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Relativistic cluster calculation of ligand-field multiplet effects on cation $L_{2,3}$ x-ray-absorption edges of SrTiO$_3$, NiO, and CaF$_2$

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A totally nonempirical relativistic cluster calculation of transition-metal $L_{2,3}$-edge x-ray-absorption near-edge structure including configuration interaction has been performed. A remarkable predictive power of this calculation has been demonstrated for three contrasting materials with different $d$-electron numbers and different coordination numbers (SrTiO$_3$, NiO, and CaF$_2$) by excellent reproduction of both the absolute peak energies and their relative intensities without any empirical parameters.

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I. INTRODUCTION

Both x-ray-absorption near-edge structure (XANES) and electron-energy-loss near-edge structure (ELNES) have been recognized as valuable probes to investigate the structural environment and chemical states of particular atomic species in a given compound.\(^1\) Sharp peaks at the thresholds of $L_1$-edge and $L_2$-edge XANES and ELNES of 3$d$ transition metals are attributed to electric-dipole transitions from the $2p_{3/2}$ and $2p_{1/2}$ core states to the unoccupied 3$d$ levels. Within the single-particle picture (one-electron approximation), the final states in both edges are equivalent and their intensity ratio (branching ratio) should follow the statistical value 2:1 expected from the ratio of the initial states. On the contrary, the observed branching ratio is generally far from this ideal value, mainly due to the correlations among the 2$p$ core hole and the 3$d$ electrons, which can be rephrased in the terminology of atomic physics as “multiplet effects.”

Currently, the most prevalent theoretical analysis is the crystal-field multiplet calculation developed by de Groot et al.\(^2\) where crystal-field effects are incorporated into an atomic multiplet program using group theoretical formalism. In the actual computational procedure, crystal fields are included as empirical parameters and the Slater integrals are constructed according to the crystal structure of SrTiO$_3$, NiO, and CaF$_2$, respectively, where the slight distortion of NiO below the Néel point was neglected for simplicity. Several thousand point charges were located at the external atomic positions so as to reproduce the effective Madelung potential.

Since the CI calculation for all N electrons in the cluster is unrealistically demanding, we adopted a relativistic many-electron Hamiltonian for selected $n$ electrons,
TABLE I. Occupancy of each type of orbital in the electronic configurations considered for the calculation of Ti$^{4+}$ and Ca$^{2+}$ $L_{2,3}$ edges. GS and ES denote the ground-state configuration and the excited-state configuration, respectively. The number of Slater determinants (SD’s) in each configuration is listed in the sixth column. The labels in the last column are used in the configuration analysis (Fig. 2).

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$$H = \sum_{i=1}^{n} h(r_i) + \sum_{i=1}^{n} \sum_{j=1}^{n} \frac{1}{|r_i - r_j|},$$  \hspace{1cm} (2.1)

where

$$h(r_i) = c \alpha p_i + \beta c^2 - \sum_{r} \frac{Z_v}{|r_i - R_v|} + V_0(r_i).$$  \hspace{1cm} (2.2)

Here $\alpha$, $\beta$ are the Dirac matrices, $c$ is the velocity of light, $p_i$ is the momentum operator, $Z_v$ is the charge of the $v$th nucleus, and $V_0(r_i)$ is the potential from the other $N-n$ electrons, and atomic units $(m = e = \hbar = 1)$ are used throughout this paper. The explicit form of $V_0(r)$ was derived by Watanabe and Kamimura\textsuperscript{a} as

$$V_0(r) = \int \frac{\rho_0(r')}{|r - r'|} \frac{3}{4} dr' + \left[ \frac{\rho(r)V_{xc}(\rho(r)) - \rho_0(r)V_{xc}(\rho_0(r))}{\rho_1(r)} - V_{xc}(\rho_1(r)) \right] d^3 r,$$  \hspace{1cm} (2.3)

where $\rho_1$ is the charge density of the selected $n$ electrons, $\rho_0$ is the charge density of the other $N-n$ electrons, $\rho$ is the charge density of all $N$ electrons ($\rho = \rho_0 + \rho_1$), and $V_{xc}$ is the Slater’s exchange-correlation potential.\textsuperscript{b} In this approach, the Coulomb interaction and the exchange-correlation interaction among the selected $n$ electrons are considered explicitly by the second term of Eq. (2.1), while those interactions between the $n$ electrons and the $N-n$ electrons are included in the form of $V_0(r)$.

