\textbf{55}Mn NMR and NQR study of the cubic Laves-phase compound UMn$_2$

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We performed $^{55}$Mn NMR and nuclear quadrupole resonance (NQR) measurements of a cubic Laves-phase compound UMn$_2$, which shows structural instability in the temperature range 210–240 K. NMR and NQR signals of two different crystallographic Mn sites, which are in nearly axial and nonaxial electric field gradients, were found below structural transitions, being consistent with the crystal structure determined from diffraction analysis and confirming the absence of magnetic ordering. Analysis of the Knight shift shows that the spin component of the isotropic hyperfine coupling constant does not change at the phase transitions, and the anisotropy of the Knight shift appreciably depends on temperature. The nuclear spin-lattice relaxation is not enhanced except around the structural transitions and is explained as simple conduction-electron relaxation, indicating absence of localized moments at both U and Mn sites. The relaxation behavior also suggests neither critical behavior nor strong electron correlation in the low-temperature range.

I. INTRODUCTION

The subject of moment stability and magnetic order in the presence of topological frustration in the Laves-phase compounds $RMn_2$ ($R =$ rare earth) continues to attract a great deal of experimental and theoretical attention. The stability of manganese moment is closely related to the lattice parameter, i.e., the Mn-Mn distance.$^{1-3}$ In general magnetic moment in the Mn sublattice becomes unstable when the Mn-Mn distance is below a critical value ($\approx$ 2.7 Å), resulting in nonmagnetic Mn atoms. On the other hand, the compounds have stable moment when the lattice parameter is above the critical value. Magnetic structures in magnetically ordered states are complicated because of competing interactions among $R$-$R$, Mn-Mn and $R$-Mn. In the vicinity of the critical lattice parameter, a mixed phase, in which magnetic and nonmagnetic Mn atoms coexist, was observed by microscopic probes such as neutron diffraction, nuclear magnetic resonance (NMR), and Mössbauer experiments.$^{4-9}$ Due to the Mn moment instability, Mn atoms in $RMn_2$ can be magnetic or nonmagnetic depending on the rare earth element, temperature, pressure, etc.

On the other hand, uranium magnetism has also been investigated extensively. The 5$f$ electrons may be itinerant or localized depending on the local environment. The interplay between the two state gives rise to exotic phenomena like heavy-fermion and spin-fluctuation behaviors. The stability of U localized moment is related with the U-U interatomic distance. It has been argued that U compounds have localized moments when the U-U distance is larger than the critical value ($\approx$ 3.5 Å), so-called Hill limit.$^{10}$ The Laves-phase compounds UT$_2$ ($T =$ transition metal) are attractive candidates to study the U moment instability since the U-U distance in UT$_2$ distributes around the critical value depending on $T$.

The Laves-phase compound UMn$_2$ exhibits the C15 cubic structure (space group $Fd\bar{3}m$) with the lattice parameter $a = 7.16$ Å at room temperature.$^{11,12}$ UMn$_2$ undergoes a rhombohedral distortion to the space group $R\bar{3}m$ on cooling below $\approx 240$ K. Further cooling below below $\approx 210$ K results in a second structural change to the orthorhombic space group $Imma.$$^{12-15}$ These transition temperatures seem to slightly depend on samples (about $\pm 10$K). Despite the discontinuity of lattice constants at the transitions, the variation in unit cell volume is continuous with temperature.$^{14}$

Although the susceptibility shows a Curie-Weiss-like behavior with an effective moment 4.15 $\mu_B$ at high temperatures ($>420$ K),$^{16}$ the temperature dependence of the susceptibility (see the inset in Fig. 6) is weak at the lower temperatures and shows a maximum at $\approx 240$ K,$^{17,18}$ which was speculated to be an antiferromagnetic transition temperature at an early stage of the study.$^{17}$ The specific heat shows a $\lambda$-type anomaly at $\approx 240$ K,$^{18}$ suggesting a second-order transition. On the other hand, no evidence of magnetic ordering has been found in neutron diffraction studies.$^{11}$ A Mössbauer study on $U(Mn_{0.9}Fe_{0.1})_2$ also exhibits the absence of localized moment.$^{19}$ Therefore, the ground-state magnetic properties of UMn$_2$ have attracted much interest. The susceptibility shows a marked upturn below $\approx 50$ K, although there seems to be a strong sample dependence.$^{16-18}$ Like iso- morphous UAl$_2$, which is one of strongly correlated U compounds, UMn$_2$ exhibits a $T^2$ dependent resistivity at low temperatures,$^{18}$ together with an enhanced $\gamma$ of 41 mJ/mol K$^2$ in specific heat,$^{15}$ suggesting strong spin fluctuations. The muon spin relaxation rate discontinuously changes below $\approx 40$ K,$^{15}$ where the susceptibility shows a marked upturn on further cooling, suggesting possible U spin fluctuations.

