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# ELECTRICAL CONDUCTIVITY OF CaSO<sub>4</sub> IN AQUEOUS SOLUTION UNDER HIGH PRESSURE

By ETSUKO INADA, KIYOSHI SHIMIZU\* AND JIRO OSUGI

The electrical conductivity of aqueous solutions of 2-2 electrolytes, CaSO<sub>4</sub> and MgSO<sub>4</sub>, has been measured within the ranges, 15~40°C, 1~1,200kg/cm<sup>2</sup> and 10-3~10-4 M. The plots of A vs C1/2 under high pressure show Kohlraush's linear relation in this concentration range. The equivalent conductance at infinite dilution A' has a maximum against pressure. The pressure at this maximum point has been found to be higher than that of the minimum viscosity of water at each temperature. The hydration numbers of Ca2+, Mg2+ and SO42- ions calculated by the Robinson-Stokes method are little changed by pressure and/or temperature. The dissociation constants of Ca2+-SO42- and Mg2+-SO42- ion-pairs are increased by pressure and decreased by temperature. The thermodynamic parameters,  $\Delta \overline{G}^{\circ}$ ,  $\Delta \overline{V}^{\circ}$ ,  $\Delta \overline{H}^{\circ}$  and  $\Delta \overline{S}^{\circ}$ , are calculated from the coefficients of pressure and temperature of the dissociation constants. The closest approach distances of the ion-pairs are also estimated by using the theoretical equation of Fuoss. These ion-pairs would be solvent-separated ones, containing some water molecules between the cation and anion, and approach contact ones, liberating the water molecules with increasing temperature.

#### Introduction

From the measurements of the conductances of electrolytes, the information on the behaviors of both free ions and ion-pair is obtained. The limiting equivalent conductance  $\Lambda^{\circ}$ , which is specific to the individual ions, is an important quantity to study the ion-solvent interaction. In order to know the effect of pressure on the solvation of ions, we have determined the values of  $\Lambda^{\circ}$  of 2-2 electrolytes under high pressure.

The dissociation constants of the ion-pairs have been obtained under high pressure for many electrolytes in water. Many of them increase as pressure increases  $^{1)}$ , but some decrease or remain constant  $^{2)}$ . The molecular structures of the ion-pairs in aqueous solution have been examined with many different techniques  $^{3,4)}$ , which has suggested that the association of divalent metal sulphates would take place through two or more interposed water molecules. However, the effect of pressure on the structure of the ion-pair was elucidated only in the case of  $[Co(NH_3)_6]^{3+} \cdot SO_4^{2-5}$ .

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<sup>1)</sup> S. D. Hamann, P. J. Pearson and W. Strauss, J. Phys. Chem., 68, 375 (1964)

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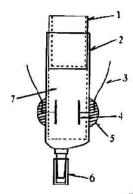
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In this paper, the pressure and temperature effects on hydration numbers of free ions and the structures of the ion-pairs of the 2-2 electrolytes, CaSO<sub>4</sub> and MgSO<sub>4</sub>, in water have been examined up to 1,200 kg/cm<sup>2</sup> at the temperatures of 15, 25 and 40°C.

#### Experimental

The conductivity cell used for high pressures was a syringe-type cell of glass and platinum, as shown in Fig. 1 (a). The oil pressure in the pressure vessel was transmitted to the sample solution by the glass piston of the syringe. The platinum electrodes in the cell were lightly coated with platinum black to avoid polarization. The cell constant  $K_{\text{cell}}$  was determined by aqueous KCl solution of  $10^{-2}\text{N}^{6}$ . The pressure-generating apparatus is shown in Fig. 1 (b). The Bourdon-type gauge was calibrated with a free piston-type gauge. The resistance R was measured by the Yanagimoto MY-7-type a.c. bridge.



5 4 4

Fig. 1 Experimental apparatus

- (a) High pressure conductivity cell
  - 1: Glass piston
  - 2: Glass cylinder
  - 3: Leading wire
  - 4: Platinum electrode
  - 5: Araldite
  - 6: Teflon capsule
  - 7: Sample solution

- (b) Pressure-generating apparatus
  - 1: Bourdon-type pressure gauge
  - 2: Hand pump
  - 3: High pressure vessel
  - 4: High pressure conductivity cell
  - 5: Leading wire
  - 6: Paraffin oil bath

The conductivity water was repeatedly distilled and in equilibrium with air. The  $1,000 \times 10^{-8}$  M stock solutions of CaSO<sub>4</sub> and MgSO<sub>4</sub> were prepared from the analytical grade reagents. The solutions in the concentration range of  $10^{-4} \sim 10^{-3}$  M were prepared by diluting the stock solutions with the conductivity water. The concentrations of these dilute solutions at high pressure were corrected with the volume of water at the corresponding pressure calculated by the Tait equation <sup>7)</sup>,

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$$\frac{V^{(1)} - V^{(P)}}{V^{(P)}} = C \log \frac{B+P}{B+1}, \tag{1}$$

where B and C are the characteristic parameters of water.