As the basis functions to diagonalize the Hamiltonian (2.1), all the possible Slater determinants for the ground-state (GS) configuration and the excited-state (ES) configuration including a core hole were prepared. In the present work, the cation $2p$ orbitals and the molecular orbitals (MO’s) mainly consisting of the cation $3d$ ($t_{2g}$ and $e_{g}$) were considered. In the case of Ti$^{4+}$ and Ca$^{2+}$, six electrons occupy these orbitals. Therefore, there is only one Slater determinant in the GS configuration, while there are 60 in the ES configuration as listed in Table I, where the Slater determinants are classified according to the occupancy for each type of orbitals. Similarly, in the case of Ni$^{2+}$, 14 electrons occupy these orbitals. Thus there are 45 and 60 Slater determinants in the GS and ES configurations respectively, as listed in Table II.

The relativistic four-component MO’s to construct the above Slater determinants were calculated self-consistently based on the Dirac-Fock-Slater formalism using the relativistic SCAT computation code originally developed by Rosén et al.,\textsuperscript{c} which has been recently utilized to clarify the relativistic effects in actinide compounds.\textsuperscript{d} The numerically generated four-component relativistic atomic orbitals ($1s \sim 4p$ for Ti, Ni, and Ca and $1s \sim 2p$ for O and F) were used as the basis functions and all integrals were carried out numerically using 100,000 sampling points.

The matrix elements of $H$ between two Slater determinants, $\Phi_p$ and $\Phi_q$, can be generally expanded as

$$H_{pq} = \langle \Phi_p | H | \Phi_q \rangle = \sum_{l=1}^{L} \sum_{j=1}^{L} A_{ij}^{pq} \langle i | h | j \rangle + \sum_{l=1}^{L} \sum_{k=1}^{L} \sum_{l=1}^{L} B_{ijkl}^{pq} \langle i | j \rangle \langle j | k \rangle \langle k | l \rangle,$$  \hspace{1cm} (2.4)

where $L$ is the number of the considered orbitals and

$$\langle i | h | j \rangle = \frac{4}{\lambda - 1} \sum_{\mu = 1}^{4} \int \phi_{\lambda \mu}^*(r) h_{\lambda \mu}(r) \phi_{\lambda \mu}(r) d^3 r \hspace{1cm} (2.5)$$

$$\langle i | j \rangle \langle j | k \rangle = \frac{4}{\lambda - 1} \sum_{\mu = 1}^{4} \sum_{\mu = 1}^{4} \int \phi_{\lambda \mu}^*(r_1) \phi_{\lambda \mu}^*(r_2) d^3 r \hspace{1cm} (2.6)$$

Here $\phi_{\lambda \mu} (\lambda = 1, 2, 3, 4)$ is the $\lambda$th component of the $i$th relativistic MO and $h_{\lambda \mu}(r)$ is the $\lambda \mu$ element of $h(r)$. The coefficients $A_{ij}^{pq}$ and $B_{ijkl}^{pq}$ can be easily obtained by expanding the Slater determinants.

By diagonalizing the Hamiltonian matrix (2.4), we can obtain the many-electron energy levels and the corresponding eigenvectors. Using the eigenvectors, the many-electron

TABLE II. Occupancy of each type of orbital in the electronic configurations considered for the calculation of Ni$^{2+}$ $L_{2,3}$ edge. GS and ES denote the ground-state configuration and the excited-state configuration, respectively. The number of Slater determinants (SD’s) in each configuration is listed in the sixth column. The labels in the last column are used in the configuration analysis (Fig. 2).