As another aspect of UMn$_2$, the structural instability of the cubic Laves phase has attracted much attention. It is now a general consensus that the structural transition is not accompanied by magnetic ordering. Among a number of Laves phases only a few of them exhibit such a low-temperature structural instability. However, the physical mechanism for the lattice instability remains to be explained.

Thus UMn$_2$ locates an interesting position in the study of manganese and uranium magnetism. However, the nature of the magnetic state of UMn$_2$ remains controversial and needs
The present study, we report the results of $^{55}$Mn NMR and structural distortion to the space group $R\overline{3}m$ with $3\overline{4}m$ as the limit of no distortion, where a point charge on nearest neighbor atomic sites indicates larger relaxation time, $T_1$, was measured by observing the recovery of the NQR or NMR spin-echo after the saturation of nuclear spin levels by a single RF pulse. The nuclear gyromagnetic ratio for $^{55}$Mn, $\gamma/2\pi = 1.050$ MHz/kOe, was used for analysis.

Details of the structural data for UMn$_2$ are summarized: Above 240 K the structure is of the cubic C15 type, whose space group is $Fd\bar{3}m$. Uranium and manganese atoms occupy the 8$a$ site with $\bar{4}3mm$ local symmetry and the 16$d$ site with $\bar{3}m$ local symmetry, respectively. The 16$d$ site is described as a network of corner-sharing regular tetrahedra, which is one of the typical geometrically frustrated lattices. A $^{55}$Mn nucleus (nuclear spin $I = \frac{7}{2}$) at the 16$d$ site feels a finite electric field gradient (EFG), $e_q = V_{zz}$, with the zero asymmetry parameter, $\eta = (V_{xx} - V_{yy})/V_{zz}$, where $V_{xx}$, $V_{yy}$, and $V_{zz}$ are diagonal components of the EFG tensor. According to Lawson et al.,$^{13,14}$ UMn$_2$ undergoes a rhombohedral structural distortion to the space group $R\bar{3}m$ at $\sim 240$ K. Further decreasing temperature it exhibits a second structural transition at $\sim 210$ K to an orthorhombic crystal structure with the space group $Imma$. The orthorhombic phase is obtained by the shearing of a pair of counter (100) planes of the cubic phase. The orthorhombic lattice constants, $a_o$, $b_o$, and $c_o$ are equal to $a_c/\sqrt{2}$, $a_c/\sqrt{2}$ and $a_c$, respectively, in the limit of no distortion, where $a_c$ means the lattice constant of the cubic phase. Lawson et al.$^{14}$ reported $a_o = 4.8163$ Å, $b_o = 5.2478$ Å and $c_o = 7.1820$ Å at 12 K. Then, the distortion to the $a_o$ and $b_o$ directions are approximately 4–5% at 12 K.

In the orthorhombic phase, U atoms occupy the 4$e$ site with $mm2$ local symmetry and the manganese site separates to two different sites, i.e., 4$b$ and 4$d$ sites. The relation between the 16$d$ Mn site in the cubic phase and the 4$b$/4$d$ sites is sketched in Fig. 1. Associated with the orthorhombic distortion, two of four Mn atoms in a tetrahedron approach each other and the other two become more distant. As a result, the Mn site separates to two different crystallographic sites with the same population ratio. The axial symmetry is lost in the 4$b$ and 4$d$ sites; site symmetry of both the sites is $2/m$. Therefore, we expect EFG with finite $\eta$ for both the sites. However, symmetry considerations taking into account only point charge on nearest neighbor atomic sites indicates larger $\eta$ for the 4$d$ site than the 4$b$ site. The local principal axis at both the sites is expected to lie in the $c$ plane.

II. EXPERIMENTAL PROCEDURES

A polycrystalline ingot of UMn$_2$ was prepared by using a tri-arc furnace in an argon atmosphere at the Oarai Branch, Institute of Materials Research, Tohoku University. For nuclear resonance experiments the ingot was crushed into a fine powder in an inert atmosphere. To insulate each particle the powder was soaked in paraffin.

