

X-ray Study of the Virgo Cluster of Galaxies with ASCA

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Abstract

We present the ASCA results of spatially resolved X-ray spectra in the central regions of the Virgo cluster, near to the central elliptical galaxy M87. We also present the result of mapping observation of the northwest region of the Virgo cluster. Since the spectra of the M87 region is complex, an adequate fit requires at least two thin thermal-plasma components. The temperatures of the hot and cool components are approximately 2.9 and 1.3 keV, respectively, and the temperature of these components are both nearly constant over the central 10' radius from the center of M87. However, the flux of the cool component is more concentrated toward the center than that of the hot component. Furthermore the surface brightness profile of the hot component can be extrapolated smoothly to that of the intracluster medium (ICM) beyond 40' from the center. These suggest that the cool component of M87 can be attributed the interstellar matter of M87, while the hot component is the ICM of the Virgo main body. The abundances of Fe, Si, and S rise towards the center of M87, though the ratios of Si/Fe and S/Si remain constant. We also found, contrary to the Einstein results, that the abundance ratio of oxygen to iron (O/Fe) is smaller than the solar value. These strongly constrain the chemical evolution scenario. The X-ray spectra of the ICM at regions beyond 40' from the center of M87 can be represented by a single temperature plasma. The temperature of the ICM decreases with radius from 0' to 50', and it is almost spatially constant beyond 50'. The metal abundance also decrease with radius from 0' to 50' and almost spatially constant beyond 50'. These temperature and abundance profiles can be a good clue to investigate the cluster formation history and cosmological parameters.

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Chapter 1

Introduction

The intergalactic space of a cluster of galaxies is filled with hot ($\sim 1 - 10$ keV) and tenuous ($\sim 1 \times 10^{-3} \text{ cm}^{-3}$) plasma, which is called the intracluster medium (ICM). The mass of the ICM is equal to or greater than that in the stellar component of the galaxies. Therefore, knowledge of the origin and evolution of the ICM is required to understand the evolution of clusters of galaxies and galaxies within them.

Major part of total gravitating mass of a cluster of galaxies is attributed to the dark matter, which cannot be observed at any wavelength. However, since the ICM is thought to be bounded in the gravitational potential of the cluster, one can estimate the amount and distribution of the dark matter using the spatial distributions of density and temperature of the ICM.

After the big-bang, only hydrogen and helium existed in the universe. However, heavy elements such as C, N, O, Ne, Mg, Si, S, Ar, Ca, Fe, Ni, and so on, which are called metals in astrophysics, are rich now. It is one of the major subjects of astrophysics to know how and when metals have increased in the universe. The fact that the ICM contains heavy elements suggests that material processed through stars can be ejected into the ICM, since heavy elements can be produced only through thermonuclear reactions in stars or by supernovae. Therefore we can know the chemical evolution of the universe by measuring the amount and spatial distribution of heavy elements in the ICM.

Thus, to know the physical condition of the ICM provides good clues to reveal the nature of the dynamical and chemical evolution of clusters and their dark-matter distributions. Since the ICM can be observed only in the X-ray band, we can get such important information only through X-ray observations of clusters of galaxies.

The ASCA satellite's (Tanaka et al. 1994 [131]) has good energy resolution over a wide energy band (0.4 - 10 keV) which has not been available with previous satellites. but its spatial

resolution is moderate. However, since Virgo is the nearest cluster which lies ~ 15 Mpc from us, we can spatially resolve it enough. Furthermore its high flux gives us X-ray data of the best quality. Especially, measurement of the spatial distribution of oxygen is possible only for the Virgo cluster. Since the O/Fe ratio is considered to be a key to clear the chemical evolution, X-ray observation of the Virgo cluster with ASCA is rather essential for the study the chemical evolution.

The Virgo cluster is commonly believed to be dynamically young (Binggeli et al. 1987 [13]). In this case, X-ray observation is the only possible way to map the distribution of the gravitating mass. For example, comparison of the distribution of the gravitating mass with that of the galaxies may give important information about evolution of clusters of galaxies.

