<table>
<thead>
<tr>
<th>Title</th>
<th>Crystallization of BaO • TiO₂-SiO₂-Al₂O₃ Glasses and Dielectric Properties of their Crystallized Products</th>
</tr>
</thead>
<tbody>
<tr>
<td>Author(s)</td>
<td>Kokubo, Tadashi</td>
</tr>
<tr>
<td>Citation</td>
<td>Bulletin of the Institute for Chemical Research, Kyoto University (1970), 47(6): 572-583</td>
</tr>
<tr>
<td>Issue Date</td>
<td>1970-03-28</td>
</tr>
<tr>
<td>URL</td>
<td><a href="http://hdl.handle.net/2433/76318">http://hdl.handle.net/2433/76318</a></td>
</tr>
<tr>
<td>Type</td>
<td>Departmental Bulletin Paper</td>
</tr>
<tr>
<td>Textversion</td>
<td>publisher</td>
</tr>
</tbody>
</table>

Kyoto University
Crystallization of \( \text{BaO} \cdot \text{TiO}_2 \cdot \text{SiO}_2 \cdot \text{Al}_2 \text{O}_3 \) Glasses and Dielectric Properties of their Crystallized Products

Tadashi Kokubo*

Received November 10, 1969

In order to prepare barium titanate ceramics having high dielectric constant by crystallization of glass, a series of glasses with the general composition \((100-x-y)\text{BaO} \cdot \text{TiO}_2 + x\text{SiO}_2 + y\text{Al}_2 \text{O}_3\), in which \(x\) and \(y\) are within the range of 15 to 60 and 0 to 20 mole %, respectively, was investigated, especially with behavior during reheating and dielectric properties of their crystallized products.

I. INTRODUCTION

BaTiO\(_3\) ceramics, which are widely employed as components of electronic devices, are usually prepared by sintering crystalline powders. Herczog\(^2\) prepared BaTiO\(_3\) ceramics by crystallization of glass which consists of melting the raw materials, forming the melts and crystallizing the formed glasses by heat treatment: Herczog investigated the crystallization of a series of glasses with the compositions \(x\text{BaTiO}_3 + (100-x)\text{BaAl}_2\text{Si}_2\text{O}_8\) (\(x\) by weight) and obtained, from a glass of this system with addition of a small amount of fluoride, a glass-ceramics with a dielectric constant of 1200. The present author has found, however, that the glass used by Herczog has a high melting temperature and, in addition, is likely to devitrify during cooling of the melt. Such behavior is undesirable for production of the crystallized glass (glass-ceramics) with constant dielectric properties.

The present study has started from a search for compositions of glasses that are easy to be melted and also formed without devitrification. Glass formation tendency and crystallization behavior during reheating have been investigated for the compositions \((100-x-y)\text{BaO} \cdot \text{TiO}_2 + x\text{SiO}_2 + y\text{Al}_2 \text{O}_3\), where \(x\) and \(y\) are varied in the range 15 to 60 and 0 to 20 in mole %, respectively. Also dielectric properties of the crystallized products have been measured and discussed on the basis of their chemical composition and microstructure.

II. EXPERIMENTAL PROCEDURE

II. 1. Preparation of Glasses

To determine the glass formation region in the system \(\text{BaO} \cdot \text{TiO}_2 \cdot \text{SiO}_2 \cdot \text{Al}_2 \text{O}_3\), glasses with the compositions \((100-x-y)\text{BaO} \cdot \text{TiO}_2 + x\text{SiO}_2 + y\text{Al}_2 \text{O}_3\), where \(x\) and \(y\) were varied in the range of 15 to 60 and 0 to 20 mole %, respectively, were melted. As

* 小久保正: Laboratory of Ceramic Chemistry, Institute for Chemical Research, Kyoto University, Uji, Kyoto.
batch materials were used reagent-grade barium carbonate, titanium oxide and aluminum hydroxide, and high-grade quartz powder of low iron content usually employed in the manufacture of optical glasses. About 50 g of the batch mixtures were put in a platinum crucible of 80 cc in capacity and melted at 1450°C for 1 hour in an electric furnace. The melts were poured on a steel plate, pressed into the form of plates approximately 2 mm thick, and immediately annealed at 650°C in another furnace. Some of the glasses thus obtained, whose compositions are given in Table 1, were subjected to the following experiments.

