

Highlights

- Influence of surrounding environment on the crack velocity in marble was studied.
- Crack velocity in air increased at higher temperature and/or humidity.
- Subcritical crack growth in marble occurs in grain boundary.
- Region II behavior of subcritical crack growth was observed in marble with low porosity in air.

Influence of surrounding environment on subcritical crack growth in marble

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Abstract

Understanding subcritical crack growth in rock is essential for determining appropriate measures to ensure the long-term integrity of rock masses surrounding structures and for construction from rock material. In this study, subcritical crack growth in marble was investigated experimentally, focusing on the influence of the surrounding environment on the relationship between the crack velocity and stress intensity factor.

The crack velocity increased with increasing temperature and/or relative humidity. In all cases, the crack velocity increased with increasing stress intensity factor. However, for Carrara marble (CM) in air, we observed a region in which the crack velocity still increased with temperature, but the increase in the crack velocity with increasing stress intensity factor was not significant. This is similar to Region II of subcritical crack growth observed in glass in air. Region II in glass is controlled by mass transport to the crack tip. In the case of rock, the transport of water to the crack tip is important. In general, Region II is not observed for subcritical crack growth in rock materials, because rocks contain water. Because the porosity of CM is very low, the amount of water contained in the marble is also very small. Therefore, our results imply that we observed Region II in CM.

Because the crack velocity increased in both water and air with increasing temperature and humidity, we concluded that dry conditions at low temperature are desirable for the long-term integrity of a carbonate rock mass. Additionally, mass transport to the crack tip is an important process for subcritical crack growth in rock with low porosity.

41 **Keywords:** subcritical crack growth, marble, relative humidity, temperature, water,
42 porosity

1. Introduction

The long-term stability of rock masses surrounding structures, such as underground repositories of radioactive waste, caverns to store liquid natural gas and liquid petroleum gas, and underground power plants, is crucial. In addition, it is important to ensure the stability of rock slopes in open-pit mines for safety. Various studies have examined time-dependent fracturing in rock to determine the time-dependency of rock stability (Atkinson, 1984; Swanson, 1984; Meredith and Atkinson, 1985; Sano, 1988; Nara and Kaneko, 2005, 2006). In particular, studies of time-dependent fracturing in rock have been conducted to examine the natural hazards related to failure in rock, such as the increase in seismicity seen prior to earthquake rupture, fault formation, growth, sliding, and volcanic eruption (Kilburn and Voight, 1998; Ciccotti et al., 2000a, 2001; Heap et al., 2011; Brantut et al., 2013, 2014a; Violay et al., 2013). Additionally, several studies have evaluated the long-term strength and time-to-failure based on the measurement of time-dependent fracturing (Schmidtke and Lajtai, 1986; Jeong et al., 2007; Nara et al., 2013; Nara, 2015).

Although classical fracture mechanics postulates that crack propagation occurs when the value of the stress intensity factor reaches that of the fracture toughness, the crack can propagate even at a stress intensity factor lower than the fracture toughness. This is known as subcritical crack growth, which is considered to be one of the main mechanisms responsible for the time-dependent behavior of rock in the brittle regime (Atkinson, 1984). Most studies of subcritical crack growth in rock have been conducted on silicate rocks, such as igneous rocks (Sano and Kudo, 1992; Nara et al., 2009, 2010), sandstones (Holder et al., 2001; Ponson, 2009; Nara et al., 2011, 2014), and novaculite (Atkinson, 1980).

Only a few studies have examined subcritical crack growth in carbonate minerals and rocks. Henry et al. (1977) reported that for micrite the crack velocity in water is higher than that in air. Røyne et al. (2011) suggested that some plastic processes might affect subcritical crack growth in calcite. Rostom et al. (2012) reported that the fluid salinity influences the crack velocity in calcite in a NaCl solution; specifically, they showed that the stress intensity factor decreased when the concentration of NaCl is <0.8 mol/L. Bergsaker et al. (2016) examined the impact of the fluid composition on subcritical crack growth in calcite single crystal, and concluded that a pH in the range of 5 – 7.5 has a negligible influences. However, subcritical crack growth in carbonate rocks under different temperature and humidity conditions is poorly understood.

In this study, we investigated subcritical crack growth in marble experimentally in both air and water. We focussed on examining the influence of the surrounding environment on the relationship between the crack velocity and stress intensity factor by conducting all measurements under controlled temperature and relative humidity.

2. Rock samples

We used examined two types of marble: Carrara marble (CM) quarried in Italy, and a marble quarried in Skopje in Macedonia (MM).

Figure 1 shows photomicrographs of CM and MM observed with thin sections of 0.03 mm thickness. As shown in the photomicrograph, the grain size is around 0.2 mm and 0.3 mm for CM, and MM, respectively. Figure 2 shows the results of X-ray diffraction analysis of the marbles. Remarkable peaks can be seen for calcite (CaCO_3) in CM and dolomite ($\text{CaMg}(\text{CO}_3)_2$) in MM. Small peaks of illite are also seen in MM.

For CM, the porosity determined by water saturation was 0.19%. The P-wave velocities in three orthogonal directions were 6.04, 5.98, and 5.90 km/s under dry conditions. CM is considered to be isotropic. The Brazilian tensile strength was 6.9 MPa. The uniaxial compressive strength, Young's modulus, and Poisson's ratio were 77.8 MPa, 51.0 GPa, and 0.32, respectively, which were determined from uniaxial compression tests with the loading rate at 10^{-5} strain/s.

For MM, the porosity measured by water saturation was 0.6%. The P-wave velocities in three orthogonal directions were 4.15, 4.06, and 3.74 km/s. We named these three orthogonal directions Axes 1, 2, and 3 in order of decreasing P-wave velocity.

Furthermore, we named the planes normal to these axes Planes 1, 2, and 3, respectively.

Slight anisotropy was observed in the P-wave velocity. Since investigation of anisotropic properties was beyond the scope of this study, we treated the marble sample as an isotropic material. The Brazilian tensile strength was 6.2 MPa when the fracturing was parallel to Plane 3. The uniaxial compressive strength, Young's modulus, and Poisson's ratio were 190 MPa, 80.2 GPa, and 0.46, respectively, which were determined from uniaxial compression tests with the loading rate at 10^{-5} strain/s.

3. Methodology

3.1 Outline of double torsion method

In this study, the double torsion (DT) method was used. The DT method is a fracture mechanics testing method used commonly to study subcritical crack growth. The loading configuration of the DT method is shown in Figure 3. Three different types of test can be performed using the DT arrangement, each using different loading conditions: the constant load method (Kies and Clark, 1969), the constant displacement rate method (Evans, 1972), and the load relaxation (RLX) method (Evans, 1972; Williams and Evans, 1973). Using the RLX method, we can obtain a large amount of data on the relationship between the stress intensity factor, K_I , and the crack velocity, da/dt (the K_I - da/dt relation), which, in general, ranges from 10^{-2} to 10^{-9} m/s, using only a single experimental run. Therefore, we used the RLX method to determine the K_I - da/dt relation in this study.

In the RLX method, the displacement of the loading points must be kept constant during the experiment while the temporally decreasing load (load relaxation) due to the crack growth is measured. The stress intensity factor and the crack velocity are expressed as follows (Williams and Evans, 1973):

$$K_I = Pw_m \sqrt{\frac{3(1+\nu)}{Wd^3d_n}} \quad (1)$$

$$\frac{da}{dt} = -\varphi_c \times \frac{Wd^3G}{3w_m^2} \frac{S_i P_i}{P^2} \frac{dP}{dt} \quad (2)$$

where P is the applied load, w_m is the moment arm (18 mm in this study), ν is Poisson's ratio, W is the width of the specimen, d is the thickness of the specimen, d_n is the

reduced thickness of the specimen, P_i is the initial value of the applied load, S_i is the compliance of the specimen at the initial crack length, dP/dt is the load relaxation rate, and G is the shear modulus. φ_c is a constant that is dependent on the shape of the crack front. We set the value of φ_c as 0.4 from observation of the crack front following Sano (1988). Evans (1972, 1973), Williams and Evans (1973), and Meredith (1983) concluded that the Mode-I stress intensity factor is evaluated from the DT test based on their experimental results using polycrystalline materials including rocks. As shown in Eq. (1), the stress intensity factor is independent of the crack length in the DT test. Because it is impossible to detect the crack tip in rock specimens, various researchers have employed DT tests to investigate subcritical crack growth (Atkinson, 1984; Atkinson and Meredith, 1987). For similar reasons, we employed the DT test in this study.

The size of the DT specimen must satisfy the following condition (Atkinson, 1979; Pletka et al., 1979):

$$12d \leq W \leq L/2 \quad (3)$$

where L is the length of the specimen. Ciccotti et al. (2000b) performed a finite element analysis to demonstrate the option of using specimens thicker than those recommended by Atkinson (1979). Previous studies (Shyam and Lara-Curzio, 2006; Madjoubi et al., 2007) recommended that the length of the specimen should be greater than twice the width.

Taking the above studies into consideration, we set the width W , length L , and thickness d to be 45, 140, and 3 mm, respectively. The width and depth of the guide groove were both 1 mm.

3.2 Experimental apparatus and conditions

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156 The experimental apparatus used in this study was the same as that used by Nara and
157 Kaneko (2005, 2006) in air, and Nara et al. (2009) in water. The apparatus was set in a
158 room where the temperature and relative humidity could be controlled over ranges of
159 278–353 K, and 40–90%, respectively.

160 The subcritical crack growth in air was measured under different temperatures at
161 fixed relative humidity and vice-versa to investigate the influences of temperature and
162 relative humidity separately. We performed experiments under low temperature (293 K,
163 47–50%), intermediate temperature (323–324 K, 50%), and high temperature (351 K,
164 50%) conditions to investigate the influence of temperature; and under low humidity
165 (323 K, 5–7%), intermediate humidity (323–324 K, 50%), and high humidity (323–324
166 K, 89–92 %) conditions to investigate the influence of relative humidity. We could only
167 control the temperature of the air in the apparatus. Therefore, the measurements in water
168 were made at slightly different temperatures than those in air. The subcritical crack
169 growth was measured at low temperature (290–291 K), and at intermediate temperature
170 (313–319 K) in water.

171

172 3.3 Experimental procedure

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174 Initially, precracking was performed. We applied a displacement of 4 μm at the
175 loading point, and then maintained the displacement at this distance to observe the
176 surface of the specimen, with a digital microscope set under the specimen to determine
177 the crack length. We continued these operations until the crack length reached 25 mm,
178 which is the minimum length required so that the stress intensity factor is independent
179 of the crack length for a DT specimen (Trantina, 1977).

After precracking, the specimen was exposed to the experimental environment at a constant temperature and relative humidity for more than 20 hours. Then, measurements following the RLX method were made.

For rock, hysteresis in the K_I - da/dt relation has been reported during measurements using the RLX method several times with a single specimen. Sano (1988) suggested that the source of this hysteresis was friction and locking on the crack surfaces, because no hysteresis was observed on soda-lime glass. When measurements using the RLX method are performed, it is essential to minimise the influence of friction and locking. Hence, it is important to open the crack as much as possible, not to repeat opening and closing of the crack, and to perform only a single experimental run with one specimen to avoid the significant influence of friction and locking.

Based on the above considerations, after applying a preload of 14–15 N (27–30% of the maximum load) to avoid hitting the specimen, we applied displacements of 0.300 mm and 0.332 mm at the loading points of CM and MM specimens, respectively, because the DT specimens completely broke if we increased the displacement.

For the measurements in water, we used the distilled water in which the marble samples had been stored for more than 1 month. The pH of the water was measured just after measuring the subcritical crack growth. Figure 4 shows a photo of the experimental apparatus and a pH measurement.

4. Results

We performed several experiments under the same conditions to verify reproducibility. Figure 5 shows the temporal changes of the applied load, which are known as load-relaxation curves. Using the relations shown in Figure 5, we estimated the crack velocity and the stress intensity factor (Williams and Evans, 1973).

The crack velocity da/dt is empirically related to the stress intensity factor K_I , as follows (Charles, 1958; Wiederhorn and Bolz, 1970):

$$\frac{da}{dt} = AK_I^n \quad (4)$$

$$\frac{da}{dt} = v_0 \exp\left(\frac{-E^\ddagger + bK_I}{RT}\right) \quad (5)$$

where $E^\ddagger$ is the stress-free activation energy, R is the gas constant, T is the absolute temperature, and the other variables are experimentally-determined constants. n is the subcritical crack growth index (Atkinson, 1984). We used these equations to summarize the experimental results. In particular, we used the following equation of the exponential law:

$$\left. \begin{aligned} \ln\left(\frac{da}{dt}\right) &= \alpha + \frac{b}{RT} K_I \\ \because \alpha &= \ln v_0 - \frac{E^\ddagger}{RT} \end{aligned} \right\} \quad (5')$$

The K_I - da/dt relation for CM and MM at constant temperature in air with different relative humidities, and in water, are shown in Figure 6. The crack velocity increased with increasing relative humidity in air. In addition, the crack velocity in water was significantly higher than that in air. For CM in air, the slope was smaller when the crack velocity was $> 10^{-4}$ m/s.

Tables 1 and 2 summarize the results from the subcritical crack growth measurements

for CM and MM in air and water under different relative humidities, respectively. The stress intensity factor for $da/dt = 10^{-5}$ [m/s], $K_I(10^{-5})$, is listed to quantitatively compare the values because the range in the crack velocity is 10^{-2} – 10^{-8} m/s. Table 1 lists the values of the crack velocity at $K_I = 1.0$ [MN/m^{3/2}], $da/dt(1.0)$. In the case of CM in air, the crack velocity values $< 10^{-4}$ m/s were analyzed. The values of the average and standard deviation were estimated from several experimental results performed under the same conditions. The crack velocity in air increases as the relative humidity increases. Additionally, the crack velocity in water is significantly higher than that in air.

Figure 7 shows the K_I - da/dt relation at different temperatures in air at a constant relative humidity, and in water for CM and MM. The crack velocity increases with increasing temperature. In Figure 7a, the slope is small when the crack velocity is $> 10^{-4}$ m/s for CM in air. This decrease in the slope is remarkable, which implies Region II subcritical crack growth (Lawn, 1974, 1993).

Tables 3 and 4 show the subcritical crack growth measurements for CM and MM, respectively, at different temperatures, in air under a constant relative humidity and in water. In the case of CM in air, the values of crack velocity $< 10^{-4}$ m/s were analyzed. As the temperature increases, the crack velocity increases, while the stress intensity factor decreases in both air and water. The crack velocity in water is higher than that in air.

5. Discussion

Water significantly affects subcritical crack growth in marble. Specifically, the increase in the crack velocity in water is remarkable.

If the fracture toughness of marble is obtained, we can verify the range of the stress intensity factor where subcritical crack growth occurs. Therefore, determining fracture toughness is important. Several researchers have measured the fracture toughness using DT tests (Atkinson, 1979; Meredith, 1983; Meredith and Atkinson, 1985; Nara, 2015; Nara et al., 2012). Since fracture toughness depends on the environmental conditions such as temperature (Meredith and Atkinson, 1985; Funatsu et al., 2004, 2014), relative humidity (Nara et al., 2012), water vapor pressure (Kataoka et al., 2015), and water (Vavro and Souček, 2013), it is necessary to conduct fracture toughness measurements under controlled environmental conditions. Consequently, we measured the fracture toughness of marble under controlled temperatures and relative humidities~~y~~ using the constant displacement rate method of DT test (Evans, 1972) with the same methodology as Nara et al. (2012) (see Appendix).

Table 5 summarizes the results of the fracture toughness measurements in the marble samples in air while controlling the temperature and relative humidity. For MM, the fracture toughness was measured in air at different temperatures with the same relative humidity. The fracture toughness of MM decreases as the temperature increases. This tendency agrees well with that for the Mode-I fracture toughness of Kimachi sandstone reported by Funatsu et al. (2004, 2014).

Table 5 also summarizes the results of the fracture toughness measurements for CM in air (293K, 47%). The results of CM and MM were used to check the range of the stress intensity factor in which subcritical crack growth occurs. Figure 8 shows the

relationships between the crack velocity and the stress intensity factor normalized by the fracture toughness determined under the same environmental conditions. The subcritical crack growth of marble occurs in the same range as the normalized stress intensity factor, which is higher than 74% of the fracture toughness in this study. If the values of the subcritical crack growth index n (in Eq. (4)) and constant b (in Eq. (5)) increase, the range of the stress intensity factor causing subcritical crack growth decreases. This can contribute to the long-term stability of rock (Nara et al., 2013).

It is important to compare the results in this study to previous studies. Henry et al. (1977) showed that the crack velocity in micrite in water is higher than that in air, and the slope (the value of subcritical crack growth index) in water is lower than that in air. These tendencies agree well with the results in this study. On the other hand, according to the result of calcite crystal by Bergsaker et al. (2016), the difference between the crack velocity in distilled water and that in air is unclear. It is considered that the extent of the influence of water on subcritical crack growth in rock completely differs from a single crystal. Røyne et al. (2011) showed the results of subcritical crack growth measurement on calcite single crystals. They reported that the variation in the crack velocity at a given energy release rate might be caused by the plastic process or other unclarified process.

Figure 9 depicts the relationships between the crack velocity and the stress intensity factor for CM, MM, and calcite crystal (Røyne et al., 2011; Rostom et al., 2012). Since the measured values of the stress intensity factor differ significantly between the marbles in this study and the calcite crystals (Røyne et al., 2011; Rostom et al., 2012), the stress intensity factors in Figure 9 are normalized by the fracture toughness. For CM and MM, the values obtained in air at the same temperature are used (see Table 5). The fracture toughness of the calcite crystal is $0.22 \text{ MN/m}^{3/2}$ (Chen et al., 2001; Shushakova

et al., 2013). The shape of the relationship for the calcite crystal is nonlinear, although the shape for marbles is linear. The nonlinearity for the calcite crystal can be recognized in different environmental conditions (Røyne et al., 2011; Rostom et al., 2012; Bergsaker et al., 2016). It is considered that the mechanism controlling subcritical crack growth in marble differs from that in calcite crystal. To understand why the mechanism controlling subcritical crack growth differs, the crack path must be observed.

Figure 10 shows images of the crack paths in CM (Figure 10a) and MM (Figure 10b) from thin sections (0.03mm thickness) observed using an optical microscope under an open nicol, because this allowed the most clear crack path to be observed. On the other hand, the crack path could not be observed clearly under crossed nicols. To prepare a thin section, first an epoxy resin was permeated into the cracks. Then thin sections were prepared to observe the tension plane (the lower plane in Figure 3). In Figure 10, green, which corresponds to the epoxy resin, indicates the crack path. The crack path is mainly inter-granular, and trans-granular crack paths are quite rare. Sano (1981) suggested that microcracking occurs ahead of the crack tip in DT specimens of granite using the source location of the acoustic emission. Swanson (1984) suggested that the fracture process zone is generated ahead of the crack tip in DT specimen of rock. Nasser et al. (2007) suggested that the fracture process zone was generated ahead of the crack tip and the crack grows by connecting smaller microcracks in the fracture process zone in granite.

It is considered that the fracture process zone is generated in marble. Considering that the inter-granular crack path is dominant for marble, microcracking in the fracture process zone occurs at the boundary of mineral grains mainly. Thus, the crack growth in the grain boundary is more important in marble than the crack growth within a mineral grain. In particular, it is suggested that fracturing in cement materials at a grain boundary is important for subcritical crack growth in marble.

The crack path in marble is not perfectly planer (Figure 10). Previous studies did not observe planer crack paths for subcritical crack growth in rocks (Meredith and Atkinson, 1983; Swanson, 1985, 1987; Kudo et al., 1992; Nara and Kaneko, 2005; Nara et al., 2006, 2011). In this study, a rectangular guide groove is put on the specimen (Figure 3), generating a zigzag path. Nara and Kaneko (2005) tried to constrain the crack path to a straight line by preparing a semi-circular guide groove and a tri-angular guide groove on the DT specimen; they demonstrated that straight crack paths are not generated. Consequently, the larger scattering is obtained due to the crack propagation away from the bottom of the semi-circular and triangular grooves, where the crack thickness is not constant. Considering this result, the rectangular guide groove has been used to measure subcritical crack growth (e.g., Nara and Kaneko, 2006; Nara et al., 2011, 2013) and fracture toughness (e.g., Nara et al., 2012).

The results in this study are also compared to the results in a previous study of subcritical crack growth in igneous rocks shown in Nara et al. (2013). In igneous rocks, the crack velocity in distilled water was higher than that in air at 50% relative humidity by two to four orders of magnitude (Nara et al., 2013). The increase in the crack velocity in marble was greater than that recorded in igneous rock. As shown in Figure 2, MM contained illite. Francisca et al. (2005) reported that the strength of sediment containing illite decreased with increasing water content. Nara et al. (2011) showed that the crack velocity increased in rock containing illite with increasing water content. The results of these two studies agreed with those of this study. Thus, the presence of clay in rock increases the crack velocity in water.

Temperature affected the increase in the crack velocity in marble. Weakening processes, i.e. stress corrosion, can occur at the crack tip under tension (Anderson and Grew, 1977). In the case of silicate materials, it has been suggested that weakening of

siloxane bonds via chemical reaction with water occurs at the crack tip under tension (Michalske and Freiman, 1982). However, alternative mechanisms should also be considered for carbonate rocks.

Additionally, other chemical reactions between a carbonate mineral and water should be considered. Various researchers have studied the dissolution kinetics of calcite (e.g., Garrels and Christ, 1965; Sjöberg and Rickard, 1984; MacInnis and Brantley, 1992; Liang et al., 1996; Shiraki et al., 2000). The solubility of many carbonate minerals in water decreases as the temperature increases (Garrels and Christ, 1965). This property may suppress subcritical crack growth in carbonate materials. However, Nara et al. (2010) suggested that the electric double layer formed around the crack tip affects the acceleration of subcritical crack growth. Since the aperture of the crack close to the crack tip is very small, it is possible that the water vapor turns to liquid water by capillary condensation in this zone. Consequently, the crack path close to the crack tip is immersed in liquid water (Thomson, 1871; Nara et al., 2010; Nakao et al., 2016). In this case, an electric double layer is formed in the condensed water around the crack tip and a repulsive force acts between the crack planes. The electric double layer increases as the temperature increases (Shaw, 1980), causing the repulsive force in the crack tip to increase, which can decrease the activation energy of subcritical crack growth. This effect can reduce the stress intensity factor applied at the crack tip at a given crack velocity.

Variations in the slope of the K_I - da/dt relation for CM in air were observed. A similar trend has been observed in soda-lime glass (Wiederhorn, 1967), and in alumina (Evans, 1972) in air. Subcritical crack growth is divided into three key regions based on the mechanisms that control the crack velocity. In Region I, the crack velocity is controlled by the rate of stress corrosion. In Region II, the crack velocity is controlled by the rate

of transport of the reactive agent to the crack tip (Lawn, 1974, 1993). In Region III, the crack propagation is insensitive to the chemical environment and occurs mechanically (Wiederhorn et al., 1974). This is the classic tri-modal behaviour of the K_I - da/dt relation for subcritical crack growth. Figure 11 shows schematic illustrations of the tri-modal behaviour of the K_I - da/dt relation (Figure 11a) and that obtained for silica glass (Figure 11b). The change in the slope can be seen clearly for glass in air.

For CM in air, the region with a low slope can be seen clearly. This is likely to represent Region II of subcritical crack growth, in which the mass-transport rate of the reactive agent (in this case, water) controls the crack velocity. Since water is included within the rock materials, Region II is not usually observed in rock in air. According to Nakao et al. (2016), rock materials contain water in cracks and pores of tiny aperture because of the capillary condensation of water vapour. In the case of CM, the porosity is very low (0.19 %), and the water content is also very low, so that the transport rate of the water to the crack tip largely depends on the surrounding environmental conditions, similar to glass and alumina. For this reason, we were able to observe the region in which the transport of the reactive agent (water) controlled the crack velocity for subcritical crack growth in CM in air. In contrast, the porosity of MM is 0.6%, which is higher than that of CM, and Region II crack growth was not observed, even in air.