The origin of metals in the ICM is considered to be elliptical galaxies (eg. Arnaud et al. 1992 [5]). Especially, giant elliptical galaxies at the center of clusters are considered to affect the physical state of the ICM based on the X-ray imaging observations (eg. Jones and Forman 1984 [70]). The Virgo cluster has the central dominant elliptical galaxy, M87. Therefore we can reveal what interaction exist between the galaxy and ICM.

ASCA observed M87 in 1993, and conducted mapping observation of the northwest region of the Virgo cluster in 1996 and 1997. We present a detailed analysis of the data from a $10'$ circle centered on M87, and from the mapping observation of the Virgo cluster, and we discuss the spatial distribution of the temperature and chemical abundances of the ICM.

In this thesis, we assume the distance of M87 to be 15 Mpc, so that a radius of $1'$ corresponds to 4.4 kpc (see chapter 4).

Chapter 2

Review of Clusters of Galaxies

2.1 Overview of Clusters of Galaxies

Clusters of galaxies are gravitationally bound systems of tens, hundreds, or even thousands of galaxies. They are among the largest known objects in the universe, having typical dimensions of roughly 1 – 6 Mpc across. Observations suggest that most galaxies belong to groups of various sizes. However, it is estimated that only 5 – 10 % of all galaxies in the universe reside in richly populated clusters. Thus, though very rich clusters of galaxies are rather impressive, they are relatively rare.

Rich clusters usually show a smooth, centrally concentrated galaxy distribution. On the other hand, poor clusters usually show little overall symmetry or central concentration. The closest example of a very rich regular cluster is the Coma cluster which lies at a distance of ~ 70 Mpc, while the Virgo cluster, which is the nearest cluster, is a typical example of a poor irregular cluster.

Clusters can also be classified according to their galaxy content. The galaxy population of rich regular clusters tend to be composed primarily of elliptical and S0 galaxies, with only a small fraction of spirals. For example, 80 % of the brightest galaxies in the Coma cluster may be ellipticals, and the few spirals are found at the outer regions of the cluster. In general, elliptical and S0 galaxies are by far the most common galaxies in the central region of rich, regular clusters. This is the converse of the situation outside of clusters, where majority of galaxies in isolation or in small groups are spirals. On the other hand, irregular clusters have a mixture of different galaxy types. For example, more than half of the brightest member galaxies in the Virgo cluster are spirals.

At the central region of many clusters, there are sometimes the largest known elliptical

galaxies in the universe, called cD galaxies. A cD galaxy is characterized by a very extended envelope of diffuse stellar light surrounding what may be an otherwise normal nucleus of a elliptical galaxy. Since the visible extent of a cD galaxy may be as much as 10 – 100 times that of a normal galaxy, the total luminosity associated with these galaxies is extremely large. The fact that many cD galaxies have multiple nuclei suggests that they may have grown through mergers of smaller galaxies.

Galaxies in a cluster move under the influence of gravity in orbits about their common center of mass. Unfortunately, it is impossible to measure the three dimensional spatial velocities of galaxies. However, we can estimate the component of velocity along the line of sight (i.e. the radial velocity) by measuring the redshift of a galaxy. Such measurements show that the member galaxies are all moving with different speeds about the cluster. Therefore, a cluster can be characterized by its velocity dispersion, which is a measure of the typical speed with which the galaxies are moving in the cluster. The typical value of the velocity dispersion of a rich cluster is ~ 1000 km/s. The velocity dispersion in many clusters shows a systematic decrease as the distance from the cluster center increases. The crossing time of a member galaxy in the inner region of a rich cluster is generally on the order of 10^9 yr (see Eq. (2.20)), which is less than the age of the Universe (the Hubble time, $\sim 10^{10}$ yr). This suggests that clusters of galaxies are well mixed, and that the regular clusters have reached a state of dynamical equilibrium, sometimes called as relaxation. On the other hand, irregular clusters are probably unrelaxed systems, having not yet reached a steady state.