The specific conductivity of the solution  $\kappa$  is defined by Eq. (2),

$$\kappa = \frac{K_{\text{coil}}}{R} \,. \tag{2}$$

By subtracting from  $\kappa$  the specific conductivity of water  $\kappa^{\circ}$  (at 25°C, 1.19×10<sup>-6</sup>ohm<sup>-1</sup>cm<sup>-1</sup> at 1 atm and 1.94×10<sup>-6</sup>ohm<sup>-1</sup>cm<sup>-1</sup> at 1,200 kg/cm<sup>2</sup>), the equivalent conductance  $\Lambda$  is obtained by Eq. (3).

$$A = \frac{1000(\kappa - \kappa^{\circ})}{C} \,. \tag{3}$$

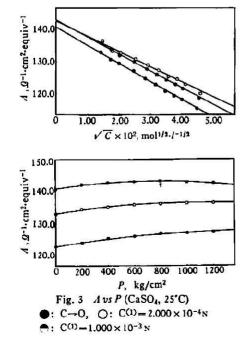
Fig. 2 1 vs V C (CaSO4, 25°C)

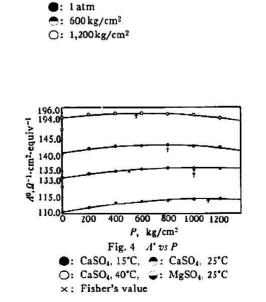
where C is the corrected equivalent concentration.

#### Results and Consideration

#### Pressure dependence of A

The plots of  $\Lambda$  against  $C^{1/2}$  have Kohlrausch's linear relation at each pressure and temperature, as shown in Fig. 2. The limiting equivalent conductance  $\Lambda^{\circ}$  is determined by the extrapolation of the  $\Lambda \sim C^{1/2}$  curve to zero concentration. Table 1 shows the values of  $\Lambda$  and  $\Lambda^{\circ}$  obtained at each concentration, temperature and pressure. The pressure dependence of  $\Lambda$  is shown in Fig. 3, where an up-





arrow,  $\uparrow$  indicates the maximum point of  $\Lambda$ . The maximum of  $\Lambda$  shifts to a higher pressure as the concentration increases. The pressure dependence of  $\Lambda$ ° at each temperature is shown in Fig. 4. The

Table 1  $\Lambda$  and  $\Lambda^0$  ( $Q^{-1} \cdot \text{cm}^2 \cdot \text{equiv}^{-1}$ )

#### (a) Aqueous solution of CaSO<sub>4</sub> (15°C)

1.000	2.000	3.000	4.000	5.000	6.000	8.000	10.00	Λ'
105.0	102.1	100.3	98.7	97.1	95.5	92.9	90.2	110.4
107.1	103.9	102.2	100.4	99.2	97.5	95.1	92.4	111.8
108.3	105.5	103.6	102.2	100.8	99.0	96.5	93.7	113.2
109.5	105.9	104_2	102.7	101.5	100.0	97,6	94.9	113.8
109.9	106.6	104.9	103.7	102.2	100.5	99.4	95.7	114.0
110.4	107.1	105.4	104.2	102.8	101.0	99.1	96.1	114.4
111.0	107.5	105.9	104.5	103.4	101.5	99.6	96.6	114.6
	105.0 107.1 108.3 109.5 109.9 110.4	105.0 102.1 107.1 103.9 108.3 105.5 109.5 105.9 109.9 106.6 110.4 107.1	105.0         102.1         100.3           107.1         103.9         102.2           108.3         105.5         103.6           109.5         105.9         104.2           109.9         106.6         104.9           110.4         107.1         105.4	105.0         102.1         100.3         98.7           107.1         103.9         102.2         100.4           108.3         105.5         103.6         102.2           109.5         105.9         104.2         102.7           109.9         106.6         104.9         103.7           110.4         107.1         105.4         104.2	105.0         102.1         100.3         98.7         97.1           107.1         103.9         102.2         100.4         99.2           108.3         105.5         103.6         102.2         100.8           109.5         105.9         104.2         102.7         101.5           109.9         106.6         104.9         103.7         102.2           110.4         107.1         105.4         104.2         102.8	105.0         102.1         100.3         98.7         97.1         95.5           107.1         103.9         102.2         100.4         99.2         97.5           108.3         105.5         103.6         102.2         100.8         99.0           109.5         105.9         104.2         102.7         101.5         100.0           109.9         106.6         104.9         103.7         102.2         100.5           110.4         107.1         105.4         104.2         102.8         101.0	105.0         102.1         100.3         98.7         97.1         95.5         92.9           107.1         103.9         102.2         100.4         99.2         97.5         95.1           108.3         105.5         103.6         102.2         100.8         99.0         96.5           109.5         105.9         104.2         102.7         101.5         100.0         97.6           109.9         106.6         104.9         103.7         102.2         100.5         99.4           110.4         107.1         105.4         104.2         102.8         101.0         99.1	105.0         102.1         100.3         98.7         97.1         95.5         92.9         90.2           107.1         103.9         102.2         100.4         99.2         97.5         95.1         92.4           108.3         105.5         103.6         102.2         100.8         99.0         96.5         93.7           109.5         105.9         104.2         102.7         101.5         100.0         97.6         94.9           109.9         106.6         104.9         103.7         102.2         100.5         99.4         95.7           110.4         107.1         105.4         104.2         102.8         101.0         99.1         96.1

