Development and Control Experiment of the Trident Snake Robot

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Abstract—This paper is concerned with the development of the trident snake robot, a new example of nonholonomic mobile robot proposed by the authors. The robot has three-pointed shape composed of a center block and three branches, each of which has a passive nonslide wheel. It is modeled as a nonnilpotent driftless system with two generators; its control is a challenging problem, not only because it cannot be treated by continuous control law, but because it cannot be converted to any easy class of nonholonomic systems such as chained form. In this paper, we realized the one-link trident snake robot and applied a periodic control algorithm based on Lie bracket motion. Effectiveness of the proposed algorithm is examined with control experiments.

Index Terms—Mobile robot, nonholonomic system, nonlinear system.

I. INTRODUCTION

Snake robots have been attracting many mechanical and control engineers since the pioneering development by Hirose [1], [2]. They are not only stimulating from theoretical viewpoints (especially in terms of nonlinear control) [3], but also useful in practice, such as their hyperredundancy or modularity [4], and mobility in rough terrain with obstacles [5] and underwater environment [6]. Since the snake robots are usually joint-driven with limited angle range, unlike ordinary wheel-driven vehicles, new challenges for actuator technology are also required [7].

In contrast with the biologically inspired snake robots, this paper presents our development and control experiment of the trident snake robot, which is a new kind of wheeled mobile robot proposed in the authors’ recent paper [8]. The robot is composed of a center block and three branches of serial links, each of which has the same mechanics as conventional serial snake robots. Each link has a passive wheel rolling on the floor, which causes a nonholonomic constraint. Its kinematic model is described by a driftless nonlinear state equation, classified as nonnilpotent and two-generator systems.

It is impossible to asymptotically stabilize the driftless systems by any continuous state feedback [9], thus many attracting topics have emerged concerning discontinuous or time-varying feedback control design. Among them, single generator systems such as chained systems [10], power systems [11], or time-state control systems [12] have been intensively studied since the early 1990s. On the other hand, driftless systems with two or more generators [13] are structurally different from single-generator systems; there have been relatively few attempts [14], [15], and no conclusive control strategy is found up to now. Thus, there are left many challenging problems for nonlinear control theory.

From this point of view, we proposed the trident snake robot as a prototypical example of two-generator system in [8]. There, we analyzed controllability Lie algebra of the system, proposed periodic control algorithms based on the principle of holonomy, and clarified its locomotion principle. We finally succeeded in achievement of physically reasonable motion, up to the level of numerical simulations.

Following these results, this paper aims at realizing the one-link trident snake robot and examining the proposed algorithms in real experiments. One important point to be observed is practical effectiveness of the control algorithm, which is based on the kinematic analysis only. There are several discrepancies between theory and practice such as unmodeled dynamics, backlashes and noises, and selection of feasible periodic trajectories; all of them may cause erroneous result. Thorough the control experiments, we will show that our main purpose of locomotion control is still achievable even with these neglected uncertainties, though the accuracy of control might be affected to some extent.

II. KINEMATIC MODEL OF TRIDENT SNAKE ROBOT

Fig. 1 shows an overview of the trident snake robot developed by the authors. Fig. 2 shows its geometric model. In the center of its body, the robot has a root block; an equilateral triangular plate with three actuated joints at its vertexes. Each joint is driven by an actuator. Three links are connected to the root block via the joints, and each link has a passive wheel on its center.
We consider only planar motion in this paper. The robot has a root block with three actuated joints and three branch legs, which are connected to the root block via the joints. Each branch has a passive wheel, which is assumed not to slip, nor slide sideways. In this paper, we assume that model of the robot is the kinematic model and control input is the angular velocity of the joint. Furthermore, we assume that the radius of the triangle is of unit length, and the distance between a joint and a passive wheel is 1.

