

Performance of Gas Turbine-Based Plants During Frequency Drops

Naoto Kakimoto, *Member, IEEE*, and Kazuhiro Baba

Abstract—A combined cycle power plant, which combines a gas turbine and a steam turbine, can achieve high energy efficiency. Many combined cycle plants have been installed in the world. However, a large-scale blackout occurred in Malaysia in 1996. Combined cycle and gas turbine plants sequentially tripped out. The cause of this chain trip was thought to be a system frequency drop. Considering these backgrounds, it is important to study dynamic behavior of combined cycle plants. Several dynamic models of the combined cycle plant have been proposed. In our analysis, we use some of them and build a model for a single-shaft combined cycle plant. We execute numerical simulations to see how the combined cycle behaves when the system frequency drops.

Index Terms—Combined cycle, dynamic models, gas turbine, plant trip-out, under frequency.

I. INTRODUCTION

A combined cycle power plant, which combines a gas turbine and a steam turbine, can achieve high energy efficiency. The plant mainly consists of a gas turbine, a waste heat recovery boiler, and a steam turbine. This type of plant has high energy efficiency which exceeds 50%. Many combined cycle plants have been installed in Japan. Their capacity is about 20 000 MW and 10% of the total generation.

However, a large-scale blackout occurred in Malaysia in 1996 [1]. Following a frequency drop of about 1.5 Hz, combined cycle and gas turbine plants sequentially tripped out. The total generation loss was 5760 MW. Because of its importance, several studies were made on responses of combined cycle power plants to frequency drops [2]–[4]. Some models were developed based on models in [5] and [6] to represent practical plants, and then used to calculate responses to frequency changes. However, detailed analysis has not been made yet regarding how plant variables behave for frequency drops.

In this paper, we analyze dynamic behavior of a combined cycle plant for frequency drops. Several dynamic models of the combined cycle plant have been proposed [2]–[6]. We combine some of them and build a model for a single-shaft combined cycle plant. We execute numerical simulations to see how the combined cycle plant behaves when the system frequency drops.

II. COMBINED CYCLE PLANT

Fig. 1 shows a single-shaft combined cycle plant. The plant consists of a compressor, combustor, gas turbine, waste heat recovery boiler, steam turbine, and a generator. The compressor compresses air, and sends it to the combustor. The combustor

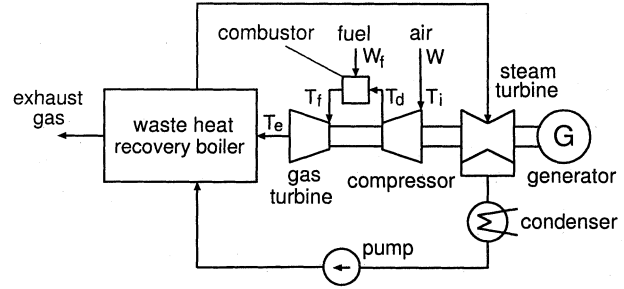


Fig. 1. Single-shaft combined cycle plant.

burns this air with fuel, and makes high temperature and high pressure combustor gas. This combustor gas drives the gas turbine. The waste heat recovery boiler collects some energy of exhaust gas, and drives the steam turbine. Plant power output is the sum of the gas turbine and the steam turbine power outputs. The gas turbine produces about two thirds of the total power output, and the steam turbine produces the rest.

Since the air is adiabatically compressed, compressor discharge temperature T_d (K) is given as follows [6]:

$$T_d = T_i \left(1 + \frac{x - 1}{\eta_c} \right) \quad (1)$$

$$x = (P_{ro} W)^{\gamma - 1/\gamma} \quad (2)$$

where T_i (K) is compressor inlet temperature and equals ambient temperature, η_c is compressor efficiency, x is compressor temperature ratio, P_{ro} is design compressor pressure ratio, W is airflow in per unit of its rated value, and γ is ratio of specific heats. The airflow W depends on the ambient temperature T_i and the atmospheric pressure P_a

$$W = W_a \frac{P_a}{P_{ao}} \frac{T_{io}}{T_i} \quad (3)$$

where subscript “o” denotes rated value, and W_a is the airflow at P_{ao} and T_{io} . We assume $P_a = P_{ao}$.