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wave functions are generally expressed as a linear combination of the Slater determinants,

\[ \Psi_i = \sum_{p=1}^{M} C_{ip} \Phi_p, \]  

(2.7)

where \( M \) is the number of the Slater determinants. Since all integrals are performed numerically without requiring any particular symmetry properties of the system, this approach can be applied to systems with any symmetry. In fact, we have recently calculated the \( d-d \) transitions of \( \text{Ca}^{3+} \) in ruby based on a similar approach within the nonrelativistic framework, and the spectrum caused by the slight trigonal distortion of the system was successfully reproduced.\(^9\)

In principle, both the energy levels in the GS configuration and those in the ES configuration should be obtained directly by a simple diagonalization of \( H \). However, we have found that this direct diagonalization slightly overestimates (typically by less than 1%) the energy difference between the GS and ES configurations. This overestimation is probably due to the underestimation of the correlation effects between the selected \( n \) electrons and the other \( N-n \) electrons in the ES configuration, because the form of \( \psi_0(r) \) describing these interactions was basically derived from the ground-state electronic structure. Mathematically, these correlation effects can be included explicitly by increasing \( n \) (number of the explicitly treated electrons) and \( L \) (number of the considered orbitals). However, the accompanying drastic increase of Slater determinants would be computationally unfavorable.

On the other hand, in the single-particle picture, these correlation effects can be included as the electronic (orbital) relaxation during transition using the so-called Slater’s transition-state (TS) method.\(^9\) As a result, the total-energy difference between two configurations in a many-electron system can be well approximated by the orbital-energy difference between the relevant single-electron orbitals in the Slater’s transition-state calculation, as demonstrated by the successful reproduction of variety of XANES and ELNES for some oxides and nitrides.\(^{10-12}\) Therefore, we adopted a combination of the CI calculation and the TS calculation in the present paper. In this approach, the energy separation between the GS and ES configurations was determined by a single-particle TS calculation.

Considering the negligibly small interaction between the GS and ES configurations, the above condition can be accomplished by modifying the matrix elements of \( H \) as

\[ H'_{pq} = \begin{cases} H_{pq} & \text{(GS)}, \\ H_{pq} + \delta_{pq} \Delta E & \text{(ES)}, \end{cases} \]

(2.8)

where \( \Delta E \) is the energy shift due to the electronic relaxation during transition, which can be expressed as \( \Delta E = E_{\text{TS}} - E_{\text{CI}} \) using the transition energy estimated by the TS calculation \( (E_{\text{TS}}) \) and that estimated by the simple CI calculation \( (E_{\text{CI}}) \). In the present work, \( \Delta E \) was calculated using the initial-state configuration and the lowest-excited-state configuration. For example, in the case of \( \text{Ti}^{4+} \), \( \Delta E \) was estimated using configurations \( A \) and \( B \) in Table I. Thus \( E_{\text{CI}} \) was calculated as the difference between the energy of configuration \( A \) and the average energy of configuration \( B \), while \( E_{\text{TS}} \) was calculated as the orbital-energy difference between \( 2p_{3/2} \) and \( t_2g \) in the \( (2p_{3/2})^3(2p_{3/2})^5(t_2g)^{0.5}(e_g)^{0} \) configuration. Similarly, configurations \( A \) and \( D \) in Table II were used for the calculation of \( \text{Ni}^{2+} \), while configurations \( A \) and \( C \) in Table I were used for \( \text{Ca}^{2+} \).

The oscillator strength of the electric-dipole transition averaged over all polarizations is generally expressed as

\[ I_{ij} = \frac{2}{3} \frac{E_{ij}}{E_i - E_j} \left( \sum_{j=1}^{n} \sum_{r} \langle \Phi_j | \sum_{n=1}^{L} \sum_{l=1}^{L} A_{njl}^T(k|r|l) \rangle \right)^2, \]

(2.9)

where \( \Psi_i \) and \( \Psi_f \) are the many-electron wave functions for the initial and final states, with energies \( E_i \) and \( E_f \). Using Eq. (2.7), the integral in Eq. (2.9) can be expanded as

\[ \langle \Psi_f | \sum_{j=1}^{n} \sum_{r} \psi_j \rangle \Psi_f = \sum_{p=1}^{M} \sum_{q=1}^{M} C_{ip}^* C_{fq} \sum_{n=1}^{L} \sum_{l=1}^{L} A_{ipq}^T(k|r|l), \]

(2.10)

where

\[ \langle k|r|l \rangle = \sum_{\lambda=1}^{4} \int \phi_{i\lambda}^*(r) \phi_{f\lambda}(r) dr. \]

(2.11)

In the actual calculation of Eqs. (2.5), (2.6), and (2.11), the summation was taken over the major components \((\lambda = 1.2 \text{ and } \mu = 1.2)\) and the terms relevant to the minor components \((\lambda = 3.4 \text{ or } \mu = 3.4)\) were neglected, because their compositions in a molecular orbital are less than 0.1% in the present case.

