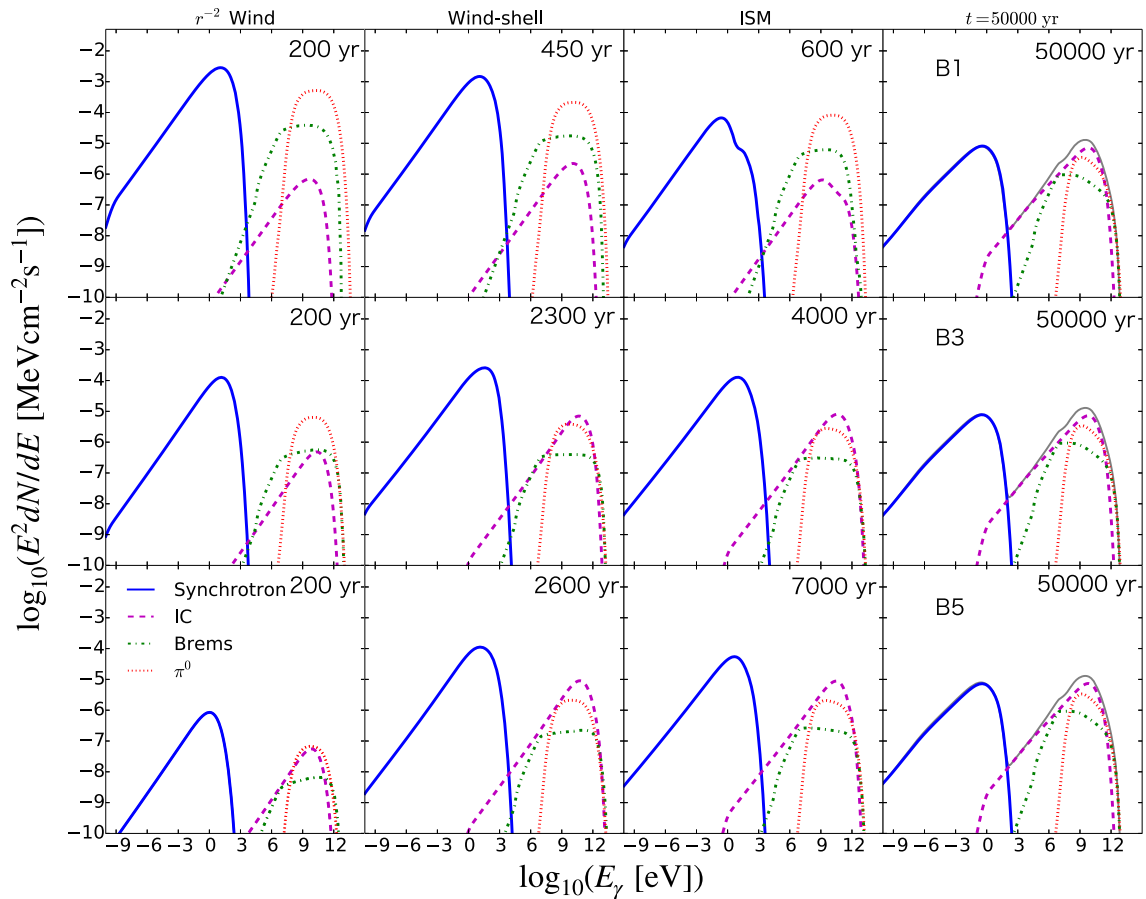


Figure 7. Same as Figure 4, but for the models in Group B. $\dot{M} = 10^{-4}, 10^{-5}, 10^{-6} M_{\odot} \text{ yr}^{-1}$ are shown from the top to the bottom, which are for models B1, B3, and B5, respectively. The ages plotted are 200, 450, 600, and 50,000 yr in B1; 200, 2300, 4000, and 50,000 yr in B3; and 200, 2600, 7000, and 50,000 yr in B5. Gray lines in the rightmost panels show the total component in model A2 at the age of 50,000 yr.

between the bumps comes from the difference in the masses in the shocked wind ($8 M_{\odot}$) and the shocked ISM at the moment.

Figure 8(a) shows the light curves at 1 GHz from Group B. The luminosities in all models decrease from the beginning in the “ r^{-2} wind phase” in contrast with Group A, and they decrease in a similar fashion among the models in accordance with the decreasing B -field and gas density with the shock radius (i.e., $L \propto \rho_0 B_0^2 \propto \rho_0^2$ at the shock where $\rho_0 \propto M r^{-2}$ with the same wind velocity), until the shock breaks out from either the inner dense wind or the dense shell outside the wind bubble at $\sim 10^3$ yr. After that, all the models converge to a radio luminosity similar to that predicted in model A2. Not surprisingly, the radio light curves after the SNR has entered the ISM phase retain no information from the mass-loss histories of the progenitor (see discussions above for possible exceptions). The ages at which the transition commences differ for each model (400, 2000, 1500, 1100, and 300 yr old for models B1 to B5, respectively) in accordance with the CSM structure shown in Figure 1. We note that since we do not consider the mass-loss history of the progenitor derived from stellar evolution models in this parametric study, these ages can alter when a more self-consistent stellar evolution model is taken into account.

In the r^{-2} wind phase, the gamma-ray luminosity decreases with time as shown by the light curves in Figures 8(b) and (c). During this phase, the gamma-ray emission is mostly dominated by the π^0 -decay component as shown in Figure 7, whose flux ($\propto \rho_0^2$) decreases monotonically with age. This is

consistent with the results presented in YL19.⁶ For models with a small mass-loss rate such as model B5, the IC component, whose flux has a weaker dependence on the wind density ($\propto \rho_0$), can become comparable to the hadronic contribution near the end of this phase, leading to a more gradual decay of the gamma-ray luminosity for such models. The major differences with YL19 begin to appear as the shock leaves the freely expanding wind and enters the wind shell and outer ISM, which were not considered in YL19. Likewise with the radio counterpart, the gamma-ray light curves merge into one similar to that of model A2.