Gas turbine inlet temperature T_f (K) is given by

$$T_f = T_d + (T_{fo} - T_{do}) \frac{W_f}{W} \quad (4)$$

where W_f is fuel flow in per unit of its rated value. The fuel flow is a negligible amount compared with the airflow.

Gas turbine exhaust temperature T_e (K) is described as follows:

$$T_e = T_f \left[1 - \left(1 - \frac{1}{x} \right) \eta_t \right] \quad (5)$$

where η_t is turbine efficiency. The exhaust gas flow is practically equal to the airflow.

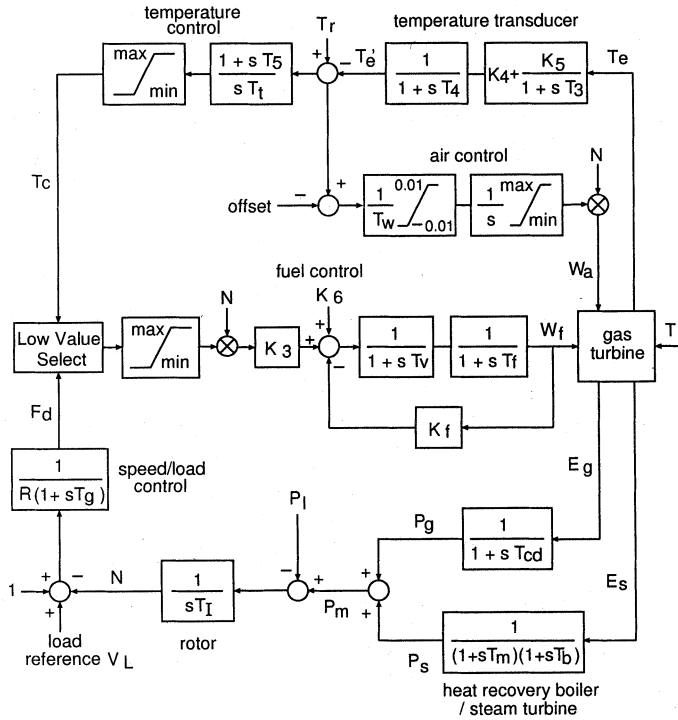


Fig. 2. Model of combined cycle.

III. MODEL

Fig. 2 shows a model of the combined cycle plant. It consists of several blocks. There are four blocks related with speed/load control, temperature control, fuel control, and air control. Remaining blocks describe gas turbine, waste heat recovery boiler/steam turbine, rotor shaft, and temperature transducer. The input and output variables of each block are linked as shown in the figure. This model is based on models of [5] and [6], whose validity has been tested in [2]–[4] and [7]. We briefly review each block.

The speed/load control block determines the fuel demand F_d according to the load reference V_L and the rotor speed deviation $(1 - N)$. Descriptions of parameters are provided in the Appendix in Table 1 and Table 2.

The temperature control block restricts the exhaust temperature T_e ($^{\circ}\text{C}$) not to injure the gas turbine. The measured exhaust temperature T'_e is compared with the reference temperature T_r ($^{\circ}\text{C}$). The output is the temperature control signal T_c .

The fuel demand F_d is compared with the temperature control signal T_c in the fuel control block. The lower value is selected by the low value selector, and it determines the fuel flow W_f .

The air control block adjusts the airflow W so as to attain the desired exhaust temperature [8]. The exhaust temperature T_e ($^{\circ}\text{C}$) is kept lower than T_r ($^{\circ}\text{C}$), by an appropriate offset, for example, 1% of its rated value. T'_e is used for T_e , again. The airflow is adjusted by compressor inlet guide vanes (IGV). Based on explanations in [8] and [2], we use the model in Fig. 2. The adjustable airflow is about 30% of the rated airflow. The adjusting speed is slow compared with the fuel flow. We assume the airflow changes at 1%/s at most from the test in [3]. The airflow W_a is proportional to the rotor speed N [6].

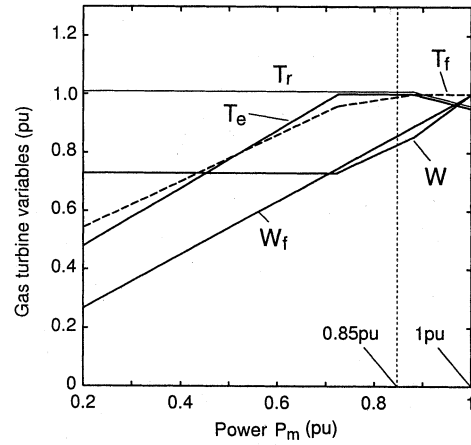


Fig. 3. Heatbalance.