The front face of the robot is supposed to be the joint of the second branch $\phi_2$. The following constants indicate the directions of the joints $\phi_i$ relative to the front face

$$\alpha_1 = -2\pi/3 \quad \alpha_2 = 0 \quad \alpha_3 = 2\pi/3. \quad (1)$$

The position of the robot is represented by the coordinates $(x, y)$ of the center $P$. The orientation of the robot is represented by the angle between the $x$-axis and the line passing through $P$ and the joint of branch 2, say $\theta_0$. The configuration vector of the robot is

$$w := [x, y, \theta_0]^T.$$ 

Next, let $\phi_i$ denote the joint angle of the $i$th branch. All the joint variables $\phi_i$ are collected in a vector

$$\phi := [\phi_1, \phi_2, \phi_3]^T$$

where $\phi$ is called the shape vector of the robot.

### A. Kinematic Model and State Equation

Now let us turn to the kinematic model of the robot. We assume that the wheels are in ideal rolling contact with the floor, i.e., do not slide nor slip. This assumption leads us to the following nonholonomic constraints

$$A(\phi) R_{\theta_0}^T \dot{w} = B(\phi) \dot{\phi}$$

where we suppose $r = 1, l = 1$ for simplicity of notations.

This model has some relevance with a specific type of omnidirectional vehicle with three caster wheels [16], but there is a fundamental difference that the wheels are actively driven in the case of omnidirectional vehicle. If we consider $u := \dot{\phi}$ is the control input to the kinematic model (2), then we obtain $w = R_{\theta_0} A(\phi)^{-1} u$. However, for the sake of technical simplicity, we suppress the matrix inverse showing up in the state equation by introducing the following input transformation:

$$v = A(\phi)^{-1} u$$

and consider $v$ as a virtual control input from now on.

If $\det A(\phi) = 0$, we say the robot is in singular posture. Typical singular postures include the cases in which the non-holonomic constraints degenerate; e.g., two or more wheels are parallel to each other, or all wheels lie on concentric circles. Complete singularity analysis would be a complicated issue; however, the authors checked it numerically and ensured that $\det A(\phi) \neq 0$ holds for $|\phi_0| < \pi/3$. This suggests that we need not care about the singularity as long as the robot’s shape is not too far from $\phi = 0$.

Finally, setting $\xi = [\phi \ w]^T$ as the state vector, we have the state equation

$$\dot{\xi} = \begin{bmatrix} A(\phi) & R_{\theta_0} \end{bmatrix} v := [g_1(\xi) \ g_2(\xi) \ g_3(\xi)] v \quad (4)$$

where $g_1(\xi)$, $g_2(\xi)$, and $g_3(\xi)$ are smooth vector fields. Thus, we obtained a three-input and six-state driftless system.

### III. CONTROLLABILITY ANALYSIS AND LOCOMOTION PRINCIPLE

#### A. Controllability Analysis

Let $G$ be a smooth distribution spanned by the input vector fields,

$$G(\xi) := C^\infty \text{span} \{g_1, g_2, g_3\}(\xi). \quad (5)$$

The controllability distribution $\tilde{G}$ of the driftless system is defined as the smallest involutive distribution that contains $G$, i.e.,

$$G \subset \tilde{G} \quad \forall f, g \in \tilde{G} \Rightarrow [f, g] \in \tilde{G}. \quad (6)$$

Local controllability of driftless system is completely characterized by the full-rankness of $\tilde{G}$ [17].

In the case of the one-link trident snake, $\tilde{G}$ is obtained as

$$\tilde{G}(\xi) = C^\infty \text{span} \{g_{12}, g_{23}, g_{123}, g_{31}\}(\xi) \quad (7)$$

where $g_{12} := [g_1, g_2], g_{23} := [g_2, g_3], g_{123} := [g_{12}, g_3], g_{31} := [g_3, g_1]$. It is easy to see that the system is locally controllable if $A(\phi)$ is
nonsingular. Indeed, for $\phi = 0$ and arbitrary $w$

$$G(0, w) = \text{span} \left[ \begin{array}{cccccc}
-\frac{\sqrt{3}}{2} & 0 & -1 & 1 & -\sqrt{3} & 1 \\
0 & -1 & -2 & 1 & 0 & -2 \\
\frac{\sqrt{3}}{2} & 0 & -1 & 1 & \sqrt{3} & 1 \\
1 & 0 & 0 & 0 & 1 & 0 \\
0 & 1 & 0 & 0 & 1 & 0 \\
0 & 0 & 1 & 0 & 0 & 0
\end{array} \right]$$

spans the full tangent space $R^6$.