Compared with our models, especially at older ages, the observed CC SNRs (Table 2) show relatively high radio and gamma-ray luminosities, probably due to a higher average ISM density encountered by the remnants (e.g., molecular clouds) and hence also higher magnetic fields than Group B. In fact, the observation data mostly fall between or above the results from models A1 and A2, suggesting a higher ambient gas density than the typical warm ISM phase. Our models suggest that observations of CC SNRs at younger ages are the most effective in probing the surrounding CSM environment. However, recent hydrodynamic simulations with stellar evolution models and the

⁶ The π^0 -decay component tends to be more luminous in our models than YL19 owing to the fact that our ejecta mass ($12.2 M_{\odot}$) is larger than that used in YL19 ($3 M_{\odot}$) but with a similar explosion energy. The resulting slower expansion of the SNR leads to a higher ambient wind density encountered by the shock at a given age.

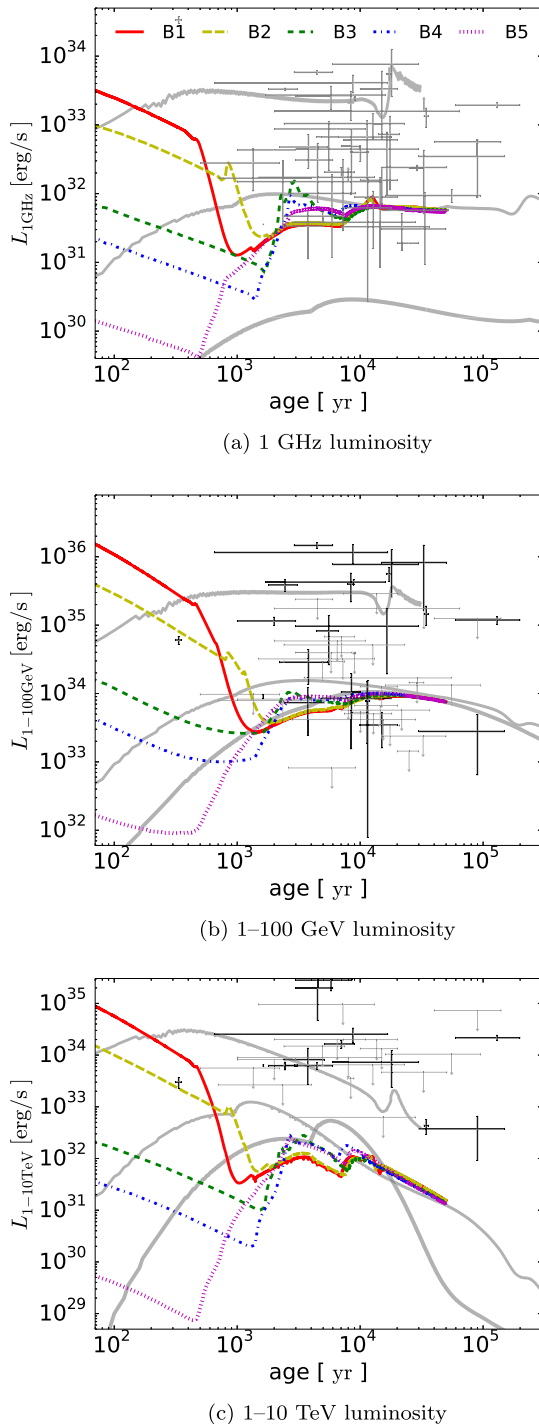


Figure 8. Same as Figure 5, but for models in Group B overlaid with CC SNR observation data. The line formats are the same as in Figure 6.

associated CSM structures taken into account self-consistently (e.g., Matsuoka et al. 2019; Yasuda et al. 2021, 2022) have shown that the nonthermal emission of an SNR at different evolutionary stages heavily depends on the progenitor type and its pre-SN activities, suggesting a promising prospect of future observations of nonthermal emission on constraining the progenitor origin of SNRs (see Section 3.4 below for an example based on our models). The incorporation of different progenitor types and their association with surrounding environments expected for CC SNRs will be accounted for based on stellar evolution models in a follow-up paper.

3.3. Effects in the Radiative Phase

Here we present results showing the impact of physical processes in the radiative phase on the calculated emission spectra. We will mainly focus on models in Group A for illustration purposes.

3.3.1. Reacceleration Effect

As the SNR shock decelerates and eventually becomes radiative, the ability of the shock in injecting and accelerating particles from thermal energies becomes weak. On the other hand, it has been shown that reacceleration of preexisting relativistic particles such as the Galactic CRs can remain effective at fast radiative shocks, which can take over as the dominant mechanism of nonthermal emission in more evolved SNRs. This effect from reacceleration of preexisting CRs in older SNRs with shock–cloud interactions has been investigated by a few recent works (e.g., Uchiyama et al. 2010; Lee et al. 2015; Cardillo 2019, and reference therein), which suggest that the bright GeV gamma-ray and radio emission observed in middle-aged SNRs such as W44 and IC 443 can be mostly accounted for by the reacceleration of Galactic CRs at their fast radiative cloud shock.⁷ These studies, however, initialized the cloud shock in an ad hoc manner without considering the dynamics of the ejecta from explosion, as well as in the earlier evolutionary stages before the SNR hits a dense cloud. This may lead to a failure in capturing the effects from the long-term evolution of the SNR and the complete history of CR acceleration from explosion to the current day. By including the essential physics similar to these previous works, our long-term simulations can serve to remedy this problem.

Based on Uchiyama et al. (2010), we take into account the reacceleration of preexisting CRs in parallel to the injection of thermal particles in the DSA process throughout the whole lifetime of an SNR until its shock dies out. In addition, by adding this effect to our self-consistent calculations, we can more accurately estimate the total amount of CRs accelerated through the lifetime of an SNR, thus helping us evaluate quantitatively the contribution of reacceleration to the total CR output from a remnant as a function of age.

To show the fractional contribution of reacceleration to the accelerated CRs, Figure 9 displays snapshots of the accelerated proton spectra integrated over the whole SNR volume in certain selected ages. For a quantitative discussion, we also adopt the time evolution of the total kinetic energy from each CR component inside the SNR,⁸ i.e., $E_{\text{CR, re}}$ for the kinetic energy in the reacceleration component and $E_{\text{CR, fresh}}$ in the freshly accelerated CR component, which is shown in Figure 10. We

⁷ This scenario has been questioned along the line of the estimated pre-shock and post-shock cloud masses being unreasonably large for remnants such as G39.2–0.3 and W44 (see, e.g., de Oña Wilhelmi et al. 2020). However, the shocked cloud mass usually cannot be estimated trivially since in such a scenario most of the nonthermal emission will be coming from a very spatially confined dense radiative cold shell behind the FS instead of a considerable fraction of the post-shock volume. This usually leads to an overestimation of the volume filling factors and so on in simple order estimations, and hence unreasonably high masses associated with the gamma-ray luminosities. This has been explained in the beginning of Section 5 in Cardillo et al. (2016), and the estimated total mass of the shocked gas responsible for the gamma-ray emission in W44 is much smaller in Lee et al. (2015) than the values cited in de Oña Wilhelmi et al. (2020), for example.