II. 2. Differential Thermal Analysis

Crystallization behavior of glass was examined by the differential thermal analysis. A solid cylindrical piece of glass just fit to the DTA sample holder (6 mm in diameter and 14 mm in height) was used as sample to minimize the effect of surface crystallization, which might be serious with powder sample. A heating rate of 10°C/min was adopted and α-Al₂O₃ was used as reference material.

II. 3. Crystallization of Glasses

Glass slabs of the size 10 × 10 × 1.5 mm cut from the plate and ground with No. 2000 Al₂O₃ powder were crystallized by heating on a platinum sheet in an electric furnace. They were heated up at a rate of 5°C/min from room temperature to 1100°C, kept there for 1 hour and cooled in the furnace. The resultant crystallized samples were subjected to the visual observation of the appearance, x-ray diffraction analysis and measurements of dielectric properties.

II. 4. X-ray Diffraction Analysis

Identification of crystals precipitating in the course of crystallization and determination of the amount of BaTiO₃ crystals found in the final crystallized products were conducted by the x-ray diffraction analysis with powdered samples. To determine the BaTiO₃ crystal content, intensity of the (101) reflection of BaTiO₃ crystals in the sample was measured with the use of the (220) reflection of fluorite (CaF₂) as an internal standard and compared with a calibration curve. The calibration curve was obtained with intimate mixtures of known amounts of BaTiO₃ crystals, glass of the composition No. 2 and fluorite crystal. Volume fraction $V$ of the BaTiO₃ crystals was calculated from the measured density $D_o$ of the crystallized sample by the formula
\[ V = x \left( \frac{D_m}{D} \right) \], where \( x \) is the weight fraction determined by the x-ray analysis and \( D = 6.06 \text{ g/cm}^3 \) is the density of BaTiO\(_3\).  

II. 5. Measurement of Dielectric Properties

Dielectric properties were measured at a frequency of 1 Mc/s at room temperature. The measurements were made by a Q-Meter (Type GM-102, Yokogawa Electric Works, Ltd.). Since some of the crystallized glasses showed non-uniform surface, all the samples were ground to rectangular pieces of the size 10\( \times \)10\( \times \)1 mm to remove the effect of original surfaces. Silver paste applied on both faces of the samples served as electrodes.

III. RESULTS

III. 1. Glass Formation Region

Glass formation region in the system BaO·TiO\(_2\)·SiO\(_2\)·Al\(_2\)O\(_3\) is shown in Fig. 1. The sign (\(\bigcirc\)) or (\(\bullet\)) in Fig. 1 refer to the composition which gave a transparent glass when the melt heated at 1450°C was poured onto a steel plate. Especially the sign (\(\bullet\)) refers to the glass composition which was used for further investigation. The numbers given correspond to those of the compositions given in Table 1. The sign (\(\triangle\)) refers to the composition which did not give an entirely transparent glass due to the formation of scums at melting temperature or partial devitrification during cooling. The sign (\(\times\)) refers to the composition whose melt was completely devitrified during cooling. A solid line L gives a tentative boundary representing a limit of glass formation.