The subcritical crack growth index n in water was lower than that in air for both types of marble. This tendency was similar to that previously observed in igneous rocks (Nara et al., 2013). Lower subcritical crack growth index results in lower long-term strength and shorter time-to-failure (Nara et al., 2013). This implies that long-term integrity will be realized under dry condition if structures are constructed in marble rock masses.

The results of this study provide insight on time-dependent fracturing under tension. Therefore, data under confining pressures is necessary to consider the long-term

390 stability in a rock mass in the underground. According to Brantut et al. (2014b),
391 pressure solution can occur in calcite under compression. In addition, data under higher
392 temperature is required. De Bresser et al. (2005) reported that the compressive strength
393 of Carrara marble at a confining pressure of 300 MPa decreases as the temperature
394 increases up to 1000 °C. Even in a compressive stress field such as underground, tensile
395 stress can occur locally. Thus, the information and knowledge under tension as well as
396 those under compression are important to ensure the long-term stability of rock masses.

6. Conclusion

Subcritical crack growth in marble was investigated experimentally in both air and water. Specifically, the influence of the surrounding environment on the relationship between the crack velocity and the stress intensity factor was investigated by conducting all measurements under controlled temperature and relative humidity.

The crack velocity in water was significantly higher than that in air. The crack velocity increased with increasing relative humidity in air, and with increasing temperature in both air and water. For CM in air, Region II crack growth was observed, which was due to the low porosity of CM.

The increasing crack velocity with increasing temperature and humidity implies that dry conditions at low temperature are desirable for the long-term integrity of carbonate rock masses. Additionally, mass transport to the crack tip represents a key process for subcritical crack growth in rock with low porosity.

Appendix – Fracture toughness measurement using double torsion test

The constant displacement rate method of the DT test (DT-CDR test) was used for the measurement of the fracture toughness in this study. In the DT-CDR test, the displacement rate of the loading points has to be kept constant during the experiment. When this method is used for the fracture toughness measurement, the displacement rate of the loading points should be large (Shyam and Lara-Curzio, 2006); this is especially important for applying this particular method to the calculation of fracture toughness. Selçuk and Atkinson (2000) reported an influence of measured stress intensity factor with loading rate when employing the DT-CDR method, with the use of a high displacement rates (above approximately 0.07 mm/s) mitigating this effect.

In the DT-CDR test as a fracture toughness measurement, the maximum value of applied load at failure is used to calculate fracture toughness via the following equation:

$$K_{Ic} = P_{\max} w_m \sqrt{\frac{3(1 + \nu)}{Wd^3 d_n}} \quad (A1)$$

where K_{Ic} is Mode-I fracture toughness, and $P_{\max}$ is the maximum value of the applied load.

Atkinson (1979), Meredith (1983) and Meredith and Atkinson (1985) applied the DT-CDR method using displacement rates of approximately 20 mm/min (around 0.33 mm/s) (Atkinson, 1979; Meredith, 1983) and 10 mm/min (around 0.17 mm/s) (Meredith, 1983; Meredith and Atkinson, 1985), respectively. These displacement rates are higher than that mentioned by Selçuk and Atkinson (2000). Meredith (1983) reported that the fracture toughness values obtained by DT-CDR method agreed well with those obtained by the short-rod method which is the standard method for Mode-I fracture toughness measurement of rock (International Society for Rock Mechanics, 1988). Based on these

considerations, DT-CDR test in this study was performed using by applying a load at a displacement rate of 0.23 mm/s, which is the maximum rate of our apparatus and higher than the rate suggested by Selçuk and Atkinson (2000).

Experimental procedure is same as Nara et al. (2012). Firstly, the rock specimens are pre-cracked in order to introduce a small starting crack as described in Section 3.3. Then the apparatus and specimen were exposed to the environmental condition of interest with the same temperature and relative humidity for approximately 20 hours. Following this period, a fracture toughness measurement with DT-CDR method was performed using by applying a load at a displacement rate of 0.23 mm/s, after applying a small amount of pre-load around 10 N.

A photo of the apparatus used in this study is shown in Figure A-1. This apparatus consists of a speed-control (stepping) motor that drives the loading axis moving perpendicular to the DT specimen. This apparatus is housed in a temperature and humidity controlled room.

In Figure A-2, a photo of the DT specimen of MM used in the fracture toughness measurement is shown. All DT specimens were completely broken in the fracture toughness measurement. In Figure A-3, examples of the raw data from CM and MM are presented in the form of load vs. time plots. Using the maximum value of the applied load, the fracture toughness can be estimated.

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Figures

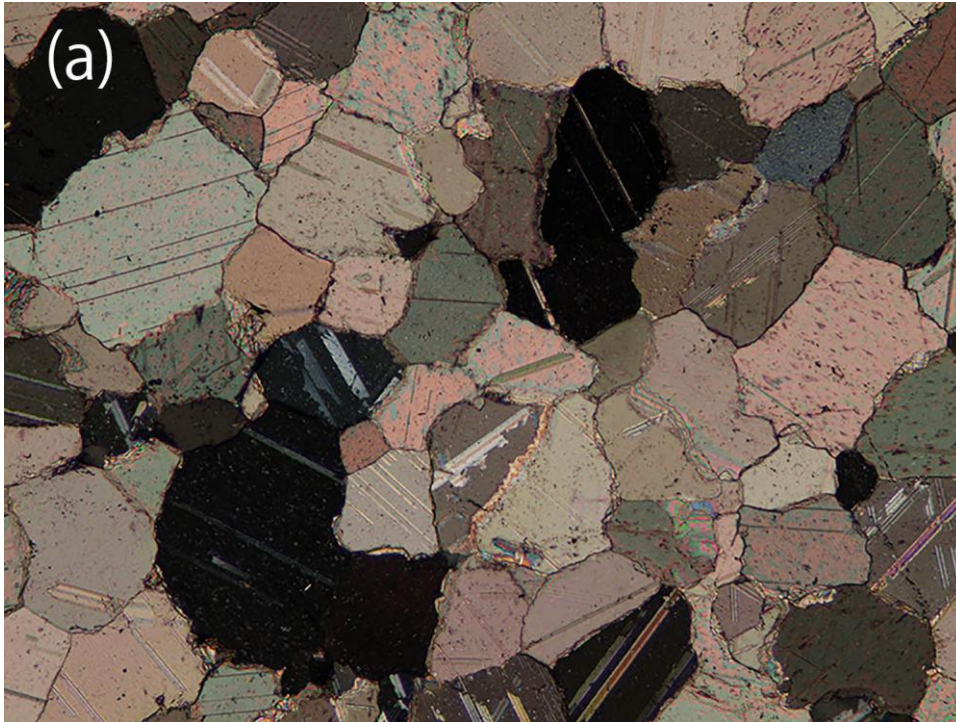


Figure 1. Photomicrographs of (a) Carrara marble (CM) and (b) Macedonian marble (MM) observed with a thin section under crossed nicols. The width and height of the sections are 1.5 mm and 1.1 mm, respectively.

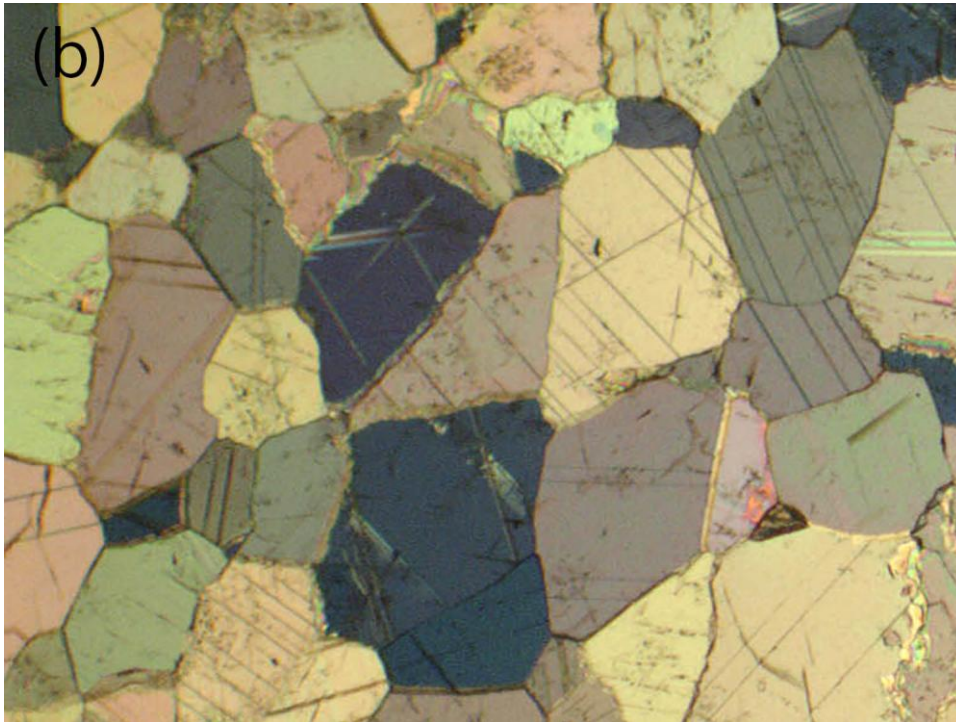


Figure 1. Photomicrographs of (a) Carrara marble (CM) and (b) Macedonian marble (MM) observed with a thin section under crossed nicols. The width and height of the sections are 1.5 mm and 1.1 mm, respectively.

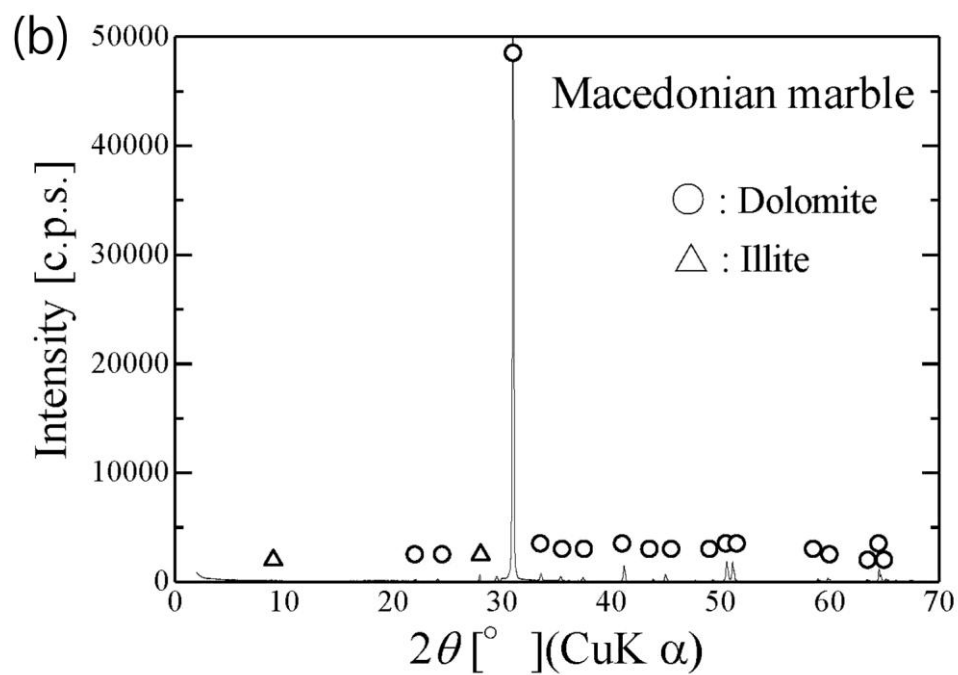
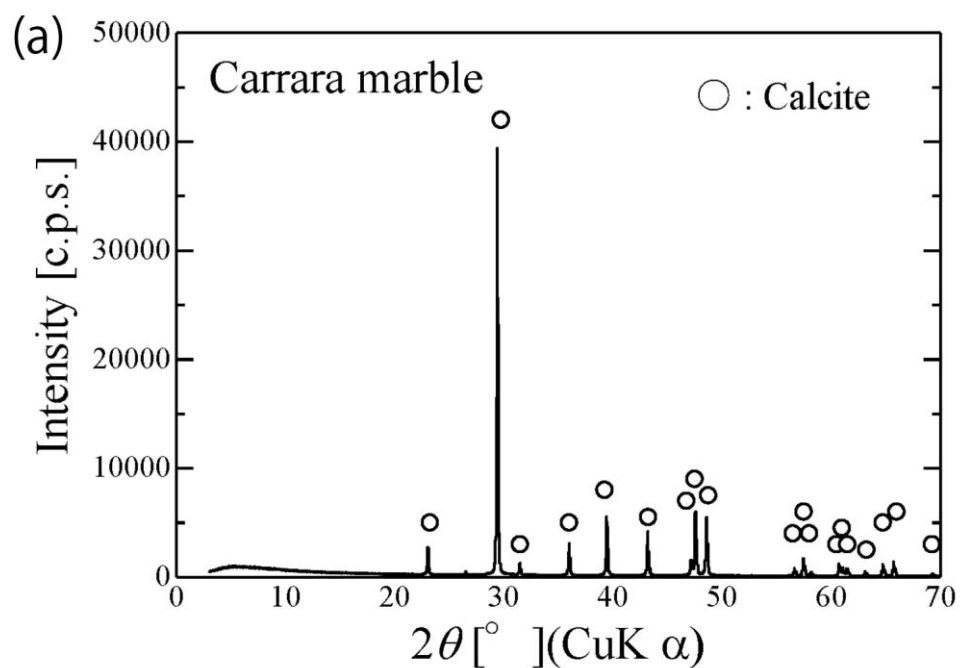


Figure 2. X-ray diffraction patterns for (a) CM and (b) MM.

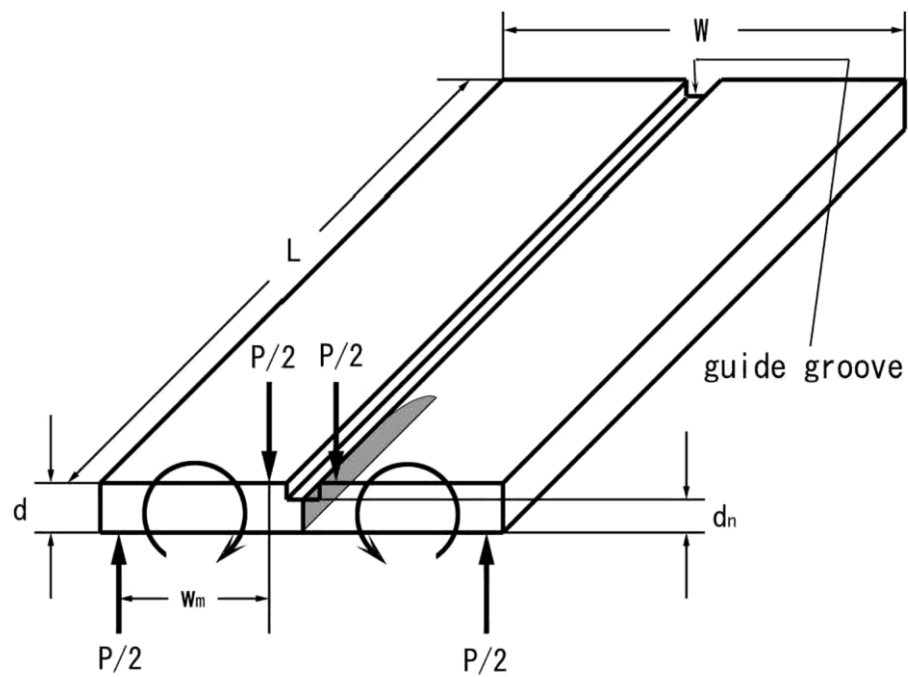
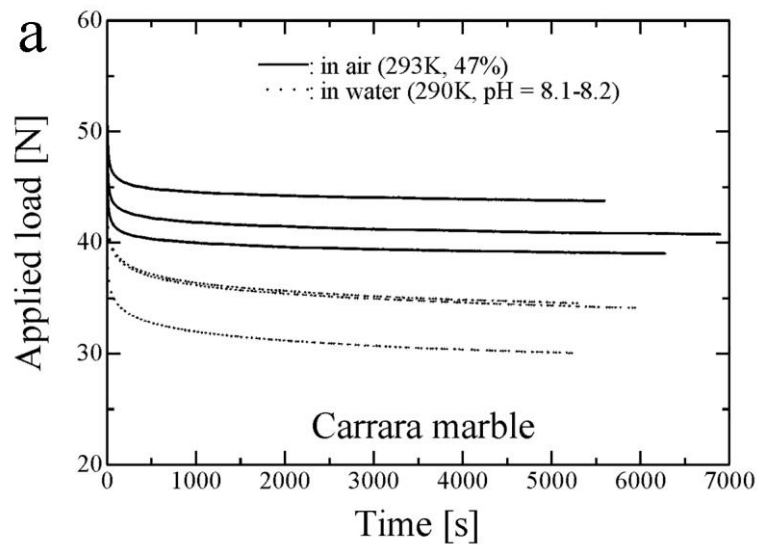


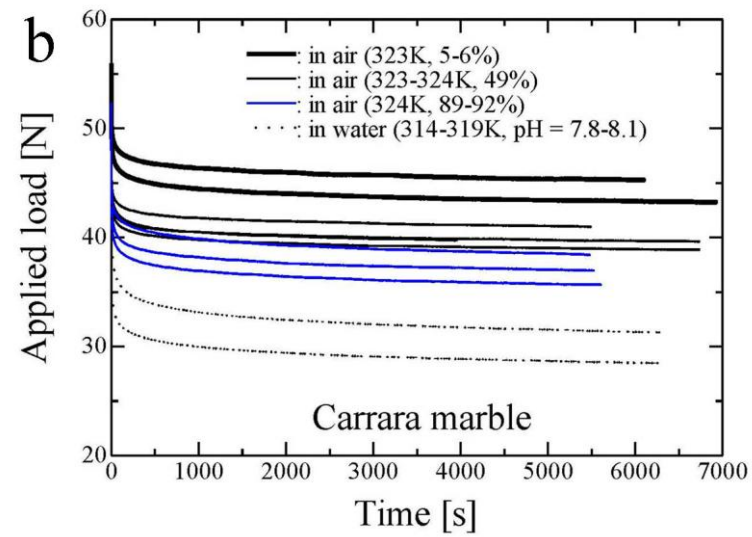
Figure 3. Schematic illustration of double torsion specimen and loading configuration.



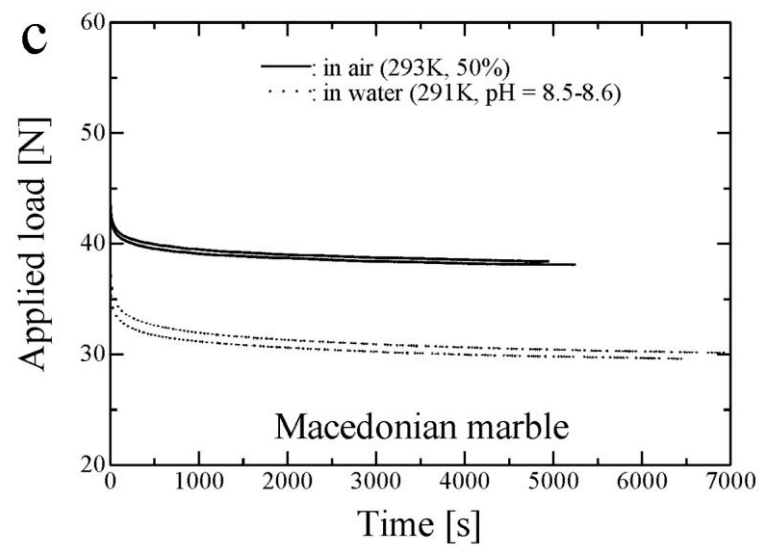
Figure 4. Photo of experimental apparatus of DT-RLX test with pH measurement.



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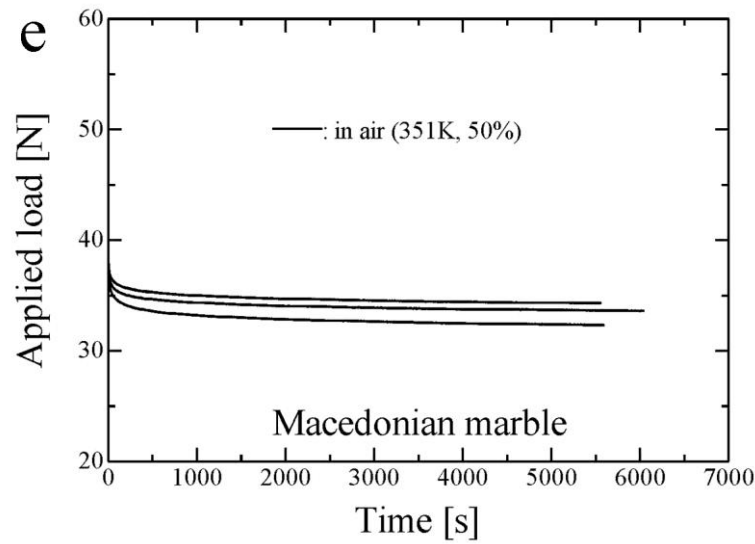
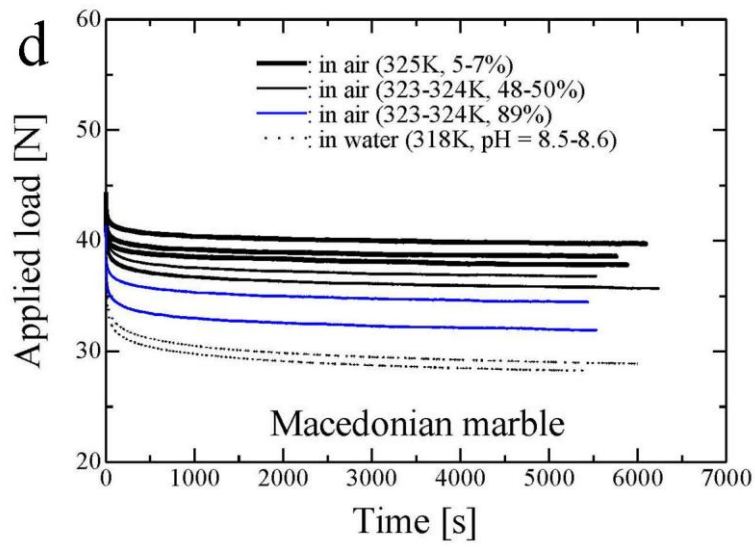


Figure 5. Load-relaxation curves for marbles. (a): CM at 290-293K, and (b): CM at 313-324K, (c): MM at 290-293K, (d): MM at 318-324K, (e): MM at 351K.