Remark 1: From the controllability point of view, the system has the same structure as the so-called first-order systems [18] given by

$$\dot{\xi} = \left[ \begin{array}{c}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1 \\
\xi_2 & -\xi_1 & 0 \\
-\xi_3 & 0 & \xi_1 \\
0 & \xi_3 & -\xi_2
\end{array} \right] v.$$  \quad (8)

Attitude control problem of 3-D spacecraft [19]–[21] is classified in the same class, too. The first-order system is structurally different from the so-called single generator systems such as chained systems [10]; its control is relatively difficult. Moreover, the system (4) is still more difficult to control than (8), because it is not nilpotent and the while the latter is nilpotent with the order of nilpotency 2. It is impossible to convert (4) to (8) exactly, approximate nilpotentization [22] is still possible.

B. Holonomy and Locomotion Principle

The following fact relates the effect of periodic control and the corresponding Lie brackets, usually known as holonomy or the area rule [17], [23].

Theorem 1: Let $q_1(t), q_2(t)$ be functions defined on $[0, T]$ and $Q_1(t), Q_2(t)$ be their integrals

$$Q_i(t) := \int_0^t q_i(\tau) d\tau, \quad i = 1, 2.$$  \quad (9)

Moreover, let $q_1(t), q_2(t)$ be $T$-periodic with mean 0

$$q_i(t + T) = q_i(t), \quad Q_i(0) = Q_i(T) = 0, \quad i = 1, 2.$$  \quad (10)

Now, suppose that we apply

$$v_i(t) = \epsilon q_i(t), \quad \text{for } i = 1, 2, \quad v_3(t) \equiv 0.$$  \quad (11)

to the driftless system (4) with $\xi(0) = \xi_0$ and $\epsilon > 0$. Then,

$$\xi(T) = \xi_0 + \epsilon^2 A[g_1, g_2](\xi_0) + O(\epsilon^3)$$  \quad (12)

holds, where $A$ is the area encircled by the closed loop on the $Q_1$–$Q_2$ plane.

According to this fact, the net change of the state $\xi(T) - \xi_0$ under sufficiently small periodic input is approximately equal to $\epsilon^3 A[g_1, g_2](\xi_0)$. For instance, consider the following periodic input

$$v(t) = \epsilon \left[ -\omega \sin \omega t, \omega \cos \omega t, 0 \right]^T.$$  \quad (13)

for $\xi_0 = 0$ and $T := 2\pi/\omega$. Then, the resulting change is

$$\xi(T) = \pi \epsilon^2 [1, 1, 0, 0, 0, 1]^T + O(\epsilon^3).$$  \quad (14)

This implies that the joints rotate in counterclockwise (CCW) by the same amount, while the root block comes back to its initial configuration (see Fig. 3).

IV. CONTROL ALGORITHM

In this section, we briefly describe the rotation and translation control algorithm for the trident snake robot. The previous method proposed in [8] has been improved in some respects to conform to physical experiments. In particular, the problem of shaping periodic trajectory $(Q_1, Q_2)$ is worth exploiting; it will be discussed in Sections IV-C and V-E.

A. Rotation Control

Rotation control is to change the orientation $q_1$ only, without changing its position $(x, y)$ and shape $\phi$. Without loss of generality, we assume that the initial state is $\xi_0 = 0$. It is easy to see that a linear combination of $g_{12}$ and $g_3$ gives

$$2g_{12}(0) + g_1(0) = [0, 0, 0, 0, 1]^T$$  \quad (15)

which corresponds to pure rotation. Thus, applying periodic input corresponding to $g_{12}$ followed by constant input corresponding to $g_3$ will result in the desired rotation. This idea is summarized by the following algorithm.