---

Fig. 1. Glass formation area in the system BaO·TiO\(_2\)·SiO\(_2\)·Al\(_2\)O\(_3\).
Crystallization of BaO·TiO₂·SiO₂·Al₂O₃ Glasses

**Fig. 2.** Differential thermal analysis of the glass: BaO·TiO₂ 60, SiO₂ 26, Al₂O₃ 14 mole % (Specimen No. 2).

- (1) 900°C
- (2) 1040°C

**Fig. 3.** X-ray diffraction patterns of the crystallized glasses of 900°C and 1040°C. Composition of the parent glass: BaO·TiO₂ 60, SiO₂ 26, Al₂O₃ 14 mole %.
III. 2. Differential Thermal Analysis and X-Ray Diffraction Analysis

A thermogram of the glass No. 2 (BaO•TiO₂ 60, SiO₂ 26, Al₂O₃ 14 mole %) is given in Fig. 2. Two exothermal peaks are observed, one at 850°C and the other at 960°C. Powder x-ray diffraction patterns of the samples heated to the temperatures 900°C and 1040°C which are a little over each peak temperature are shown in Fig. 3. It is seen from Fig. 3(1) that in the sample heated at 900°C a considerable amount of perovskite-type BaTiO₃ crystals are precipitated as indicated by the strong lines designated by (×). In addition, there is an unidentified crystalline species to which the lines at 2θ=18.7°, 25.9°, 28.6°, 32.7°, 37.9°, 39.5° and 43.9° are attributed. In the sample heated at 1040°C (Fig. 3(2)), there are a great amount of BaTiO₃ crystals and a less amount of the unidentified crystal, as evidenced from the growth and weakening of the corresponding diffraction lines. Further, a series of new diffraction lines designated by the sign (○) in the figure appears. These lines can be attributed to the hexacelsian (BaAl₂Si₂O₈). Herczeg also found that the BaTiO₃ crystals are precipitated at lower temperatures and then hexacelsian crystals are precipitated at higher temperatures in the course of crystallization of the glass having the composition BaTiO₃ 74 and BaAl₂Si₂O₈ 26% by weight (BaO 42.4, TiO₂ 34.8, SiO₂ 15.1 and Al₂O₃ 7.7 mole %). No description was made, however, of the unidentified crystal by Herczeg.

The kind of crystals and the amount of BaTiO₃ crystal found in the samples

![Fig. 4. Appearance of crystallized products obtained by heating up to 1100°C.](576)
Crystallization of $\text{BaO}\cdot\text{TiO}_2\cdot\text{SiO}_2\cdot\text{Al}_2\text{O}_3$ Glasses

Table 2. Crystalline Phases and Dielectric Properties.

<table>
<thead>
<tr>
<th>Specimen No.</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
</tr>
</thead>
<tbody>
<tr>
<td>Crystalline phases*</td>
<td>BT</td>
<td>BT</td>
<td>BT</td>
<td>BT</td>
<td>BT</td>
<td>BT</td>
<td>—</td>
</tr>
<tr>
<td>BAS</td>
<td>BAS</td>
<td>BAS</td>
<td>BAS</td>
<td>BAS</td>
<td>BAS</td>
<td>BAS</td>
<td>BAS</td>
</tr>
<tr>
<td>—</td>
<td>—</td>
<td>BTS</td>
<td>BTS</td>
<td>BTS</td>
<td>BTS</td>
<td>BTS</td>
<td>BTS</td>
</tr>
<tr>
<td>X</td>
<td>X</td>
<td>X</td>
<td>X</td>
<td>X</td>
<td>X</td>
<td>X</td>
<td>X</td>
</tr>
<tr>
<td>Content of $\text{BaTiO}_3$ (vol %)</td>
<td>19</td>
<td>23</td>
<td>15</td>
<td>8</td>
<td>18</td>
<td>7</td>
<td>0</td>
</tr>
</tbody>
</table>