⁸ The escaped CRs are not included here since they do not contribute to the nonthermal emission from the remnant.

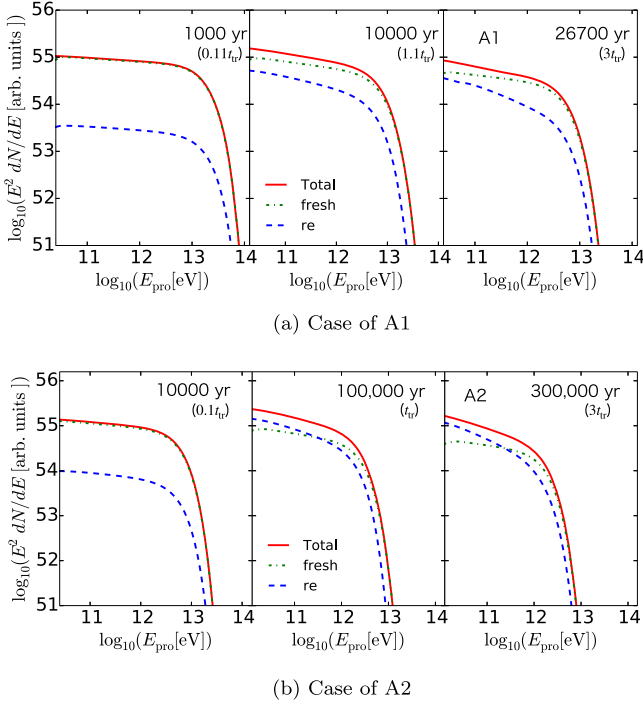


Figure 9. Time snapshots of CR proton spectra at three different dynamical ages integrated over the whole SNR volume for models A1 and A2. The total spectra (red solid) are decomposed into components from the freshly accelerated CRs (green dashed–dotted) and the reaccelerated CRs (blue dashed–dotted) to visualize their relative contributions to the accelerated CRs.

calculate $E_{\text{CR},i}$ (where $i = \{\text{re}, \text{fresh}\}$) as

$$E_{\text{CR},i} = \iint (\gamma - 1) m_p c^2 f_i(x, p) 4\pi p^2 dp d^3x \quad (6)$$

$$E_{\text{CR}} = E_{\text{CR, re}} + E_{\text{CR, fresh}}, \quad (7)$$

where γ is the Lorentz factor and $f(x, p)$ is the phase-space distribution function of the nonthermal particles. From Figure 9 and the top and middle panels of Figure 10, the flux of the reacceleration component remains approximately constant from $1 t_{\text{tr}}$ to $3 t_{\text{tr}}$, whereas the flux of the freshly accelerated component decreases due to an inefficient injection and acceleration as the shock weakens. The fresh component is now dominated by the CRs accelerated in the past which is suffering from adiabatic loss. We note that at a certain age the fresh and reaccelerated CR populations are both composed of the accumulation of particles with spectra of different indices as they were accelerated by the shock at different velocities. Furthermore, since the time evolution of the acceleration efficiency of the fresh versus reaccelerated CRs is typically different in our models, the resulting overall spectral index can be different as well.

As shown in the bottom panel of Figure 10, the ratio between the reacceleration component and the total CR content increases with the SNR age up to a few t_{tr} , indeed indicating an increasing importance of the reacceleration effect in older objects. However, the ratio increases only up to $\sim 35\%$ (A1 and A3) and $\sim 60\%$ (A2) by $3t_{\text{tr}}$, which is far from a total domination used by the previous works. Admittedly, these numbers should depend on parameters such as the ISM density, mass-loss history, and so on, as is shown by the differences between models A1 and A3, but our results clearly illustrate

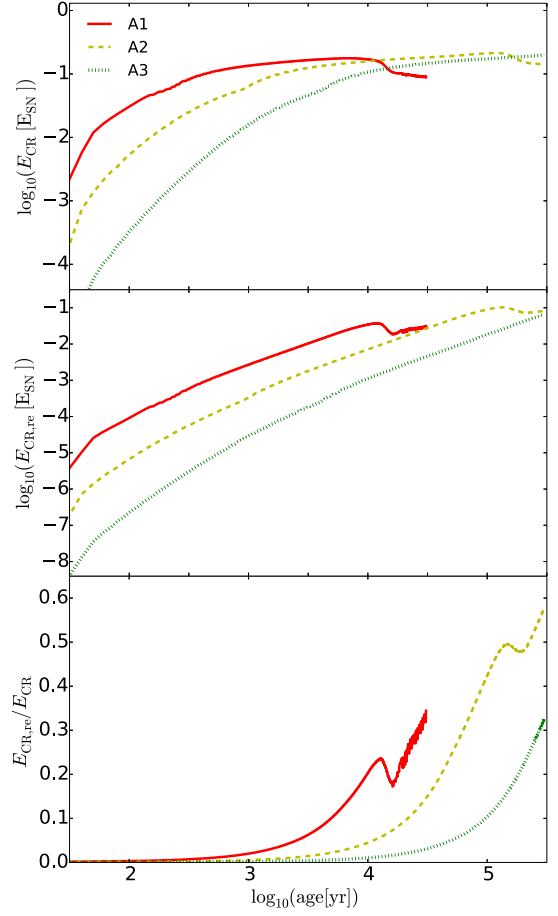


Figure 10. The total kinetic energy in the accelerated CRs integrated over the SNR volume as a function of age for models A1 to A3. The line formats are the same as in Figure 3. The top panel shows the time evolution of the total energy in all CRs inside the SNR in units of the SN explosion energy E_{SN} . Likewise, the middle panel shows the evolution of the reacceleration component. The bottom panel shows the energy ratio between the reacceleration component and the total.

that it is important to account for the CR acceleration history coherently starting from the explosion itself in order to obtain an accurate estimation of the CR energy budget and spectra, and hence the nonthermal emission properties.