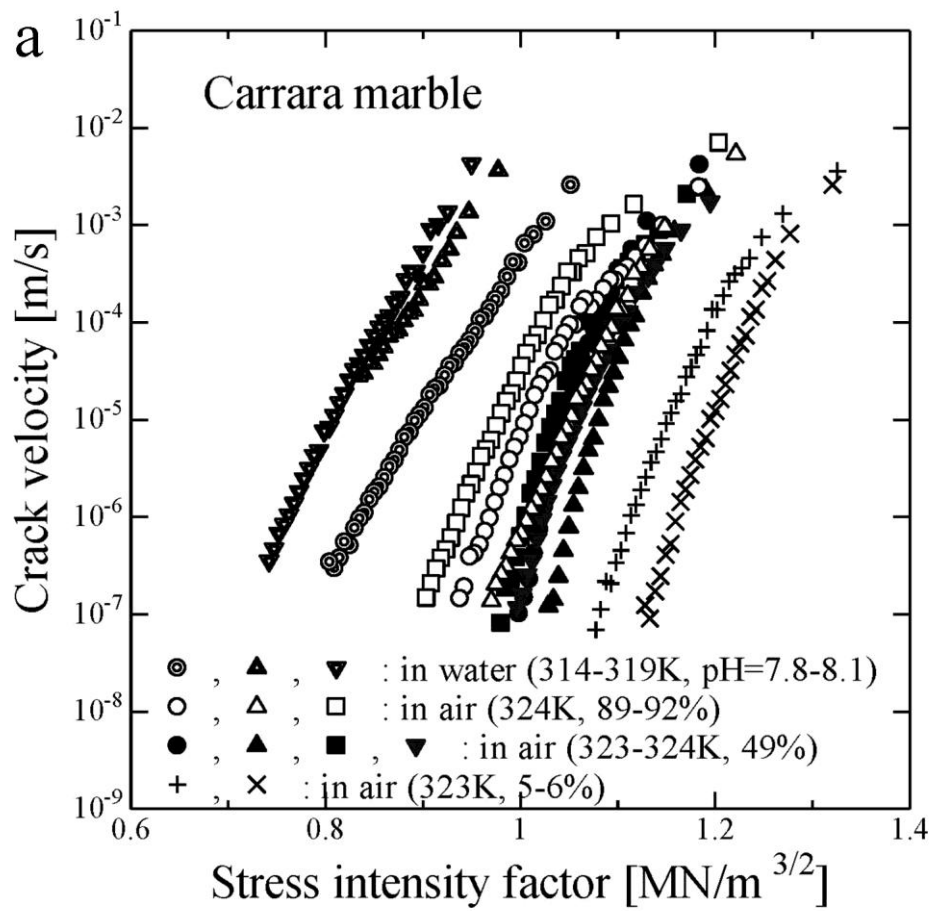


Figure 6. Relationship between crack velocity and stress intensity factor for (a) CM and (b) MM in air with different relative humidities, and in water.

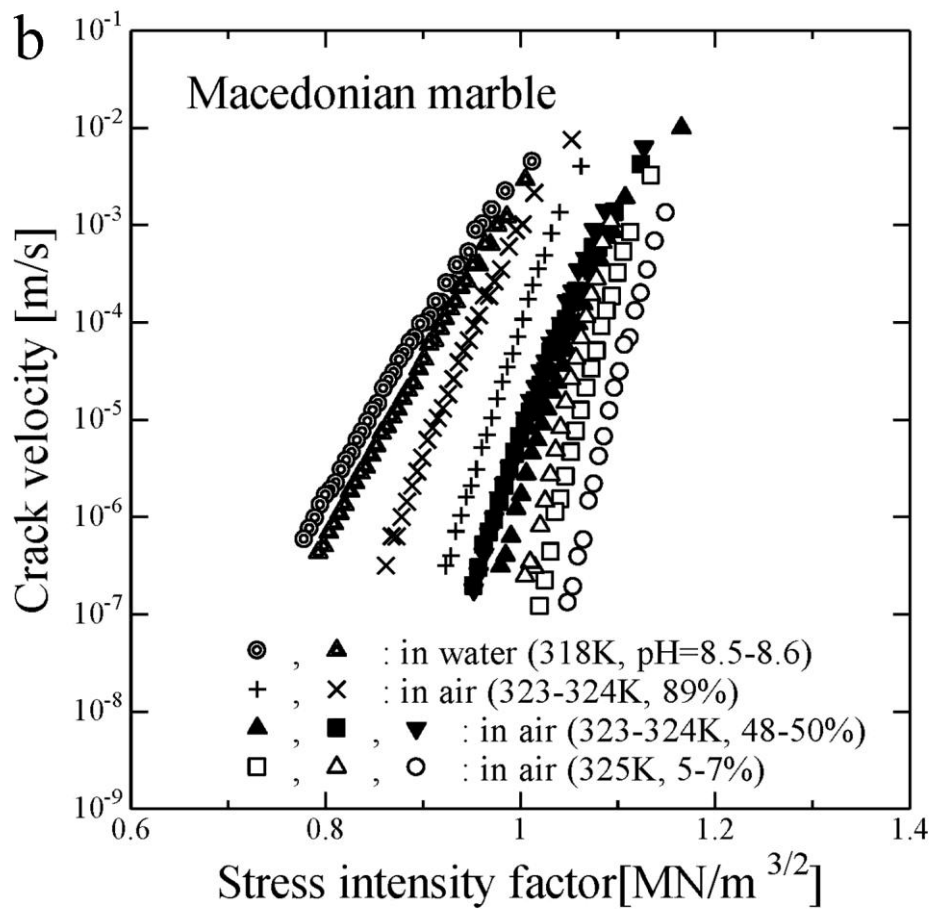


Figure 6. Relationship between crack velocity and stress intensity factor for (a) CM and (b) MM in air with different relative humidities, and in water.

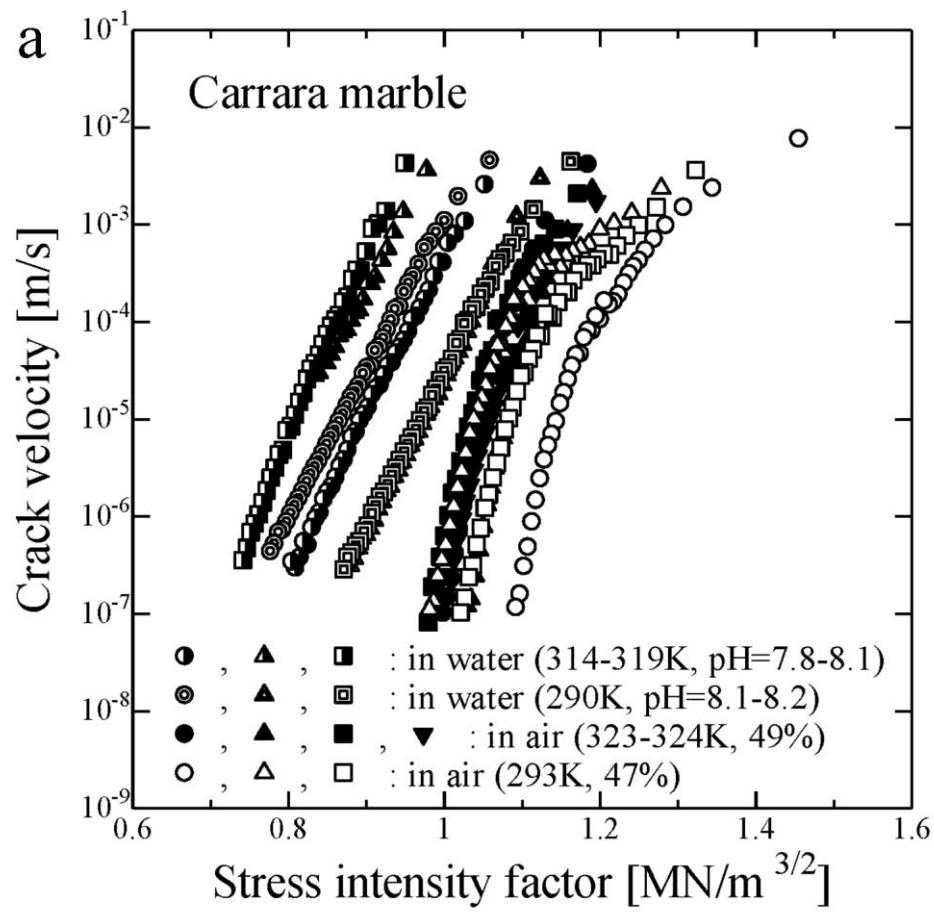


Figure 7. Relationship between crack velocity and stress intensity factor for (a) CM and (b) MM in air and water at different temperatures.

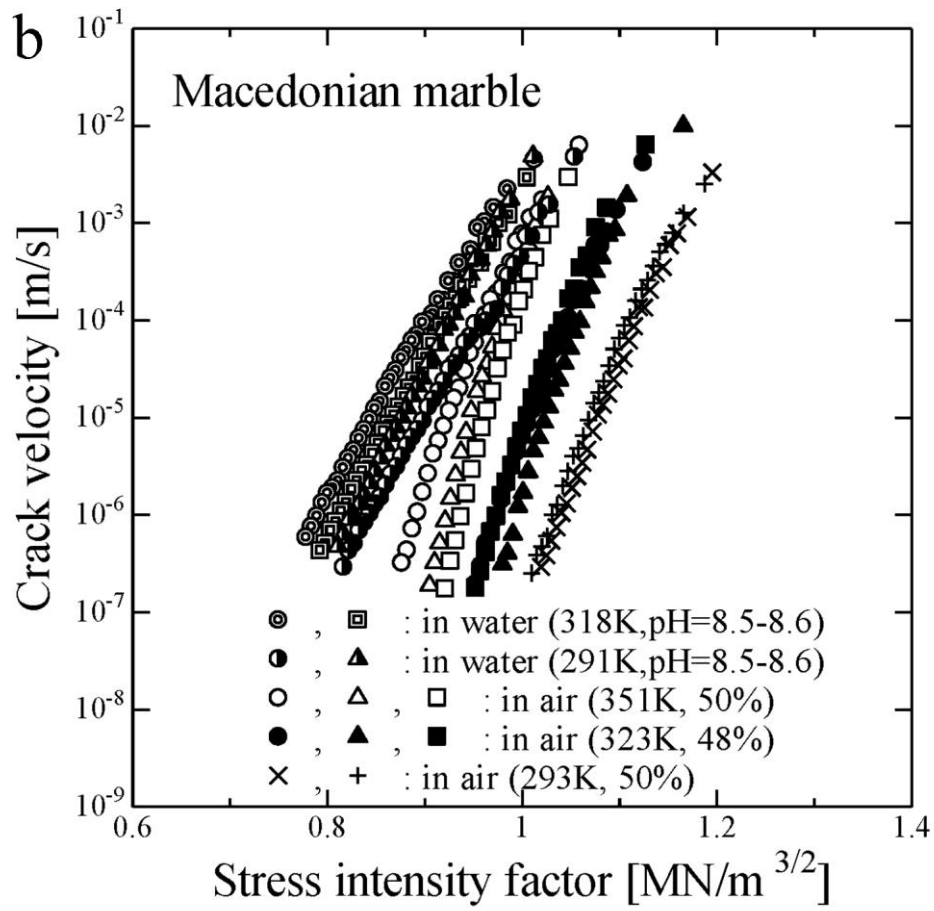


Figure 7. Relationship between crack velocity and stress intensity factor for (a) CM and (b) MM in air and water at different temperatures.

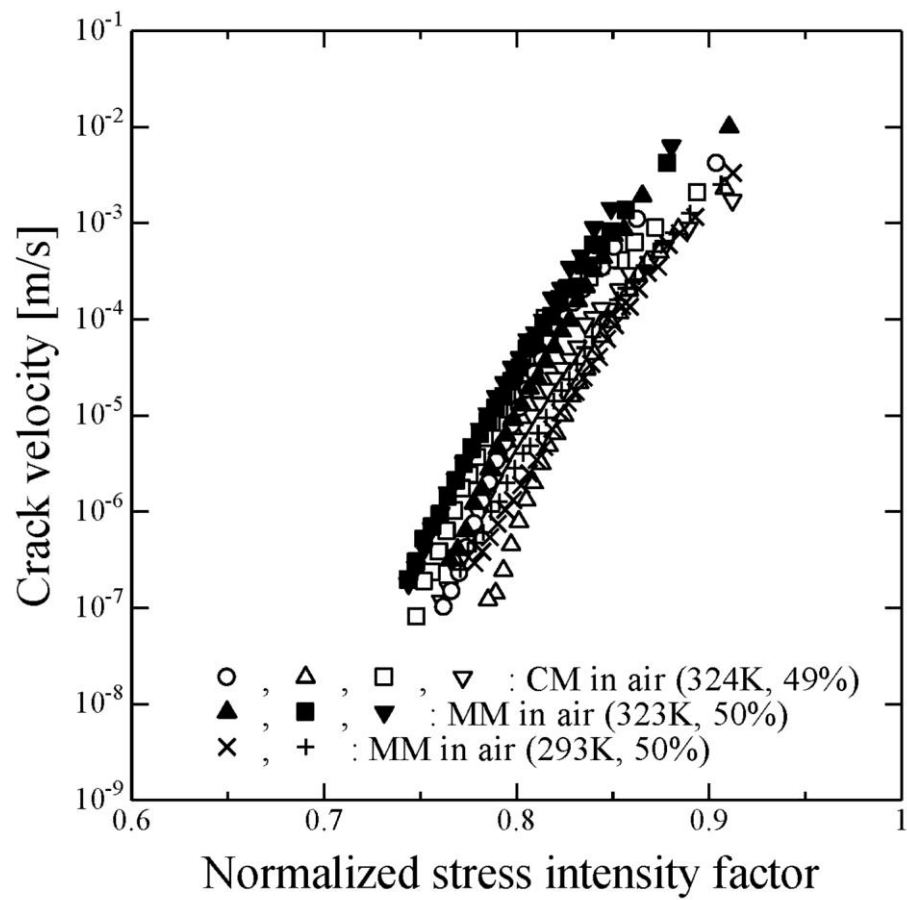


Figure 8. Relationship between crack velocity and stress intensity factor normalized by fracture toughness for marble in air.

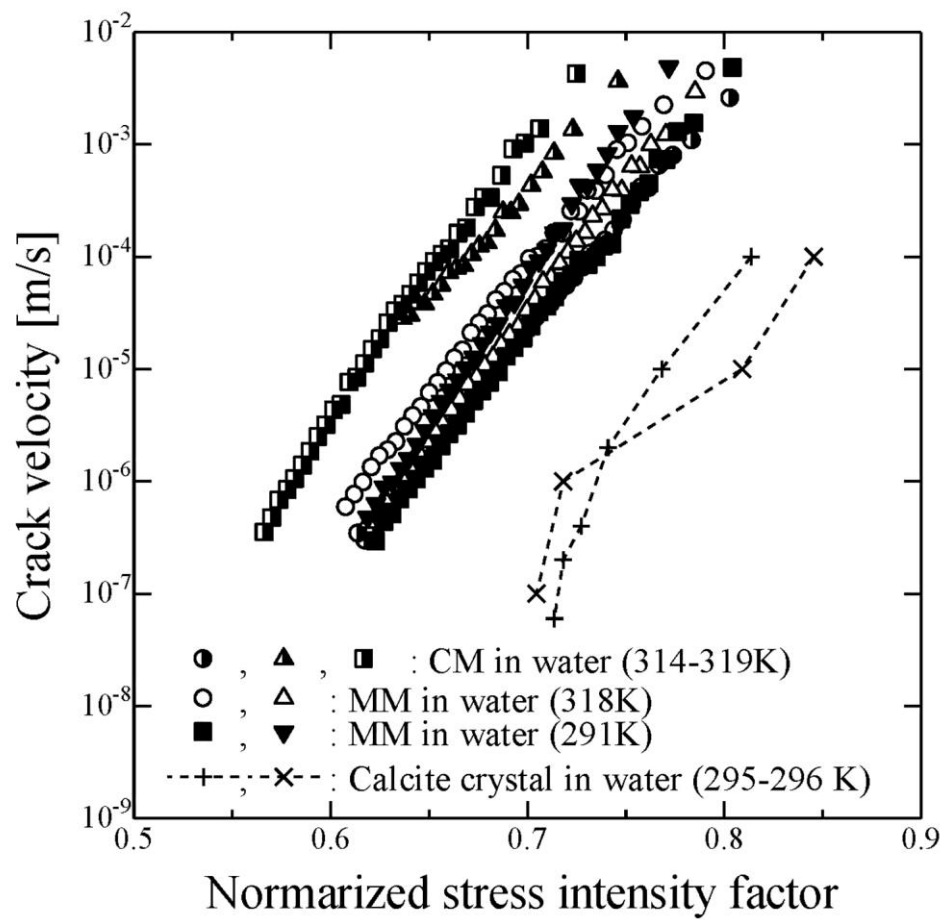


Figure 9. Relationship between crack velocity and stress intensity factor normalized by fracture toughness for marble and calcite crystal. “×” and “+” are the relationships obtained by Røyne et al. (2011) and Rostom et al. (2012), respectively.

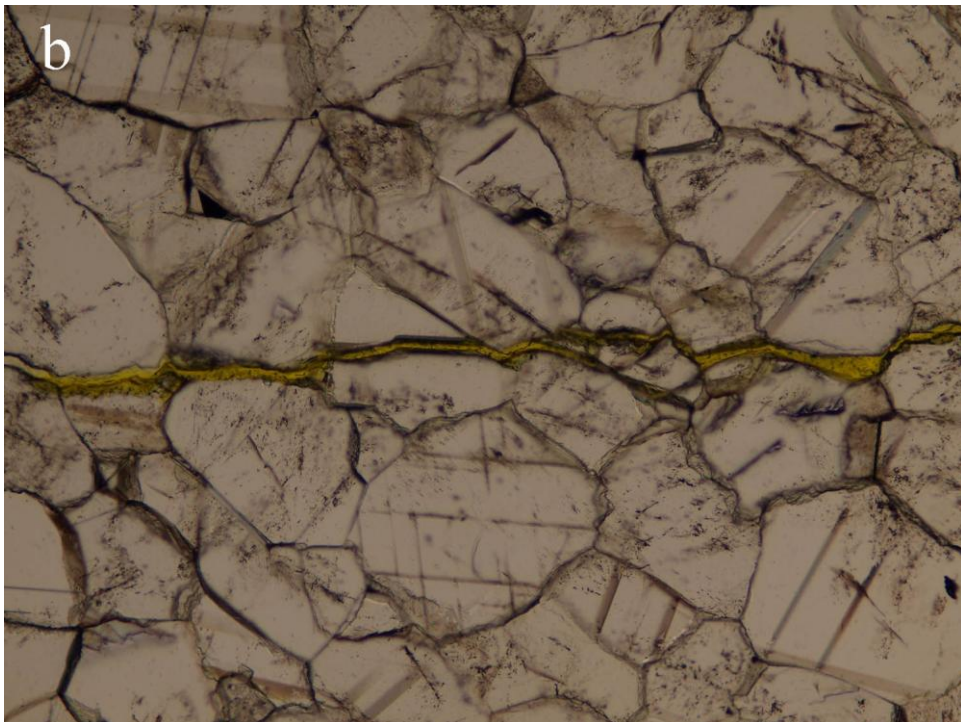
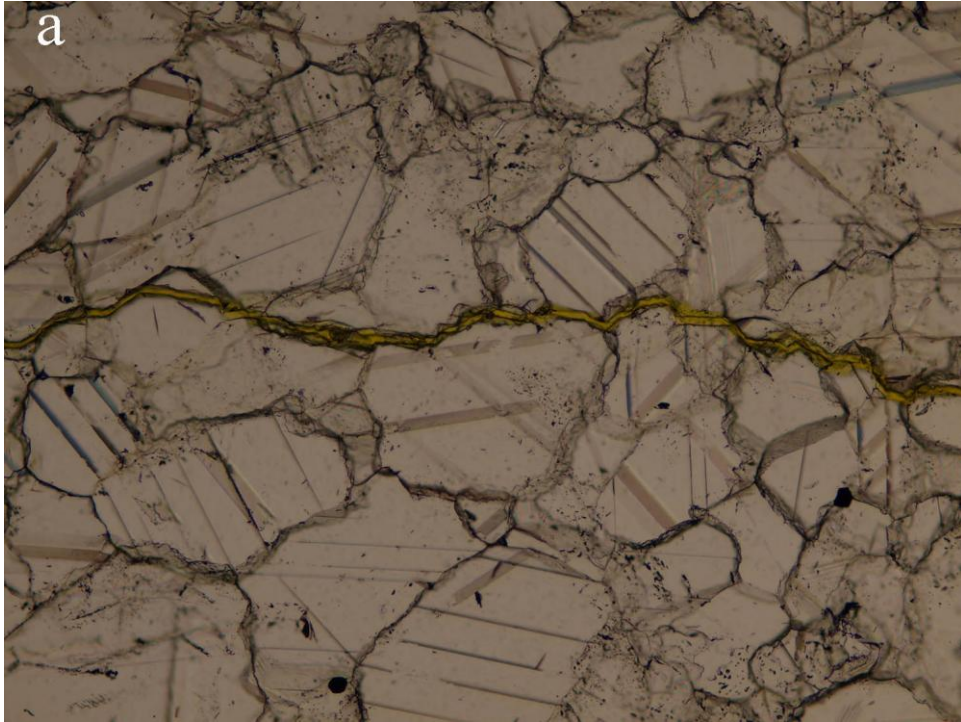


Figure 10. Images of crack path observed for (a) CM and (b) MM. The width and height of the images are 1.5 mm and 1.1 mm, respectively.

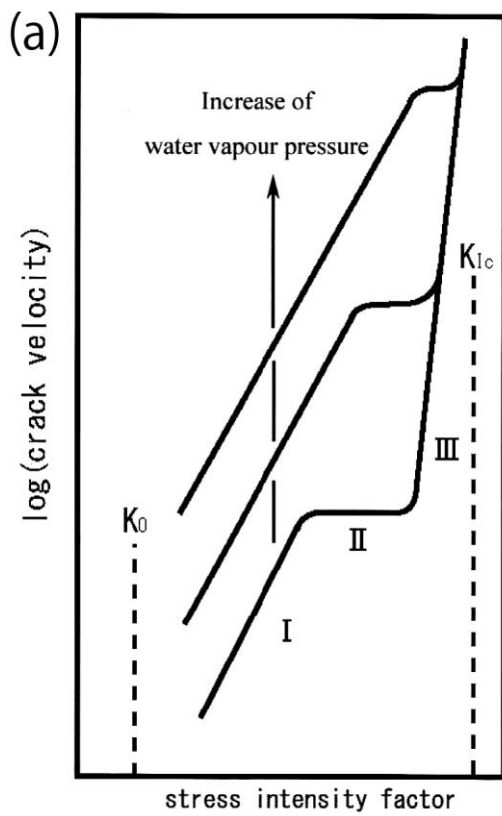


Figure 11. Tri-modal behaviour of relationship between crack velocity and stress intensity factor for subcritical crack growth. (a): Schematic illustration, (b): Relationship in silica glass in air.