## (b) Aqueous solution of CaSO<sub>4</sub> (25°C)

M×10 <sup>4</sup> Pressure	1.000	1.500	2.000	3.000	4.000	5.000	6.000	7.000	8.000	10.00	Λ*
1 atm	133.1	130.8	129.5	127.3	124.9	122.9	120.9	119.5	118.1	115.3	140.7
$200  \text{kg/cm}^2$	134.5	132.5	130.8	128.6	126.1	124.0	122.2	120.9	119.3	116.2	142.1
400	135.2	133.4	131.7	129.3	126.3	125.3	123.5	122.1	120.1	117.4	142.7
600	135.8	133.8	132.2	130.0	127.8	126.1	124.3	123.0	121.6	118.6	143.0
800	136.1	133.5	132.7	130.6	123.5	126.9	125.0	123,6	122.1	119.4	143.2
1,000	136.3	133.5	132.9	130.9	123.7	127.0	125.4	124.2	122.7	120.1	142.9
1,200	136.4	133.4	132.9	131.0	129.1	127.3	125.5	124.3	122.9	120.1	142.6

## (c) Aqueous solution of CaSO4 (40°C)

M×10 <sup>4</sup>	1.500	2.000	2.500	3.000	4.000	5.000	A*
1 atm	178.4	176.1	173.8	171.9	168.1	165.2	194.6
200 kg/cm <sup>2</sup>	179.7	177.5	175.6	173.5	169.8	166.9	195.6
400	179.7	178.0	176.0	173.5	170.6	167.2	195.8
600	179.9	178.2	176.2	174.1	171.0	167.9	195.8
800	179.8	178.2	176.3	174.2	171.3	168.0	195.6
1,000	179.5	178.1	176.2	174.2	171.3	168.1	195.3
1,200	179,2	177.9	175.9	174.0	171.7	168.1	194.4

## (d) Aqueous solution of MgSO<sub>4</sub> (25°C)

M×104 Pressure	2.000	2.500	3.000	3.500	4.000	5.000	A*
1 atm	123.5	121.5	120.7	119.2	118.0	116.5	133.1
200 kg/cm <sup>2</sup>	124.8	123.4	122.2	121.2	120.4	118.5	134.4
400	125.3	124.6	123,3	122,3	121.4	118.8	135.0
600	126,2	125.3	123.9	123.2	122.1	119.6	135.8
800	126.5	135.6	124.1	123,4	122.4	120.1	136.0
1,000	126.8	126.1	124.3	123,6	122.6	120.3	136.0
1,200	126.9	125.8	124.7	124.0	122,5	120.4	136.0

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pressure of the maximum  $\Lambda^{\circ}$ ,  $P(\Lambda^{\circ})$  shifts to a lower pressure as temperature increases, and  $P(\Lambda^{\circ})$  of CaSO<sub>4</sub> is lower than that of MgSO<sub>4</sub> at 25°C.

Now, in the case of the dissociation of the symmetrical electrolyte  $(z_+ = |z_-|)$  into its free ions, the specific conductivity of the electrolyte,  $\kappa - \kappa^{\circ}$ , is given by Eq. (4),

$$10^{3}(\kappa - \kappa^{\circ}) = \sum C_{i} \lambda_{i} = C\alpha \sum \lambda_{i}. \tag{4}$$

where  $C_i$  and  $\lambda_i$  are the equivalent concentration and equivalent conductance of *i*-ion, respectively and  $\alpha$  the degree of dissociation. From Eqs. (3) and (4),

$$\Lambda = \alpha \sum \lambda_i \,, \tag{5}$$

that is, the equivalent conductance is proportional to the degree of dissociation and the sum of the ionic conductances. Therefore, the shift of P(A), the pressure of the maximum A, to a higher pressure with the increase of the concentration is ascribed to the fact that the pressure coefficient of  $\alpha$  is more effective for A in the lower dilute solution than in the higher.