**III. RESULTS AND DISCUSSIONS**

In order to illuminate the ligand-field multiplet effects, theoretical spectra based on the one-electron approximation [single-particle (SP) calculation] were compared with the final theoretical spectra including the multiplet effects, as reported for \( \text{Ti}^{4+} \) based on the traditional atomic calculation.\(^{13}\)

The SP calculations were carried out using the Slater’s transition-state method, where a half electron was removed from \( 2p_{3/2} \) or \( 2p_{1/2} \) and put in the lowest unoccupied orbital for the \( L_3 \) and \( L_2 \) edges, respectively. In this case, the oscillator strengths were calculated by

\[ I_{ij} = \frac{2}{3} (E_{ij} - E_i) |\langle \phi_i | \phi_f \rangle|^2, \]

(3.1)

where \( \phi_i \) and \( \phi_f \) are the single-electron orbitals for the initial and final states, with orbital energies \( E_i \) and \( E_f \).

In Fig. 1, the calculated peak energies and the oscillator strengths are shown by solid straight lines and compared with the experimental spectra reported by several authors.\(^{14,15,16}\) Here we do not intend to perform a complete simulation of the observed spectra, since the broadening factor of each peak is determined by variety of phenomena such
as the core-hole lifetime broadening, the Coster-Kronig Auger broadening, and the solid-state (dispersional and vibrational) broadening as described by de Groot et al., which is currently too complicated to estimate nonempirically. Therefore, in the present paper, the curves obtained by the simple Gaussian broadening are shown together for easy comparison with the experimental spectra.

The SP calculation of the Ti $L_{2,3}$-edge XANES in SrTiO$_3$ reproduced the absolute transition energies of peaks $c$, $d$, $e$, and $f$ quite well. In contrast to this, the intensity ratios follow the statistical values $L_2/L_3 = 2/1$ and $t_{2g}/e_g \sim 3/2$, which are qualitatively opposite to the observed spectrum.

The relative intensities of peaks are drastically improved by the relativistic CI calculation, where the ligand-field multiplet effects considerably decrease both $L_2/L_3$ and $t_{2g}/e_g$ ratios. Moreover, the small leading peaks $a$ and $b$ are also reproduced and the resultant theoretical spectrum is in excellent accordance with the observed one. These results are essentially consistent with the atomic multiplet calculation.

In order to analyze the origin of each peak in detail, a configuration analysis of the many-electron wave functions has been carried out. Thanks to the orthonormality of the Slater determinants, the composition of the $i$th Slater determinant within the $p$th eigenstate is simply given by $|C_{ip}|^2$. The contributions from each configuration in Table I are shown in Fig. 2, which clearly indicates that peaks $c$, $d$, $e$, and $f$ mainly correspond to $(2p_{3/2})^2(2p_{3/2})^2(t_{2g})^1(e_g)^0$, $(2p_{3/2})^2(2p_{3/2})^2(t_{2g})^2(e_g)^0$, and $(2p_{3/2})^2(2p_{3/2})^2(t_{2g})^3(e_g)^0$, respectively, and that the small leading peaks $a$ and $b$ originate from the multiplet splitting of the same configuration with peak $c$.

The SP calculation of the Ni $L_{2,3}$-edge XANES of NiO shows only two peaks corresponding to the transitions to the $e_g$ state, as expected from the complete occupancy of the $t_{2g}$ orbitals in the ground state. Although the absolute transition energies are reproduced quite well, observed fine structures in each edge are missing.

The relativistic CI calculation shows that the ligand-field multiplet effects split each peak and clearly reproduce the fine structures in the experimental spectrum. The configuration analysis attributes peaks $a$ and $b$ to $(2p_{3/2})^2(2p_{3/2})^2(t_{2g})^5(e_g)^2$ and peaks $c$, $d$, and $e$ to $(2p_{3/2})^2(2p_{3/2})^2(t_{2g})^6(e_g)^3$. Although the small peak $c$ mainly corresponds to a two-electron excitation state $(2p_{3/2})^2(2p_{3/2})^3(t_{2g})^5(e_g)^2$, the configuration interaction slightly allows a transition to this state through the small composition of $(2p_{3/2})^2(2p_{3/2})^3(t_{2g})^6(e_g)^3$ in this state.