NMR and NQR measurements were carried out with a phase-coherent pulsed spectrometer. The nuclear spin-lattice relaxation time, $T_1$, was measured by observing the recovery of the NQR or NMR spin-echo after the saturation of nuclear spin levels by a single RF pulse. The nuclear gyromagnetic ratio for $^{55}$Mn, $\gamma/2\pi = 1.050$ MHz/kOe, was used for analysis.

In the orthorhombic phase, U atoms occupy the 8$a$ site with $4.8163$ Å, $5.2478$ Å and $7.1820$ Å at 12 K. Then, the distortion to the $a_o$ and $b_o$ directions are approximately 4–5% at 12 K. In the orthorhombic phase, U atoms occupy the 4$e$ site with $mm2$ local symmetry and the manganese site separates to two different sites, i.e., 4$b$ and 4$d$ sites. The relation between the 16$d$ Mn site in the cubic phase and the 4$b$/4$d$ sites is sketched in Fig. 1. Associated with the orthorhombic distortion, two of four Mn atoms in a tetrahedron approach each other and the other two become more distant. As a result, the Mn site separates to two different crystallographic sites with the same population ratio. The axial symmetry is lost in the 4$b$ and 4$d$ sites; site symmetry of both the sites is $2/m$. Therefore, we expect EFG with finite $\eta$ for both the sites. However, symmetry considerations taking into account only point charge on nearest neighbor atomic sites indicates larger $\eta$ for the 4$d$ site than the 4$b$ site. The local principal axis at both the sites is expected to lie in the $c$ plane.

III. EXPERIMENTAL RESULTS

A. NQR results

At 4.2 K and in the zero external field condition, we found several nuclear resonance lines, which are shown in Fig. 2. Two pairs of lines were found at around 4 and 8 MHz. All the lines are well reproduced by Lorentzian functions as shown by solid curves in the figure. These lines are interpreted as $^{55}$Mn NQR. For the nuclear spin $I = \frac{7}{2}$ and in the case of sufficiently small $\eta$, the NQR lines are, in general, observed at

$$\nu_1 = \nu_Q \left(1 + \frac{59}{54} \eta^2\right), \quad \nu_2 = 2 \nu_Q \left(1 + \frac{11}{54} \eta^2\right),$$

where

FIG. 1. Mn sites in UMn$_2$. One tetrahedron formed by four Mn atoms is shown. Figure (a) shows the distortions of atomic displacement in the orthorhombic phase with respect to the cubic phase. Figure (b) shows a projection on the $c$ plane of the orthorhombic structure, where the distortion is exaggerated. Closed and open circles represent nearly axial 4$b$ and nonaxial 4$d$ sites, respectively.

FIG. 2. $^{55}$Mn NQR lines at 1.4 K. The resonances in (a) and (b) correspond to the transitions of $m = \pm 1/2 \leftrightarrow \pm 3/2$ and $m = \pm 3/2 \leftrightarrow \pm 5/2$, respectively.
\[ v_Q = \frac{3e^2 q Q}{2hI(2I-1)} \] (3.2) is the quadrupole resonance frequency. The low- and high-frequency lines, \( v_1 \) and \( v_2 \), correspond to transitions of \( m = \pm \frac{3}{2} \leftrightarrow \pm \frac{1}{2} \) and \( m = \pm \frac{1}{2} \leftrightarrow \pm \frac{3}{2} \), respectively. The experimental result indicates that at low temperature there are two different Mn sites which feel different EFG. The lines centered at \( v_1 = 4.010 \pm 0.001 \) and \( v_2 = 7.977 \pm 0.002 \) MHz are assigned to one of the sites and those at \( v_1 = 4.569 \pm 0.001 \) and \( v_2 = 8.309 \pm 0.002 \) MHz to the other. On using Eq. (3.1), we obtain two sets of quadrupolar parameters \( v_0 = 3.992 \pm 0.001 \) MHz and \( \eta = 0.065 \pm 0.003 \), and \( v_0 = 4.219 \pm 0.001 \) MHz and \( \eta = 0.282 \pm 0.001 \), from the former and latter sets of the lines, respectively. We also confirmed by the numerical diagonalization of the full nuclear spin Hamiltonian that Eq. (3.1) is valid for these \( \eta \) values. These \( \eta \) values indicate that one of the Mn sites feels roughly axial EFG whereas the other feels more asymmetric EFG. Hereafter, we will call them axial and nonaxial sites, which are considered to correspond to the 4\( b \) and 4\( d \) Mn sites, respectively, in the orthorhombic phase taking account of the symmetry consideration given in last section. The spectral intensity seems to be consistent with the 1:1 population ratio of the 4\( b \) and 4\( d \) sites. Thus the present NQR results are in good agreement with the crystallographic results. At the same time, the observation of NQR confirms no magnetic ordering at least down to 1.4 K, being in accordance with the results of other microscopic experiments.