For a quick comparison, we also show the results from the models in Group B in Figure 11, and we found that the final ratio is close to that predicted by model A2 (with the same $n_{\text{ISM}} = 0.1 \text{ cm}^{-3}$). In the young wind–shell interaction phase, the total (and fresh) component is roughly proportional to the pre-SN mass-loss rates, which can be understood as coming from the different masses in the gas swept up by the shock (and hence the number of particles injected into DSA) at any given age. On the other hand, $E_{\text{CR, re}}$ shows a much weaker dependence on the wind properties, mainly due to the different nature of the seed particles involved, i.e., the preexisting Galactic CRs, whose density profile is assumed to be not affected by the mass loss. We can still observe a slight difference among the models, which scales inversely with the mass-loss rate and can be interpreted as coming from the small difference in the shock velocities. These different behaviors between $E_{\text{CR, re}}$ and $E_{\text{CR, fresh}}$ lead to an interesting outcome that the ratio $E_{\text{CR, re}}/E_{\text{CR}}$, as shown in the bottom panel of Figures 10 and 11, scales with the upstream gas density in an almost opposite way from the total E_{CR} in the young phase.

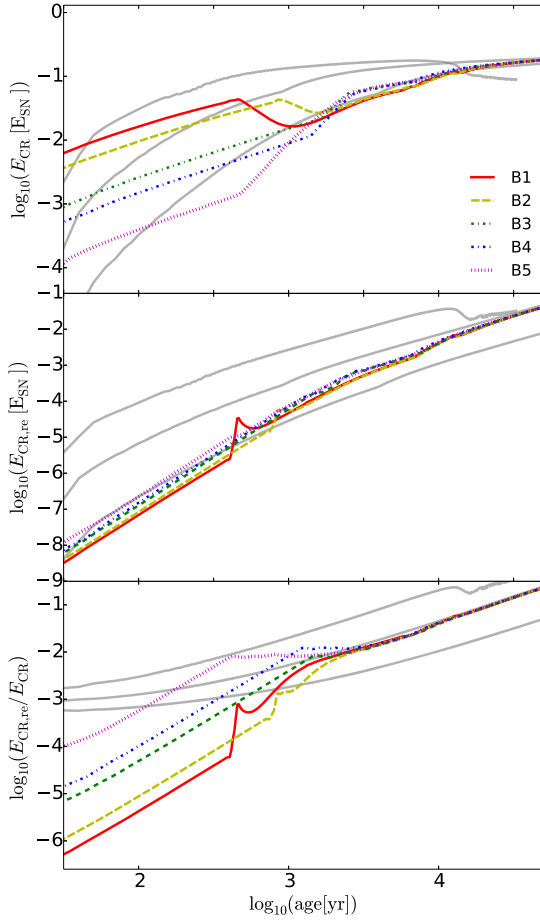


Figure 11. Same as Figure 10, but for the models in Group B. The line formats are the same as in Figure 6.

When the shock is still strong, propagating in the stellar wind, E_{CR} is mostly dominated by the freshly accelerated particles. This is quite different from the situation we expected for older SNRs, which are often found to be interacting with dense molecular clouds and the shocks have already become radiative. In the latter case, $E_{\text{CR},\text{re}}$ is expected to play a much more important role than in the younger phase. At around a few $\times 10^2$ yr to 10^3 yr, however, the ratio can reach around 1% for model B5, implying that reacceleration of preexisting CRs does contribute to the nonthermal emission for progenitors with smaller mass-loss rates. Here we have ignored the possibility of the evacuation of low-energy Galactic CRs by the magnetized stellar wind before the SN explosion and hence a reduced injection of preexisting CRs in the wind region. However, as one can see in the leftmost panels of Figures 9(a) and (b), the contribution of the reaccelerated CRs is small compared to the total component (lower than 10%), which means that reacceleration during the younger phase does not affect the overall broadband emission in a significant way.

As noted in the beginning of this section, while it has been believed that the reacceleration of Galactic CRs is sufficient to explain the nonthermal emission in older SNRs interacting with high-density environments, our long-term simulation indicates that any CRs accelerated in the past before shock–cloud interaction cannot be ignored and should be treated self-consistently with the hydrodynamic evolution of the remnant from the explosion up to the current epoch, even though the shock has already become radiative now.

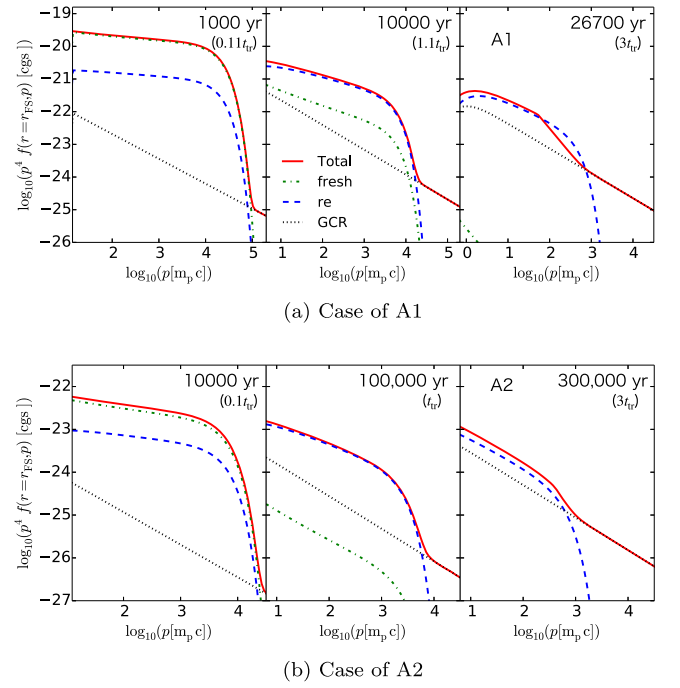


Figure 12. Local phase-space distribution of CR protons at the shock plotted at three time epochs. Same as Figure 9, the total spectrum (red solid) is decomposed into components from the freshly accelerated CRs (green dashed-dotted) and the reaccelerated CRs (blue dashed-dotted). The spectral break from the ion–neutral damping effect is applied to the total spectrum only for clarity. The background Galactic CRs are also plotted for reference (gray dotted line).