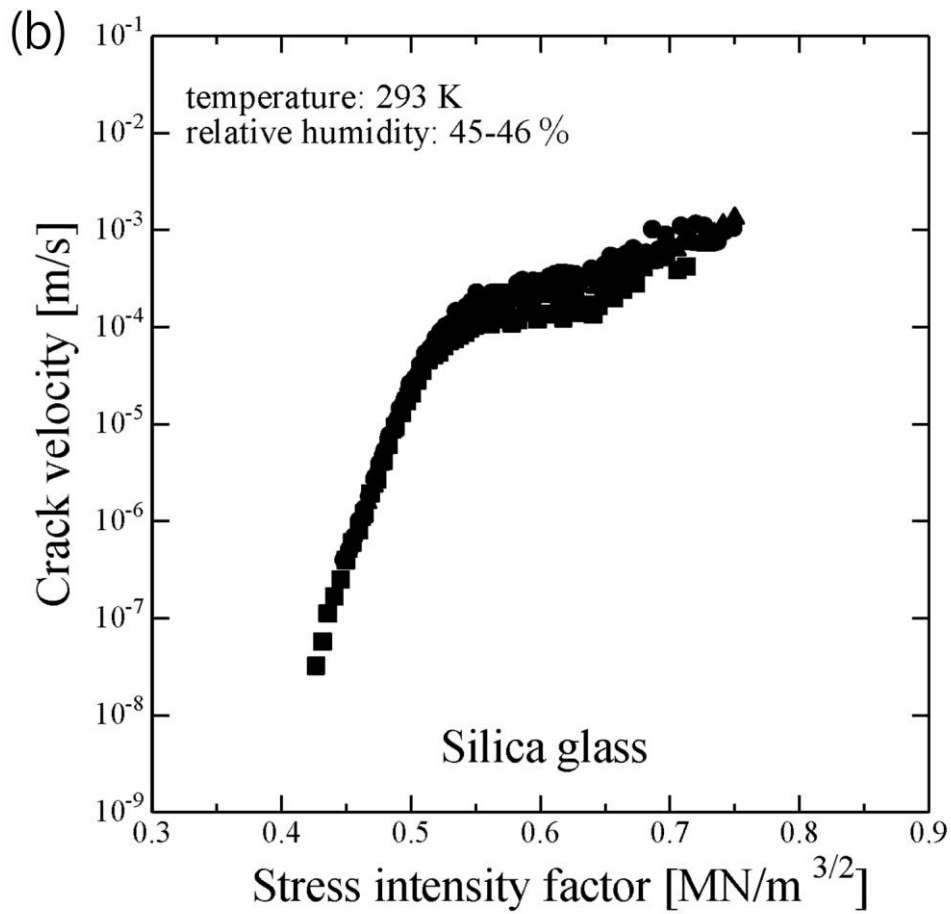


Figure 11. Tri-modal behaviour of relationship between crack velocity and stress intensity factor for subcritical crack growth. (a): Schematic illustration, (b): Relationship in silica glass in air.

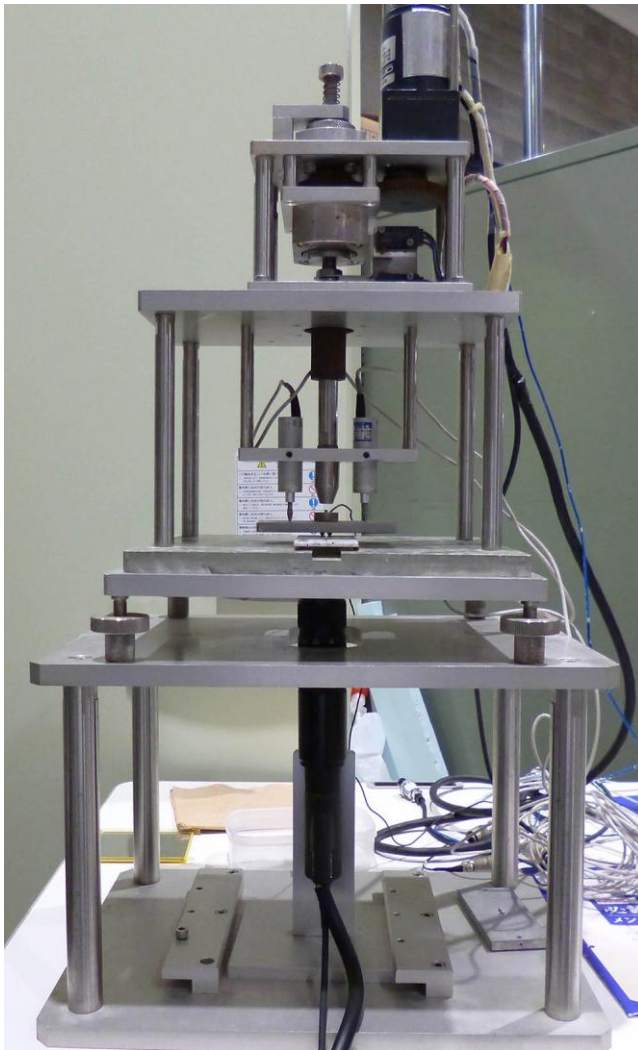


Figure A-1. Photo of apparatus of fracture toughness measurement by DT-CDR test.

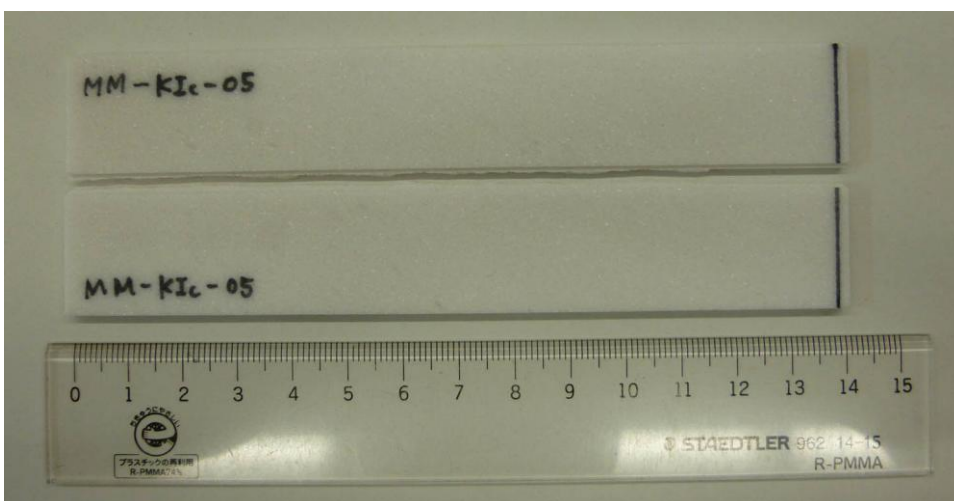


Figure A-2. Photo of DT specimen of Macedonian marble used in fracture toughness measurement

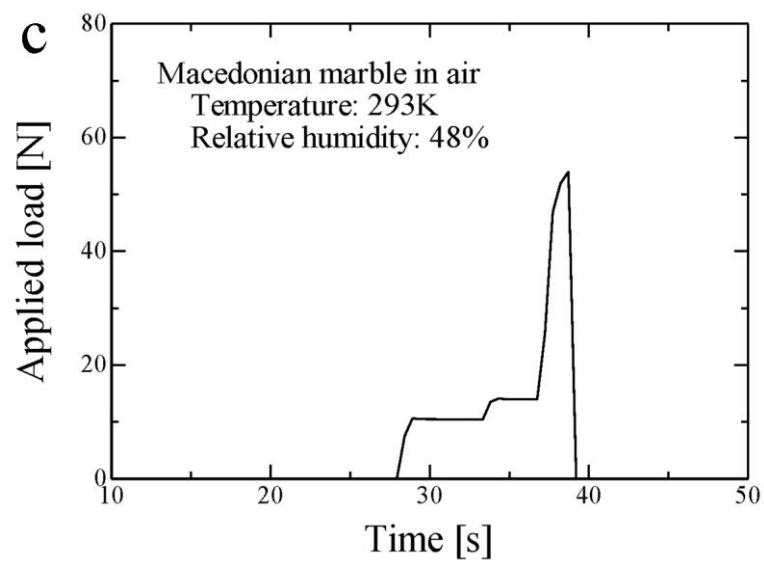
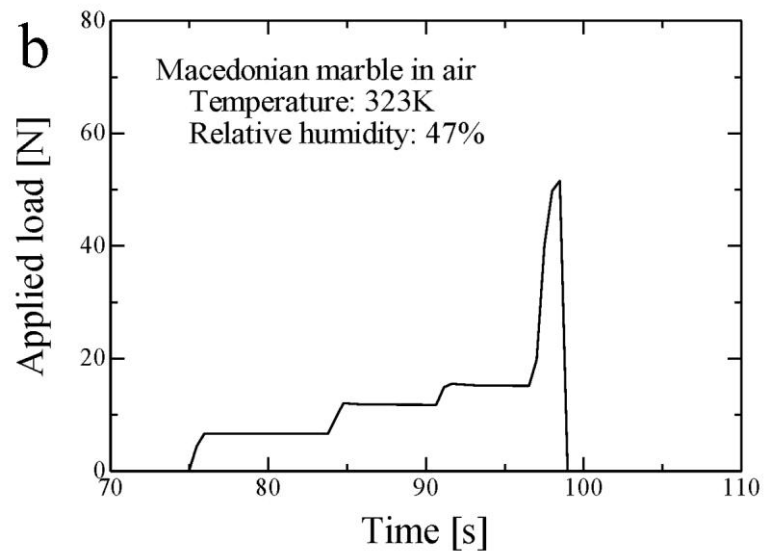
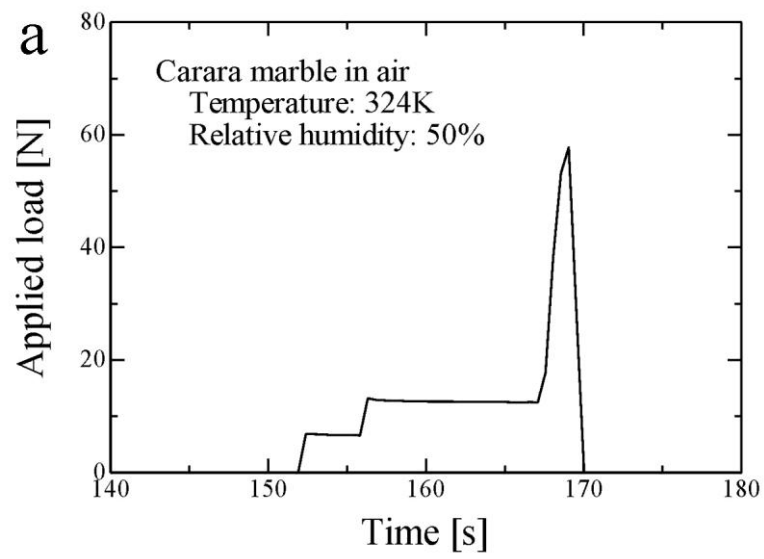


Figure A-3. Temporal change of applied load on DT specimen for fracture toughness

753 measurement. (a): CM in air at 324 K with 50 % relative humidity, (b) MM in air
754 at 323 K with 47% relative humidity, (c): MM in air at 293 K with 48 % relative
755 humidity.
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758 **Tables**

759 Table 1. Summary of subcritical crack growth measurements for Carrara marble in air

760 with different relative humidities, and in water.

Condition		n	$\log A$	$K_I(10^{-5})$ [MN/m ^{3/2}] (power law)	$da/dt(1.0)$ [m/s] (power law)	b [m ^{5/2} /mol]	α	$K_I(10^{-5})$ [MN/m ^{3/2}] (exponential law)	$da/dt(1.0)$ [m/s] (exponential law)
air	323K, 5%	69	-9.26	1.15	5.50×10^{-10}	0.132	-68.3	1.15	9.08×10^{-10}
	323K, 6%	71	-11.15	1.20	6.31×10^{-12}	0.179	-91.3	1.20	1.95×10^{-11}
	average	70 ±1	-10.21 ±1.33	1.18 ±0.04	ave: 6.17×10^{-11} std: 2.14×10^1 (in log)	0.156 ±0.033	-79.8 ±16.3	1.18 ±0.04	ave: 1.33×10^{-10} std: 1.51×10^1 (in log)
	324K, 49%	92	-6.91	1.05	1.23×10^{-7}	0.239	-104.6	1.05	1.41×10^{-7}
	324K, 49%	88	-7.97	1.08	1.07×10^{-8}	0.221	-100.1	1.08	1.48×10^{-8}
	324K, 49%	80	-6.23	1.04	5.89×10^{-7}	0.211	-92.7	1.04	6.25×10^{-7}
	323K, 49%	69	-6.73	1.06	1.86×10^{-7}	0.177	-81.4	1.06	1.93×10^{-7}
	average	82 ±10	-6.96 ±0.73	1.06 ±0.02	ave: 1.10×10^{-7} std: 5.37×10^0 (in log)	0.212 ±0.026	-94.7 ±10.1	1.06 ±0.02	ave: 1.26×10^{-7} std: 4.79×10^0 (in log)
	324K, 89%	56	-5.19	1.01	6.46×10^{-6}	0.152	-68.6	1.01	6.21×10^{-6}
	324K, 92%	54	-6.15	1.05	7.08×10^{-7}	0.142	-66.9	1.05	6.95×10^{-7}
	324K, 91%	53	-4.50	0.98	3.16×10^{-5}	0.147	-65.1	0.98	3.20×10^{-5}
	average	54 ±2	-5.28 ±0.83	1.01 ±0.04	ave: 5.25×10^{-6} std: 6.76×10^0 (in log)	0.147 ±0.005	-66.9 ±1.8	1.01 ±0.04	ave: 5.13×10^{-6} std: 6.92×10^0 (in log)
water	319K, pH8.0	34	-3.37	0.89	4.27×10^{-4}	0.102	-46.0	0.90	5.64×10^{-4}
	314K, pH7.8	25	-2.63	0.80	2.34×10^{-3}	0.075	-34.5	0.80	3.20×10^{-3}
	314K, pH8.1	39	-1.34	0.81	4.57×10^{-2}	0.128	-51.1	0.81	1.19×10^{-1}
	average	33 ±7	-2.45 ±1.03	0.83 ±0.05	ave: 3.57×10^{-3} std: 1.05×10^1 (in log)	0.102 ±0.027	-43.9 ±8.5	0.84 ±0.06	ave: 5.99×10^{-3} std: 1.55×10^1 (in log)

761 ave: average, std: standard deviation

762

763

764 Table 2. Summary of subcritical crack growth measurements for Macedonian marble
765 in air with different relative humidities, and in water.

766

Condition		n	$\log A$	$K_I(10^{-5})$ [MN/m ^{3/2}] (power law)	$da/dt(1.0)$ [m/s] (power law)	b [m ^{5/2} /mol]	α	$K_I(10^{-5})$ [MN/m ^{3/2}] (exponential law)	$da/dt(1.0)$ [m/s] (exponential law)
air	325K, 7%	97	-7.54	1.06	2.88×10^{-8}	0.245	-107.9	1.06	3.44×10^{-8}
	325K, 5%	106	-6.96	1.04	1.10×10^{-7}	0.274	-117.3	1.04	1.31×10^{-7}
	325K, 5%	104	-8.96	1.09	1.10×10^{-9}	0.256	-115.0	1.09	1.67×10^{-9}
	average	103 ±5	-7.82 ±1.03	1.06 ±0.03	ave: 1.51×10^{-8} std: 1.07×10^{-1} (in log)	0.258 ±0.015	-113.4 ±4.9	1.06 ±0.03	ave: 1.96×10^{-8} std: 9.33×10^0 (in log)
	324K, 48%	61	-5.25	1.08	5.62×10^{-6}	0.150	-71.8	1.08	1.03×10^{-7}
	324K, 49%	66	-5.72	1.03	1.91×10^{-6}	0.166	-74.9	1.03	1.77×10^{-6}
	323K, 50%	65	-5.19	1.01	6.46×10^{-6}	0.170	-75.5	1.01	5.21×10^{-6}
	average	64 ±2	-5.39 ±0.29	1.03 ±0.04	ave: 4.11×10^{-6} std: 1.95×10^0 (in log)	0.162 ±0.011	-74.1 ±2.0	1.03 ±0.04	ave: 9.83×10^{-7} std: 7.56×10^0 (in log)
	324K, 89%	70	-4.07	0.97	8.51×10^{-5}	0.191	-80.6	0.97	6.37×10^{-5}
	323K, 89%	52	-3.00	0.92	1.00×10^{-3}	0.148	-62.0	0.92	1.05×10^{-3}
water	318K, pH8.5	35	-2.43	0.84	3.72×10^{-3}	0.106	-44.8	0.84	8.92×10^{-3}
	318K, pH8.6	37	-2.66	0.87	2.19×10^{-3}	0.111	-47.8	0.87	2.94×10^{-3}
	average	36 ±1	-2.55 ±0.16	0.86 ±0.02	ave: 2.85×10^{-3} std: 1.45×10^0 (in log)	0.109 ±0.035	-46.3 ±2.1	0.86 ±0.02	ave: 5.12×10^{-3} std: 2.19×10^0 (in log)

767 ave: average, std: standard deviation

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771

772 Table 3. Summary of subcritical crack growth measurements for Carrara marble in air
773 and water at different temperatures.

774

Condition		n	$\log A$	$K_I(10^{-5})$ [MN/m ^{3/2}] (power law)	$da/dt(1.0)$ [m/s] (power law)	b [m ^{5/2} /mol]	α	$K_I(10^{-5})$ [MN/m ^{3/2}] (exponential law)	$da/dt(1.0)$ [m/s] (exponential law)
air	293K, 47%	81	-9.85	1.15	1.41×10^{-10}	0.174	-93.5	1.15	2.70×10^{-10}
	293K, 47%	75	-6.31	1.04	4.90×10^{-7}	0.179	-88.1	1.04	4.47×10^{-7}
	293K, 47%	73	-7.59	1.09	2.57×10^{-8}	0.165	-85.2	1.09	2.65×10^{-8}
	average	77 ±4	-7.92 ±1.79	1.09 ±0.06	ave: 1.21×10^{-8} std: 6.17×10^1 (in log)	0.173 ±0.007	-88.9 ±4.2	1.09 ±0.06	ave: 1.47×10^{-8} std: 4.17×10^1 (in log)
	324K, 49%	92	-6.91	1.05	1.23×10^{-7}	0.239	-104.6	1.05	1.41×10^{-7}
	324K, 49%	88	-7.97	1.08	1.07×10^{-8}	0.221	-100.1	1.08	1.48×10^{-8}
	324K, 49%	80	-6.23	1.04	5.89×10^{-7}	0.211	-92.7	1.04	6.25×10^{-7}
	323K, 49%	69	-6.73	1.06	1.86×10^{-7}	0.177	-81.4	1.06	1.93×10^{-7}
	average	82 ±10	-6.96 ±0.73	1.06 ±0.02	ave: 1.10×10^{-7} std: 5.37×10^0 (in log)	0.212 ±0.026	-94.7 ±10.1	1.06 ±0.02	ave: 1.26×10^{-7} std: 4.79×10^0 (in log)
water	290K, pH8.2	30	-3.14	0.87	7.24×10^{-4}	0.093	-46.0	0.90	6.25×10^{-4}
	290K, pH8.1	35	-4.58	0.97	2.63×10^{-5}	0.088	-47.0	0.97	2.91×10^{-5}
	290K, pH8.2	35	-4.52	0.97	3.02×10^{-5}	0.088	-46.9	0.97	3.11×10^{-5}
	average	33 ±3	-4.08 ±0.81	0.94 ±0.06	ave: 8.32×10^{-5} std: 6.46×10^0 (in log)	0.090 ±0.003	-46.6 ±0.6	0.95 ±0.04	ave: 8.27×10^{-5} std: 5.75×10^0 (in log)
	319K, pH8.0	34	-3.37	0.89	4.27×10^{-4}	0.102	-46.0	0.90	5.64×10^{-4}
	314K, pH7.8	25	-2.63	0.80	2.34×10^{-3}	0.075	-34.5	0.80	3.20×10^{-3}
	314K, pH8.1	39	-1.34	0.81	4.57×10^{-2}	0.128	-51.1	0.81	1.19×10^{-1}
	average	33 ±7	-2.45 ±1.03	0.83 ±0.05	ave: 3.57×10^{-3} std: 1.05×10^1 (in log)	0.102 ±0.027	-43.9 ±8.5	0.84 ±0.06	ave: 5.99×10^{-3} std: 1.55×10^1 (in log)

775 ave: average, std: standard deviation

776

777

778 Table 4. Summary of subcritical crack growth measurements for Macedonian marble
779 in air and water at different temperatures.

780

Condition		n	$\log A$	$K_I(10^{-5})$ [MN/m ^{3/2}] (power law)	$da/dt(1.0)$ [m/s] (power law)	b [m ^{5/2} /mol]	α	$K_I(10^{-5})$ [MN/m ^{3/2}] (exponential law)	$da/dt(1.0)$ [m/s] (exponential law)
air	293K, 50%	61	-7.02	1.08	9.55×10^{-8}	0.136	-71.8	1.08	1.19×10^{-7}
	293K, 50%	60	-6.75	1.07	1.78×10^{-7}	0.133	-70.0	1.07	2.10×10^{-7}
	average	61 ±1	-6.89 ±0.19	1.08 ±0.01	ave: 1.30×10^{-7} std: 1.55×10^0 (in log)	0.135 ±0.002	-70.9 ±1.3	1.08 ±0.01	ave: 1.58×10^{-7} std: 1.48×10^0 (in log)
	324K, 48%	61	-5.25	1.08	5.62×10^{-6}	0.150	-71.8	1.08	1.03×10^{-7}
	324K, 49%	66	-5.72	1.03	1.91×10^{-6}	0.166	-74.9	1.03	1.77×10^{-6}
	323K, 50%	65	-5.19	1.01	6.46×10^{-6}	0.170	-75.5	1.01	5.21×10^{-6}
	average	64 ±2	-5.39 ±0.29	1.03 ±0.04	ave: 4.11×10^{-6} std: 1.95×10^0 (in log)	0.162 ±0.011	-74.1 ±2.0	1.03 ±0.04	ave: 9.83×10^{-7} std: 7.56×10^0 (in log)
	351K, 50%	55	-3.14	0.93	7.24×10^{-4}	0.167	-64.7	0.93	5.84×10^{-4}
	351K, 50%	74	-3.34	0.95	4.57×10^{-4}	0.224	-84.4	0.95	4.99×10^{-4}
	351K, 50%	77	-3.79	0.96	1.62×10^{-4}	0.228	-87.0	0.96	1.46×10^{-4}
water	average	69 ±12	-3.42 ±0.33	0.95 ±0.02	ave: 4.55×10^{-4} std: 2.14×10^0 (in log)	0.206 ±0.034	-78.7 ±12.2	0.95 ±0.02	ave: 3.49×10^{-5} std: 2.14×10^0 (in log)
	291K, pH8.6	37	-3.29	0.90	5.13×10^{-4}	0.096	-47.3	0.90	5.39×10^{-4}
	291K, pH8.5	42	-2.56	0.87	2.75×10^{-3}	0.112	-52.3	0.88	2.54×10^{-3}
	average	40 ±4	-2.93 ±0.52	0.89 ±0.02	ave: 1.19×10^{-3} std: 3.31×10^0 (in log)	0.104 ±0.011	-49.8 ±3.5	0.89 ±0.01	ave: 1.17×10^{-3} std: 3.02×10^0 (in log)
	318K, pH8.5	35	-2.43	0.84	3.72×10^{-3}	0.106	-44.8	0.84	8.92×10^{-3}
	318K, pH8.6	37	-2.66	0.87	2.19×10^{-3}	0.111	-47.8	0.87	2.94×10^{-3}
	average	36 ±1	-2.55 ±0.16	0.86 ±0.02	ave: 2.85×10^{-3} std: 1.45×10^0 (in log)	0.109 ±0.035	-46.3 ±2.1	0.86 ±0.02	ave: 5.12×10^{-3} std: 2.19×10^0 (in log)

781 ave: average, std: standard deviation

782

783 Table 5. Summary of fracture toughness measurement for marble in air.

Rock	Condition	Fracture toughness [MN/m ^{3/2}]
CM	323K, 50%	1.36
	323K, 50%	1.32
	323K, 50%	1.26
	average	1.31±0.05
MM	293K, 47%	1.32
	293K, 48%	1.30
	average	1.31±0.01
	323K, 45%	1.33
	323K, 48%	1.27
	323K, 47%	1.25
	average	1.28±0.04

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788 The English in this document has been checked by at least two professional editors, both

789 native speakers of English, from an English editing service company:

790 <https://www.zenis.co.jp/eng/index.html>

791

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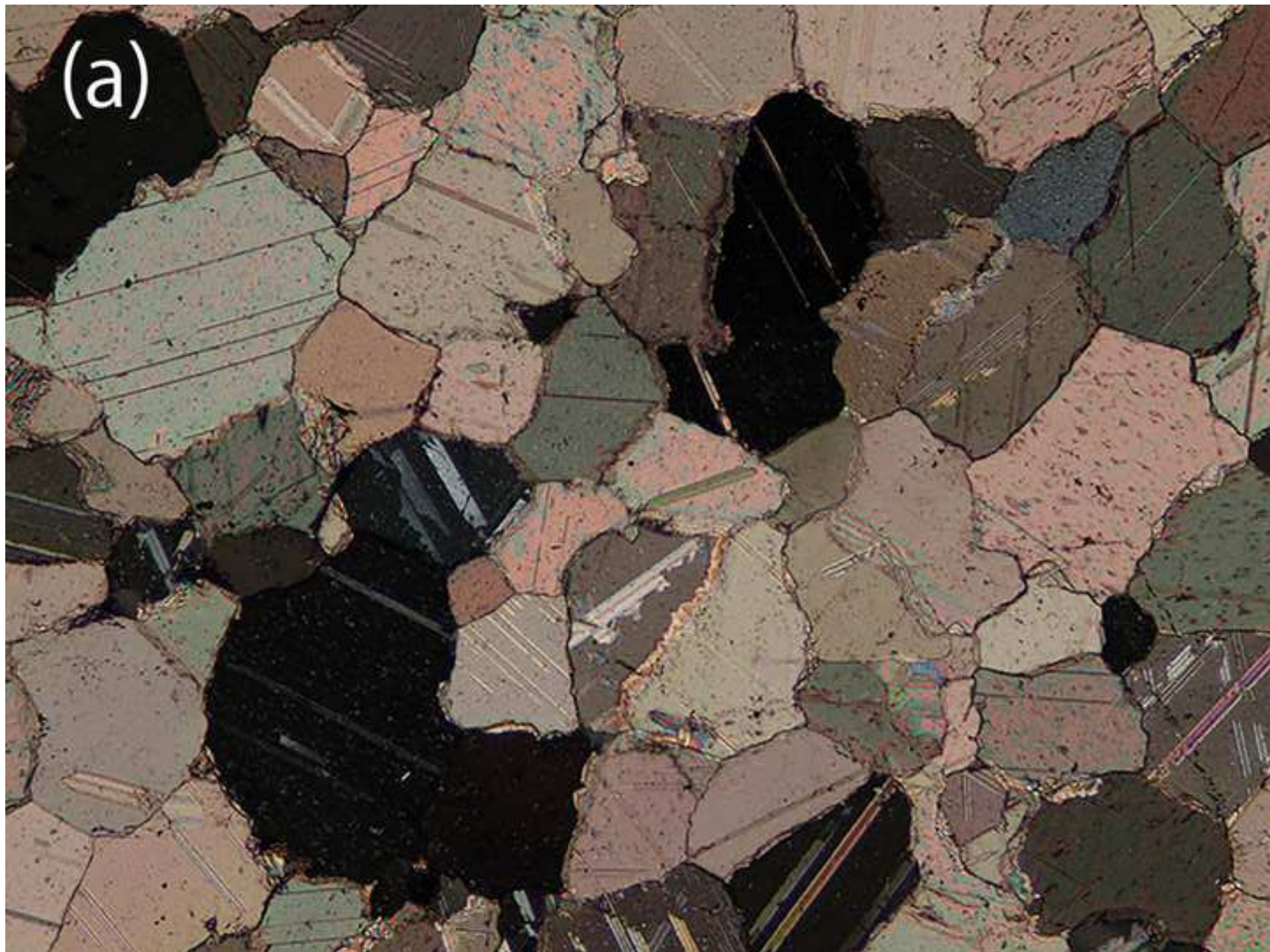


Figure1b
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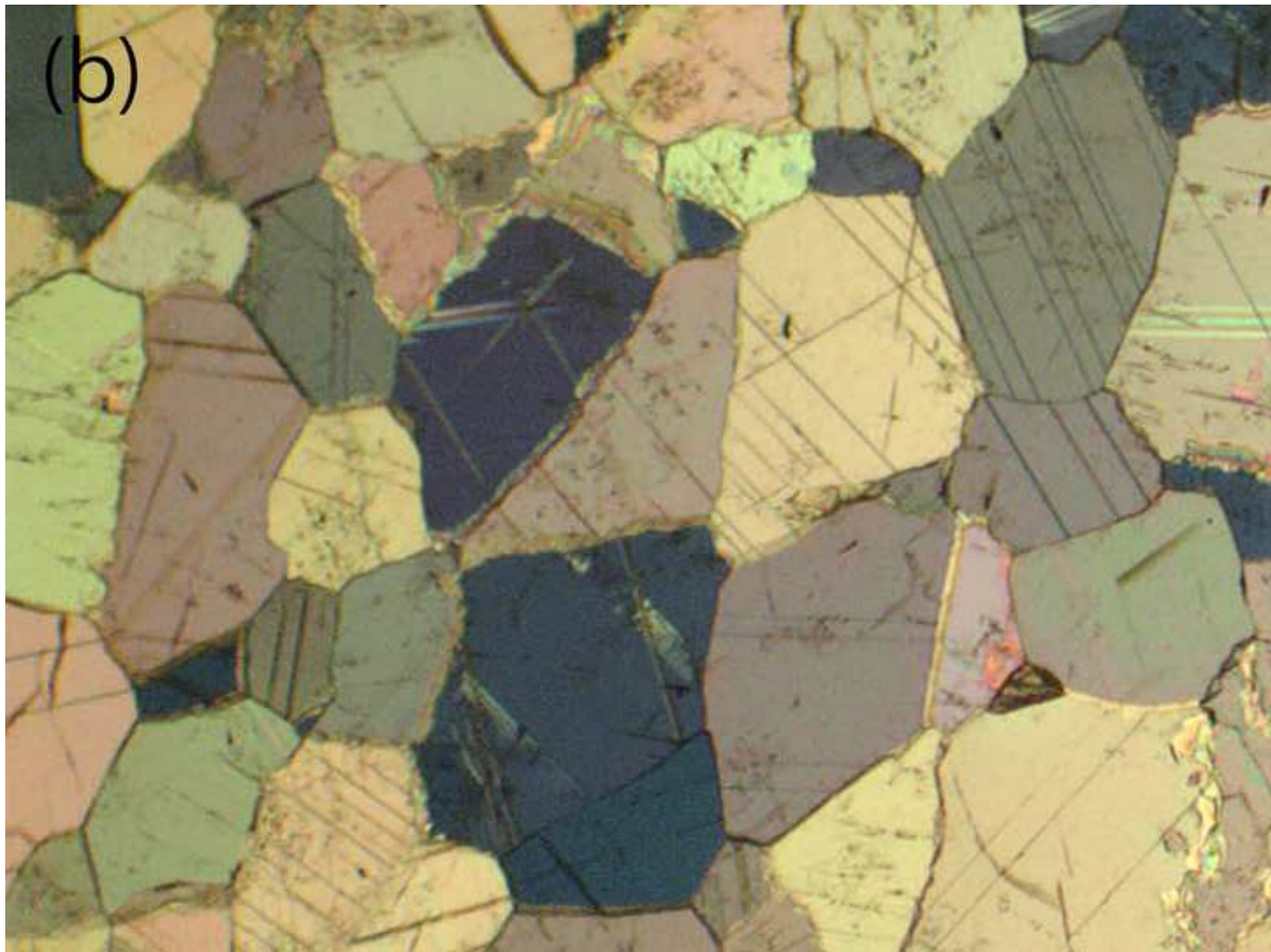


Figure2a

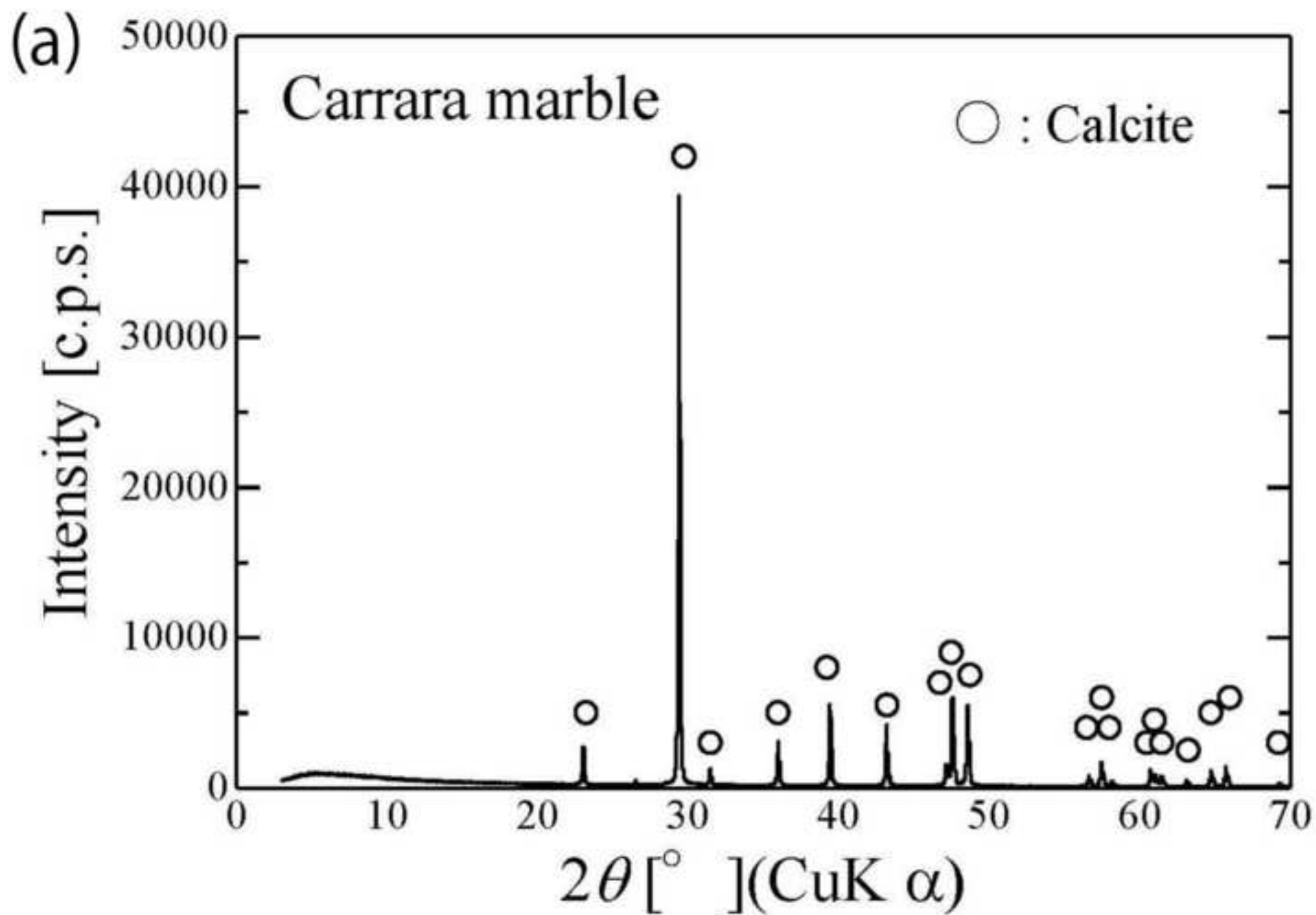
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Figure2b

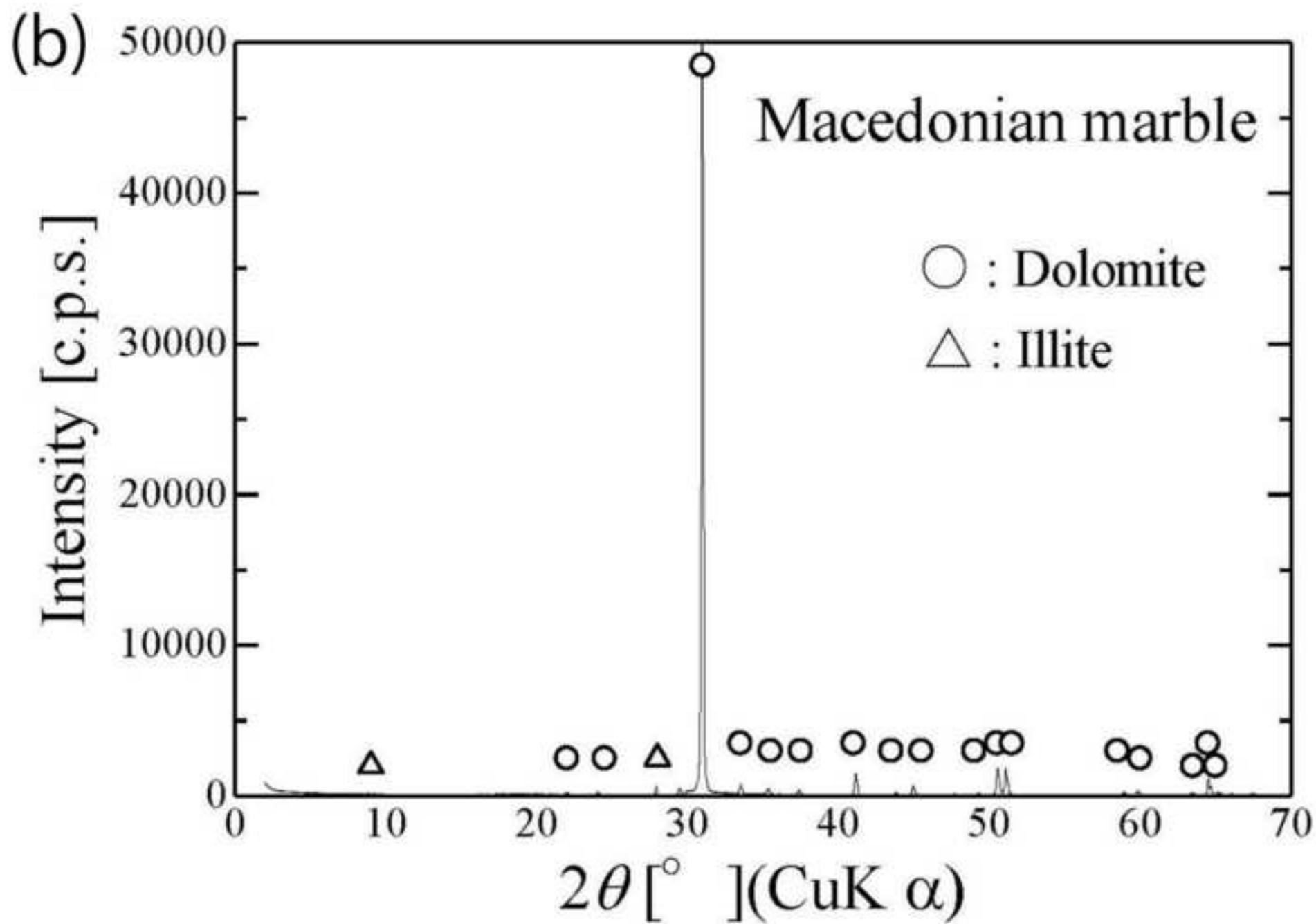
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Figure3

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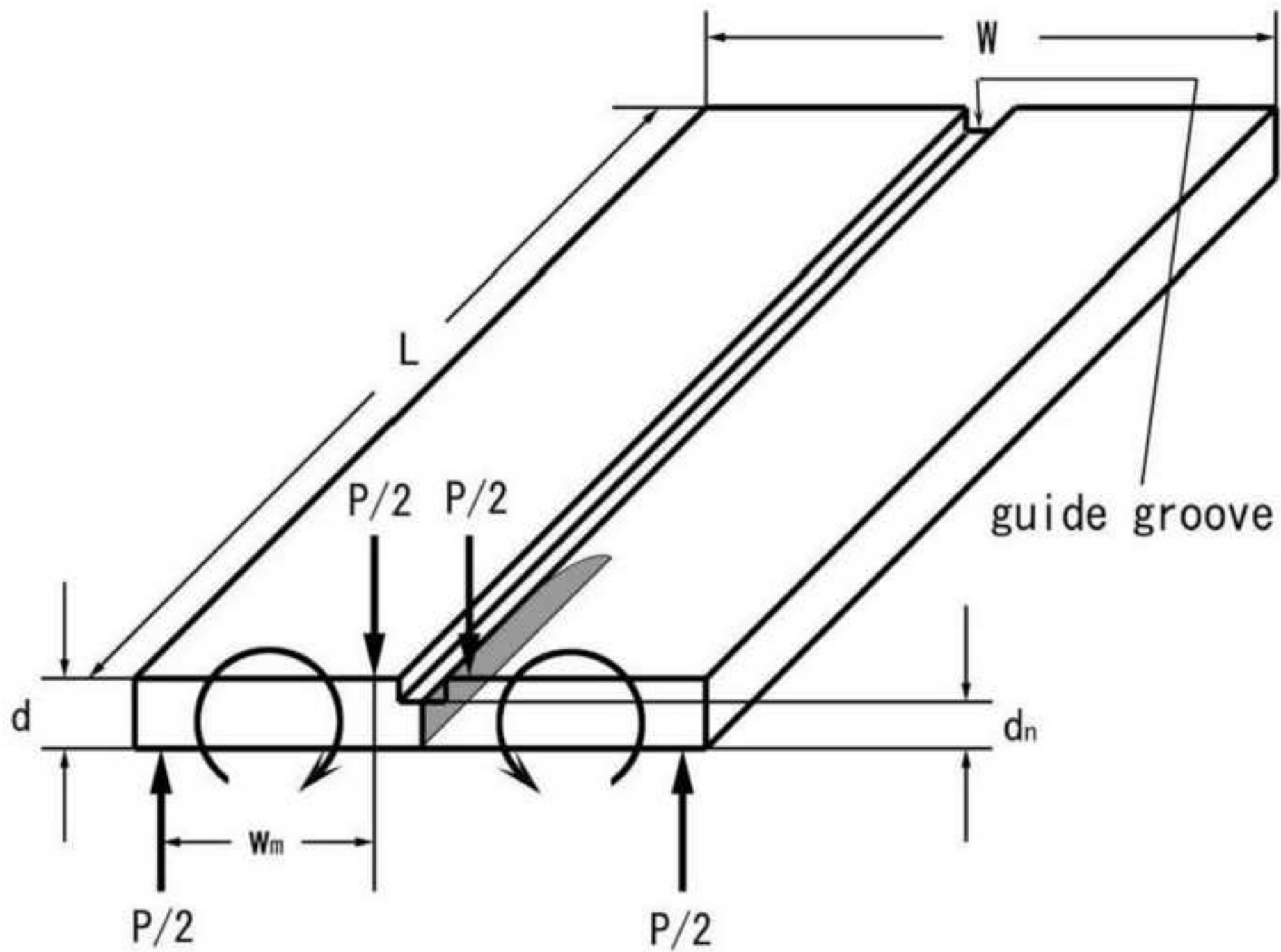


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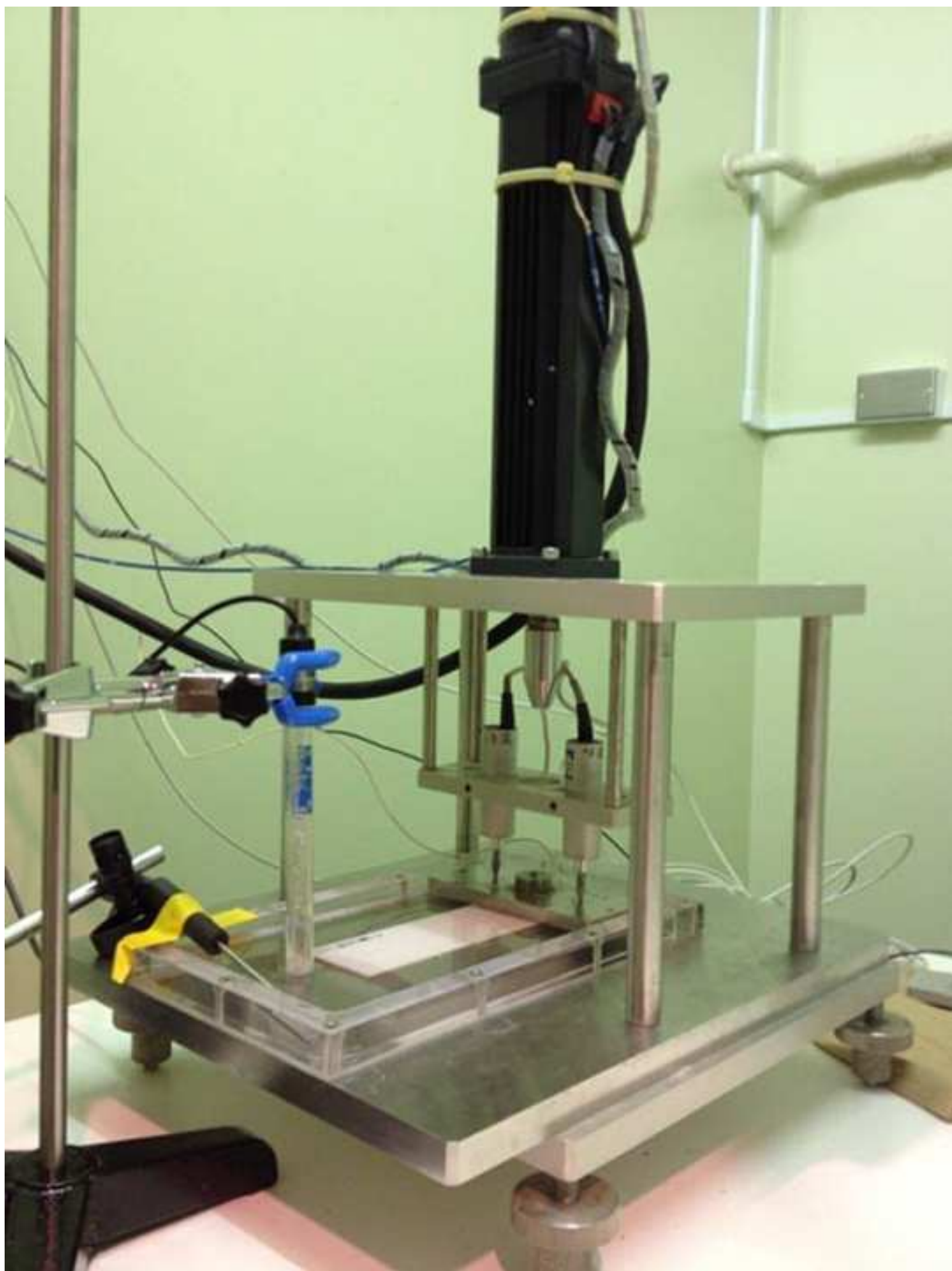