The temperature variation of the NQR frequencies \( \nu_2 \) were followed up to 200 K for both the sites and plotted in Fig. 3. Intensities are too poor to be detected above 200 K. Instead, crude values of \(-2 \nu_0 \) estimated from first-order satellites of the NQR spectrum (will be discussed in next subsection) arising from the axial site (16\( d \) site of the cubic C15 phase above 240 K) are also plotted in the figure. Above the structural transition at \( \sim 240 \) K, the resonance frequency shows weak temperature dependence, while below \( \sim 240 \) K the frequency separates to two different components, which start to decrease with decreasing temperature. At the rhombohedral-orthorhombic transition (\( \sim 210 \) K), no appreciable anomaly was found. Generally the origin of EFG consists of two contributions; one is of intra-atomic electron configurations and the other is the lattice and conduction-electron term made up of outside charge. The reduction of \( \nu_0 \) below 240 K may be related to the symmetry lowering of the crystal and/or electron configurations. It is notable that the temperature variation of \( \nu_0 \) (and probably also \( \eta \)) is continuous at the transition points.

**B. NMR results**

We measured field-swept spectra in the high-field condition to check the quadrupolar parameters and to estimate the values of the Knight shift. Here, we determine the parameters by mainly comparing experimental spectra with computer simulated line shapes. Assuming the coincidence of the principal axes of the Knight shift and EFG tensors, and within the second-order perturbation limit of the quadrupolar interaction, the resonance frequency of the \( m \leftrightarrow m-1 \) transitions as a function of the angles between the external field and EFG axes, \( \theta \) and \( \phi \), is given by

\[ v_0(\theta, \phi) = v_0(1 + K_{iso}) + \frac{1}{2} v_0 K_1 (3 \cos^2 \theta - 1) - \frac{1}{2} v_0 K_2 \sin^2 \theta \cos 2 \phi + \frac{1}{2} v_0(m - \frac{1}{2})(3 \cos^2 \theta - 1 - \eta \sin^2 \theta \cos 2 \phi) + \frac{v_0^2}{32 v_0} \sin^2 \theta (g_A \cos^2 \theta - g_B) + \frac{\eta v_0^2}{48 v_0} \sin^2 \theta (g_C \cos^2 \theta + g_B) \cos 2 \phi + \frac{\eta^2 v_0^2}{72 v_0} \{g_A - (g_A + g_B) \cos^2 \theta - \frac{1}{2} g_C \sin^4 \theta \cos^2 2 \phi\}, \] (3.3)

with

\[ g_A = 24m(m-1) + 9 - 4I(I+1), \]

\[ g_B = 6m(m-1) + 3 - 2I(I+1), \]

\[ g_C = 4g_A + g_B, \]

and with a conventional definition for the Knight shift,

\[ K_{iso} = \frac{1}{5} (K_X + K_Y + K_Z), \]

\[ K_1 = \frac{1}{5} (2K_Z - K_X - K_Y), \]

\[ K_2 = K_Y - K_X, \] (3.4)
where $K_X$, $K_Y$ and $K_Z$ are diagonal components of the Knight shift tensor. The resonance field $[H_m(\theta, \phi)]$ of the constant-frequency experiment is obtained by solving Eq. (3.3) for $H_m(\theta, \phi) = \nu_m/\gamma$ where $\nu_m$ is the operating frequency. The coincidence of the principal axes of the Knight shift and EFG tensors is not necessarily justified in the low-symmetric phases, but it was found that this assumption does not lead to serious contradiction to the analysis of UMn$_2$. In the case of a homogeneous distribution of the powder orientation, the theoretical field-swept powder pattern for the $m\leftrightarrow m-1$ transitions is calculated as

$$S_m(H) = \left( \frac{d^2H_m(\theta, \phi)}{\sin \theta d\theta d\phi} \right)^{-1}. \quad (3.5)$$

The actual spectrum is obtained by convoluting an appropriate distribution function, $g(\nu)$, as

$$I_m(H) = C \int g(H-H')S_m(H)dH'. \quad (3.6)$$

where $C$ is a normalizing constant. The whole line shape is given by summing up all $m$ components. The computer generated line shape thus obtained is compared with experimental spectra.