Once the fuel flow W_f , the airflow W_a , and the inlet temperature T_i are given, the temperatures T_d , T_f , T_e , and the airflow W are determined by (1)–(5). With these values, the net energy supplied to the gas turbine is given by

$$E_g = K_0 \{ (T_f - T_e) - (T_d - T_i) \} W \quad (6)$$

where K_0 is a constant. This energy is converted to the power P_g after a transport delay T_{cd} .

The energy collected by the heat recovery boiler and the steam turbine is

$$E_s = K_1 T_e W \quad (7)$$

where K_1 is a constant. This energy changes to the power P_s after time delays denoted by T_m and T_b .

By summing P_g and P_s , we obtain the plant power output P_m . The rotor speed N varies if there is any difference between the power output P_m and the load power P_l . In this paper, P_l is assumed to be proportional to N^α , where α is a constant. T_l is the time constant of the rotor.

IV. CASE STUDY

There are many power plants in practical power systems. In this study, we consider a small system composed of a combined cycle plant and a load. Their models have been described in the preceding section. We regard this system as a part of a large system.

A. System Parameters

As an example, we consider a 1100 $^{\circ}\text{C}$ class single-shaft combined cycle plant. Its rated power output is 160 MW (gas turbine 106.7 MW, steam turbine 53.3 MW). On the gas turbine, we use typical parameters provided in [5], while they change for practical turbines [7]. As for the steam turbine, we use parameters in [6]. The parameters are listed in the Appendix.

Fig. 3 specifies how to control the exhaust temperature. The fuel flow W_f linearly increases with the power output P_m . The exhaust temperature T_e rises and reaches its rated value. The airflow control in Fig. 2 begins to increase the airflow W in order to keep T_e constant. If T_e exceeds the reference temperature T_r ,

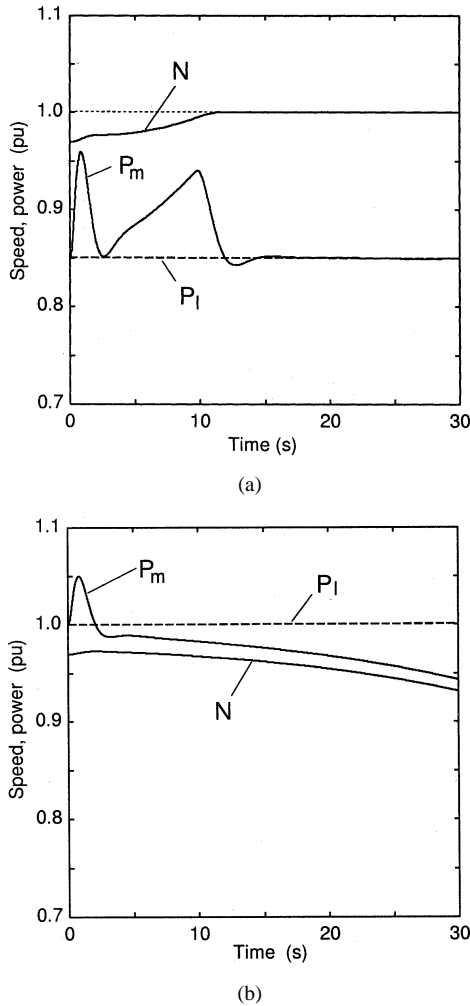


Fig. 4. Response to frequency drop (0.97 p.u.). (a) $P_{mi} = 0.85$ p.u. (b) $P_{mi} = 1$ p.u.

the temperature control acts. Its dynamics is shown in Fig. 2, too. T_r is higher than T_e by 1%. The turbine inlet temperature T_f still increases. If T_f reaches its rated value, W increases more rapidly for T_f not to rise any more. T_e decreases as a result to 95% at the rated power. The exhaust temperature is thus kept high at part load conditions. This airflow control facilitates collection of exhaust gas energy in the waste heat recovery boiler [8].