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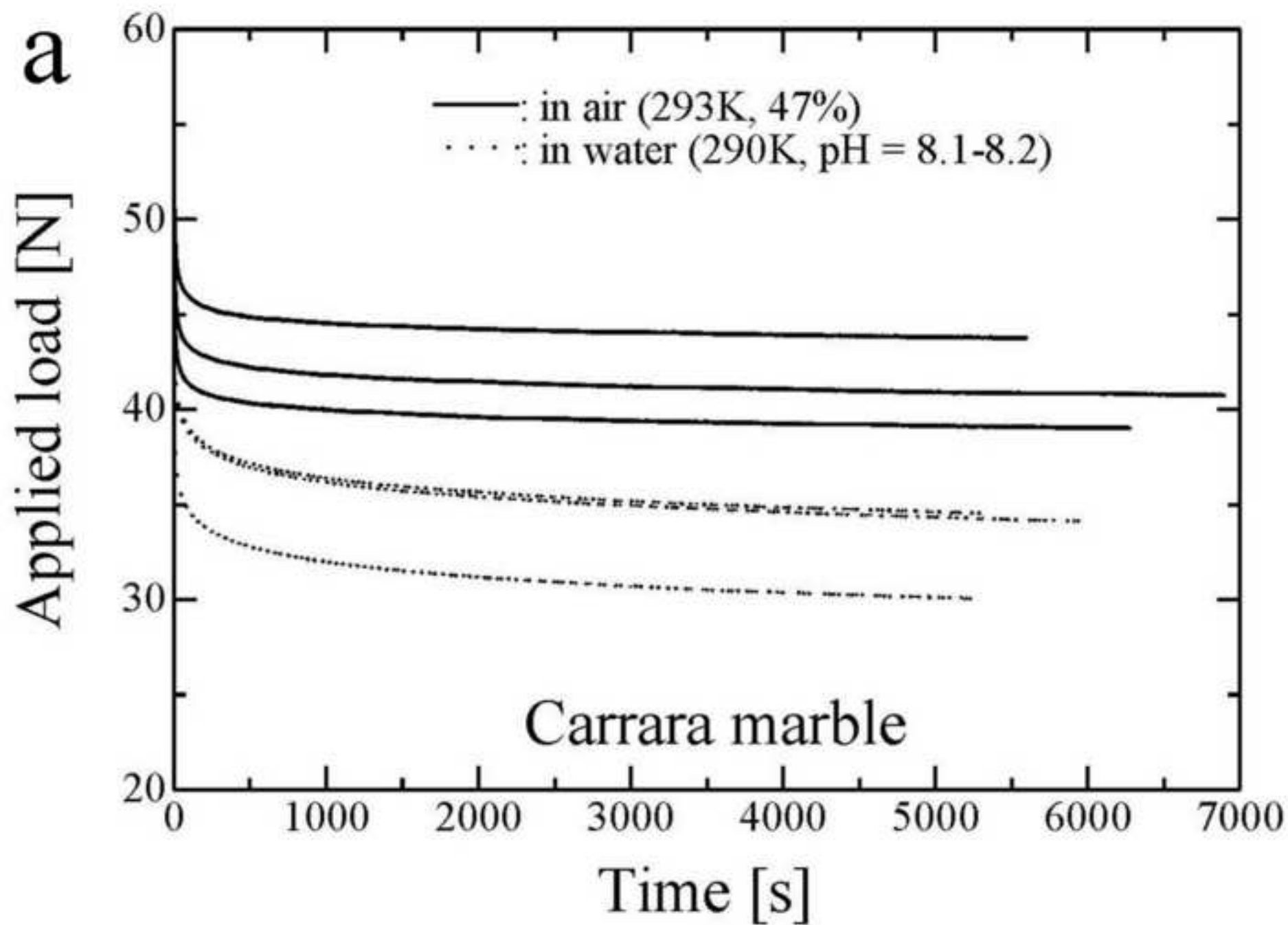


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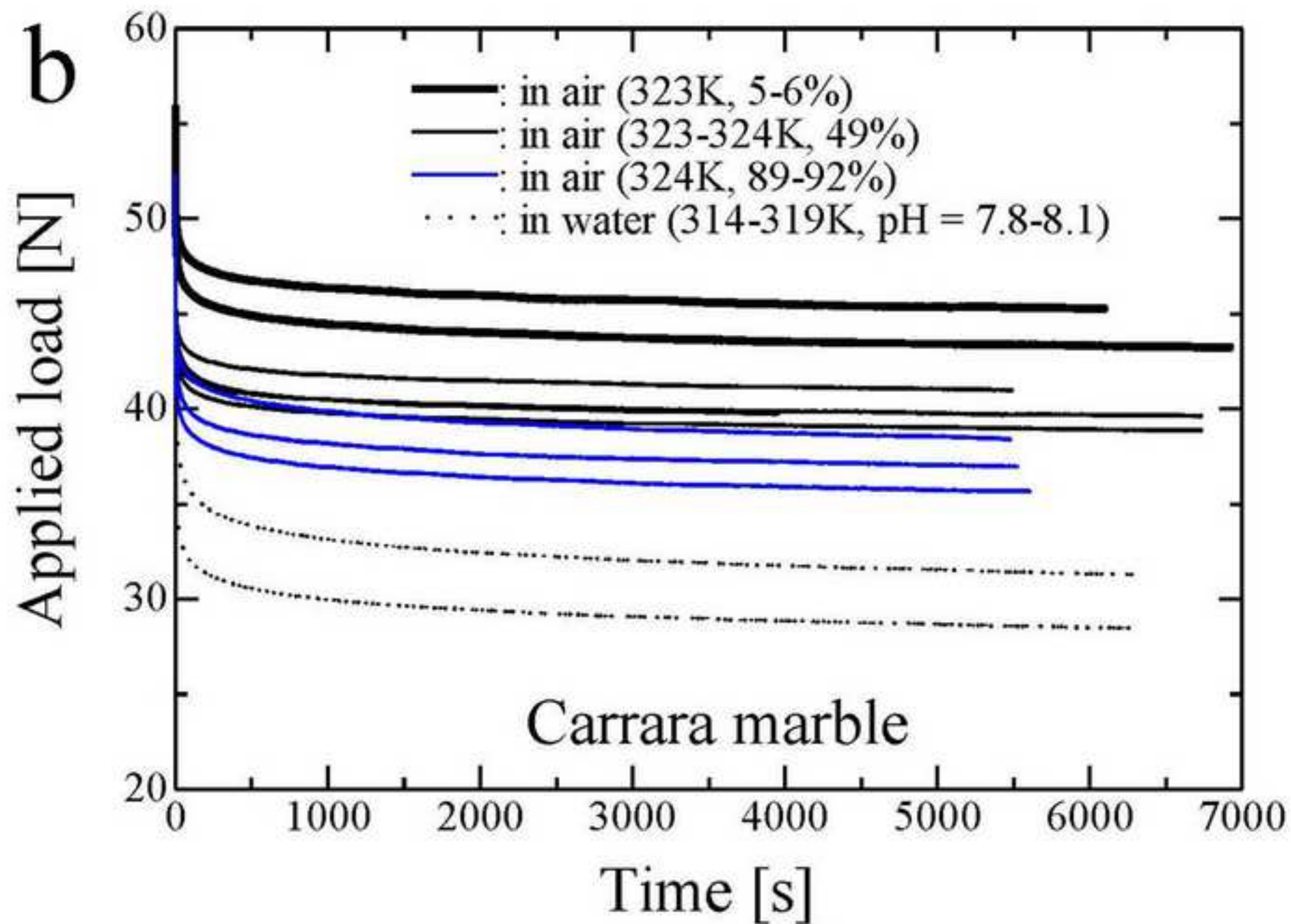


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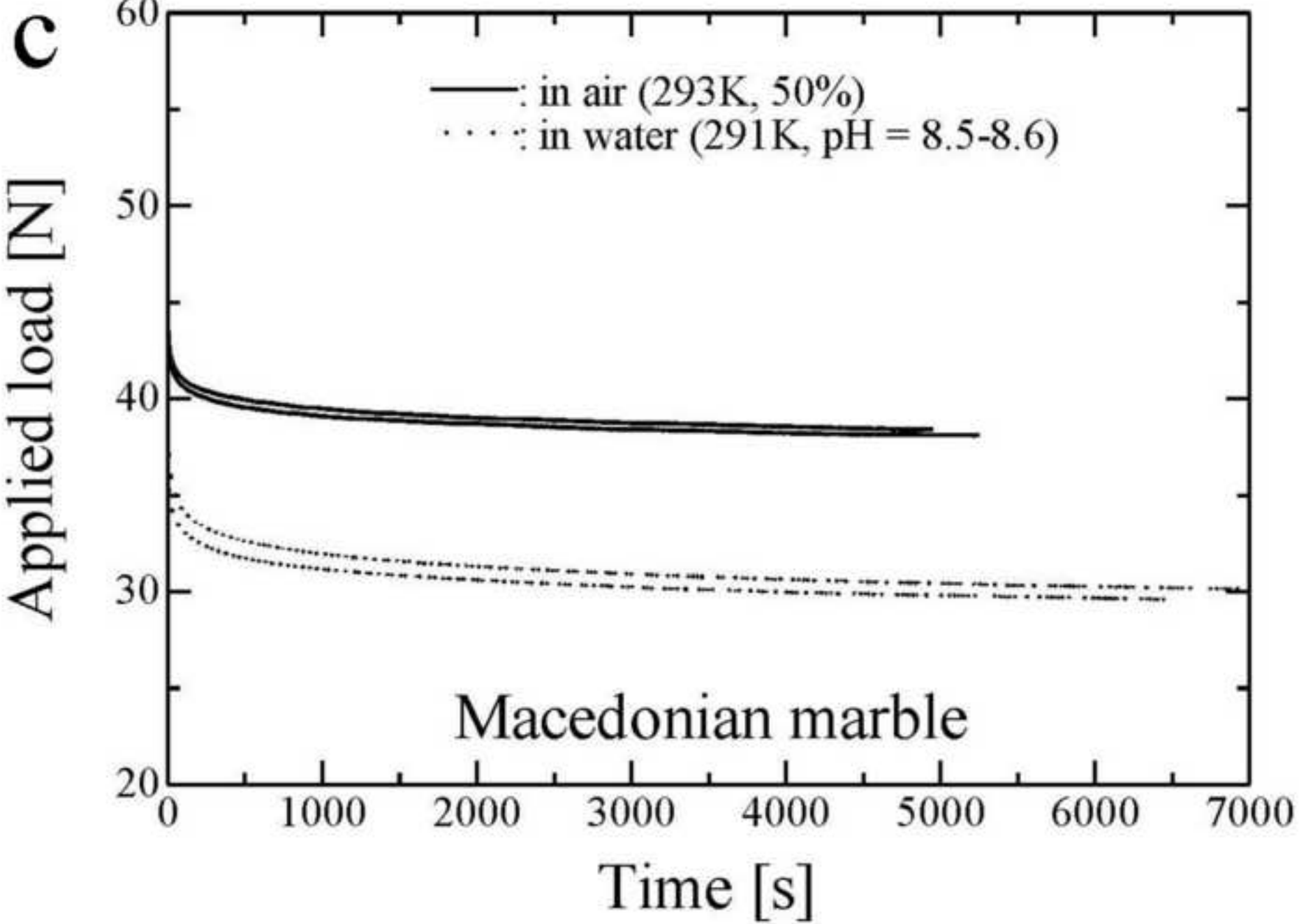


Figure5d

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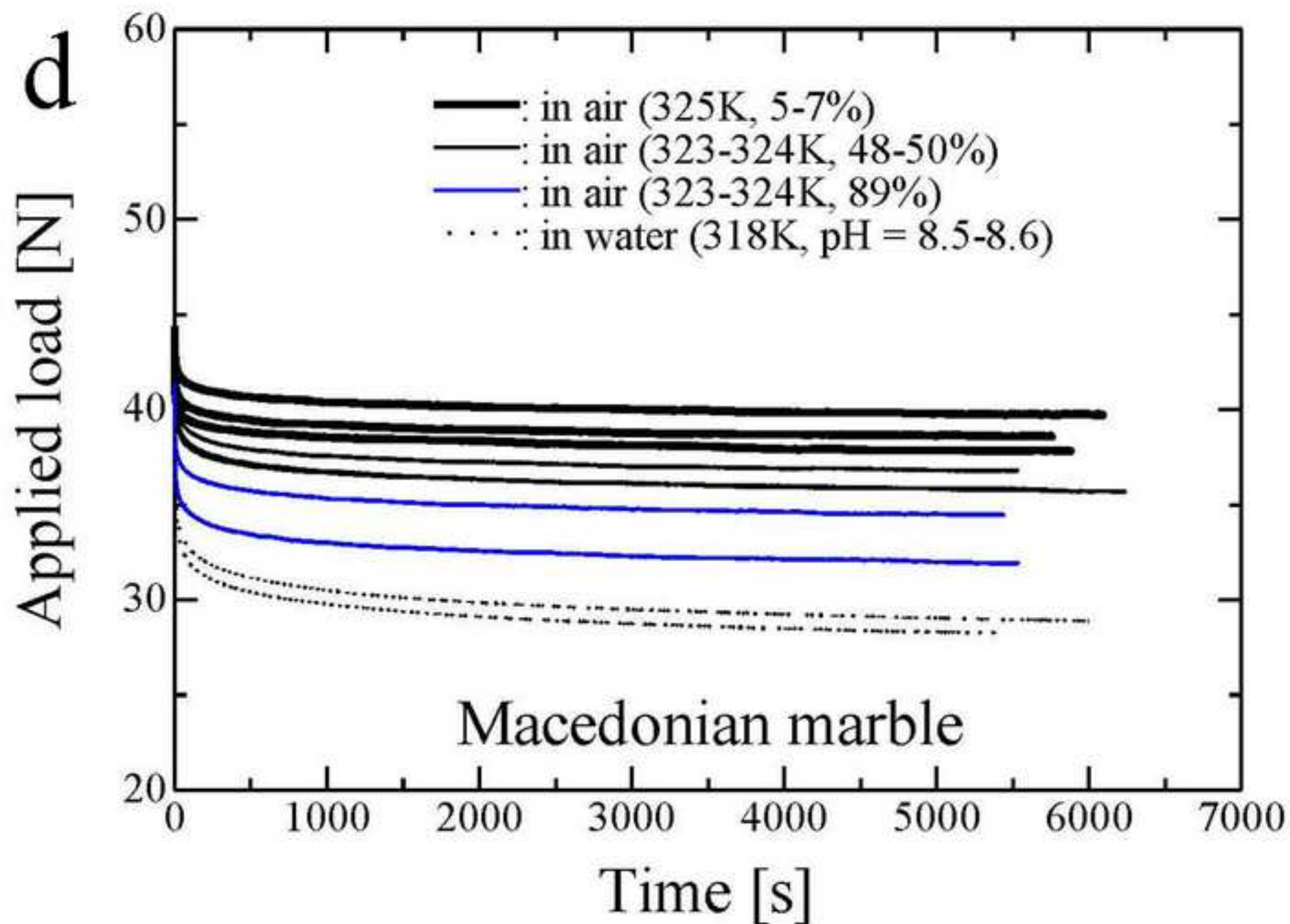


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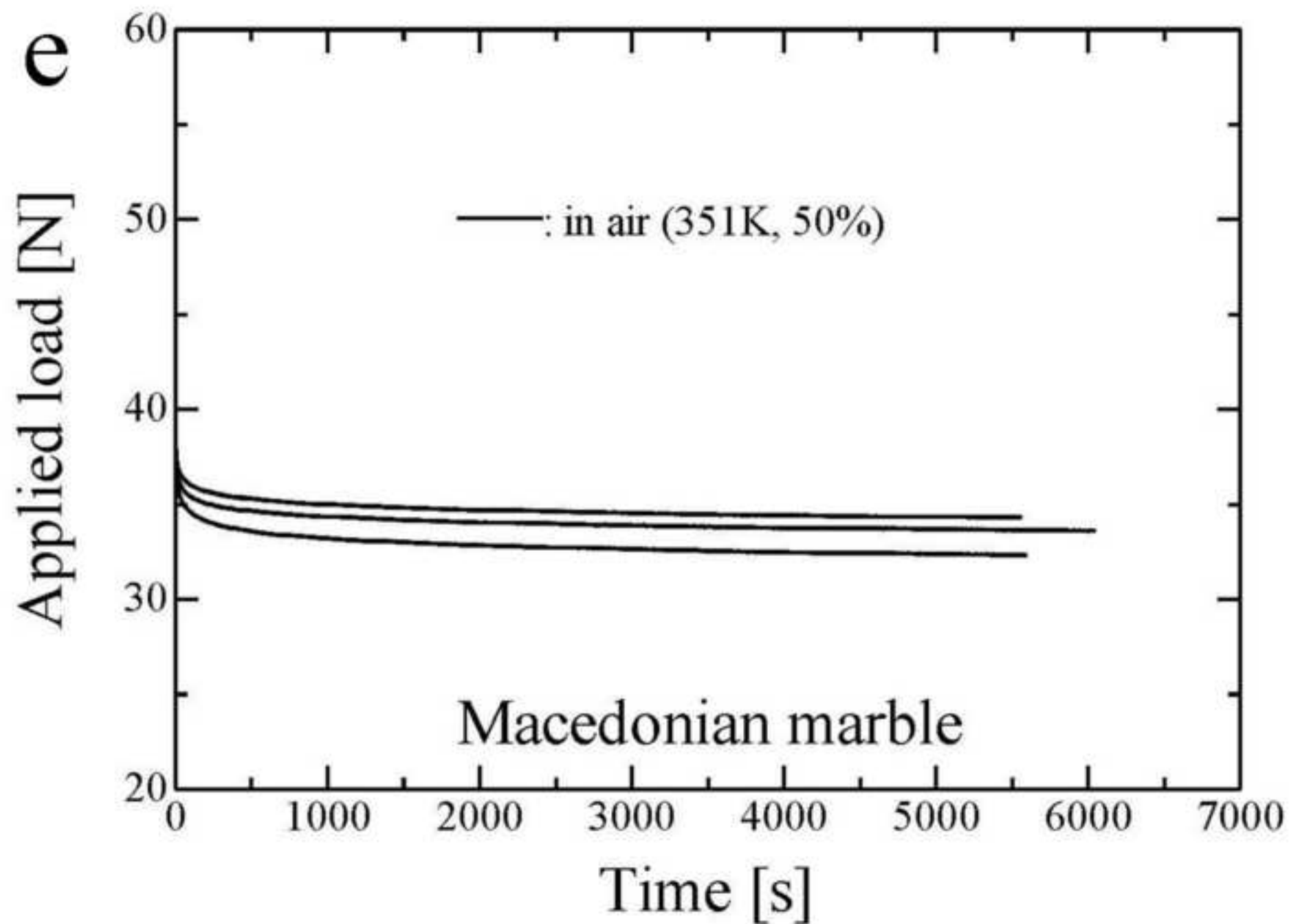


Figure6a

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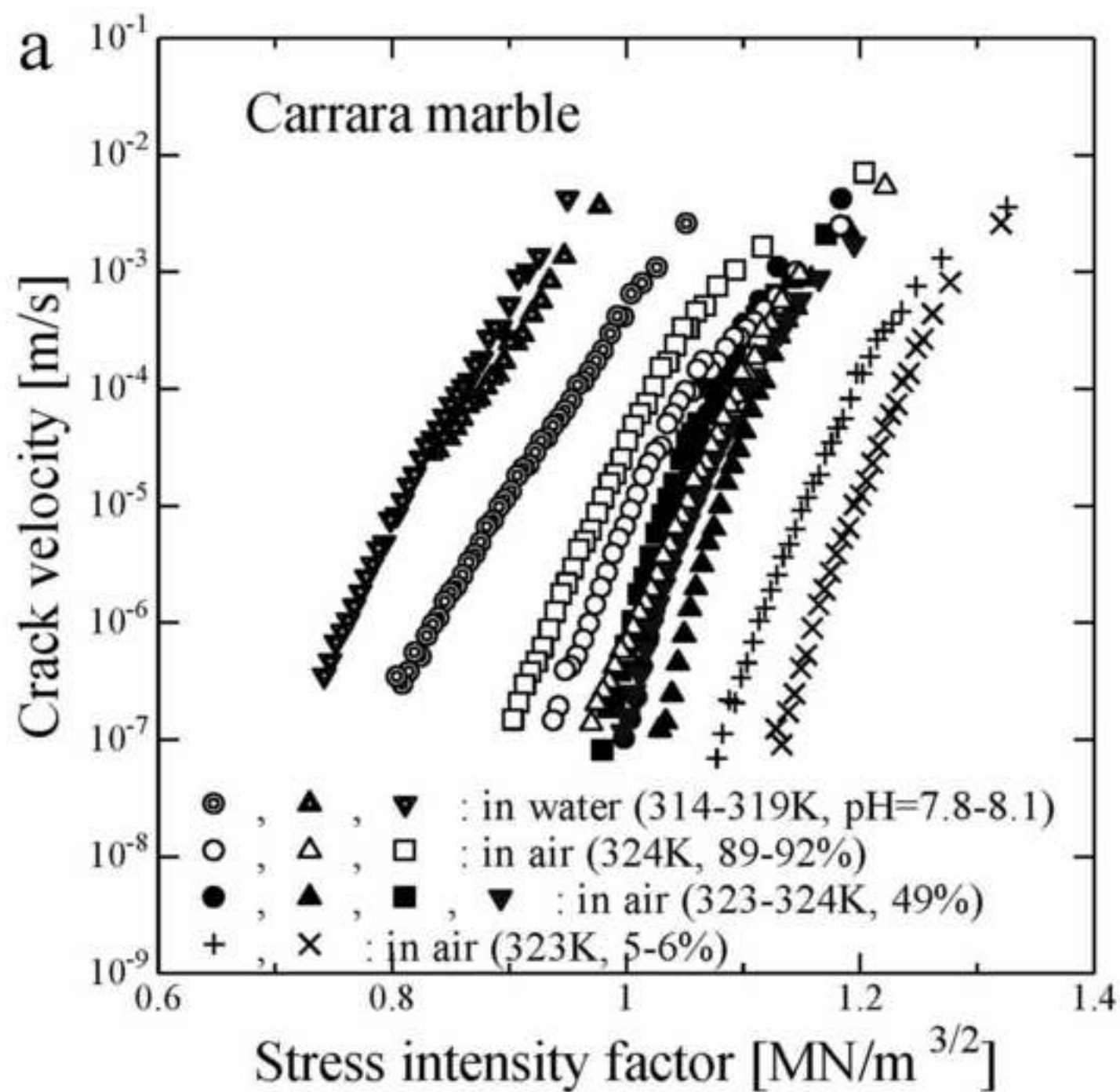


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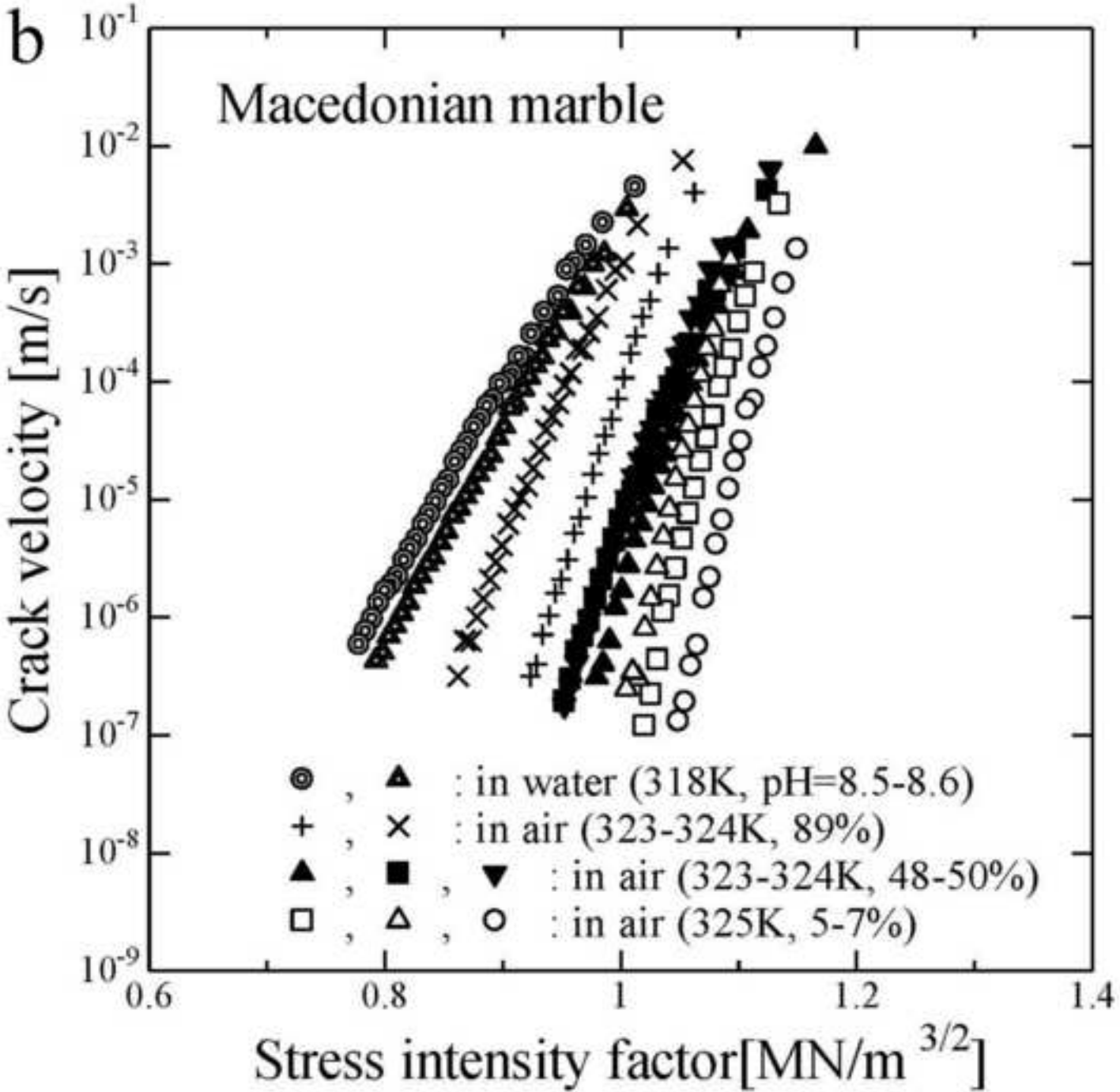