Dielectric properties

<table>
<thead>
<tr>
<th>Parent glass</th>
<th>$\varepsilon$</th>
<th>tan$\delta$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>18</td>
<td>0.0021</td>
</tr>
<tr>
<td></td>
<td>17</td>
<td>0.0023</td>
</tr>
<tr>
<td></td>
<td>17</td>
<td>0.0020</td>
</tr>
<tr>
<td></td>
<td>16</td>
<td>0.0023</td>
</tr>
<tr>
<td></td>
<td>17</td>
<td>0.0020</td>
</tr>
<tr>
<td></td>
<td>17</td>
<td>0.0022</td>
</tr>
<tr>
<td></td>
<td>14</td>
<td>0.0019</td>
</tr>
<tr>
<td>Crystallized product</td>
<td>$\varepsilon$</td>
<td>tan$\delta$</td>
</tr>
<tr>
<td></td>
<td>168</td>
<td>0.0174</td>
</tr>
<tr>
<td></td>
<td>500</td>
<td>0.0250</td>
</tr>
<tr>
<td></td>
<td>284</td>
<td>0.0207</td>
</tr>
<tr>
<td></td>
<td>77</td>
<td>0.0119</td>
</tr>
<tr>
<td></td>
<td>415</td>
<td>0.0304</td>
</tr>
<tr>
<td></td>
<td>76</td>
<td>0.0173</td>
</tr>
<tr>
<td></td>
<td>23</td>
<td>0.0020</td>
</tr>
</tbody>
</table>

* BT; BaTiO$_3$ (perovskite-type), BAS; Hexacelsian ($\text{BaAl}_2\text{Si}_2\text{O}_8$), BTS; $\text{BaTiSiO}_5$, X; Unidentified crystal.

crystallized by heating to 1100°C by a schedule described in paragraph II.3. are given in Table 2. It can be seen from Table 2 that crystals precipitated in the crystallized glasses are perovskite-type BaTiO$_3$, hexacelsian, $\text{BaTiSiO}_5$, and unidentified crystals.

III. 3. Defects of Crystallized Glasses

The appearances of the crystallized glasses obtained by heating to 1100°C are shown in Fig. 4. Although most of the crystallized glasses show no defect, the crystallized sample of the composition No. 1 has a great number of cracks and that of the composition No. 5 has surface ripple. In general, the compositions containing too much amount of $\text{Al}_2\text{O}_3$ or $\text{BaO}\cdot\text{TiO}_2$ tend to give the crystallized glasses having defects such as cracks or surface ripples.

III. 4. Dielectric Properties

III. 4-1. Effects of Heat Treatment

Figure 5 shows the dielectric properties (dielectric constant and tan$\delta$) of the glass No. 2 as a function of temperature of heat treatment. All the measurements were made at room temperature. The glass was heated up at a rate of 5°C/min from room temperature to a temperature (temperature of heat treatment mentioned above) and then taken out immediately from the furnace. It can be seen from the figure that the dielectric constant of the glass first remains almost the same at about 17 up to 700°C and then increases as the temperature of heat treatment is raised. The rate of increase is particularly great in the temperature range from 800°C toward 1100°C, where the value reaches 560. The heating up to still higher temperatures affects the dielectric constant only slightly.

Dielectric properties of the same glass kept at 1100°C for various periods are shown in Fig. 6. The glass was heated at a rate of 5°C/min from room temperature to 1100°C. The figure shows that both dielectric constant and tan$\delta$ do not vary with heating time. In other words, at 1100°C dielectric properties characteristic of the maximum heating

(577)
temperature (1100°C) are attained as soon as the temperature is reached.

III. 4-2. Effects of Chemical Composition

The values of dielectric constant and tanδ of the crystallized glasses obtained by heating to 1100°C are shown in Table 2. The data on the glasses before heat treatment are also shown in the table. The dielectric constants of the crystallized glasses are reproduced in a composition triangle in Fig. 7. In this figure the values shown by parentheses represent the amounts (volume fraction) of BaTiO₃ crystal precipitated in the crystallized samples. It is seen from Table 2 that the dielectric constant of the parent glass shows only slight dependence on the chemical composition, varying within the range from 14 to 18, whereas that of the crystallized glass is very much dependent on the chemical composition of the parent glass, varying from 23 to 500. Figure 7
Crystallization of $\text{BaO} \cdot \text{TiO}_2 - \text{SiO}_2 - \text{Al}_2\text{O}_3$ Glasses

Fig. 6. Dependence of dielectric properties upon heating time.
Heating temperature: 1100°C.
Composition of glass: $\text{BaO} \cdot \text{TiO}_2$ 60, $\text{SiO}_2$ 26, $\text{Al}_2\text{O}_3$ 14 mole %.

