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Author(s)
Senami, M; Yamamoto, K

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Leptogenesis via multiscalar coherent evolution in a supersymmetric neutrino seesaw model

Masato Senami* and Katsuji Yamamoto†
Department of Nuclear Engineering, Kyoto University, Kyoto 606-8501, Japan

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A novel scenario of leptogenesis is investigated in the supersymmetric neutrino seesaw model. The right-handed sneutrino \( \bar{N} \) and the \( \phi \) field in the \( \vec{L} \vec{H}_u \) direction of the slepton and Higgs doublets together start coherent evolution after inflation with a right-handed neutrino mass \( M_N \) smaller than the Hubble parameter of inflation. Then, after some period the motion of \( \bar{N} \) and \( \phi \) is drastically changed by the cross coupling \( M_N h \bar{N}^* \phi \) from the \( M_N \bar{N} \bar{N} \) and \( h_N \bar{NLH}_u \) terms, and the significant asymmetries of \( \bar{N} \) and \( \vec{L} \) are generated. The \( \vec{L} \) asymmetry is fixed later by the thermal effect as the lepton number asymmetry for baryogenesis, while the \( \bar{N} \) asymmetry disappears through the decays \( \bar{N} \rightarrow \vec{L} \vec{H}_u, \vec{L} \vec{H}_u \) with almost the same rate but opposite final lepton numbers.

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Baryogenesis via leptogenesis is considered one of the promising scenarios to explain the baryon number asymmetry in the Universe [1]. Leptogenesis is interesting particularly from the point of view that it may be related to the neutrino mass generation. In the supersymmetric standard model, as investigated fully so far, leptogenesis may be realized via the Affleck-Dine mechanism [2,3] in the \( \vec{L} \vec{H}_u \) flat direction of the slepton and Higgs doublets, \( \vec{L} \) and \( H_u \), requiring a very small mass of the lightest ordinary neutrino [4]. It is also possible to realize the leptogenesis on the flat manifold of \( \vec{L} \vec{H}_u \vec{H}_d \), where the restriction on the lightest neutrino mass may be considerably moderated [5]. In this article, we investigate another novel scenario of leptogenesis in the supersymmetric seesaw model for neutrino masses [6]. The lepton number asymmetry is indeed generated via the coherent evolution of the multiscalar fields, the right-handed sneutrino \( \bar{N} \) and the \( \phi \) field in the \( \vec{L} \vec{H}_u \) direction. The potential terms provided with the supersymmetric neutrino seesaw and also the thermal effect [7] play important roles for leptogenesis in the respective epochs. The leptogenesis is completed when the generated lepton number asymmetry is fixed to some significant value by the thermal effect at the scale much higher than the gravitino mass \( m_{3/2} \sim 10^5 \) GeV. Hence, this scenario is not restricted by the low-energy electroweak physics.

In the present scenario of leptogenesis, it is supposed that some of the masses \( M_N \)‘s of the right-handed neutrinos \( N \)‘s (antineutrinos strictly) are smaller than the Hubble parameter \( H_{\text{inf}} \sim 10^{13} \) GeV during inflation. Specifically, we describe the generation of lepton number asymmetry by considering the simple case that

\[ M_{N_1} < H_{\text{inf}} \tag{1} \]

for one \( N_1 \) while \( M_{N_2}, M_{N_3} > H_{\text{inf}} \) for the others \( N_2, N_3 \). The lepton doublets are arranged with unitary transformation so that only \( L_1 \) has the Yukawa coupling with \( N_1 \). Then, the right-handed sneutrino \( \bar{N}_1 \) and the \( \phi \) field in \( \vec{L}_1 \vec{H}_u \) together start coherent evolution with large initial field values after the inflation in the manner of Affleck and Dine. The motions of \( \bar{N}_1 \) and \( \phi \) are linked through the superpotential term \( h_N \bar{N}_1 \vec{L}_1 \vec{H}_u \). (\( \bar{N}_2 = \bar{N}_3 = 0 \) due to the large masses \( M_{N_2}, M_{N_3} > H_{\text{inf}} \).) Henceforth the generation indices are suppressed by considering only the one generation for leptogenesis, and the relevant scalar fields are specified as

\[
\bar{N}, \vec{L} = \begin{pmatrix} \phi / \sqrt{2} \\ 0 \end{pmatrix}, \quad \vec{H}_u = \begin{pmatrix} 0 \\ \phi / \sqrt{2} \end{pmatrix}.
\]