Figure7a

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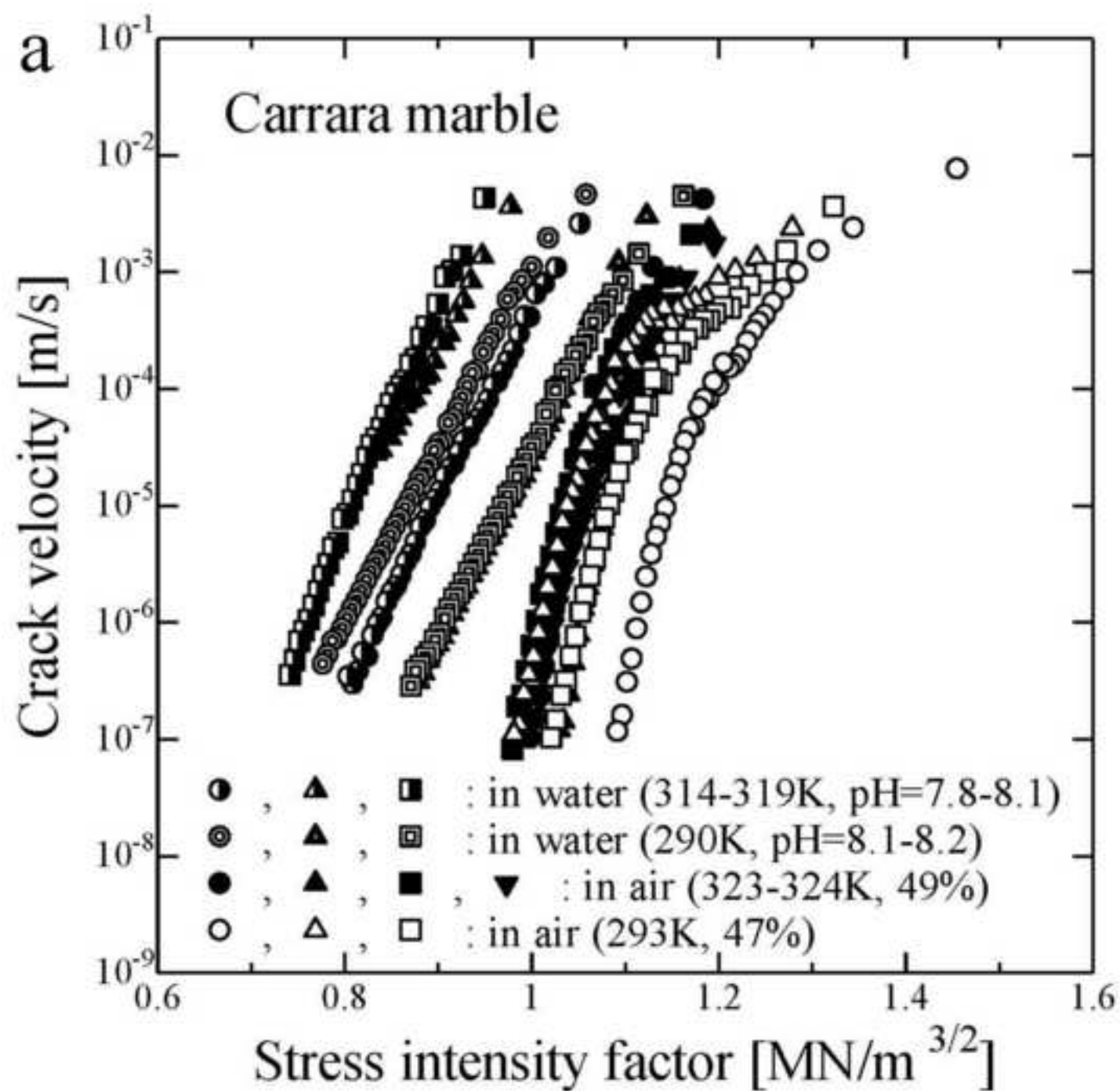


Figure7b

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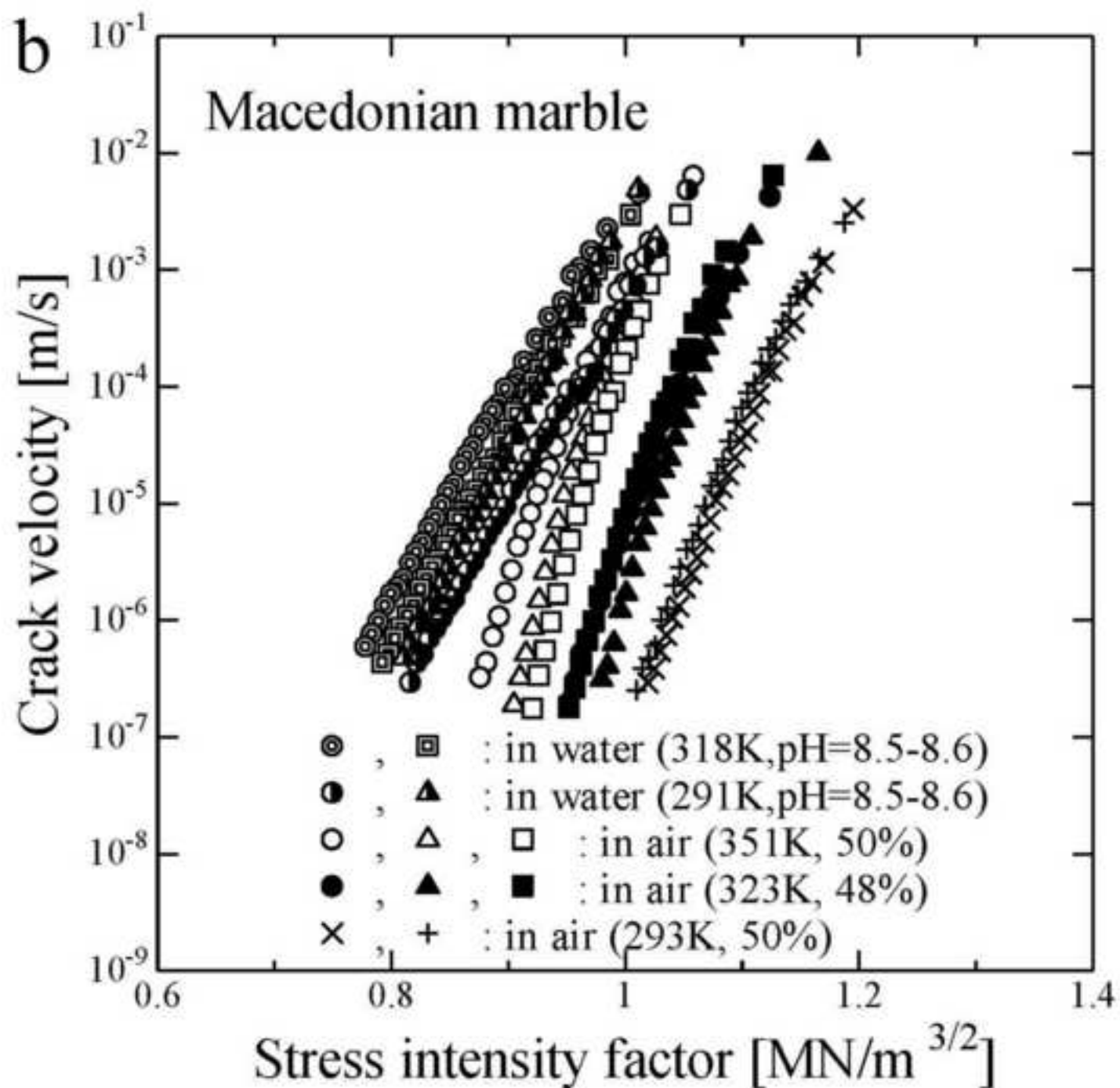


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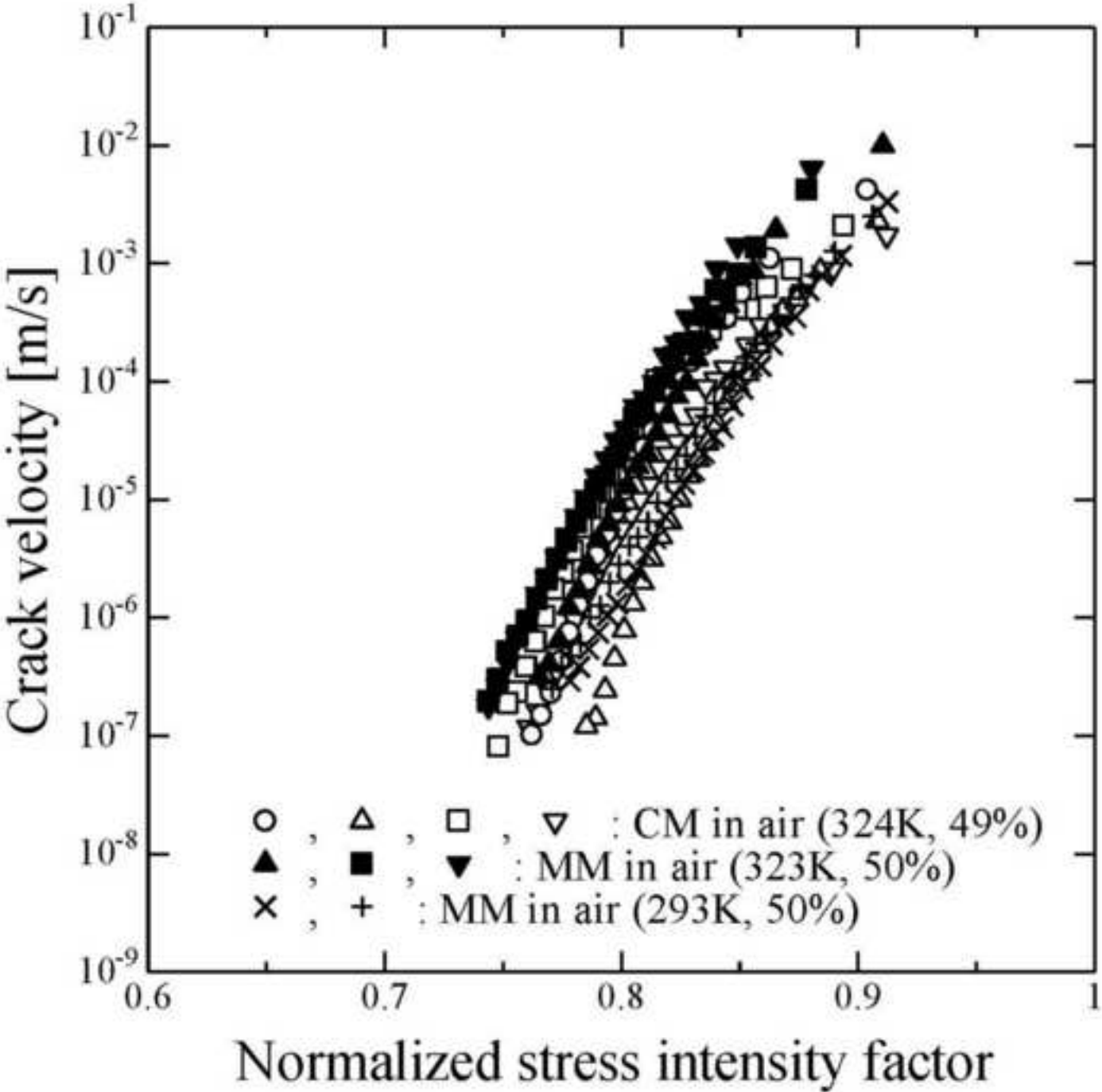


Figure9

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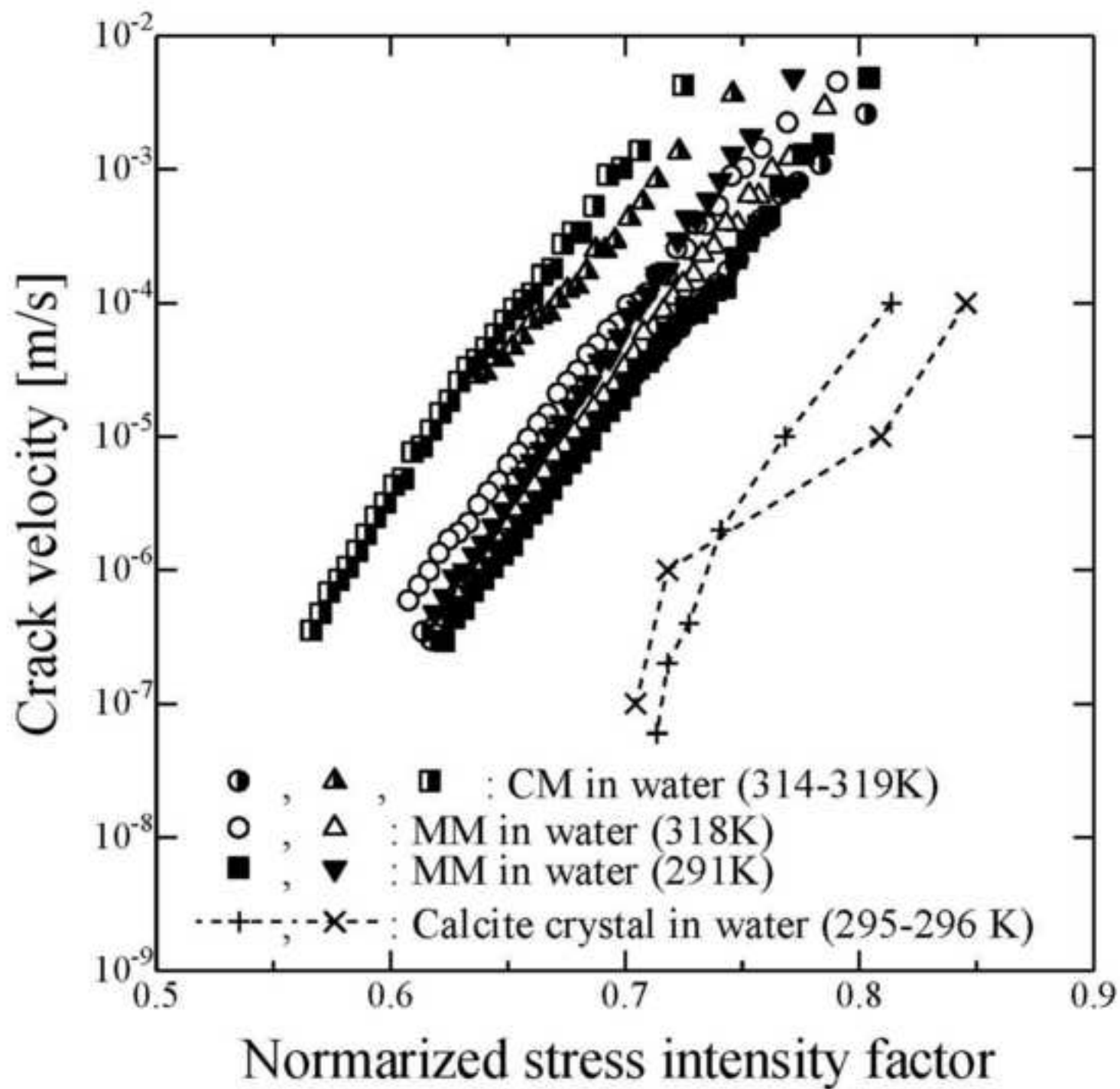


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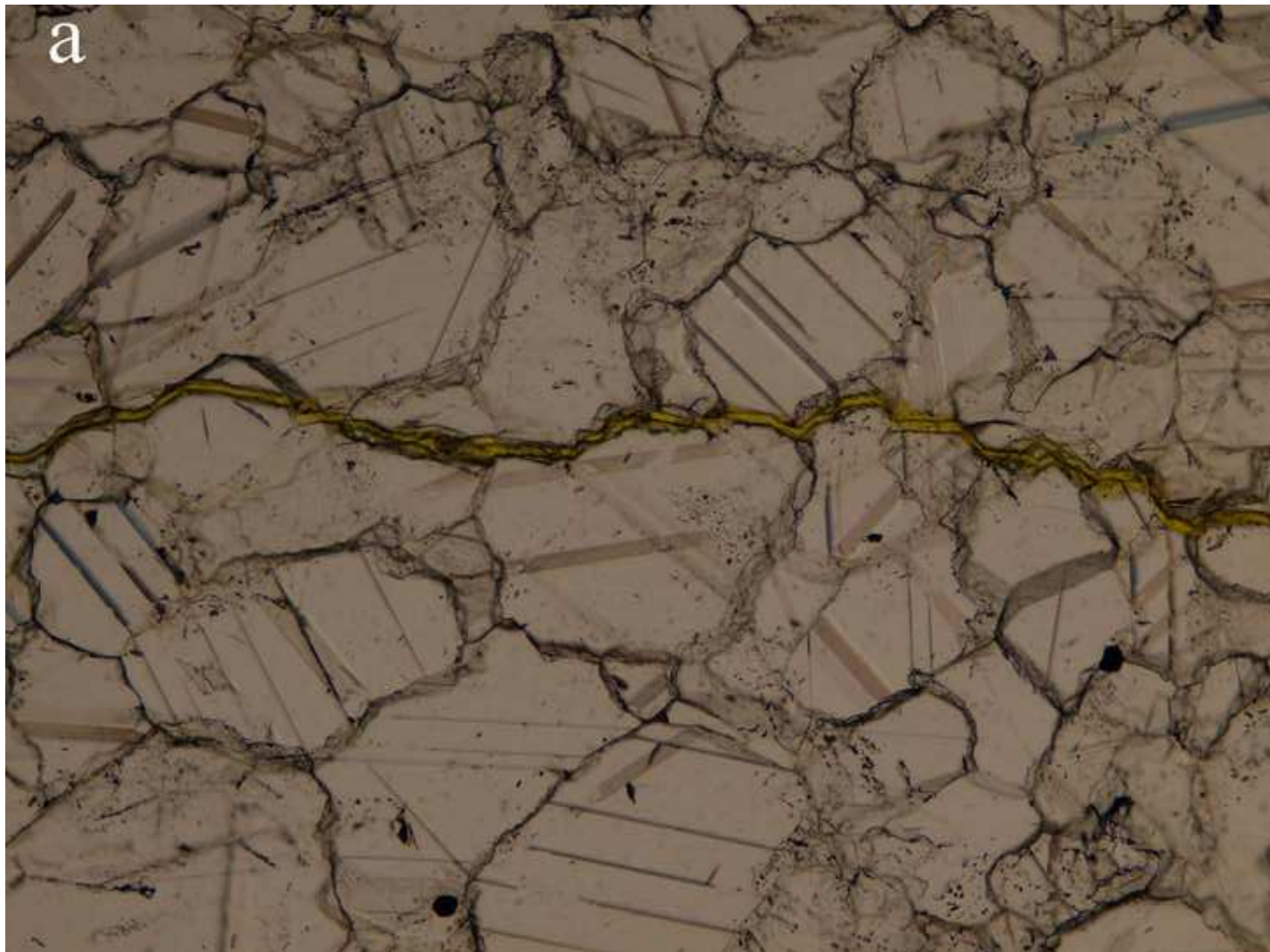


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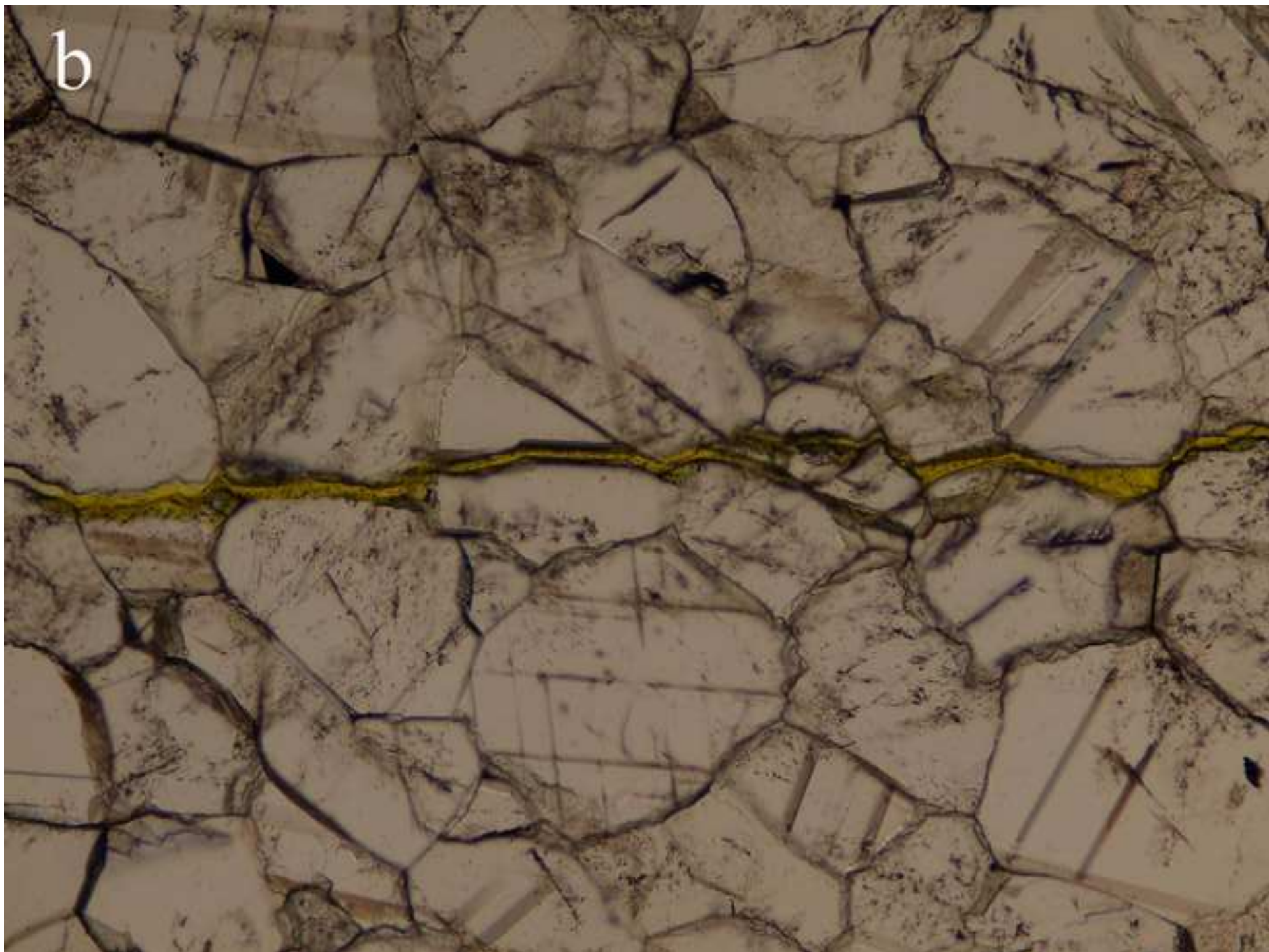