Examples of field-swept $^{55}$Mn NMR spectra of UMn$_2$ measured at 76.3 MHz are shown in Fig. 4(a), all of which locate at around the zero Knight shift position. Above 240 K the NMR spectrum consists of a single component with sharp first-order quadrupolar satellites, being consistent with a unique Mn site with $\eta=0$. The center line, i.e., the transitions of $m=-\frac{1}{2} \leftrightarrow m=+\frac{1}{2}$, shows a double peak structure, which is a typical second-order quadrupolar powder pattern. On the other hand, at low temperatures we observed smeared satellite and center-line structures. Nevertheless the line shape can satisfactorily be explained assuming the presence of two different chemical sites. Figure 4(b) shows calculated lines using the quadrupolar parameters obtained from the NQR analysis for the axial and nonaxial sites at 4.2 K, where we used appropriate values of the Knight shift (discussed below). The first-order satellites of both the sites are rounded out to certain extents due to the appearance of $\eta$. The total spectrum is thus obtained as a sum of two components, which is also shown in Fig. 4(b) after convoluting a Gaussian function with an appropriate width. The calculated line shape reproduces satisfactorily the experimentally obtained spectrum at 4.2 K. In the intermediate temperature range of 210–240 K the situation seems to be more complicated, which will be discussed by simulating the center-line shape.

Examples of only center lines measured at different temperatures are shown in Fig. 5(a). Above 240 K, the line shape can again be reproduced with a single component with appropriate quadrupolar and Knight shift parameters; see the result at 250 K in Fig. 5(a), where bold and fine solid curves indicate calculated $S_{1/2}(H)$ and $I_{1/2}(H)$, respectively. Note that the spectral shape, especially the separation between two peaks, cannot be reproduced without introducing nonzero $K_1$ indicating an appreciable anisotropy of the Knight shift. Below 210 K center lines are well reproduced by assuming two components with appropriate quadrupolar and Knight shift values; see the spectrum at 160 K in Fig. 5(a). Figure 5(b) shows the temperature dependence of the center line spectrum measured in the intermediate temperature range around the phase transitions. Below 240 K, additional components appear other than the axial component. The new components seem to exhibit a broad inhomogeneous linewidth. Neutron diffraction experiments by Lawson et al.\(^{14}\) suggested the coexistence of the R$^3m$ and Imma phases in the temperature range, which gives rise to more than two or a distribution of chemical sites. Therefore, our NMR results seem to be consistent with the diffraction analysis. Here, tentatively, we try to simulate the line shape assuming the presence of only two different components as below 210 K. As shown in Fig. 5(a) (the spectrum at 220 K), the line shape can roughly be reproduced. The obtained quadrupolar and Knight-shift parameters show a reasonably continuous temperature variation (see Figs. 3 and 6).

To evaluate the Knight shift we assume uniaxial anisotropy ($K_2=0$) of the principal shift tensors for all the temperature range. This is reasonable above 240 K, where the Mn site is axially symmetric, while below 240 K it is just an assumption for simplicity. Figure 6 shows the temperature dependence of the Knight shift obtained by analyzing the whole spectra (including both center and satellite lines) mea-
sured at several different frequencies. These values may include some ambiguity below 240 K due to the simplification of $K^2$ but are enough reliable above 240 K. The anisotropic components $K_1$ (for both the axial and non-axial components) are slightly negative in all the temperature range and show rather appreciable temperature dependences. There is no site dependence of $K_1$ within the experimental accuracy. The isotropic components $K_{iso}$ are negative at high temperatures and increase to positive values on further cooling from 240 K. Below the structural transition, $K_{iso}$ depends on the site. Below $\sim 50$ K, one can see slight reductions of $K_{iso}$. The Knight shift is discontinuous with temperature at $\sim 240$ K but not at $\sim 210$ K. If the temperature dependence is caused by the Mn 3$d$-spin component only, as usually in 3$d$ magnets, the positive $K_{iso}$ at low temperatures suggests a comparable or larger positive offset of Van Vleck-type orbital and/or conduction-electron contributions because the on-site $d$-spin hyperfine coupling (via core polarization) is always negative. The transferred hyperfine field from U moments, if any, may be one of the origins of the temperature dependence but is expected to be much smaller than the on-site Mn-3$d$ contribution.