We consider the simplest case of the circular Kepler motion. If a test particle of mass of m are rotating around an object of mass of M (assuming $M \gg m$), the equation of motion is

$$m \frac{v^2}{r} = G \frac{Mm}{r^2}, \quad (2.1)$$

where v is the velocity of the test particle, and r is the orbital radius. This equation reduces to

$$2T + W = 0, \quad (2.2)$$

where T is the kinematic energy defined as $T = mv^2/2$, and W is the gravitational energy defined as $W = -GMm/r$. Eq. (2.2) is the virial theorem, which holds for more complex situations if the system is in dynamical equilibrium. Assuming that the clusters of galaxies are in dynamical equilibrium, it is possible to determine their total gravitating mass using the virial theorem. In this case, Eq. (2.2) reduces to

$$M_{tot} = \frac{\langle v^2 \rangle R}{G}, \quad (2.3)$$

where M_{tot} is the total gravitating mass of the cluster, R is its characteristic size, and $\langle v^2 \rangle$ is the average of three dimensional velocities of member galaxies. Because $\langle v^2 \rangle = 3\sigma_r^2$, where σ_r is the cluster velocity dispersion, we get

$$M_{tot} = \frac{3R\sigma_r^2}{G} = 7.0 \times 10^{14} M_{\odot} \left[\frac{\sigma_r}{1000 \text{ km/sec}} \right]^2 \left[\frac{R}{1 \text{ Mpc}} \right]. \quad (2.4)$$

One can estimate the visible mass by simply counting the number of galaxies (This mass should probably be doubled to also include the X-ray intracluster gas). The visible mass thus obtained is usually 10 % of the virial gravitating mass. This is the missing mass problem, which is one of the most important unsolved problems of modern astrophysics. What it tells us that as much as 90 % of the matter in clusters is in a form that is invisible and can be detected only by the gravitational influence. The invisible matter is called the dark matter. What the dark matter may be is still pure speculation at present. There have been many suggestions, raging from faint low-mass stars, to black holes, to exotic forms of matter predicted by elementary particle physics.

In the following section, we summarize the X-ray properties of the clusters of galaxies, especially focusing on the recent ASCA results.

2.2 X-ray Properties of Clusters of Galaxies

2.2.1 Overview

The luminous material in clusters of galaxies falls primarily into two forms: (1) the visible galaxies; (2) the hot and tenuous gas which fills the whole region of the clusters of galaxies. The latter is called the IntraCluster Medium (ICM). Although emission from individual galaxies in a cluster is sometimes seen, the primary source of X-ray emission from clusters of galaxies is the hot ICM. X-ray luminosity of clusters range from $1 \times 10^{42} - 1 \times 10^{45}$ erg/s with gas temperatures of 1 – 10 keV, which is comparable to the equivalent temperatures as measured by the velocity dispersions for the galaxies in the cluster (i.e. $\beta_{spec} \sim 1$; see section 2.3). The ICM is a major observed luminous component of clusters with a mass equal to or greater than that in the stellar component of the galaxies. However, the visible galaxies and the X-ray emitting ICM do not comprise most of the cluster mass, most of which is the dark matter. Though the dark matter is not directly observable at any wavelength, one can estimate the amount and distribution of the dark matter using the X-ray data.

Table 2.1: Cluster morphology and dynamical evolution (Forman and Jones 1982).

	Non-x-ray-dominant galaxy (nXD)	X-ray-dominant galaxy (XD)
Irregular (less evolved)	Low $L_x \lesssim 10^{44}$ ergs/sec Cool gas $T_g = 1-4$ keV X-ray emission around many galaxies Irregular x-ray distribution High spiral fraction $> 40\%$ Low central galaxy density Prototype: A1367	Low $L_x \lesssim 10^{44}$ ergs/sec Cool gas $T_g = 1-4$ keV Central galaxy x-ray halo Irregular x-ray distribution High spiral fraction $> 40\%$ Low central galaxy density Prototype: Virgo/M87
Regular (more evolved)	High $L_x \gtrsim 10^{44}$ ergs/sec Hot gas $T_g \gtrsim 6$ keV No cooling flow Smooth x-ray distribution Low spiral fraction $\lesssim 20\%$ High central galaxy density Prototype: Coma (A1656)	High $L_x \gtrsim 3 \times 10^{44}$ ergs/sec Hot gas $T_g \gtrsim 6$ keV Cooling flow onto central galaxy Compact, smooth x-ray distribution Low spiral fraction $\lesssim 20\%$ High central galaxy density Prototype: Perseus (A426)