B. Response to Frequency Drop

First, we consider cases in which this system is separated from the large system with a balanced load following a frequency drop. Fig. 4 shows two cases where the frequency instantly drops to 0.97 p.u., and the initial power output P_{mi} is 0.85 or 1 p.u. P_l is assumed to be constant (i.e., $\alpha = 0$), and accordingly $P_l = P_{mi}$.

Fig. 4(a) shows the case where the initial power output P_{mi} is 0.85 p.u. The rotor speed N drops to 0.97 p.u., but returns to the normal value in 12 s. The system is stable in this case. The power output P_m quickly increases, and quickly decreases. Since its value is nearly equal to P_l , the rotor is not accelerated for a few moments. However, P_m slowly increases, and exceeds P_l . The rotor consequently recovers speed.

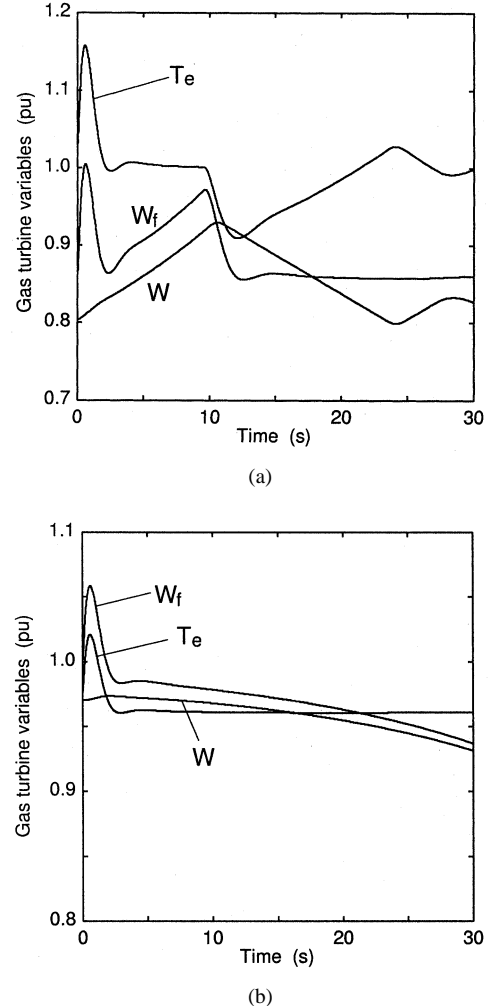


Fig. 5. Response to frequency drop (0.97 p.u.). (a) $P_{mi} = 0.85$ p.u. (b) $P_{mi} = 1$ p.u.

Fig. 4(b) shows the case where P_{mi} is 1 p.u. In this case, the rotor speed N continues to fall, and does not return to the normal value. This is an unstable case. The initial increase and decrease in P_m is similar to the stable case. However, after that, P_m slowly decreases. Its value is lower than P_l , and accordingly the rotor loses speed with time.

C. Analysis of Plant Outputs

As observed in Fig. 4, the rotor speed is governed by P_m , so it is important to understand its behavior.

Fig. 5 shows three variables W_f , T_e , and W . The time variation of the fuel flow W_f is similar to that of P_m in Fig. 4. Since the rotor speed N drops, the speed control increases W_f . However, the exhaust temperature T_e rises simultaneously, and it exceeds the reference temperature T_r . The temperature control then acts to restrict the fuel flow. These controls explain the initial behavior of P_m .

The exhaust temperature T_e lowers below the reference temperature $T_r = 1.01$ pu in Fig. 5(a). However, T_e remains above $T_r = 0.96$ pu in Fig. 5(b). This difference is caused by the airflow control. The airflow is adjusted by the IGVs in reference to the exhaust temperature T_e . When the initial power output P_{mi} is 0.85 p.u., the airflow W increases slowly. As a result,