If some of the \( M_N \)‘s are smaller than \( H_{\text{inf}} \) in general, the coherent evolution after the inflation may be much more multidimensional involving the \( \bar{N} \)‘s, \( \vec{L} \)‘s and \( H_u \). The leptogenesis scenario is essentially valid even in such cases, where the main source for asymmetry generation is the cross coupling \( M_N h \bar{N}^* \phi \) from the \( M_N \bar{N} \bar{N} \) and \( h_N \bar{NLH}_u \) terms of the supersymmetric neutrino seesaw model.

The relevant superpotential is given by

\[
W = \frac{M_N}{2} \bar{NN} + e^{i\delta_N} \frac{4M}{2} \bar{NNNN} + h_N \bar{NLH}_u.
\]

The \( \bar{NNNN} \) term may originate in the physics of Planck scale, and its phase factor \( e^{i\delta_N} \) is included here with real \( M_N \). The \( \bar{NN} \) term is discarded for simplicity by requiring the R parity. The \( L\vec{H}_u\vec{L}\vec{H}_u \) term is not considered either, since it does not provide a significant effect if the Yukawa coupling \( h_N > 0 \) is not extremely small. As seen later in Eqs. (6) and (7), the Yukawa coupling \( h_N \sim 3 \times 10^{-3} \) is relevant for the present scenario of leptogenesis starting at the large scale \( \sim 10^{13} \) GeV. Then, its value at the electroweak scale \( M_W \) is evaluated as \( h_N(M_W) \sim 10^{-3} \) by considering the renormalization group effects mainly provided by the top quark loop for the \( H_u \) field. The ordinary neutrino mass via seesaw mechanism is roughly estimated as

*Email address: senami@nucleng.kyoto-u.ac.jp
†Email address: yamamoto@nucleng.kyoto-u.ac.jp
depending on $h_\nu(M_W)$ and $M_N$. (The neutrino mixing is present in general with the matrix form of $h_\nu$.) Hence, this neutrino relevant for leptogenesis should be identified with the lightest one, being compatible with the data on the atmospheric and solar neutrino experiments [8,9]. It is interesting that the lightest neutrino mass is expected to be $m_\nu \sim 10^{-4}$ eV for the present leptogenesis with $\bar{N}$ and $\phi$, while $m_\nu \lesssim 10^{-8}$ eV is required for the conventional Affleck-Dine leptogenesis in the $L\tilde{H}_u$ flat direction [4].

The scalar potential is given with $W$ in Eq. (3) as

$$V = - c_N H^2 |\bar{N}|^2 - c_\phi H^2 |\phi|^2 + M_N \bar{N} \phi + \frac{h_\nu}{2} \phi^2 + h_\nu^2 |\bar{N}|^2 |\phi|^2 + H \left( b_2 \frac{M_N}{\sqrt{2}} \bar{N} \phi + a_2 \frac{e^{i\delta_N}}{4M} \frac{\bar{N} \bar{N} \phi}{H} + \text{h.c.} \right) + V_{\phi}(\phi) \tag{5}$$

Here the soft supersymmetry breaking terms are induced by the expansion of the universe with the Hubble parameter $H$. The thermal terms [7] are also included in $V_{\phi}(\phi)$. The $D^2$ terms are vanishing for the $\phi$ field. The evolution of the scalar fields is governed by the equations of motion with this potential $V$ and the redshift of $H$.