Figure 7 shows the isotropic component of the Knight shift plotted against the susceptibility with the temperature as an implicit parameter ($K$-$\chi$ plot). For this analysis, we measured the temperature dependence of the susceptibility of the present sample, which is shown in the inset of Fig. 6 and is basically the same as that reported in Ref. 18. Above 240 K, $K_{iso}$ is in proportion to $\chi$ (the broken line). Below 240 K, the points lie on different straight lines depending on the sites (full lines). It is interesting to note that the isotropic part of the hyperfine coupling constants, $A_{iso}$ obtained from the slopes of the lines do not change at 240 K and do not depend on the site within the experimental accuracy, indicating that the spin component of the hyperfine coupling does not change at the structural transformation. Note that the coupling constants are the same for both the axial and nonaxial sites in spite of different absolute values of $K_{iso}$, implying that only temperature independent terms depend on the site. We cannot find a notable discontinuity at 210 K again. The hyperfine coupling constant is estimated from the $K$-$\chi$ plot as $A_{iso} = 2N\mu_B d K_{iso} / d \chi = -220 \pm 20$ kOe/\mu_B (where, $N$ and $\mu_B$ are Avogadro’s number and the Bohr magneton, respectively), on the assumption that only Mn moments contribute to the temperature dependence of susceptibility through out the whole temperature range, though the contribution of U
FIG. 7. The isotropic component of the Knight shift plotted against the susceptibility with temperature as an implicit parameter ($K$-$\chi$ plot). Closed and open circles represent the axial and nonaxial sites, respectively. The broken and full straight line gives hyperfine coupling constants for the high-temperature cubic and low-temperature orthorhombic phases, respectively.

magnetism cannot be excluded. The value of $A_{\text{iso}}$ for UMn$_2$ is large compared to the value of other RMn$_2$ systems in the ordered state.$^{8,22}$ However, this value is comparable to the value of YMn$_2$ in the paramagnetic state.$^{23,24}$ Below $\sim$50 K, the plots deviate markedly from the straight lines and seem to come on other lines with different slopes. This phenomenon may be related to a marked upturn of the susceptibility on further cooling, and hence to a certain evolution of the electronic state suggested, for example, by muon spin relaxation measurements.$^{15}$ However, since it is known that the low-temperature susceptibility strongly depends on samples, we do not discuss further the low-temperature anomaly.

It should be noted that the temperature dependence of the anisotropic Knight shift $K_1$ is appreciable. If we formally assume that the susceptibility is isotropic, the anisotropic component $A_{\text{aniso}} \equiv \frac{1}{3}(A_1 - A_\text{iso})$ is roughly estimated as $K_1 - \chi$ plot to be $A_{\text{aniso}} = -80$ and $-140 \text{ kOe}/\mu_B$ for below and above the structural transition, respectively. These are the coupling constants primarily estimated from the temperature-dependent part of $K_1$. These magnitudes are appreciably large and comparable to the isotropic component. It is interesting to note that $A_{\text{aniso}}$ reduces to about half at the high-temperature phase contrast to no change in $A_{\text{iso}}$. The origin of this large anisotropy is of interest. In general, the anisotropy is caused by dipole or orbital contribution, and the Van Vleck-type orbital contribution is independent of temperature. Since the magnitude is apparently much larger than the conventional lattice dipolar field, it is presumed that the LS coupling is rather larger in UMn$_2$ and that the effect of the nonquenched Mn-3$d$ orbitals is more or less responsible for the large temperature-dependent anisotropy of the Knight shift.

C. Nuclear spin-lattice relaxation time

We measured the $^{55}$Mn nuclear spin-lattice relaxation time, $T_1$ by using NQR and NMR signals at low- and high-temperature ranges, respectively. The NQR-$T_1$ was measured by using $\nu_2$ lines (transitions of $m_s = \frac{3}{2} \leftrightarrow m_s = \frac{1}{2}$) for both the axial and nonaxial sites. In general, the recovery of the nuclear magnetization, $M(t)$ for the $I = \frac{5}{2}$ NQR (Refs. 25 and 26) is described by two exponential functions as

$$M(t) = M_0 \left[ 1 - a_1 \text{exp}\left( -\frac{b_1}{T_1} t \right) - a_2 \text{exp}\left( -\frac{b_2}{T_1} t \right) \right],$$