Algorithm 1. (Rotation control)

For given $\epsilon$ and $\omega$,

\begin{itemize}
  \item \textbf{Step 1:} Apply the periodic input (12) for $t \in [0, T]$ to bring about the displacement (13).
  \item \textbf{Step 2:} Apply constant input $v = [0, 0, 1]^T$ until $\phi$ comes back to 0.
\end{itemize}

Continuous rotation is also possible by repeating these two steps. It rotates in clockwise if $\omega$ is set negative ($T := |2\pi/\omega|$ in this case).

B. Translation Control

The purpose of translation control is to change the position of the robot $(x, y)$ in a desired direction by neither changing $q_1$ nor the joint angles $\phi$. 
The control strategy is similar to the previous one. Again, the initial shape is supposed to be $\phi_0 = 0$. Now let $\beta$ be the angle of the desired direction relative to the $x$-axis and define

$$g_T := (\cos \beta) g_1 + (\sin \beta) g_2$$

$$g_N := (\sin \beta) g_1 - (\cos \beta) g_2.$$ 

Now, we find a relation

$$[g_N, g_3](0) + 2g_T(0) = [0, 0, 0, \cos \beta, \sin \beta, 0]^T.$$ 

This implies that applying periodic input corresponding to $[g_N, g_3]$ followed by constant input corresponding to $g_T$ will result in pure translation (see Fig. 4). This idea is summarized by the following algorithm.

\begin{algorithm}
1) Apply the periodic input corresponding to $[g_N, g_3]$

$$v(t) = \epsilon [\cos \beta \sin \omega t, \cos \beta \cos \omega t, \cos \omega t]^T$$

2) Apply the constant input $v = [\cos \beta, \sin \beta, 0]^T$ corresponding to $g_T$, until $\phi$ comes back to 0.
\end{algorithm}

Continuous propulsion is also possible by repeating these two steps.

C. Selection of Periodic Inputs for Lie Bracket Motion

Let us briefly discuss the selection of suitable periodic inputs $(\epsilon q_1(t), \epsilon q_2(t))$ in the Step 1 corresponding to the desired Lie bracket.

First, we should note that the approximation (13) is effective as long as $\epsilon$ is sufficiently small. If we set $\epsilon$ too large, the amount of the approximation error increases; namely, the resulting motion is far different from the desired one. On the other hand, the smaller $\epsilon$ is, the slower the robot moves. Thus, moderate $\epsilon$ should be chosen considering this tradeoff.

Second, let us turn to discuss freedom in choosing periodic factors $(q_1, q_2)(t)$. There are infinitely many candidates whose integrals $(Q_1, Q_2)$ encircle a closed loop having area $A$. Three of such candidates are shown in Fig. 5 ($O$ is the origin of $Q_1-Q_2$ space).

\begin{algorithm}
Case (a): This is the simplest case. Just apply

$$(q_1, q_2) = (-\omega \sin(\omega t + \phi), \omega \cos(\omega t + \phi))$$
\end{algorithm}

where $\phi \in [0, 2\pi]$ is a constant parameter (initial phase) that determines the center of the circle.

\begin{algorithm}
Case (b): This is slightly modified so that the center of the closed loop coincides with $O$

$$(q_1, q_2) = \begin{cases} (1, 0), & t \in [0, \sigma] \\ (-\omega \sin(\omega t - \sigma), \omega \cos(\omega t - \sigma)), & t \in [\sigma, \sigma+T] \\ (-1, 0), & t \in [\sigma + T, 2\sigma + T]. \end{cases}$$
\end{algorithm}

In this case, the approximation error is relatively reduced because the maximal distance from $O$ to the points on the curve is smaller than that in case (a).

\begin{algorithm}
Case (c): The sign of $\phi$ is flipped alternatively, by combining two periods into a single set

$$(q_1, q_2) = \begin{cases} (-\omega \sin(\omega t + \phi), \omega \cos(\omega t + \phi)), & t \in [0, T] \\ (-\omega \sin(\omega t - \phi), \omega \cos(\omega t - \phi)), & t \in [T, 2T]. \end{cases}$$
\end{algorithm}