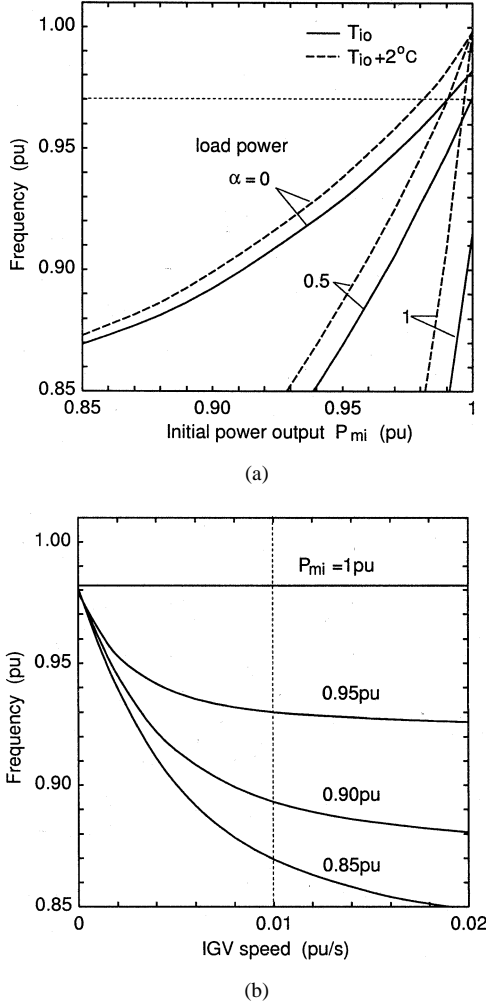


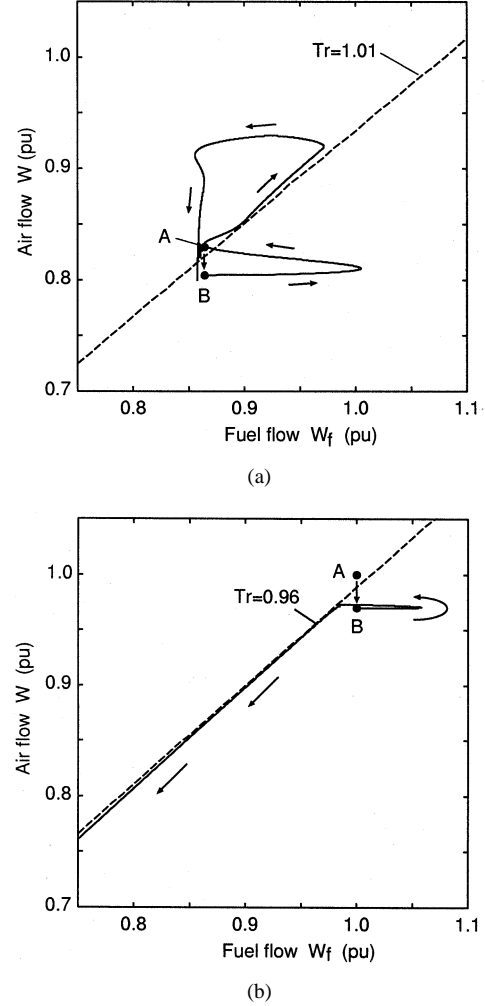
Fig. 6. Critical frequency.

the exhaust temperature lowers, which subsequently allows the fuel flow W_f to increase. The slow increase in P_m is thus explained. However, when P_{mi} is 1 p.u., the IGVs are fully open and the airflow does not increase any more. Hence, any increase in the fuel flow is suppressed by the temperature control.

D. Critical Frequency

The system is stable for the frequency drop to 0.97 p.u. when P_{mi} is 0.85 p.u. However, if the frequency drops below a critical value, the system becomes unstable. Fig. 6 shows some variations of the critical frequency.

In Fig. 6(a), the initial power output P_{mi} is changed, where the load power P_l is proportional to N^α . The solid lines show cases in which the ambient temperature T_i is T_{io} . First, we observe the case of $\alpha = 0$ (i.e., constant power). The critical frequency rises as P_{mi} increases. For example, the system is stable for a 13% frequency drop at $P_{mi} = 0.85 \text{ p.u.}$, but it becomes unstable for a 2% frequency drop at $P_{mi} = 1 \text{ p.u.}$ The system at $P_{mi} = 1 \text{ pu}$ is therefore weak for frequency drops. Next, we change α from 0 to 3. Since the load power P_l decreases in proportion to N^α , the system becomes more stable as α increases. If $\alpha > 1.26$, the system is stable for 15% or more frequency drops. The broken lines in the figure show cases where the ambient temperature is higher than T_{io} by 2°C . In these cases, the

Fig. 7. Fuel flow and air flow. (a) $P_{mi} = 0.85 \text{ p.u.}$ (b) $P_{mi} = 1 \text{ p.u.}$

critical frequency moves upward. This is conspicuous when P_{mi} is 1 p.u. The system becomes unstable for a frequency drop to 0.997 p.u. These results are related with the frequency characteristics of the power output P_m . We examine it in Section VI.