The pressure dependence of A would be explained qualitatively by Stokes law,

$$\lambda^{\circ}_{i} = \frac{|z_{i}|eF}{6\pi r_{i} n^{\circ}}, \tag{6}$$

where  $\lambda^{\circ}_{t}$ ,  $z_{t}$  and  $r_{t}$  are the limiting ionic equivalent conductance of *i*-ion, its ionic valence and its Stokes radius, respectively, and F the Faraday constant, e the electronic charge, and  $\eta^{\circ}$  the viscosity of water. The viscosity of water has a minimum against pressure at lower temperatures, because the structure of water would be broken down by pressure. The minimum point disappears at about  $36^{\circ}\text{C}^{8\sim10}$ , above which the viscosity increases monotonously with increasing pressure. The pressures at the minimum  $\eta^{\circ}$ ,  $P(\eta^{\circ})$  are  $950\text{kg/cm}^{2}$  at  $15^{\circ}\text{C}$  and  $600\text{kg/cm}^{2}$  at  $25^{\circ}\text{C}^{-11}$ ). When the hydrated ion with the constant effective radius migrates in a continuous medium whose viscosity is  $\eta^{\circ}$  under pressure.  $P(\Lambda^{\circ})$  should be equal to  $P(\eta^{\circ})$  according to Eq. (6). As shown in Fig. 4, this is not the case;  $P(\Lambda^{\circ})$  is higher than  $P(\eta^{\circ})$  at each temperature. The maximum point of  $\Lambda^{\circ}$  is found even at  $40^{\circ}\text{C}$ , where the viscosity of water increases monotonously with increasing pressure. These discrepancies would be explained from the view point of the decrease in the radius of the hydrated ion by pressure according to the Robinson-Stokes method 12), though there have been other standpoints of the local viscosity in the vicinity of the ion 13) and of the effect of dielectric relaxation on ionic motion 2.14.15).

#### Hydration numbers of the free ions

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The Robinson-Stokes method <sup>16)</sup> has been applied to calculate the hydration number of Ca<sup>2+</sup>, Mg<sup>2+</sup> and SO<sub>4</sub><sup>2-</sup> ions under high pressure as follows <sup>12)</sup>.

$$\lambda_{t(P)} = \Lambda^{\circ}(P) \cdot t^{\circ}_{t(P)} \,, \tag{7}$$

where  $t^{\circ}_{i(P)}$  is the limiting transference number of i-ion at pressure P. It is assumed that  $t^{\circ}_{i(P)} = t^{\circ}_{i(1)}$ . The values of the cationic transference number are as follows,

$$t^{\circ}_{+(P)} = t^{\circ}_{+(1)} = \frac{\lambda^{\circ}_{+(1)}}{\lambda^{\circ}_{(1)}}, \quad 0.427 \text{ at } 15^{\circ}\text{C}$$

$$0.426 \quad 25^{\circ}\text{C}$$

$$0.419 \quad 40^{\circ}\text{C}$$

$$0.399 \quad 25^{\circ}\text{C} \quad \text{Mg}^{2+}$$

$$(8)$$

where  $\lambda^{\circ}(1)$  were cited from the literatures <sup>16,17)</sup>. From Eqs. (6) and (7), the Stokes radius  $r_i$  is obtained. Introducing the correction factor  $f_{R-S}$  for  $r_i$ , the effective radius of hydrated ion  $r_e$  is obtained. The volume of the hydration sheath in the neighborhood of the ion is

$$V_{A} = \frac{4}{3}\pi \left(r_{e}^{3} - r_{e}^{3}\right), \tag{9}$$

where  $r_c$  is the crystal radius of i-ion. Then the hydration number is given by the equation,

$$h = \frac{V_A}{V_W},\tag{10}$$

where Vw is the average volume of one water molecule in the hydration sheath and was assumed to be equal to that of the bulk water at each pressure. These numerical values of  $\lambda^{\circ}_{i}$ ,  $f_{R-S_i}$ ,  $r_{\epsilon}$  and h are listed in Table 2. As shown in Table 2, the hydration numbers of  $Ca^{2+}$ ,  $Mg^{2+}$  and  $SO_4^{2-}$  ions are invariant within the experimental error as temperature increases. Also, the hydration numbers of these ions are little changed by pressure as in the case of  $[Co(NH_3)_6]^{3+}$  and  $SO_4^{2-}$  ions<sup>12)</sup>. This is not in agreement with Horne's opinion of the dehydration of ions by pressure<sup>18)</sup>.