The approximation error in each half period $T$ is as same as in case (a). Since the proposed control algorithms are based on the approximation of the form (13), this approximation error is inevitable. This term results from the infinite series expansion of higher-order Lie brackets, so it is quite difficult to handle it exactly. Nevertheless, it is observed through numerical simulations [8] that the $O(\epsilon^3)$ term is dependent on the choice of the center of the circle. If we trace a pair of circles with antipodal centers as in case (c) of Fig. 5, their $O(\epsilon^3)$ terms would nearly cancel each other and leave smaller error as a result.

This technique is basically a trial to improve the approximation from $O(\epsilon^3)$ to order $O(\epsilon^4)$ by considering the second-order Lie brackets in addition to the first-order one, although its mathematical analysis is still on the way. At this moment, we adopt case (c) as a practical choice in the control experiments. We also compare it with cases (a) and (b) in Section V-E.

V. EXPERIMENTS

A. System Setup

The experimental setup is illustrated in Figs. 6 and 7. Radius of the root block (the distance between the center and a vertex) is $r = 0.1$ m and the distance between each joint and wheel is also $l = 0.1$ m. Total weight of the robot is 1.25 kg and the size is approximately 540 mm in diameter.

As for the joint control, we adopted R/C servomotor (Hitec HSR-5995GT; speed 7 rad/s, torque 24 kg-cm, weight 62 g, and size 40 mm $\times$ 20 mm $\times$ 37 mm) as actuator. This is a compact
B. Tracking Control of Joint Trajectories

The proposed control algorithms discussed so far were based on kinematics, where the control input \( u \) was supposed to be joint angular velocities. In order to realize them with voltage-input dc motors, we introduce simple trajectory tracking control as follows.

Let \( \mathbf{v}^*(t) \) be the control input computed by one of the proposed control algorithms. Recalling the input transformation (3), the reference joint trajectory \( \mathbf{\phi}^*(t) \) is obtained easily by integrating an ordinary differential equation

\[
\dot{\mathbf{\phi}}^*(t) = A(\mathbf{\phi}^*(t)) \mathbf{v}^*(t) \quad \mathbf{\phi}^*(0) = \mathbf{0}.
\] (15)

The desired joint angular acceleration \( \ddot{\mathbf{\phi}}^*(t) \) is computed by

\[
\ddot{\mathbf{\phi}}^*(t) = A(\mathbf{\phi}^*(t)) \dot{\mathbf{\phi}}^*(t) + \sum_{i=1}^{3} \frac{\partial A}{\partial \phi_i}(\mathbf{\phi}^*(t)) \dot{\phi}_i^*(t) \mathbf{v}^*(t)
\]

or more easily, just by numerical differentiation of \( \dot{\mathbf{\phi}}^*(t) \).

Now, the task has been reduced to make \( \dot{\mathbf{\phi}}(t) \) track the reference \( \dot{\mathbf{\phi}}^*(t) \). Roughly neglecting the interference between joints, dynamics of each joint can be modeled as a linear second-order system

\[
M_i \ddot{\phi}_i(t) + D_i \dot{\phi}_i(t) = e_i(t), \quad i = 1, 2, 3
\] (16)

where \( e_i \) is the applied voltage and \( M_i, D_i \) are mass–damper parameters. Consider the following feedback control law:

\[
e_i(t) = k_i (\phi_i^*(t) - \phi_i(t)) + M_i \ddot{\phi}_i^*(t) + D_i \dot{\phi}_i^*(t)
\] (17)

where \( k_i > 0 \). Then, the tracking error \( \ddot{\phi}_i(t) := \ddot{\phi}_i^*(t) - \ddot{\phi}_i(t) \) obeys the following stable error dynamics:

\[
M_i \ddot{\phi}_i(t) + D_i \dot{\phi}_i(t) + k_i \ddot{\phi}_i(t) = 0
\] (18)

implying \( \ddot{\phi}_i(t) \rightarrow 0 \).