3.3.2. Spectral Break due to Ion–Neutral Damping

As mentioned above, we cannot confirm any clear break feature caused by the ion–neutral damping effect in the volume-integrated spectra in Figure 9. But this does not necessarily mean that ion–neutral damping is not happening at all, and in some models in this study, ion–neutral damping indeed takes effect.

Figure 12 shows the local proton spectra accelerated at the shock (i.e., without the CRs accelerated in the past in the downstream) separated into the freshly accelerated and reaccelerated CR components. Panel (a) shows the result of model A1 up to an age of 26,700 yr ($3t_{\text{tr}}$), where we can see that the reaccelerated CRs become the dominant component after 10,000 yr ($1.1t_{\text{tr}}$), and model A2 in panel (b) shows a similar behavior at the same dynamical ages. At $t = 3t_{\text{tr}}$, we can indeed see a spectral break feature at the momentum $p_{\text{br}} \lesssim 10^2 m_p c$ for model A1 and $p_{\text{br}} \sim$ a few $\times 10^2 m_p c$ for model A2, which comes from the ion–neutral damping effect.⁹ This feature does not appear in the photon spectra (Figure 4) since in the context of our model parameter space the total CR spectra are mainly dominated by the particles accelerated in the past before the shock has become radiative, consistent with our discussion above on the CR energy budget.

The presence or absence of a spectral break in the gamma-ray spectrum depends on the detailed structure of the ambient environment. In our study, the maximum ISM density covered by the parameter space is $n_{\text{ISM}} = 10 \text{ cm}^{-3}$ and is assumed to be uniform in space. In many older SNRs, the shocks are currently

⁹ Note that we intentionally apply the spectral break to the total spectra (red lines) only but not to the individual components in order to illustrate the effect of the spectral break on the shape of the particle distribution.

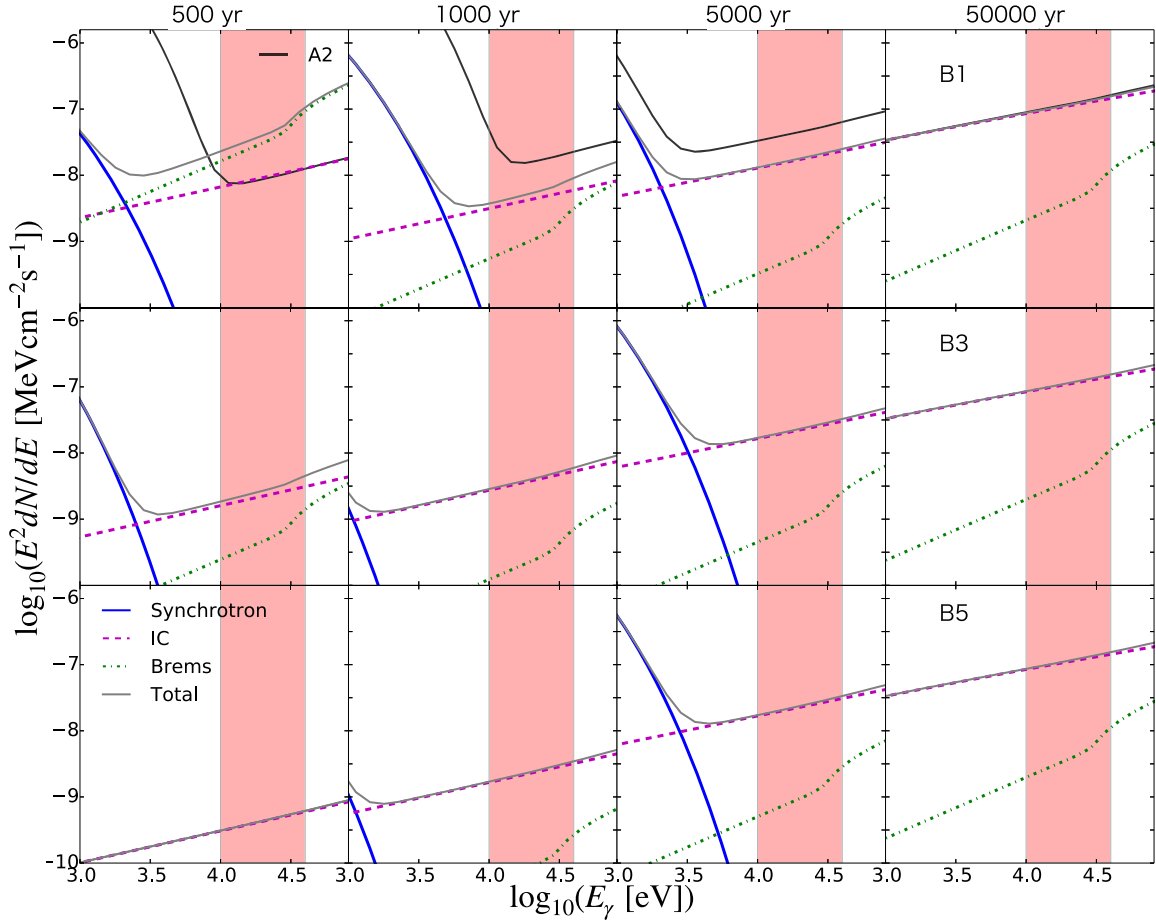


Figure 13. Same as Figure 7, but zoomed into the energy range of 1–80 keV. In the top panel, the total SED of Model A2 is overlaid as a black solid line. The red shaded area indicates the 10–40 keV range, in which future observations by FORCE are optimal.

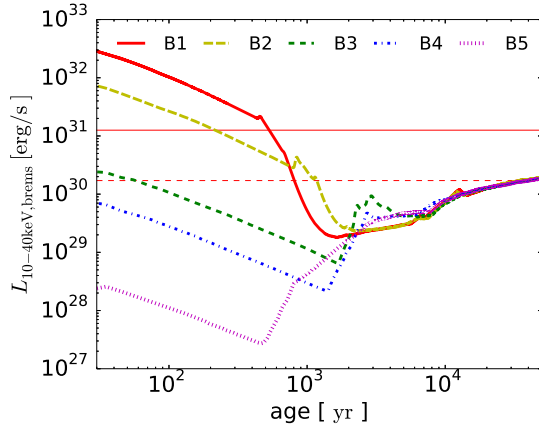
interacting with molecular clouds with a density at least an order of magnitude higher. A more realistic environment may also contain a moderately dense region in the vicinity of the ejecta and denser clouds in the outer region at a few $\times 10$ pc (Slane et al. 2015). Assuming such an environment, it is possible that we can see a pronounced ion–neutral break feature in the overall gamma-ray spectra at late times when the emission from the shock–cloud interaction region becomes the dominant component in the SED. We will consider such a situation in a future work.