(i) Inflation epoch: $H = H_{\text{inf}}$

The scalar fields settle into one of the minima ($\bar{N}_0$, $\phi_0$) of $V$ during the inflation with $H = H_{\text{inf}}$, which are determined as

$$|\bar{N}| \sim |\phi| \sim 3 \times 10^{15} \text{ GeV} \left( \frac{H_{\text{inf}} M_N}{10^{13} \text{ GeV} \times 10^{18} \text{ GeV}} \right)^{1/2} \tag{6}$$

for the Yukawa coupling

$$h_\nu \sim 3 \times 10^{-3} \left( \frac{H_{\text{inf}} M_N}{10^{13} \text{ GeV} \times 10^{18} \text{ GeV}} \right)^{1/2}. \tag{7}$$

(We henceforth take $H_{\text{inf}} = 10^{13}$ GeV typically.) We consider for definiteness the case with this range of $h_\nu$, though it does not require a fine-tuning. If $h_\nu < (H_{\text{inf}} / M_N)^{1/2}$, $|\bar{N}_0|$, and $|\phi_0|$ take larger values. If $h_\nu > (H_{\text{inf}} / M_N)^{1/2}$, on the other hand, $\phi_0 = 0$ may be obtained due to the $h_\nu^2 |\bar{N}|^2 |\phi|^2$ term. The leptogenesis can be realized even in these cases with some modifications of scenario, which will be described elsewhere.

(ii) Oscillation epoch: $H_{\text{inf}} > H > H_{\text{tr}}$

After the inflation the Hubble parameter decreases as $H = (2/3) t^{-1}$ in the matter dominated universe, and the multiscalar coherent evolution of $\bar{N}$ and $\phi$ starts with the initial condition $(\bar{N}, \phi) = (\bar{N}_0, \phi_0)$ at $t = t_0 \sim H_{\text{inf}}^{-1}$, as given in Eq. (6). The higher order potential terms suppressed by $M$ are soon reduced by redshift, and the quartic couplings $h_\nu^2 |\phi|^4$ and $h_\nu^2 |\bar{N}|^2 |\phi|^2$ dominate in this epoch with $h_\nu$ as given in Eq. (7). Then, driven by these quartic couplings, the scalar fields oscillate in magnitude with scaling by redshift as

$$|\bar{N}| \sim |\phi| \sim (H_{\text{inf}} M_N)^{1/2} (H/H_{\text{inf}})^{2/3} \times H^{2/3}. \tag{8}$$

The field phases, however, remain almost constant except for the vicinities of $\bar{N} = 0$ and $\phi = 0$, and the significant asymmetries of $\bar{N}$ and $\tilde{L}$ do not appear in this epoch.

(iii) Transition epoch: $H_{\text{tr}} \geq H > H_{\text{th}}$

Since $\bar{N}$ and $\phi$ decrease with $H$ as given in Eq. (8), the mass term $M_N^2 |\bar{N}|^2$ and $M_N h_\nu N^* \phi \phi$ become comparable to the quartic couplings $h_\nu^2 |\phi|^4$ and $h_\nu^2 |\bar{N}|^2 |\phi|^2$ with $|\bar{N}| \sim |\phi| \sim M_N / h_\nu$, and the Hubble parameter

$$H_{\text{tr}} \sim 10^{10} \text{ GeV} \left( \frac{M_N}{10^{11} \text{ GeV}} \right)^{3/2}, \tag{9}$$

where $h_\nu (H_{\text{inf}} / M_N)^{1/2}$ with $H_{\text{inf}} = 10^{13}$ GeV is taken from Eq. (7). The thermal mass term should also be considered at $H = H_{\text{tr}}$, which is given by $(v T_p)^2 |\phi|^2$ with relevant coupling $y$ under the condition $y |\phi| < T_p$ [7]. The temperature $T_p$ of the dilute plasma of inflaton decay products is given in terms of the reheating temperature $T_R$ of the universe after the inflaton decay is completed:

$$T_p \sim (T_R^2 H m_p)^{1/4}, \tag{10}$$

where $m_p = 2.4 \times 10^{18}$ GeV is the reduced Planck mass. The thermal mass is constrained at $H = H_{\text{tr}}$ as $y (T_p)^2 |\phi|^2 \sim T_p < T_p^2 |\phi|^2 / (H_{\text{tr}})^2 |\bar{N}|^2$ for $y |\phi| < T_p$ with $|\bar{N}| \sim |\phi| \sim M_N / h_\nu$. Hence, the thermal mass term $(y T_p)^2 |\phi|^2$ is smaller than the $M_N^2 |\bar{N}|^2$ and $M_N h_\nu N^* \phi \phi$ terms at $H = H_{\text{tr}}$ for the right-handed neutrino mass

$$M_N \gtrsim 10^{10} \text{ GeV} \left( \frac{h_\nu}{3 \times 10^{-3}} \right)^{4/5} \left( \frac{T_R}{10^9 \text{ GeV}} \right)^{4/5}. \tag{11}$$