2.2.2 Morphology

Forman and Jones (1982) [44] and Jones and Forman (1984) [70] proposed a two-dimensional cluster classification system for the X-ray morphology of galaxies, which they relate to the evolutionary state of the cluster as determined by its optical properties. The system is summarized in table 2.1. In this scheme, an X-ray cluster having a central dominant galaxy is called an XD cluster, while a cluster with no central dominant galaxy is called a nXD cluster. The Virgo cluster is a typical example of the XD and irregular (less evolved) cluster.

2.2.3 Gas Temperature

If gas densities in the central region of the cluster is enough high, the gas can radiate its energy, and cool on relatively short time scales ($\sim 10^9$ yr). The cooled gas is then expected to flow toward the cluster center, which is called a cooling flow (a detailed review of the cooling flow can be seen in Fabian (1994) [36]).

Fukazawa (1997) [47] observed a large sample of XD clusters with ASCA, and found that there are at least two temperature-plasma components at the central region of all the XD clusters. Since the cool component cannot be seen in the outer region of the clusters, it can be attributed to the central dominant galaxy, and may be due to the cooling flow. On the other hand, the hot component is likely to be the ICM of the cluster.

Markevitch et al. 1997 [87] analyzed spatially resolved X-ray spectra of 26 bright clusters obtained with ASCA, and found that most of them show a temperature decrease with radius. Honda et al. (1996) [62] found that the Coma cluster have significant temperature variation. This strongly suggest that the Coma cluster is not a dynamically relaxed system, though its optical appearance is quite smooth and rich. These temperature profile can be a good clue to investigate the cluster formation history and cosmological parameters.

2.2.4 Metal Abundance

There are emission lines from iron and other heavy elements in the energy spectrum of the ICM. Since heavy elements can be produced only through thermonuclear reactions in stars or by supernovae, these emission lines suggest that material processed through stars can be ejected into the ICM. The correlation of total Fe mass with total light from member elliptical galaxies suggested that the metals in the ICM originated from elliptical galaxies and that the metals were driven out into the ICM by supernova (SN) driven winds (Arnaud et al. 1992 [5]; Tsuru 1993 [137]). The type Ia SNe, whose progenitors are old, light stars, make mainly iron, while the type II SNe, which occur at the death of massive stars, make mainly the α elements (O, Ne, Mg, Si, and S) (figure 2.1). Since a low mass star have a long time life, the SNe Ia are thought to be important in relatively recent chemical enrichment, while SNe II are thought to be important at the early galaxy formation phase of the cluster. Thus we can know the chemical evolution of the universe by measuring the amount and spatial distribution of heavy elements in the ICM. The abundance ratio of α element (especially oxygen) to iron is one of the most important parameters.

The range of the iron abundance seen in rich clusters are rather narrow (0.25 – 0.4 solar) (eg. Edge and Stewart 1991 [32]; Yamashita 1992 [144]) as opposed to the wide range seen in poor clusters from 0.1 (NGC2300; Davis et al. 1996 [27]) to 1.0 solar (central region of Centaurus; Fukazawa et al. 1994 [45]).

Mushotzky et al. (1996) [105] measured the abundances of O, Ne, Mg, Si, S, Ca, Ar, and Fe for 4 clusters of galaxies using the ASCA data, and found that the obtained abundance ratio is similar to that of the SN II.

With ASCA data, it was found that some of such XD clusters as the Centaurus (Fukazawa et al. 1994 [45]; Ikebe 1996 [64]), AWM7 (Ohashi et al. 1994 [108]; Xu et al. 1997 [142]; Ezawa et al. 1997 [35]), and Hydra-A cluster (Ikebe et al. 1997 [66]) have abundance increase towards the cluster centers. Fukazawa (1997) [47], using a larger sample of XD clusters, found that this