3.4. Prospects for FORCE

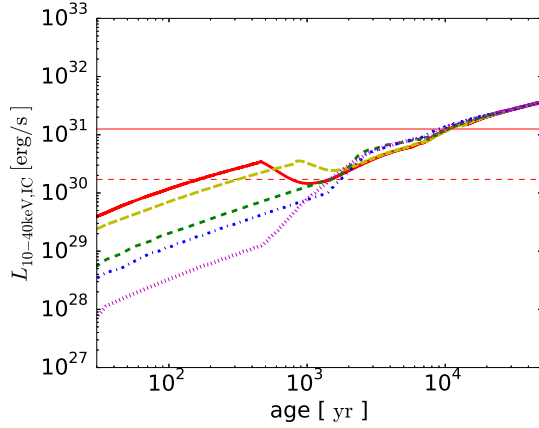
Before we end our discussion, we will employ our models to assess the prospects of FORCE on SNR research, which is a next-generation space-based hard X-ray imaging and spectroscopy instrument planned to be launched in the near future (later 2020s). This instrument excels at hard X-ray imaging with a superior angular resolution ($<15''$) and possesses a large effective area at energies >10 keV to ensure high photon statistics for spatially resolved spectroscopy (https://www.cc.miyazaki-u.ac.jp/force/wp-content/uploads/force_proposal.pdf). In this section, we will compare our results with the sensitivity of FORCE in the 10–40 keV band to discuss possible science achievable by this future mission. For a discussion on the Cherenkov Telescope Array (CTA) for TeV observations, we refer the readers to YL19.

Figure 13 shows the SED from models B1, B3, and B5 in the 1–80 keV X-ray band, which will be covered by the baseline design of FORCE. The 10–40 keV band is shown by the shaded region in red. First of all, the synchrotron components in our CC SNR models are found to be faint in this energy band, due to a weak averaged magnetic field inside the wind during the younger stage and a low-energy cutoff from synchrotron loss during the ISM phase. We thus focus the discussion of the nonthermal X-ray observation on the two other components of IC and nonthermal bremsstrahlung. Within the context of our models, the SED evolution is almost homologous from an age of a few $\times 10^3$ yr (see Figure 8), so in order to extract information like mass-loss histories, observations of younger remnants are necessary. For reference, the total SED from model A2 is plotted in the top panel. The result suggests that young (~ 1000 yr old) Type Ia SNRs interacting with a tenuous environment may emit synchrotron radiation well into the >10 keV range.

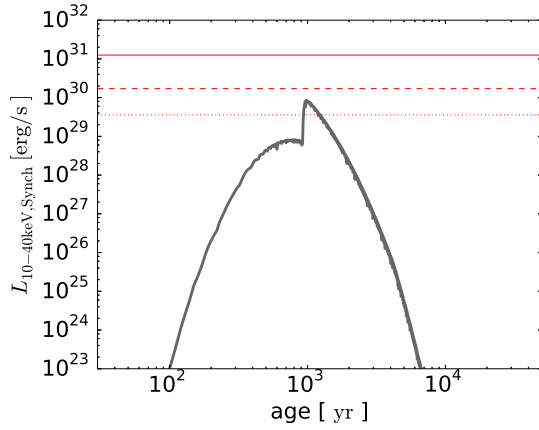
Figure 14 shows the model X-ray light curves in the 10–40 keV band compared with the 3.5σ sensitivities for a point source with an angular resolution of $15''$ and exposure times of 10 and 100 ks (https://www.cc.miyazaki-u.ac.jp/force/wp-content/uploads/force_proposal.pdf). Here a distance of 1 kpc is assumed. The bremsstrahlung luminosity up to around 10^3 yr for the models with a high mass-loss rate such as B1 and B2 here is bright compared to the sensitivity



(a) Non-thermal bremsstrahlung



(b) Inverse-Compton



(c) Synchrotron (model A2)

Figure 14. Light curves in the 10–40 keV energy range separated into the (a) nonthermal bremsstrahlung and (b) IC components. The line formats are the same as in Figure 1. The horizontal solid, dashed, and dotted lines indicate the 3.5σ sensitivity of FORCE at 1 kpc with exposure times of 10^4 , 10^5 , and 10^6 s, respectively. (c) Same as panels (a) and (b), but for the synchrotron component from model A2 in the black solid line.

curve. A future detection of this component will bring about information on the CSM structure and mass-loss histories of the progenitors. Moreover, the nonthermal bremsstrahlung depends on the upstream gas density $\rho_{0,H}$ as $K_{ep}\rho_{0,H}^2$. In the case that one can simultaneously detect the π^0 -decay gamma-

ray emission and obtain its flux ratio with the bremsstrahlung component, it is possible to obtain a stringent constraint on the K_{ep} parameter to understand the electron injection process in DSA at strong collisionless shocks. The IC component becomes bright enough to be detectable at an age older than $\sim 10^3$ yr at 1 kpc, during which the emission is dominated by the electrons accelerated in the shocked ISM.