In Fig. 5(a), the airflow varies slowly. If it varies faster, the fuel flow can increase more rapidly while keeping the exhaust temperature under T_r . Its speed may affect the stability of the system. Fig. 6(b) shows some variation of the critical frequency with the IGV speed, where $\alpha = 0$. For $P_{mi} = 0.85 \sim 0.95 \text{ pu}$, the critical frequency lowers as the IGV speed increases. Conversely, it rises as the IGV speed reduces. This is what we expected. However, if $P_{mi} = 1 \text{ p.u.}$, the IGV speed does not influence the critical frequency at all. The reason is that the IGVs are fully open, and that the airflow does not increase.

V. EFFECT OF TEMPERATURE CONTROL

The temperature control is a crucial factor in the above phenomenon. The exhaust temperature is determined by the fuel flow and the airflow, and it determines whether the temperature control operates or not. In this section, we examine the phenomenon in terms of the fuel flow and the airflow.

Fig. 7 shows how the fuel and air flows move on the W_f - W plane, where their values are taken from Fig. 4. For simplicity,

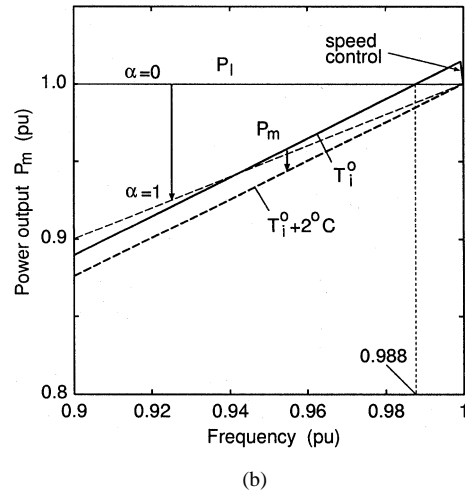
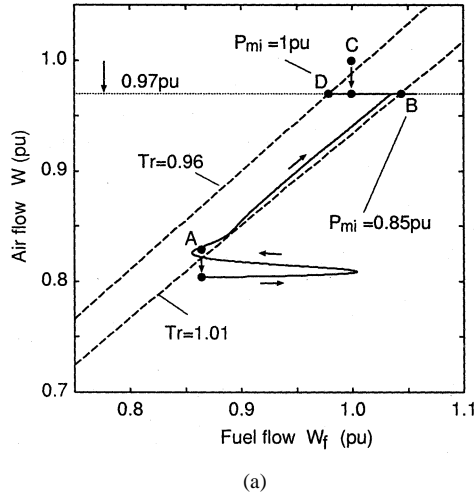


Fig. 8. Response to constant frequency drop.

we call a point (W_f, W) “state.” In Fig. 7(a), the state moves from A to A via B. The broken line shows combinations of W_f and W corresponding to the exhaust temperature 1.01 p.u. or 0.96 p.u. Under the line, the exhaust temperature is higher than the reference temperature T_r , and the temperature control acts.

Fig. 7(a) shows the case where the initial power output P_{mi} is 0.85 p.u. The state jumps from A to B immediately after the frequency drop, and then it moves right due to the speed control. Since the state is under the broken line, the temperature control moves the state left. As the airflow slowly increases, the state moves upward along the broken line. Once the rotor recovers speed, the state moves left and then downward. The state finally returns to A.

Fig. 7(b) shows the case where P_{mi} is 1 p.u. The broken line corresponds to the exhaust temperature 0.96 p.u. The state jumps from A to B, moves right, and then left. This is similar to Fig. 7(a). However, the inlet guide vanes are full-open, and the airflow does not increase. Furthermore, the airflow slowly decreases because it is proportional to the rotor speed. The fuel flow is restricted by the temperature control. As the rotor loses speed, the state moves downward along the broken line.

It is thus observed that the state moves along the broken line under the temperature control.