In this situation, the $M_N^2 |\bar{N}|^2$ and $M_N h_\nu N^* \phi \phi$ terms as well as the $h_\nu^2 |\phi|^4$ term dominate for $H \lesssim H_{\text{tr}}$, so that the motion of $\bar{N}$ and $\phi$ is changed drastically. Specifically, the $\bar{N}$ field oscillates mainly driven by the mass term $M_N^2 |\bar{N}|^2$ with $|\bar{N}| \approx H$. The motion of $\phi$ follows after $\bar{N}$ toward the new stable configuration with $(h_\nu / 2) \phi \phi = - M_N \bar{N}$ so as to make $|F_{\phi}|^2 - |F_{\phi}|^2 \approx M_N^2 |\bar{N}|^2$ in $V$, where $F_{\phi} = M_N \bar{N} + (h_\nu / 2) \phi \phi$ and $F_{\phi} = h_\nu \bar{N} \phi$. Consequently, the scalar fields decrease roughly as

$$|\bar{N}| \sim (M_N / h_\nu) (H / H_{\text{tr}}) \times H. \tag{12}$$
Here the reheating temperature is restricted as $T_R \leq 10^8 \times 10^{10}$ GeV to avoid the gravitino problem [10–12]. The lepton number asymmetry is converted to the baryon number asymmetry through the electroweak anomalous effect as $n_B/s = -(8/23) n_L/s$ [13]. Hence, the sufficient baryon-to-entropy ratio can be provided for the nucleosynthesis with $\eta = (2.6–6.2) \times 10^{-10}$ [14].

The motion of $\tilde{N}$ after the decoupling from $H$ is $\tilde{N} \approx H \gg m_{\tilde{N}2}$, and the analytic solution is obtained in a good approximation with $H \ll M_N$ for the two eigenmodes $\eta_R(t)$ and $\eta_l(t)$ in $\tilde{N}(t)$ as

$$\eta_R(t) = \tilde{\eta}_R \cos(M_N t + \sigma_{R1}[|b_N|/3] \ln t + \delta_{R1})$$

$$\eta_l(t) = \tilde{\eta}_l \cos(2|b_N|/3 \ln t + \delta_{R1} - \delta_{l1}).$$

The parameters $\tilde{\eta}_{R1}$ and $\delta_{l1}$ are determined as the result of $\tilde{N}$ motion from $t = t_0 - H_{\tilde{N}}^{-1}$ through $t > H_{\tilde{N}}^{-1} \gg M_N^{-1}$. The $\tilde{N}$ asymmetry is evaluated with Eqs. (21) and (22) as

$$n_{\tilde{N}}(t) = -2H^2 M \tilde{\eta}_R \tilde{\eta}_l \cos(2|b_N|/3 \ln t + \delta_{R1} - \delta_{l1}),$$

where the rapid oscillations of $\eta_R$ and $\eta_l$ with $M_N t$ in Eq. (21) are canceled.

This $\tilde{N}$ asymmetry oscillates slowly in $\ln t$ for some while due to the $b_N$ term, as seen in Eq. (23). Then, the incoherent decays of $\tilde{N}$ become significant with the dominant modes

$$\tilde{N} \to \tilde{L} H_{\tilde{d}}[L = -1], \quad \tilde{L} H_{\til{d}}[L = +1],$$

where the decay products are ultra-relativistic with $h_\nu \tilde{N} \ll M_N/2$. The motion of $\tilde{N}$ is significantly decelerated by these $\tilde{N}$ decays at $H \sim \Gamma_{\tilde{N}} \approx (h_\nu^2/4 \pi) M_N \approx 10^5 \text{GeV}$ nu-