(3.7)

where $t$ is the time between the saturation pulse and the spin-echo first pulse, and $a_1$, $a_2$, $b_1$ and $b_2$ are constants depending on $\eta$, which are given as a function of $\eta$ in Ref. 26. The value of $M_0$ was obtained by spin-echo experiment without the saturation pulse, and the values of $a$ and $b$ parameters were obtained as a function of $\eta$, of which temperature dependence was taken into account properly by using the NQR results at different temperatures. Therefore, the spin-lattice relaxation time, $T_1$ was the only fitting parameter in Eq. (3.7). Typical recovery curves of the nuclear magnetization for both the sites (at 20 K) are shown in Fig. 8 together with the fitting of Eq. (3.7), where we took into account the site and temperature dependence of $\eta$. We found appreciably different $T_1$ values depending on the chemical sites; $T_1$ is shorter by about 30% for the axial site. The estimated values of $1/T_1$ vary linearly with temperature till 100 K which are plotted in the inset of Fig. 9. Average values of $1/T_1$ for the two sites are shown by open circles in Fig. 9.

Above $\sim$100 K, it becomes difficult to estimate reliable $T_1$ values from NQR experiments due to poor signal-to-noise ($S/N$) ratio. Above 120 K, instead, crude values of $1/T_1$ were estimated by using superposed NMR signals in external field. The recovery of the nuclear magnetization was not described by a single exponential function. Although the distribution of chemical sites may also cause the nonsingle exponential behavior, we try to estimate rather forcibly a unique value of $T_1$ by attributing the behavior to the quadrupole interaction. In general, the recovery curve of the $I = \frac{5}{2}$ NMR affected by the quadrupole interaction is described by three-exponential functions as$^{27}$
The coefficients, $c_1$, to the experimental values. Thus, the relaxation is considered localized moments at both Mn and U sites and also the absence above values of $K$ the total temperature independent Knight shift, using the contribution of conduction electron to the Knight shift from other sites, respectively. These values are small comparing with other gas of noninteracting spins we have magnetic $T$-is $0$; also indicating that the electronic state of UMn$_2$ is Mn-3 $d$-orbitals is not negligible. Then, the band $M(t) = M_0 \left[ 1 - c_1 \exp \left( -\frac{t}{T_1} \right) - c_2 \exp \left( -\frac{6}{T_1} t \right) - c_3 \exp \left( -\frac{15}{T_1} t \right) \right].$ (3.8)

The coefficients, $c_1$, $c_2$ and $c_3$ depend on the initial occupation condition at each nuclear level. The experimental recovery is reasonably reproduced by Eq. (3.8) with treating $T_1$, $c_1$, $c_2$ and $c_3$ as free parameters. In this analysis, due to the many fitting parameters poor $S/N$ ratio at high temperatures results in the large ambiguity in the $T_1$ value. The estimated $1/T_1$ values are shown by filled squares in Fig. 9. The relaxation rate shows an anomaly at $\sim 240$ K being in accordance with the structural phase transition. On the other hand, no appreciable anomaly was found at $\sim 210$ K.

As seen above, $1/T_1$ is roughly linear to temperature ($T_1 T=\text{const}$) at low temperatures. The constant values of $1/(T_1 T)$ are 6.4 and 5.0 s$^{-1}$K$^{-1}$ for the axial and nonaxial sites, respectively. These values are small comparing with other magnetic materials. Since it is difficult to extract the contribution of conduction electron to the Knight shift from the total temperature independent Knight shift, using the above values of $K_\text{ano}$, we roughly estimate $T_1 TK^2$ to be of the order of $10^{-6} - 10^{-5}$ s for UMn$_2$. In the case of Fermi gas of noninteracting spins we have $T_1 TK^2 = \frac{\hbar}{4} \times (\gamma_e/\gamma_f)^2 \times 2 \times 10^{-6}$ s K (for $^{55}$Mn), which is comparable to the experimental values. Thus, the relaxation is considered to be dominated by the conduction electron contribution (the Korringa mechanism), indicating clearly the absence of localized moments at both Mn and U sites and also the absence of the enhanced density of states at the Fermi level. The relaxation rates of UMn$_2$ are compared with another nonmagnetic RMn$_2$, ScMn$_2$, for which $1/(T_1 T) = 17.5$ s$^{-1}$K$^{-1}$, also indicating that the electronic state of UMn$_2$ is less enhanced. The $T_1 T=\text{const}$ behavior at low temperatures indicates that there is no sign of a critical phenomena on further cooling at least down to 4.2 K, being in contrast to the susceptibility behavior. Well above the transitions, values of $1/T_1$ come on a extrapolated line from low temperatures (Fig. 9), indicating no localized magnetic moment above the transitions.