#### Dissociation of the ion-pairs

The ion-pairs of Ca2+.SO42- and Mg2+.SO42- would be in equilibrium with their free ions,

$$M^{2+} \cdot SO_4^{2-} \Longrightarrow M^{2+} + SO_4^{2-}, \qquad (11)$$

$$m(1-\alpha) \qquad m\alpha \qquad m\alpha$$

where  $M^{2+}$  represents the metal ion and m is the stoichiometric molar concentration. Then the dissociation constant K in the system of Eq. (11) is defined as follows,

$$K = \frac{m\alpha^2}{(1-\alpha)} \cdot \frac{f_1 f_2}{f_3} \,, \tag{12}$$

R. A. Robinson and R. H. Stokes, "Electrolyte Solutions", Butterworths Scientific Publications, London (1965)

<sup>17)</sup> A. G. Keenan, H. C. Mcleod and A. R. Gordon, J. Chem. Phys., 13, 466 (1965)

R. A. Horne, "Advances in High Pressure Research", Vol. 2, Chap. 3, ed. by R. S. Bradley, Academic Press, London (1969)

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## Electrical Conductivity of CaSO4 in Aqueous Solution under High Pressure

Table 2  $\lambda^* t$ ,  $f_{R-S}$ ,  $r_t$ , h and  $V_W$ 

# (a) CaSO<sub>4</sub> (15°C)

n		Ca2. r.	=0.99Å			SO <sub>4</sub> 2- r.	. = 2.73Å		12 ( 3 2)
Pressure -	λ°i	∫R-S	re(Å)	h	1.4	∫R-N	r. (Å)	h	Vw (Å3)
1 atm	47.1	1.36	4.09	9.4	63.3	1.62	3.63	3.8	30.0
200 kg/cm <sup>2</sup>	47.7	1.36	4.09	9.5	64.1	1.62	3.63	3.9	29.8
400	48.3	1.36	4.08	9.5	64.9	1.62	3.61	3.8	29.5
600	48.6	1.36	4.08	9.6	65.2	1.62	3.61	3.8	29.3
800	48.7	1.36	4.08	9.7	65.3	1.62	3.63	4.0	29.0
,000	48.8	1.36	4.08	9.7	65.6	1.62	3.61	3.9	28.8
,200	48.9	1.37	4.08	9.8	65.7	1.62	3.60	3.9	28.6

# (b) CaSO<sub>4</sub> (25°C)

D		Ca	2+	1		SC	42-		Vw (Å3)
Pressure	λ°ε	∫ <sub>R-S</sub>	r. (Å)	h	λ.,	$f_{ m R-S}$	r. (Å)	h	IW(A)
1 atm	59.9	1.35	4.10	9.5	80.8	1.61	3.64	3.9	30.0
200 kg/cm <sup>2</sup>	60.5	1.35	4.09	9.5	81.6	1.61	3.62	3.8	29.8
400	60.9	1.36	4.11	9.7	81.9	1.62	3.63	3.9	29.5
600	60.9	1.36	4.11	9.6	82.1	1.62	3.63	3.9	29.3
800	61.0	1.36	4.09	9.7	82.2	1.62	3.63	4.0	29.0
,000	60.9	1.37	4.11	10.0	82.0	1.62	3.61	3.9	28.8
,200	60.7	1.37	4.11	10.0	81.9	1.63	3.62	4.0	28.6

# (c) CaSO<sub>4</sub> (40°C)

		Ca	ì <sup>2+</sup>			SC	42-		
Pressure	λ°ε	$f_{ m R-S}$	r. (Å)	h	λ°ε	$f_{ m R-S}$	r. (Å)	h	Vw (Å3)
1 atm	81.5	1.35	4.13	9.7	113.1	1.63	3.60	3.7	30.0
200 kg/cm <sup>2</sup>	82.0	1.36	4.12	9.7	113.6	1.64	3.59	3.7	29.7
400	82.0	1.36	4.11	9.7	113.8	1.64	3.58	3,6	29.5
600	82.0	1.36	4.09	9.6	113.8	1.64	3.56	3.5	29.3
800	82.0	1.37	4.08	9.6	113.6	1.65	3.55	3.5	29.1
,000	81.8	1.37	4.07	9.6	113.5	1.66	3.55	3.5	28.9
,200	81.5	1.38	4.07	9.7	112.9	1.66	3.54	3.5	28.7