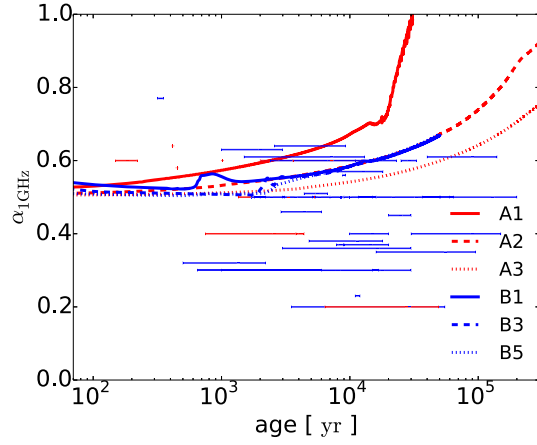
In contrast with the radio and gamma-ray light curves, which decline with age at late time, it is interesting to observe that the hard X-ray luminosities from both the bremsstrahlung and IC components generally rise with age in the ISM phase. This different behavior can be explained by an accumulation of electrons at low energies due to the adiabatic and synchrotron loss of the higher-energy electrons, as well as the steepening of the electron spectrum at the shock, which weakens as the SNR evolves. This implies that older SNRs, especially those interacting with a dense environment, are good targets for FORCE. On the other hand, even with a long observation time of 1 Ms, the synchrotron emission is barely detectable by FORCE (see panel (c); note that only model A2 is shown here with the highest synchrotron luminosity among the models), although there is a possibility that the synchrotron from secondary electrons/positrons may increase the luminosity to some extent, which is beyond the scope of this paper. The synchrotron luminosity drops rapidly with age after the peak at around 10^3 yr owing to severe synchrotron loss of the electrons close to their maximum energy. The sudden enhancement near the peak comes from the nonlinear DSA effect and CR-induced B -field amplification as explained above. Despite the difficulty, however, an upper limit from FORCE combined with observations at softer X-rays and other wave bands will serve to constrain spectral models further to obtain a possible range of key parameters such as the magnetic field strength and maximum electron energy.

With a high spatial resolution, nonthermal SNRs with angular sizes of $\sim 10'$ or bigger such as the Galactic SNR RX J1713.7–3946 can be resolved. It is anticipated that observations by FORCE will reveal the spatial distribution of the accelerated CRs in such SNRs, providing invaluable information not yet available from current observations to confront hydrodynamic and spectral models and constrain the progenitor nature and particle acceleration physics.

3.5. Caveats

In this section, we will elaborate on a few aspects that have not been fully considered or discussed within the scope of this work, as well as some possible future improvements on our models.

As proposed in some scenarios, bright gamma-ray emission from evolved SNRs has been interpreted to be partially coming from the interaction between the escaped CRs and the surrounding dense clouds (at a distance from the SNRs), which appears to be successful in explaining the gamma-ray emission from RX J1713.7–3946 (H.E.S.S. Collaboration et al. 2018d) and W28 (Hanabata et al. 2014), for example. Focusing on the EM emission from the CRs confined inside the SNRs, this illuminated cloud emission component is currently beyond our scope and thus not included in this work. We do expect an increase of detected samples of gamma-ray emission associated with escaped CRs around SNRs from future observations by, e.g., the Cherenkov Telescope Array. We plan to include such a component, as well as a more detailed discussion on the difference between the CR escape model (e.g., Celli et al. 2019)



(a) Radio spectral index at 1 GHz

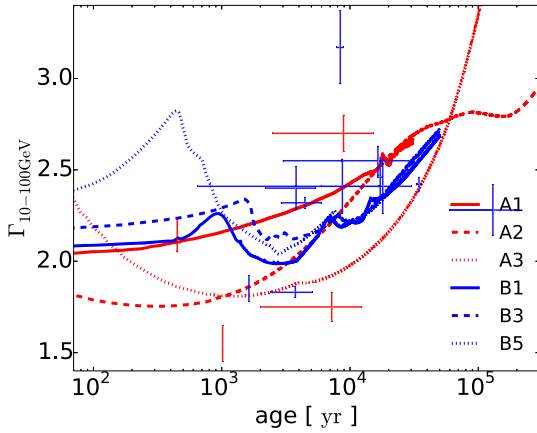

 (b) Gamma-ray index Γ in 10–100 GeV

Figure 15. Spectral index evolution at 1 GHz and 10–100 GeV. We denote α as in $S_\nu \propto \nu^{-\alpha}$, where S_ν is the flux density at frequency ν , and Γ is defined by $dN/dE \propto E^{-\Gamma}$. Indices from observations are overlaid as data points for reference, with the red and blue points for Type Ia and CC remnants, respectively.

and the Alfvénic drift model (for the emission from the confined CRs), in a follow-up paper.

A trend of spectral hardening has been observed in low energy with SNR age (Zeng et al. 2019, Figure 3(b)), which is not well represented by our results (Figure 15(a)). This can be stemming from the following reasons. As Zeng et al. (2019) suggested, the spectral hardening effect in older SNRs can be caused by several reasons, e.g., reacceleration of the CR electron, Coulomb collision loss, and a secondary stochastic acceleration in the downstream. In fact, Lee et al. (2015) have used a framework similar to ours to investigate the radio spectral evolution in evolved SNRs interacting with molecular clouds, which seems partially responsible for the hardening trend in Zeng et al. (2019). They found that a fast radiative cloud shock embedded inside a dense ($n \gtrsim 200 \text{ cm}^{-3}$) cloud that reaccelerates Galactic CR electrons can indeed successfully explain the radio spectral hardening in old SNRs (Lee et al. 2015; see the left side of Figure 3(a)). Such emission including the gamma-rays is mainly contributed by a dense radiatively cooled shell right behind the forward shock (FS), whereas the CRs trapped in the now-tenuous interior of the SNR have already suffered from considerable adiabatic loss to become unimportant players for the overall spectrum at old

ages. The difference of the 2015 work and this paper is that the parameter space surveyed in our models here (with a maximum $n = 10 \text{ cm}^{-3}$ and uniformly distributed ISM-like ambient medium) does not probe such a crushed cloud situation and hence cannot reproduce the spectral hardening result. Since the included physics are almost identical, an expansion of our parameter space in a follow-up work will be able to show such an effect. However, we note that older SNRs shown in Zeng et al. (2019) are not always interacting with dense clouds, and the crushed cloud scenario can only be a partial explanation to the spectral hardening effect witnessed in older SNRs in general.