The contributions from each configuration in Table I are shown in Fig. 2, which clearly indicates that peaks $c$, $d$, $e$, and $f$ mainly correspond to $(2p_{3/2})^2(2p_{3/2})^2(t_{2g})^1(e_g)^0$, $(2p_{3/2})^2(2p_{3/2})^2(t_{2g})^2(e_g)^0$, and $(2p_{3/2})^2(2p_{3/2})^2(t_{2g})^3(e_g)^0$, respectively, and that the small leading peaks $a$ and $b$ originate from the multiplet splitting of the same configuration with peak $c$.

The SP calculation of the Ni $L_{2,3}$-edge XANES of NiO shows only two peaks corresponding to the transitions to the $e_g$ state, as expected from the complete occupancy of the $t_{2g}$ orbitals in the ground state. Although the absolute transition energies are reproduced quite well, observed fine structures in each edge are missing.

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Similarly, the small shoulder $h$ originates from a two-electron excitation state $(2p_{1/2})^1(2p_{3/2})^4(t_{2g})^5(e_g)^4$ interacting with $(2p_{1/2})^1(2p_{3/2})^3(t_{2g})^6(e_g)^3$. In the present calculation, peaks $a$ and $e$ could not be reproduced because they are attributed to the states relevant to a ligand hole. The present approach can be also easily extended to include the ligand holes by taking into account the molecular orbitals mainly consisting of the ligand orbitals.

The experimental $\text{Ca}_1{\text{SrTiO}}_3$ $L_{2,3}$-edge XANES of $\text{CaF}_2$ is at first sight somewhat similar to the $L_{2,3}$-edge XANES of SrTiO$_3$. However, this resemblance is accidental and the origins of the peaks are quite different. The most essential difference is the opposite sign of the octahedral crystal field due to the different coordination number; the former is in eight-fold (simple cubic) coordination and the latter is in sixfold (octahedral) coordination. The theoretical spectra by the SP calculation clearly manifest this difference. Interestingly, this underlying difference is obscured by the totally opposite intensity redistribution between $t_{2g}$ and $e_g$ due to the ligand-field multiplet effects, where the ratio $t_{2g}/e_g$ is increased in the Ca $L_{2,3}$ edge of CaF$_2$, while it is decreased in the Ti $L_{2,3}$ edge of SrTiO$_3$. The theoretical spectrum of the former based on the relativistic CI reproduces all peaks except a small peak $f$. The origin of this peak is not clear yet, which could not be reproduced in the atomic calculations either. The configuration analysis attributes peaks $b$, $d$, $e$, and $g$ to $(2p_{1/2})^2(2p_{3/2})^3(t_{2g})^0(e_g)^1$, $(2p_{1/2})^2(2p_{3/2})^3(t_{2g})^1(e_g)^0$, $(2p_{1/2})^1(2p_{3/2})^4(t_{2g})^0(e_g)^1$, and $(2p_{1/2})^1(2p_{3/2})^4(t_{2g})^1(e_g)^0$, respectively, and the small peaks $a$ and $c$ to the same configurations with peaks $b$ and $d$, respectively.

**IV. CONCLUSION**

In the present paper, we have demonstrated an excellent predictive power of the relativistic cluster calculation including CI for the reproduction of $3d$ transition-metal $L_{2,3}$-edge XANES and ELNES by showing the results of three simple but contrasting materials (SrTiO$_3$, NiO, and CaF$_2$). The effect of crystal-field splitting and the effect of hybridization of anion orbitals are included naturally by the use of molecular orbitals. Not only the absolute peak energies, but also their relative intensities are reproduced excellently without any empirical parameters. Such a nonempirical approach can directly correlate the observed spectra with the actual local atomic arrangements and hence is indispensable for the full utilization and proper interpretation of the recent accumulation of experimental XANES and ELNES for a variety of advanced materials.

**ACKNOWLEDGMENTS**

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16. The adopted values of the full width at half maximum is 1.0 eV for Ti and Ni and 0.4 eV for Ca.