C. Rotation Control

Now, we are ready to examine the proposed control algorithm. Figs. 9–12 show an experimental result of rotation control in CCW, where \( \epsilon = 0.3 \) and \( \omega = 4.5 \text{ rad/s} \). As mentioned earlier, the periodic pattern (c) in Fig. 5 is used for step 2.

Fig. 9 shows the time response of the joint angles. The solid line shows the actual angle \( \phi_i(t) \) while the dotted one shows the reference \( \phi_i^*(t) \). Nice tracking performance to the trajectory is observed despite tininess of the actuators. Note that all the joint angles come back to their initial position \( \phi = 0 \) at the end of step 2 (\( \tau \approx 1.8, 3.6[s] \)).

Fig. 10 shows parametric plot of the position \( (x,y) \) on the \( x-y \) plane, and Fig. 11 shows the time response of the orientation \( \theta_0 \); the solid lines show the experimental result and the dotted ones show the simulation. Note that the position \( (x,y) \) comes back to the origin at the end of step 2 \( (\tau \approx 1.8, 3.6[s]) \), while \( \theta_0 \) increases by about 0.18 [rad] per iteration. Some tracking error in shape control that was not fully compensated is found in Fig. 10. For further improvement of the tracking performance, it is worth trying to redesign the controller parameters \( M_i, D_i, k_i \).

Finally, Fig. 12 shows snapshots of an experiment where the algorithm is repeated three times.
Fig. 9. Time response of joint angles (rotation, CCW).

Fig. 10. Parametric plot of position $(x, y)$ (rotation, CCW) (unit added).

Fig. 11. Time response of $\theta_0$ (rotation, CCW).

**D. Translation Control**

Let us turn to an experimental result of translation control along the $x$-axis ($\beta = 0$), where $\epsilon = 0.3$ and $\omega = 4.0$ rad/s. Fig. 13 shows the time response of $x$, which increases by about 3.5 cm per iteration. Fig. 14 shows snapshots of the result, where the algorithm is repeated three times. We also succeeded in translation control in arbitrary direction specified by $\beta$.

**E. Comparison With Cases (a) and (b)**

In this paper, we performed experiments with the periodic input of case (c) in Fig. 5. Let us compare them with the other choices.

Experimental result of rotation control using case (a) is shown in Fig. 15. This is a parametric plot of the position $(x, y)$, where the small dots show the position at the instances of the end of
step 1. It is easy to see that the circles drift from the original one as the iteration goes on, due to the approximation error discussed in Section IV-C. This choice is significantly inferior to case (c) on comparing with Fig. 10.

On the other hand, case (b) shows nice performance in Fig. 16 in terms of the time response of the orientation $\theta_0$, which is even better than case (c) in Fig. 10. As mentioned in Section IV-C, this is mainly because the position $(x, y)$ is closer to the origin than cases (a) and (c). But the motion of the robot is quicker and smoother in case (c) relative to the speed.

As a consequence, case (c) is comparatively practical for speedy and ceaseless motion, but case (b) may be an alternative choice for slow and precise.

VI. CONCLUSION AND FUTURE WORK

In this paper, we implemented the one-link trident snake robot and performed physical experiments of rotation and translation control. We confirmed that the proposed algorithm is practical enough with proper choice of periodic input patterns.

The authors expect that this robot will be a common test bed for studying this class of nonholonomic systems (nonnilpotent and two generators). Other approaches, such as discontinuous feedback control [19], switching control [24] or averaging-based control [25], [26] are worth investigating. There remain several tasks to be dealt with in future works. First, the experimental setup needs refinement such as extending the robot to the multi-link version and developing the wireless control system with embedded microcomputer. Second, for accurate positioning and/or tracking under the presence of wheel slippage, on-line localization of the robot’s position and its feedback is inevitable [27]; the authors are currently working on point-to-point feedback. Other future topics include improvement of the robot’s dynamic behavior (16) and intelligent navigation problem including obstacle avoidance [5], [28].

REFERENCES


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