In the “Alfvénic drift” formalism we have adopted (e.g., Bell & Lucek 2001; Caprioli et al. 2009), the magnetic waves are assumed to have a velocity the same as that of the local Alfvén waves. The effective compression ratio S_{sub} as written in Section 2 leads to a spectral softening with time (see also Caprioli et al. 2009) as we can see in Figure 15(b). We have not considered the effect suggested by Vainio et al. (2003) that the magnetic waves in the downstream can be dominated by an outgoing component such that $S_{\text{sub}} = (u_1 - v_{A,1}) / (u_2 - v_{A,2})$ can be the case instead. As in Caprioli et al. (2009), we have considered particle–wave interaction only in the upstream of the shock and ignored those in the downstream. In addition, following the approach of Caprioli et al. (2009, 2010b), we are using an approximated scheme for the magnetic field amplification process in the shock precursor by extrapolating the quasi-linear regime with resonant scatterings only to a highly turbulent (Bohm) situation. A more self-consistent scheme is desirable for the treatment of particle–wave interactions, including the downstream regions. The behavior of magnetic turbulence and particle–wave interactions has been investigated through various paths, e.g., particle-in-cell and hybrid simulations, MHD simulations, Monte Carlo approach, and so on (Reville & Bell 2013; Bykov et al. 2014; van Marle et al. 2018; Inoue et al. 2021), but the synergy with a long-term global hydrodynamic evolution with NLDSA applicable to the interpretation of broadband emission is still lacking. While we have restricted ourselves to the current more simplistic implementation of magnetic field amplification in our models, we are on our way to incorporating a more sophisticated scheme to our framework, and the results will be reported in a future work.

4. Summary

We have performed long-term simulations to study the evolution of nonthermal emission from SNRs in various kinds of environments. To realize these simulations, we adapt the CR-Hydro code from YL19 to our purposes by the implementation of several physical effects particularly relevant for SNRs in the radiative phase, such as a computationally efficient exact-integration scheme for radiative cooling, the reacceleration of preexisting CR populations, and a scheme for ion–neutral damping of magnetic waves. We studied two groups of models with a Type Ia ejecta expanding into a purely uniform ambient medium (Group A) and with an ejecta from an RSG star surrounded by a CSM structure created by the pre-SN stellar wind (Group B), respectively. We analyzed the characteristics of the hydrodynamic evolution, multiwavelength light curves, and spectral evolution for each model and discussed their dependence on the diversified ambient environment. Compared to YL19, we extend their calculation

self-consistently to an age way past the onset of the radiative phase ($t = 3 \times t_{\text{tr}}$) and follow the consequence on the nonthermal emission at the late-time evolutionary stage of an SNR. The main results can be summarized as follows:

1. Results from models in Group A are found to be in agreement with YL19 for the first 5000 yr, as well as for the first 1000 yr or so for Group B when the shock is propagating in a simple $\rho_0 \propto r^{-2}$ wind, confirming the robustness of our calculations.
2. The nonthermal spectral evolution from the Sedov phase to the radiative phase can now be followed coherently in a common platform, improving on the ad hoc treatments adopted by previous studies, which only focused on the local behavior of radiative shocks in a dense cloud.
3. Characteristic spectral steepening is witnessed across the electromagnetic spectrum to various degrees for all models in the radiative phase owing to a rapid decrease of the Alfvénic Mach number and hence the effective compression ratio of the shock, consistent with recent radio and gamma-ray observations of evolved SNRs.
4. Depending on the mass-loss history and ejecta mass of the progenitor, the nonthermal spectrum of a CC SNR can “lose memory” from the past, i.e., after a few $\times 10^3$ yr the SED no longer retains any information of the CSM structure around the ejecta and gradually converges to a homologous evolutionary track very similar to that without any density features created by the stellar wind. Exceptions are expected for stripped envelope SNRs with an enhanced mass loss.
5. We investigated the age dependence of the importance of the reacceleration of preexisting Galactic CRs in terms of the long-term CR production history of an SNR in various environments. The fractional energy contribution of the reaccelerated CRs to the total CR population inside an SNR rises with age in general. The maximum fraction is reached in the radiative phase and is found to be in the ballpark of a few tens of percent depending on the ambient environment. This is far from a complete domination in contrast to the conclusions of previous studies, which claimed that reaccelerated CRs alone are sufficient to explain the nonthermal emission properties of evolved SNRs. The implication is that even in the radiative phase, when the shock is no longer strong enough to sustain efficient particle acceleration of the thermal particles, there exists a nonnegligible contribution to the emission from CRs accelerated in the past. As a result, it is crucial to follow the SNR evolution coherently from the explosion to current days in order to obtain an accurate estimate of the energy budget of the CRs and hence the interpretation of the observed nonthermal emission.
6. A spectral break in the radiative phase from ion–neutral damping as predicted by some previous studies cannot be confirmed in the overall SED of our models. While a momentum break indeed appears locally at the radiative shock in some models, the volume-integrated SED is found to be dominated by the CRs accelerated before the ion–neutral damping effect becomes important. A future study involving shock interaction with dense molecular clouds, as well as a more realistic spatial structure of the environment, may yield model spectra in which a clear spectral break can be observed.

7. We also assessed the prospect of FORCE on the study of nonthermal SNRs in the near future. In the 10–40 keV band, most of the emission in our models is dominated by the nonthermal bremsstrahlung and IC components. For models with a higher CSM/ISM density, we predict that FORCE detection together with gamma-ray observations will be able to constrain the crucial electron-to-proton number ratio (K_{ep}) at relativistic energies to help us understand the poorly understood electron injection and acceleration mechanism at strong collisionless shock. The superior angular resolution and large effective area of FORCE will allow for space-resolved spectroscopy of extended nonthermal SNRs in the important hard X-ray band, which is essential for revealing any inhomogeneous distribution of CR protons and electrons inside the remnant, as well as providing constraints on key parameters like the magnetic field strength.

This work has established a robust platform for simulating the long-term evolution of nonthermal emission from SNRs interacting with various types of CSM/ISM environments. We plan to implement stellar evolution models for different types of progenitor stars and their associated CSM structures in our next step (e.g., Yasuda et al. 2022), so that we can provide a systematic survey on a rich diversity of SNR models for comparison with observation data from new missions such as FORCE, CTA, and so on, in the near future. Further improvements are underway as described in Section 3.5 on aspects such as the inclusion of the contribution from the escaped CRs and a revision on the particle–wave interaction scheme in the NLDSA framework. Another line of studies focusing on the thermal aspect of SNR emission is also underway in parallel (e.g., Martínez-Rodríguez et al. 2018; Jacovich et al. 2021, and references therein). We plan to join efforts with these thermal emission studies in the near future to construct a comprehensive model for multiwavelength emission from Type Ia and CC SNRs.

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ORCID iDs

Haruo Yasuda  <https://orcid.org/0000-0002-0802-6390>
Shiu-Hang Lee  <https://orcid.org/0000-0002-2899-4241>

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