## (d) MgSO<sub>4</sub> (25°C)

		Mg <sup>2+</sup> ,	.=0.65Å						
Pressure	λ*ε	∫ <sub>R-S</sub>	r. (Å)	h	λ*,	$f_{ m R-S}$	r. (Å)	h	Vw (Å3)
l atm	53.1	1.25	4.31	11.1	80.0	1.60	3.66	4.0	30.0
200 kg/cm <sup>2</sup>	53.6	1.25	4.30	11.1	80.8	1.60	3,65	4.0	29.8
400	53.9	1.26	4.32	11.4	81.1	1.60	3.65	4.0	29.5
600	54.2	1.26	4.30	11.3	81.6	1.61	3.65	4.0	29.3
800	54.3	1.26	4.28	11.3	81.7	1.61	3.64	4.0	29.0
,000	54.3	1.27	4.31	11,6	81.7	1.62	3.65	4.1	28.8
,200	54.3	1.27	4.29	11.5	81.7	1.62	3.63	4.0	28.6

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where  $f_1$ ,  $f_2$  and  $f_3$  are the activity coefficients of  $M^{z_+}$ ,  $SO_4^{z_-}$  and  $M^{z_+} \cdot SO_4^{z_-}$ , respectively. In the dilute solution, the activity coefficients,  $f_1$  and  $f_2$ , are calculated from the Debye-Hückel limiting equation 7),

$$-\log f_i = z_i^2 \frac{1.291 \times 10^8}{(DT)^{3/2}} \Gamma^{1/2}, \qquad (13)$$

where  $\Gamma$  is the ional concentration  $\sum_{i} m_{i} z_{i}^{2}$ , D the dielectric constant of water and T the absolute temperature, and the activity coefficient of  $M^{2+} \cdot SO_{4}^{2-}$ ,  $f_{3}$  is assumed to be unity. Using the Onsager theoretical equation? for the equivalent ionic conductance in the right of Eq. (5), we obtain

$$\Lambda = \alpha (\Lambda^{\circ} - 4S\sqrt{m\alpha}), \tag{14}$$

where S is the function of D,  $\eta^{\circ}$  and  $\Lambda^{\circ}$ . The values of  $\alpha$  in Eq. (14) is solved by means of successive approximation. The dielectric constant of water at pressure P,  $D^{(P)}$  is determined from the Owen-Brinkley equation <sup>19)</sup>,

$$1 - \frac{D^{(1)}}{D^{(P)}} = AD^{(1)} \log \frac{B+P}{B+1}, \tag{15}$$

where A and B are characteristic parameters of water. The viscosity data are graphically interpolated values from the measurements of Cappi  $^{11}$ ). The dissociation constant K thus determined from Eqs. (12), (13) and (14) at each pressure and temperature are listed in Table 3.

The dissociation constant increases with increasing pressure at each temperature. When the dissociation constant of the ion-pair, Ca<sup>2+</sup>·SO<sub>4</sub><sup>2-</sup> is compared with that of the ion-pair, Mg<sup>2+</sup>·SO<sub>4</sub><sup>2-</sup> at

Pressure	CaSO <sub>4</sub> (15°C)	CaSO <sub>4</sub> (25°C)	CaSO <sub>4</sub> (40°C)	MgSO <sub>4</sub> (25°C)
1 atm	$6.0 \times 10^{-3}$	4.9 × 10 <sup>-3</sup>	3.1 × 10 <sup>-3</sup>	5.8 × 10 <sup>-3</sup>
	5,3 × 10 <sup>-3</sup> (18°C)*)	$4.9 \times 10^{-3}$ b)	$4.1 \times 10^{-3}$ c)	4.4 × 10 <sup>-3</sup> e)
			$3.4 \times 10^{-3}$ d)	6.2 × 10-3 ()
200 kg/cm <sup>2</sup>	$7.1 \times 10^{-3}$	$5.0 \times 10^{-3}$	$3.3 \times 10^{-3}$	$6.7 \times 10^{-3}$
400	$7.7 \times 10^{-3}$	$5.5 \times 10^{-3}$	$3.4 \times 10^{-3}$	$7.4 \times 10^{-3}$
600	$8.1 \times 10^{-3}$	$5.8 \times 10^{-3}$	$3.5 \times 10^{-3}$	$7.5 \times 10^{-3}$
800	$9.9 \times 10^{-3}$	$6.3 \times 10^{-3}$	$3.7 \times 10^{-3}$	$7.7 \times 10^{-3}$
,000	$1.0 \times 10^{-2}$	$7.3 \times 10^{-3}$	$3.8 \times 10^{-3}$	8.1 × 10 <sup>-3</sup>
,200	$1.2 \times 10^{-2}$	$8.0 \times 10^{-3}$	$4.1 \times 10^{-3}$	$8.7 \times 10^{-3}$

Table 3 Dissociation constants of the ion-pair

- a) from conductivity 21)
- b) from solubility 22)
- c) from solubility 22)