Fig. 7. Dielectric constant and content of barium titanate of the crystallized products.

(579)
T. Kokubo

shows that with constant Al₂O₃ content the dielectric constant of the crystallized glass decreases as the SiO₂/BaO·TiO₂ mole ratio increases and with constant BaO·TiO₂ content the dielectric constant reaches a maximum when the Al₂O₃/SiO₂ mole ratio is 35/65.

IV. DISCUSSION

IV. 1. Dependence of Dielectric Constant on Chemical Composition

It was shown in the foregoing section that the dielectric constant of the crystallized glass is very much dependent on the chemical composition of the parent glass. This may be attributed to the dependence of the amount of BaTiO₃ crystal precipitated in the crystallized glass on the chemical composition. The comparison of the dielectric constant with BaTiO₃ crystal content (Fig. 7) confirms that, in general, the dielectric constant increases with increasing volume fraction of BaTiO₃ crystal. The crystallized glass of the composition No. 1 (dielectric constant 168 and crystal content 19 in Fig. 7) exhibits a considerably low dielectric constant, however, in spite of relatively high content of BaTiO₃ crystal present: The reason for this rather exceptional case may be explained in terms of cracks present in the crystallized glass.

IV. 2. Microstructure of Crystallized Glass

The crystallized glasses in the present system are regarded as the mixture of a high dielectric constant phase consisting of BaTiO₃ crystals and a low dielectric constant phase consisting of residual glass and other crystals than BaTiO₃. In general, the dielectric constant of the mixture depends on the dielectric constant, volume fraction, shape and arrangement (regular or irregular) of the constituent phases and the type of mixing. Mixtures are divided into two classes by the type of mixing, one is “pure mixture” consisting of only particles and the other is “porphyritic mixture” in which particles are dispersed in another continuous phase.

Bruggeman3' has derived relationships between the dielectric constant of the mixture (ε) and the volume fractions (δ₁ and δ₂) of the constituent phases for the following four cases.

(A) Three dimensional pure mixture of lamellar particles irregularly dispersed:

\[ \varepsilon = \frac{1}{2}(\varepsilon_1 + \varepsilon_2 + \sqrt{\varepsilon_1(2\varepsilon_2 + \varepsilon_2(2\varepsilon_1 + \varepsilon_2))}) \]

(B) Three dimensional pure mixture of spherical particles irregularly dispersed:

\[ \varepsilon = \frac{1}{4}(2\varepsilon_1 - \varepsilon_1' + \varepsilon_1 - \varepsilon_1'/\varepsilon_1 + \varepsilon_2) \]

(C) Three dimensional porphyritic mixture in which lamellar particles are irregularly dispersed in matrix:

\[ \varepsilon = \varepsilon_1\left(3\varepsilon_2 + 2\delta_1(\varepsilon_1 - \varepsilon_2)/\varepsilon_1 + \varepsilon_2\right) \]

(D) Three dimensional porphyritic mixture in which spherical particles are irregularly dispersed in matrix:

\[ 1 - \delta_1 = (\varepsilon_1 - \varepsilon)(\varepsilon_2/\varepsilon)^{1/2}/(\varepsilon_1 - \varepsilon_2) \]

Here

( 580 )
Crystallization of BaO·TiO$_2$·SiO$_2$·Al$_2$O$_3$ Glasses

\[
\begin{align*}
\frac{1}{\varepsilon_\perp} &= \frac{1}{\varepsilon_1} + \frac{1}{\varepsilon_2}, \\
\varepsilon_1 &= \varepsilon_1/\varepsilon_2, \\
\varepsilon'_1 &= \varepsilon_1\varepsilon_2 + \varepsilon_2\varepsilon_1, \\
\varepsilon_1 \text{ and } \varepsilon_2 &= \text{dielectric constant of each constituent phase.}
\end{align*}
\]