The field phase is accelerated by this thermal log term with the change of field scaling

$$|\phi| \approx H^{1/2} \to H^{3/2}$$

while keeping $|\tilde{N}| \approx H$. After a while the top quark enters the plasma at $H \sim 0.1 H_{\tilde{d}}$, with $|\phi| \sim T_p (h_\nu \sim 1)$. Then, the thermal mass term $T_p^2 |\phi|^2$ instead becomes important, and the field phase decreases as $|\phi| \approx H/7^{1/8}$. In the preceding epoch, the significant change of asymmetries, $n_{\tilde{N}} \approx n_L$, took place through the $\tilde{N}$-$\phi$ couplings, as seen in Eqs. (14) and (15).
numericaly), so that it is linked again to $\phi$, tracking the instantaneous minimum of $V$ as $\tilde{N} = -(h_e/2M_N)\phi$ with $|\tilde{N}| \approx |\phi| \times H^{1/4}$ in magnitude and $d\tilde{N}/dt = 2d\theta_e/dt \times H^{1/4}$ in phase. Then, the $\tilde{N}$ asymmetry remaining after the transition epoch diminishes rapidly through the decays as $n_{\tilde{N}} = 2(d\tilde{N}/dt)|\tilde{N}| \times H^{3/4}$. It is the essential point that the decay modes (24) have almost the same rate $\Gamma_{t}/2$ but the opposite final lepton numbers $L = \pm 1$. This means that the $\tilde{N}$ asymmetry does not leave any significant lepton number asymmetry.

The equations of motion for $\tilde{N}$ and $\phi$ are solved by numerical calculations to confirm the present scenario of leptogenesis. The typical time variations of $n_{\tilde{N}}(t)$ and $n_L(t)$ are depicted in Fig. 1 in terms of the asymmetry fractions $n_{\tilde{N}}/[(3/2)H^2M]$. Here the model parameters are taken for example as $H_{\text{inf}} = 10^{13} \text{ GeV}$, $M = 5 \times 10^{16} \text{ GeV}$, $M_N = 10^{11} \text{ GeV}$, $e^{i\phi} = e^{i(3/10)\pi}$, $h_e = 3 \times 10^{-3}$.

c_N = 1.2, \quad c_\phi = 0.8, \quad b_N = 1.3e^{i(2/3)\pi}, \quad a_N = 1.5e^{i(5/4)\pi}, \quad a_h = 0.8e^{i(1/4)\pi}, \quad T_R = 10^9 \text{ GeV}$. The relevant scales, $H_{\text{inf}}$, $H_u$, and $H_{\text{th}}$, are marked together specifying the respective epochs. We really observe the expected changes of the asymmetries through $H_{\text{inf}} \rightarrow H_u \rightarrow H_{\text{th}}$, resulting in the desired lepton number asymmetry $\epsilon_L \equiv 1$. Particularly, the variations of $\epsilon_L$ and $\epsilon_{\tilde{N}}$ are separated for $t > H_{\text{th}}^{-1}$. $\epsilon_{\tilde{N}}$ is fixed to some significant value while $\epsilon_L$ oscillates slowly in $\ln t$ as given in Eq. (23). It is also checked that the sum $n_{\tilde{N}} + n_L$ varies rather moderately in the transition epoch, while the respective asymmetries oscillate rapidly.

In summary, we have investigated the leptogenesis via multiscalar coherent evolution in the supersymmetric seesaw model. The right-handed sneutrino $\tilde{N}$ and the $\phi$ field in $\tilde{L}H_u$ of the slepton and Higgs doublets together start coherent evolution after the inflation with $M_N$ smaller than $H_{\text{inf}}$. Then, after some period the motion of $\tilde{N}$ and $\phi$ is drastically changed by the cross coupling $M_N h_e \tilde{N}^* \phi$, and the significant asymmetries of $\tilde{N}$ and $L$ are generated. The $L$ asymmetry is fixed later by the thermal effect as the lepton number asymmetry $n_L$. The $\tilde{N}$ asymmetry, on the other hand, disappears through the incoherent decays $\tilde{N} ightarrow \tilde{L}H_u, \tilde{L}H_u$ with almost the same rate but opposite final lepton numbers. The sufficient amount of $n_L$ for baryogenesis can be obtained with the lightest neutrino mass $m_1 \approx 10^{-3} \text{ eV}$ given by the seesaw mechanism with the right-handed neutrino mass $M_N \sim 10^{10} - 10^{14} \text{ GeV} \approx H_{\text{inf}}$.

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