IV. DISCUSSIONS

The observation of $^{55}$Mn NQR signals at low temperatures confirm microscopically that there is no magnetic ordering in UMn$_2$ at least down to 1.4 K, being consistent with neutron, Mössbauer, and $\mu$-SR (Ref. 15) results. The two chemical Mn sites confirmed by NQR measurements below the structural transition are completely in agreement with the structural analysis by neutron diffraction. The relaxation rate is small in all the temperature range of measurements and is explained as the Korringa-type conduction-electron relaxation, indicating that there is no localized moment on both Mn and U sites both above and below the structural transition. These experimental observations are consistent with the fact that both the Mn-Mn and U-U interatomic distances in UMn$_2$ ($\sim 2.5$ and $\sim 3.4$ Å, respectively) are well below the critical values ($\sim 2.7$ and $\sim 3.5$ Å, respectively) which discriminate the stability of the localized moment.

Although neither magnetic ordering nor critical behavior has been detected at the lowest temperature range, the Knight shift shows a somewhat anomalous temperature dependence below $\sim 50$ K, which may be related to the marked upturn of the susceptibility and hence to some magnetic instability at much lower temperatures.

According to high resolution diffraction experiments, UMn$_2$ undergoes a rhombohedral distortion to the space group $R3\bar{m}$ at $\sim 240$ K and again to orthorhombic Imma at $\sim 210$ K. At $\sim 240$ K we observed a clear symmetry breaking by NMR/NQR experiments. On the other hand, at $\sim 210$ K all of the quantities measured by NMR/NQR exhibit no anomaly. These results suggest that the first rhombohedral distortion is a precursor to the orthorhombic phase and that only the transition at $\sim 240$ K is a real lattice instability associated with an additional atomic displacement on further cooling. This is consistent with the fact that specific heat shows a large anomaly at $\sim 240$ K but not at $\sim 210$ K.

The mechanism of the lattice instability in UMn$_2$ is still open question. Marpoe and Lander proposed that the structural transition is caused by the formation of strong $5f$ bonds of U atoms. Although they assumed the presence of localized moment at U site above the structural transition, this is not justified in various experiments and characteristic scales of U electronic energy seems to be much smaller than the transition temperature. Lawson et al. suggested that the structural transformation in UMn$_2$ is reminiscent of those in other cubic Laves phases HfV$_2$ and ZrV$_2$. For these materials, recently, Chu et al. proposed that the structural instability is due to the large density of states at the Fermi level, $\rho(E_F)$, and Fermi surface nesting, which give rise to phonon softening. This scenario does not seem to be applicable to UMn$_2$ because $\rho(E_F)$ is not enhanced in this material as seen from the small relaxation rate. The large temperature-dependent anisotropy of the Knight shift suggested that the effect of unquenched Mn-3$d$ orbitals is not negligible. Then, the band Jahn-Teller distortion driven mainly by Mn-3$d$ bands may be one of possible origins of the lattice instability since we may expect orbital degeneracies in the axially symmetric Mn...
site in the high-temperature cubic phase. This interpretation may be consistent with the larger Knight-shift anisotropy for the high-temperature phase. However, since Mn-3d bands should come at the Fermi level in this case, it is again unlikely that the small $\rho(E_F)$ is in accord with this model. On the other hand, quite large value of $\gamma$ in specific heat at low temperature\textsuperscript{15} is in contrast to the small relaxation rate. If only U spin fluctuations are responsible to the large $\gamma$ value, and if the Mn site has no substantial coupling with the U magnetism, this contradiction may be reconciled. The origin of structural instability at low temperature still remains to be explained which may highlight such ambiguity. For further understanding, calculations of electronic structures may be helpful.

In summary, we performed $^{55}$Mn NMR and NQR measurements of UMn$_3$, which shows lattice instability at around 210–240 K. We clearly observed by NMR and NQR that the Mn-16d site in the cubic phase separates to two different crystallographic sites in the orthorhombic phase below the structural transformation ($4b$ and $4d$ sites). The nuclear resonance results indicate the absence of localized moments at both Mn and U sites and also the absence of enhanced electron correlation. The origin of the lattice instability remains to be elucidated.

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