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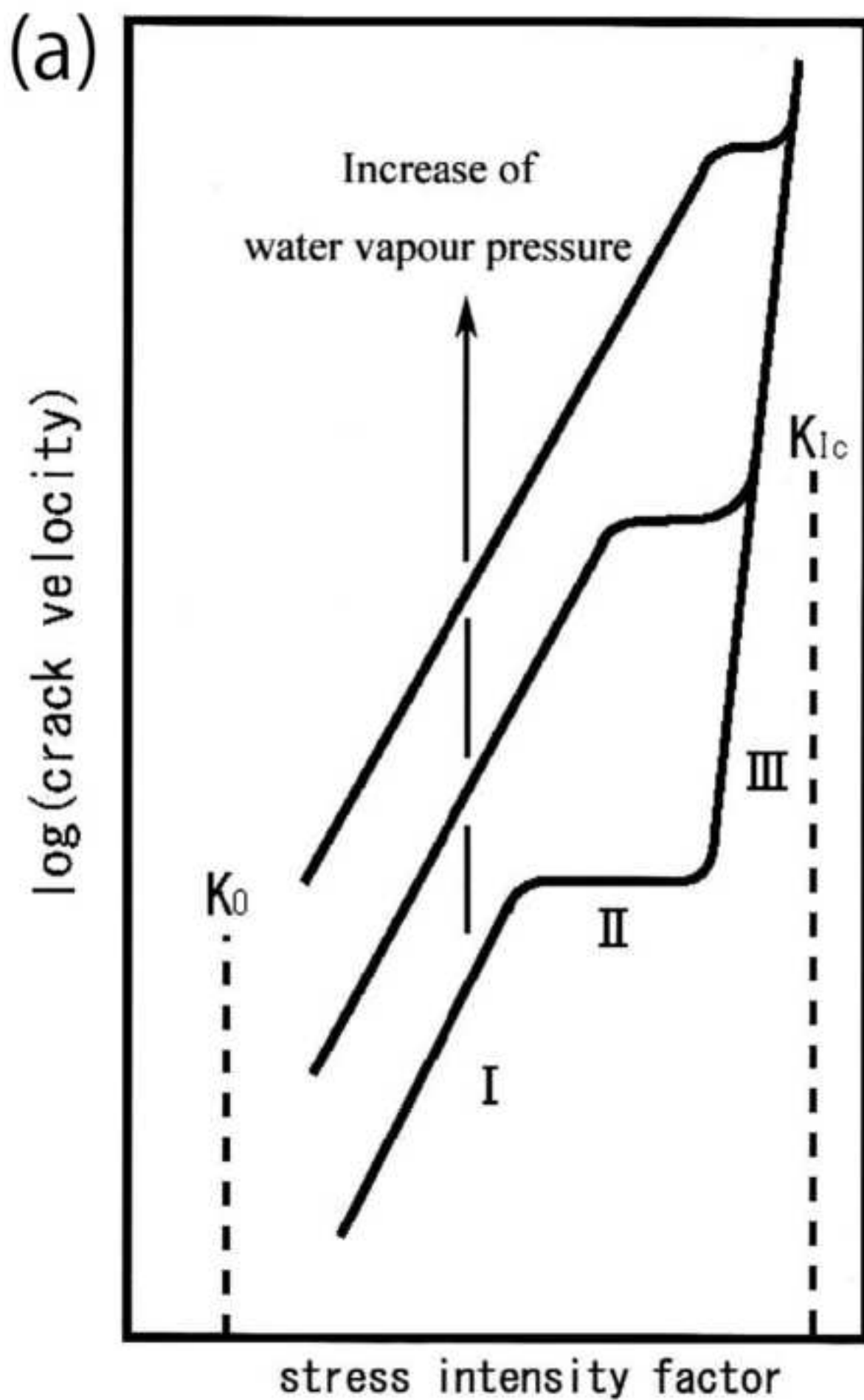
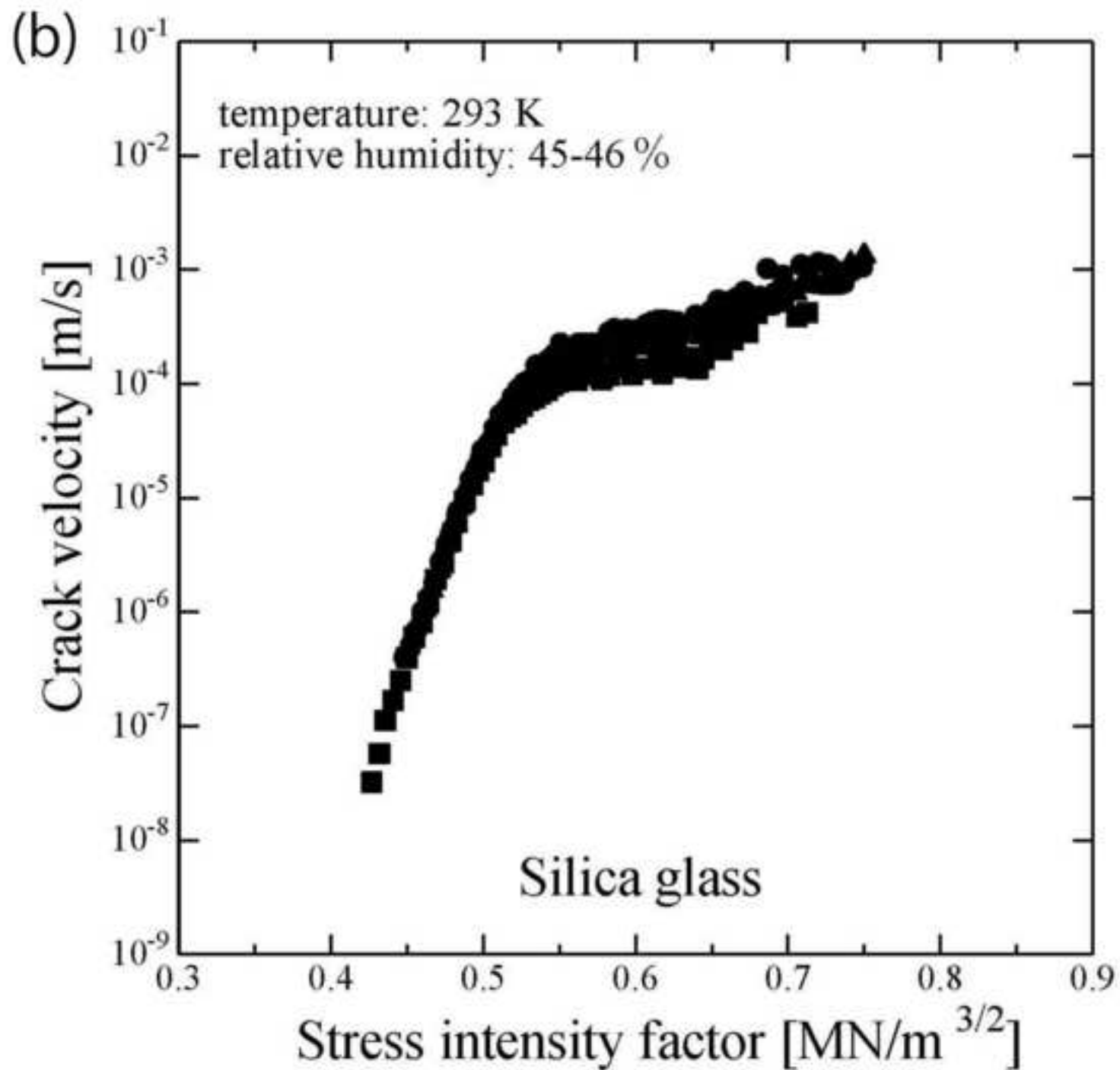
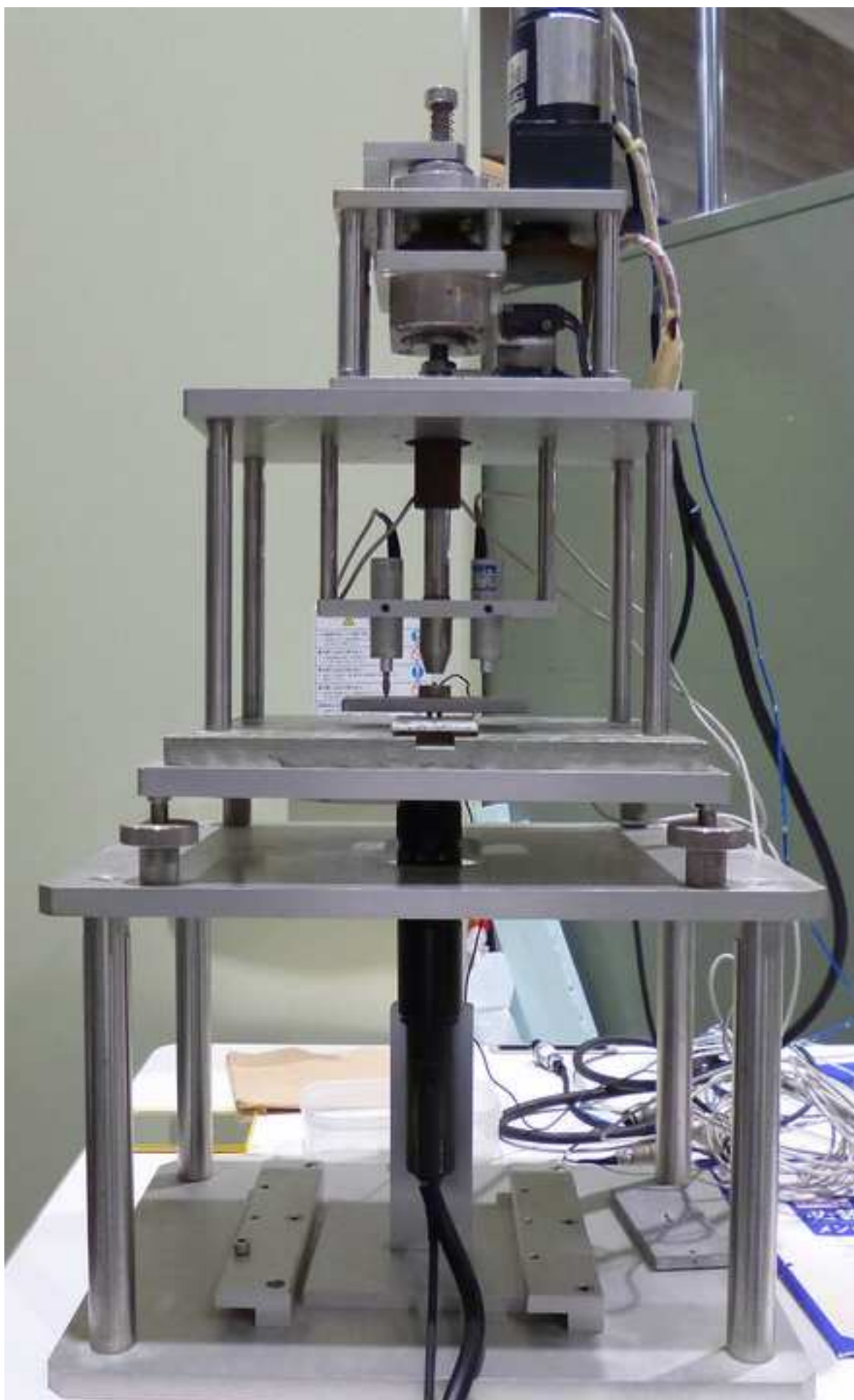


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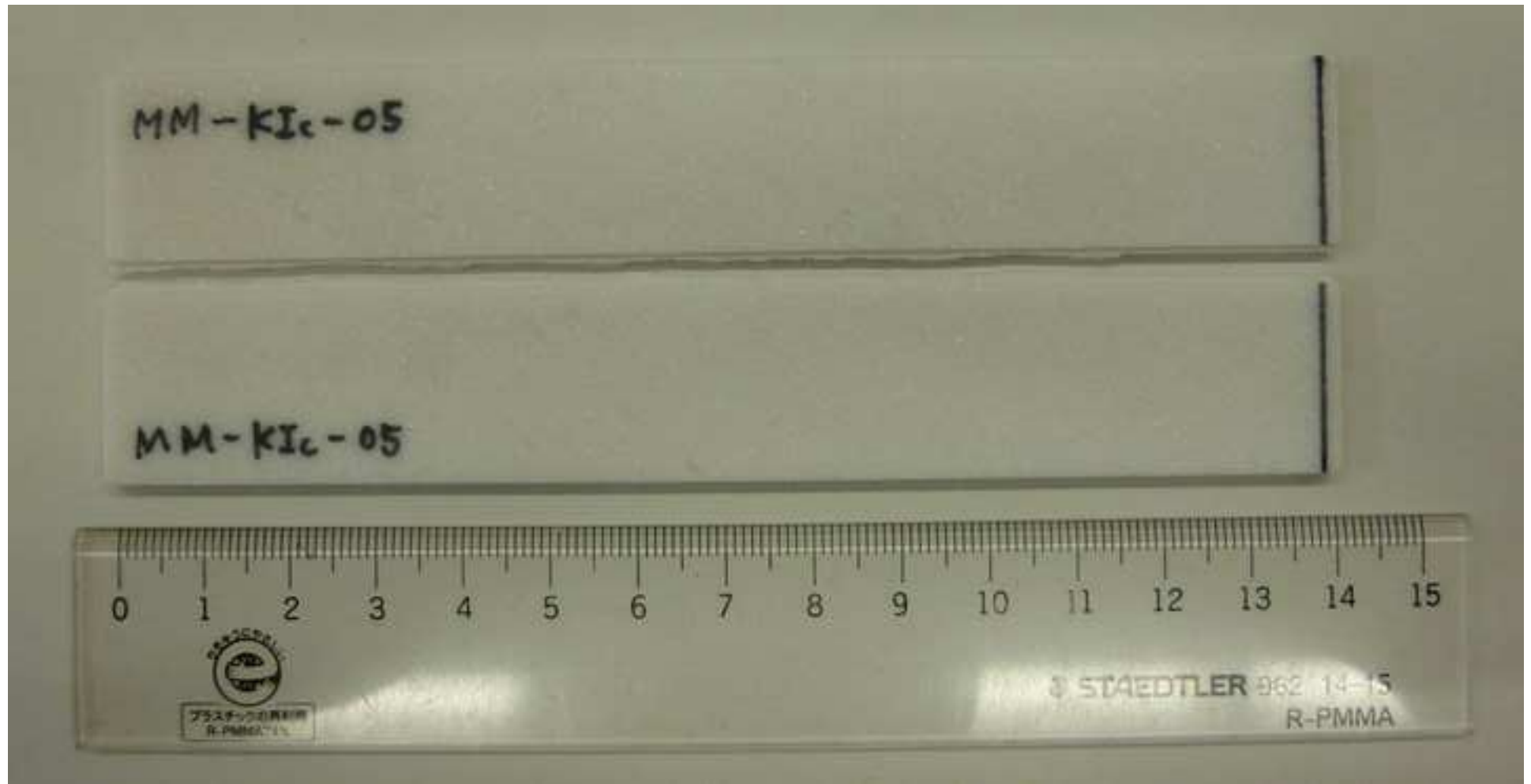


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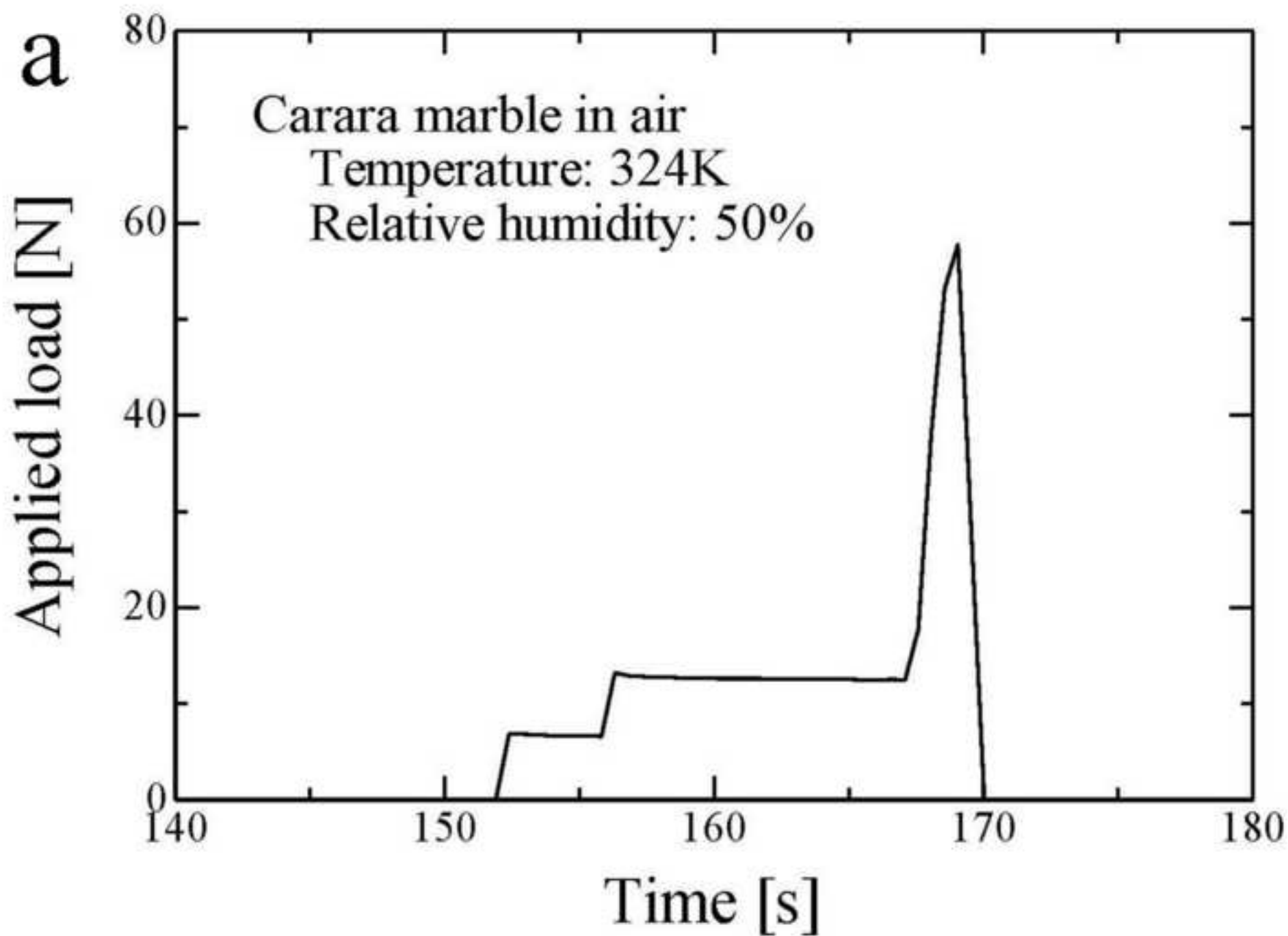


FigureA2

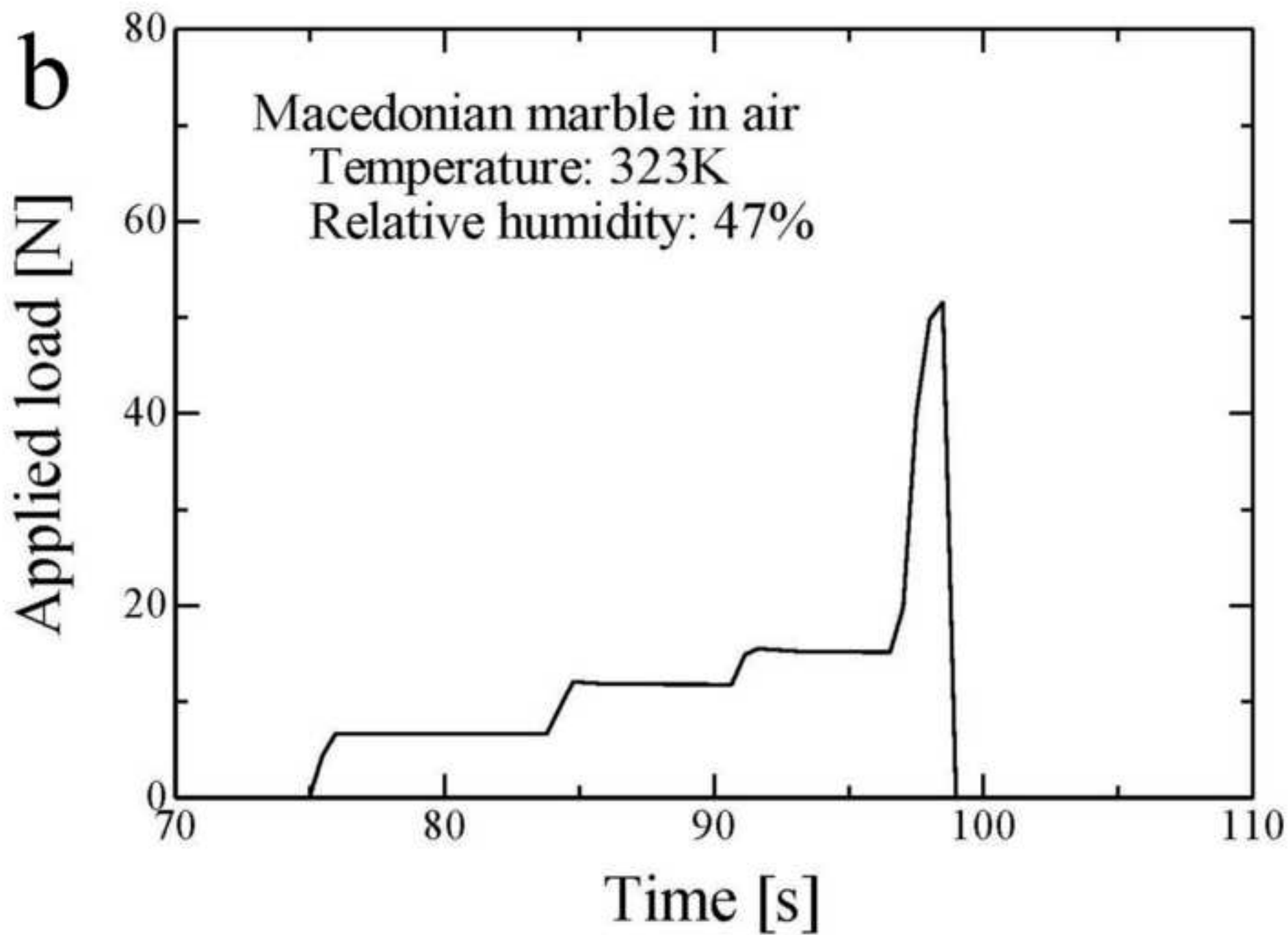
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FigureA3a
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