- d) from solubility 23)
- e) from e.m.f. 24)
- f) from conductivity 25)
- 19) B. B. Owen and S. R. Brinkley, Phys. Rev., 64, 32 (1943)
- 20) K. W. Kunttz and R. M. Fuoss, J. Phys. Chem., 67, 914 (1962)
- 21) C. W. Davies, Trans. Faraday Soc., 23, 351 (1927)
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- 23) A. W. Gardner and E. Gluekauf, ibid., 66, 1081 (1970)
- 24) H. W. Jones and C. B. Monk, ibid., 48, 929 (1952)
- 25) H. S. Dunsmore and J. C. James, J. Chem. Soc., 1951, 2925

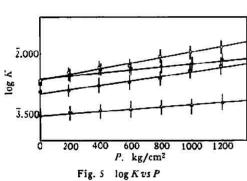
25°C, the former is smaller at each pressure. It was observed by Kuntz and Fuoss  $^{20)}$  that in NaCl, KCl and RbCl solutions, the larger the crystal radius of a cation is, the smaller the dissociation constant. Figs. 5 and 6 show the variation of  $\log K$  with pressure and temperature, respectively. From these plots, the thermodynamic parameters concerning the dissociation of the ion-pair (Eq. (11)) were calculated from the following relations,

$$\Delta \overline{G}^{\circ} = -RT \ln K \,, \tag{16}$$

$$\left(\frac{\partial \ln K}{\partial P}\right)_T = -\frac{\Delta \overline{V}^c}{RT},\tag{17}$$

$$\left(\frac{\partial \ln K}{\partial (1/T)}\right)_{P} = -\frac{\Delta \overline{H}^{0}}{R}.$$
 (18)

$$d\overline{S}^{\circ} = \frac{\Delta \overline{H}^{\circ} - \Delta \overline{G}^{\circ}}{T} \,. \tag{19}$$



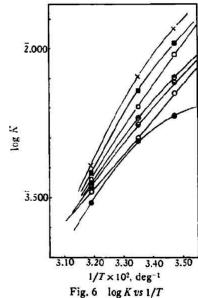


Fig. 6  $\log K vs 1/T$ atm.  $\bigcirc$ : 200k

1 atm,
 200 kg/cm²
 600 kg/cm²
 800 kg/cm²
 1,000 kg/cm²
 1,000 kg/cm²

×: 1,200 kg/cm<sup>2</sup>

The derived thermodynamic parameters are given in Table 4. Our value of  $\Delta \overline{V}^{\circ}$  in the dissociation of  $Mg^{2+} \cdot SO_4^{2-}$  at 25°C, -7.7 cc/mole, is in good agreement with Fisher's value,  $-7.3 \pm 0.4$  cc/mole <sup>26</sup>. The negative values of  $\Delta \overline{V}^{\circ}$ ,  $\Delta \overline{H}^{\circ}$  and  $\Delta \overline{S}^{\circ}$  would be due to the change of hydration number and the

<sup>26)</sup> F. H. Fisher, J. Phys. Chem., 66, 1607 (1962)

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Table 4	Thermodynami	c parameters	concerned	with the	dissociation	of the ion-pair
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		$\Delta \overline{V}$ (m	l/mole)		∆H̄.	⊿G* (kcal/mole)	₫а (e.u.)
Pressure	CaSO <sub>4</sub> (15°C)	CaSO <sub>4</sub> (25°C)	CaSO <sub>4</sub> (40°C)	MgSO <sub>4</sub> (25°C)	(kcal/mole) CaSO <sub>4</sub>	CaSO <sub>4</sub> (25°C)	CaŠO, (25°C)
1 atm				T	-4.7	3.1	- 26.2
200 kg/cm <sup>2</sup>			"		- 5.4	3.1	<b>— 28.5</b>
400					-5.7	3.1	- 29.5
600	-12.9	-10.2	-5.7	-7.7	-5.8	3.0	- 29.5
800				Ţ	-6.8	3.0	- 32.9
1,000					-7.1	2.9	-33.5
1,200			ĕ		<b>-7.4</b>	2.9	- 34.5