Figure 8 shows the dependences of dielectric constant of the mixture on volume fraction of BaTiO$_3$ calculated for the above four cases. In the calculation the dielectric constant of BaTiO$_3$ crystals was assumed 3300, a value which was obtained by extrapolating the measured dielectric constants of the crystallized glasses to the BaTiO$_3$ volume fraction of unity. The dielectric constant of the other phase was assumed 20, a value which is nearly equal to the dielectric constants of the parent glasses and their crystallized products containing no BaTiO$_3$ crystal. The solid circles in Fig. 8 represent the experimental data obtained on the crystallized glasses of the composition given in Table 1. The solid line was drawn so that it might fit best to the experimental data. It can be seen from the figure that the equation (C) describes the experimental results.

Fig. 8. Dielectric constant as a function of BaTiO$_3$ content.
Therefore the crystallized glasses in this system are assumed to have the structure of porphyritic mixture in which lamellar barium titanate crystals with dielectric constant of 3300 are irregularly dispersed in matrix consisting of residual glass and crystal phases such as BaAl₂Si₂O₈ and BaTiSiO₅ with dielectric constant of 20. Deviation of experimental data from Bruggeman's relationship at the region of low BaTiO₃ content may be attributed to the different size or shape of the BaTiO₃ crystals at low BaTiO₃ content from at high BaTiO₃ content. More detailed studies, however, are required for elucidating this matter.

Herczogl' also investigated the relation between the dielectric constant of the crystallized glass and the volume fraction of constituent BaTiO₃ crystal for the glasses with the composition \( x \text{BaTiO}_3 + (100-x) \text{BaAl}_2\text{Si}_2\text{O}_8 \) (\( x \) by weight) and reported that experimental data fit best to the relationship for pure mixture of spherical particles, in contrast to the present results obeying the relationship. The reason for this is not known. Further study is required.

V. SUMMARY

1. Glass formation region in the system BaO-TiO₂-SiO₂-Al₂O₃ was determined and it was confirmed that the glasses containing higher amounts of BaO and TiO₂ components can be prepared in the present system containing Al₂O₃ than in the system BaO-TiO₂-SiO₂.

2. Crystallization of the glasses in this system started at about 850°C and was essentially completed at about 1100°C. Crystals precipitated in the glasses heated to 1100°C were perovskite-type BaTiO₃, hexacelsian (BaAl₂Si₂O₈), BaTiSiO₅ and some unidentified crystals. Crystallized products obtained from the present glasses containing too much amount of BaO-TiO₂ or Al₂O₃ showed defects such as cracks and surface ripples.

3. Dielectric properties of the crystallized products varied with the composition of the parent glass. With constant Al₂O₃ content, the dielectric constant decreased with increasing SiO₂/BaO-TiO₂ mole ratio. With constant BaO-TiO₂ content, it reached a maximum when the Al₂O₃/SiO₂ mole ratio was 35/65. Generally, the dielectric constant increased with increasing amount of BaTiO₃ crystals precipitated in the crystallized products. The highest dielectric constant measured in the present experiments was 500 at a frequency of 10⁶c/s, that was obtained with the crystallized glass of the composition BaO-TiO₂ 60, SiO₂ 26, Al₂O₃ 14 mole %.

4. The dielectric constant-BaTiO₃ volume fraction relationship of the crystallized glass agreed best with a Bruggeman’s theoretical formula obtained by assuming that the crystallized glass has the structure of porphyritic mixture in which lamellar BaTiO₃ crystals are dispersed in matrix of residual glass and other crystals.

ACKNOWLEDGMENT

The author wishes to thank Professor M. Tashiro and Professor S. Sakka for their helpful advice.
Crystallization of BaO·TiO$_2$–SiO$_2$–Al$_2$O$_3$ Glasses

REFERENCES