TABLE I
GAS TURBINE PARAMETERS

parameter	value
T_{i0}	compressor inlet temperature 30 (°C)
T_{d0}	compressor discharge temperature 390 (°C)
T_{f0}	gas turbine inlet temperature 1085 (°C)
T_{e0}	gas turbine exhaust temperature 532 (°C)
P_{r0}	compressor pressure ratio 11.5
γ	ratio of specific heat 1.40
η_c	compressor efficiency 0.85
η_t	turbine efficiency 0.85
K_0	gas turbine output coefficient 0.003030
K_1	steam turbine output coefficient 0.000428

TABLE II
COMBINED CYCLE PARAMETERS

parameter	value
R	speed regulation 25
T_g	governor time constant 0.05
K_4	gain of radiation shield 0.8
K_5	gain of radiation shield 0.2
T_3	radiation shield time constant 15
T_4	thermocouple time constant 2.5
T_5	temperature control time constant 3.3
T_t	temperature control integration rate 250
T_{cmax}	temperature control upper limit 1:1
T_{cmin}	temperature control lower limit 0
F_{dmax}	fuel control upper limit 1.5
F_{dmin}	fuel control lower limit -0.1
K_3	ratio of fuel adjustment 0.77
K_6	fuel valve lower limit 0.23
T_v	valve positioner time constant 0.05
K_f	fuel system feedback constant 0
T_f	fuel system time constant 0.4
W_{max}	air control upper limit 1.0
W_{min}	air control lower limit 0.73
T_w	air control time constant 250
T_{cd}	compressor volume time constant 0.2
T_m	tube metal heat capacitance time constant of waste heat recovery boiler 5
T_b	boiler storage time constant of waste heat recovery boiler 20
T_I	turbine rotor time constant 18.5

VI. FIXED FREQUENCY

Fig. 7 corresponds to cases where a combined cycle plant is separated from a large system, and its rotor speed varies with time. In this section, we consider a plant in a large system whose frequency is not affected by the plant.

Fig. 8(a) shows some variation of the fuel and air flow. The frequency instantly drops to 0.97 p.u. again, and the rotor speed N is fixed at this value. If P_{mi} is 0.85 p.u., the state moves from A to B. The airflow increases till the inlet guide vanes fully open, and the fuel flow increases until the exhaust temperature reaches 1.01 p.u. If P_{mi} is 1 p.u., the state moves from C to D. The inlet guide vanes are full-open, and the fuel flow is restricted by the temperature control. If T_r is adjusted to 0.96 p.u. to protect the gas turbine, the point B moves to D.

Fig. 8(b) shows the power output P_m at the point D. P_m varies with the frequency. P_m is smaller than P_t (1 p.u.) for frequencies below 0.988 p.u. For example, P_m decreases to 0.977 p.u. at the frequency 0.97 p.u., so the system needs 2.3% power reserve for 3% frequency drop. If the ambient temperature T_i is higher than T_{i0} by 2°C, P_m moves downward. This is because the exhaust temperature T_e rises according to (1)–(5), and the temperature

control overrides the speed/load control. Almost the same result is obtained when the offset in the air control is zero, and accordingly T_r is 0.95 p.u. The power output P_m is nearly proportional to $N^{1.26}$. This explains the results in Fig. 6(a). When P_l is constant ($\alpha = 0$) or proportional to N ($\alpha = 1$), P_m decreases faster than P_l , so appropriate power reserve must be prepared. It has been shown by tests that many loads have $\alpha \leq 1$ [9], [10]. The characteristics of P_m is therefore important, and some investigation has been made in [4].

VII. CONCLUSIONS

In this paper, we examined how a single-shaft combined cycle plant behaves for frequency drops. The obtained results are summarized as follows:

- 1) Following a frequency drop, the temperature control soon overrides the speed control, and restricts the fuel flow about its initial value.
- 2) The fuel flow then slowly increases as the inlet guide vanes open. Their speed considerably affects the stability of the plant.
- 3) If the inlet guide vanes open fully, the temperature control and the frequency determine the fuel flow and accordingly the power output.
- 4) The power output is approximately proportional to $N^{1.26}$ in our model. This frequency characteristics must be considered in estimating power reserve.

Lastly, although this paper addresses a combined cycle plant, the above results are applicable to any gas turbine-based plant which operates at or near exhaust gas temperature limits.

APPENDIX

See Table 1 and Table 2 on previous page.

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