contraction of the hydrated molecules by the electrostriction in the dissociation process. The  $|\overline{JV}^\circ|$  of the dissociation of  $\operatorname{Ca^{2+}} \cdot \operatorname{SO_4^{2-}}$  decreases with increasing temperature as in the case of  $[\operatorname{Co}(\operatorname{NH_3})_6]^{3+} \cdot \operatorname{SO_4^{2-}} 5$ . According to Mukerjee<sup>27)</sup>, the volume change ammounts to -56 cc/mole in the process of the dissolution of the salt MgSO<sub>4</sub> into water and perhaps the similar ammount would be expected for the salt, CaSO<sub>4</sub>. But the value of  $|\overline{JV}^\circ|$ , |-7.7 cc/mole| obtained in this experiment are far smaller than the value, |-56 cc/mole| mentioned above. This would indicate that the ion-pairs,  $\operatorname{Ca^{2+}} \cdot \operatorname{SO_4^{2-}}$  and  $\operatorname{Mg^{2+}} \cdot \operatorname{SO_4^{2-}}$  are already hydrated to some extent and attract its surrounding water molecules with electrostrictive force. The  $|\overline{JV}^\circ|$  of the ion-pair,  $\operatorname{Ca^{2+}} \cdot \operatorname{SO_4^{2-}}$  is larger than that of the ion-pair,  $\operatorname{Mg^{2+}} \cdot \operatorname{SO_4^{2-}}$ . It may be due to less hydration of  $\operatorname{Ca^{2+}} \cdot \operatorname{SO_4^{2-}}$  than that of  $\operatorname{Mg^{2+}} \cdot \operatorname{SO_4^{2-}}$ .

The closest approach distance, a, is obtained by putting the dissociation constant in this experiment into the theoretical equation of Fuoss<sup>28</sup>),

$$K = \frac{3000}{4\pi N a^3} \exp\left(-\frac{|z_+ \cdot z_-|e^2|}{aDkT}\right), \qquad (20)$$

where k is the Boltzmann constant and N Avogadro's number. The results are listed in Table 5. At 40°C the closest approach distance gradually decreases with increasing pressure, but at other temperatures the systematic changes by pressure are not observed. The bulk dielectric constant was used for the calculation of the closest approach distance. In the vicinity of the ion, the dielectric constant would be smaller than that of bulk water, as the dipoles of the water molecules in the vicinity of the ion are oriented by electrostrictive force. Using the effective dielectric constant, the values of the closest approach distance would become larger than those in Table 5. Therefore, the closest approach distances at 15 and 25°C in aqueous solution would be larger than the sum of the crystal radii cited in Table 5 and also at 40°C those may be somewhat larger. Hence, the ion-pair may contain some water molecules between the cation and anion. This is in good agreement with the result by ultrasonic absorption 4). The closest approach distance of the Ca<sup>2+</sup>·SO<sub>4</sub><sup>2-</sup> ion-pair is smaller than that of the Mg<sup>2+</sup>·SO<sub>4</sub><sup>2-</sup> ion-pair at 25°C at each pressure, in spite of the fact that the former has a larger sum of the

<sup>27)</sup> P. Mukerjee, J. Phys. Chem., 65, 740 (1960)

<sup>28)</sup> R. M. Fuoss, J. Am. Chem. Soc., 80, 5059 (1958)

#### Electrical Conductivity of CaSO4 in Aqueous Solution under High Pressure

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Table 5	Changes in	the closect ar	proach distances	hy pressure
I AUIC J	CHUIL CO III	rite creasear at	DIOUCH GISCAHCES	Dy prossure

Pressure	$a(\mathbf{\mathring{A}})$			
	CaSO <sub>4</sub> (15°C)	CaSO <sub>4</sub> (25°C)	CaSO <sub>4</sub> (40°C)	: MgSO <sub>4</sub> (25°C)
1 atm	4.10	4.02	3.72	4.17
200 kg/cm <sup>2</sup>	4,21	3.95	3.71	4.26
400	4.22	3.97	3.68	4.29
600	4.19	3.95	3.65	4.23
800	4,34	3.97	3.63	4.19
1,000	4.35	4.03	3.60	4.17
1,200	4.42	4.10	3,60	4.19
Sum of the crystal radii		3,72		3,38

crystal radii. This corresponds to the larger value of  $|\overline{\Delta V}|$  of the Ca<sup>2+</sup>·SO<sub>4</sub><sup>2-</sup> ion-pair than that of the Mg<sup>2+</sup>·SO<sub>4</sub><sup>2-</sup> ion-pair and to the smaller hydration number of Ca<sup>2+</sup> than that of Mg<sup>2+</sup>. These would mean that the Ca<sup>2+</sup>·SO<sub>4</sub><sup>2-</sup> ion-pair has less number of water molecules between the cation and anion than the Mg<sup>2+</sup>·SO<sub>4</sub><sup>2-</sup> ion-pair. The closest approach distance decreases with increasing temperature in Ca<sup>2+</sup>·SO<sub>4</sub><sup>2-</sup> ion-pair as in the case of [Co(NH<sub>3</sub>)<sub>6</sub>]<sup>2+</sup>·SO<sub>4</sub><sup>2-</sup>. That is, the ion-pair would gradually approach to contact one with increasing temperature 29.30).

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<sup>29)</sup> T. Ellingsen and J. Smid, J. Phys. Chem., 73, 2712 (1969)

<sup>30)</sup> J. H. Beard and P. H. Plesch, J. Chem. Soc., 1964, 4879.