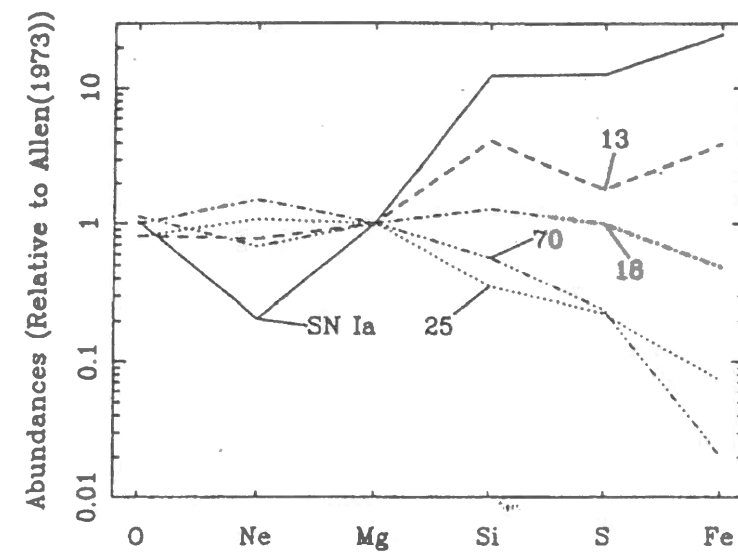


Figure 2.1: The predicted relative abundances of synthesized heavy elements (Tsujimoto et al. 1995). The ratios to the cosmic abundance of Allen (1973) are plotted for SN Ia and SN II of 13, 18, 25, and $70M_{\odot}$ stars.

abundance increase is common for the XD clusters. Therefore he concluded that this is due to the metal ejection from dominant galaxies. One of the exception is A1060, the ASCA data of which were analyzed by Tamura et al. (1996) [130]. A1060 is a XD cluster, but shows no abundance gradient. This may be due to the dynamical nature of the dominant galaxy, which has an accompanying giant elliptical galaxy at the projected distance of 35 kpc and is very likely to form a tight binary with the galaxy.

Ezawa et al. (1997) [35] observed AWM7 with ASCA and found that the iron distribution traces the galaxy distribution. This discovery and the metal concentrations around dominant galaxies are the direct evidence that metals are ejected from galaxies.

2.2.5 Gravitational Potential

From X-ray surface brightness distribution, we can know the density profile of the ICM. Assuming the hydrostatic equilibrium of the ICM, one can estimate the structure of the gravitational potential of the clusters of galaxies (see section 2.3).

If one fit the X-ray surface brightness profile with the β model (Eq. (2.39)), many XD clusters have excess emissions at the central regions (Jones and Forman 1984 [70]). This central excess was considered to be due to the cooling flow in the cluster core, because the flow is expected to make the gas density and emissivity further high at the central region of the cluster. If this explanation is true, one can not see the central excess in the X-ray surface brightness profile obtained in the high energy band (> 4 keV). ASCA is the first satellite having capability of imaging in the high energy band. Ikebe et al. (1997) [66] analyzed the X-ray brightness profile of the Hydra-A cluster, and found that the central excess can be seen

in the high energy band as well as in the soft energy band. This discovery suggests that the central excess is not due to the dense cool gas, but is due to the structure of the gravitational potential of the cluster. The potential structure must have an additional central dimple, which can be attributed to the central dominant galaxy and at least partially causes the central excess brightness. This suggests that the dark matter exhibits hierarchical clustering. The Centaurus cluster is almost identical with the Hydra-A (Ikebe 1996 [64]).

More convincing result was obtained by the observation of the Fornax cluster (Ikebe et al. 1996 [65]). The ICM of the Fornax cluster is almost spatially constant with ~ 1 keV, and hence is considered to have no cooling flow. The surface brightness profile can not be fitted with a single-component β model, but can be fitted with a two-component β model. The extent of each component corresponds to the central dominant galaxy NGC1399, and to the whole region of the Fornax cluster. This also resulted in the double structure of the gravitational potential (figure 2.2).

However it seems to be strange for us that though we can see the hierarchical structure in the distribution of the dark matter, we cannot see that in the stellar distribution at all. Since the β model is not a good approximation of the ICM distribution beyond 5 times the core radius (see section 2.3), we think the shoulder-like structure of the dark matter distribution may be depend on surface brightness models.

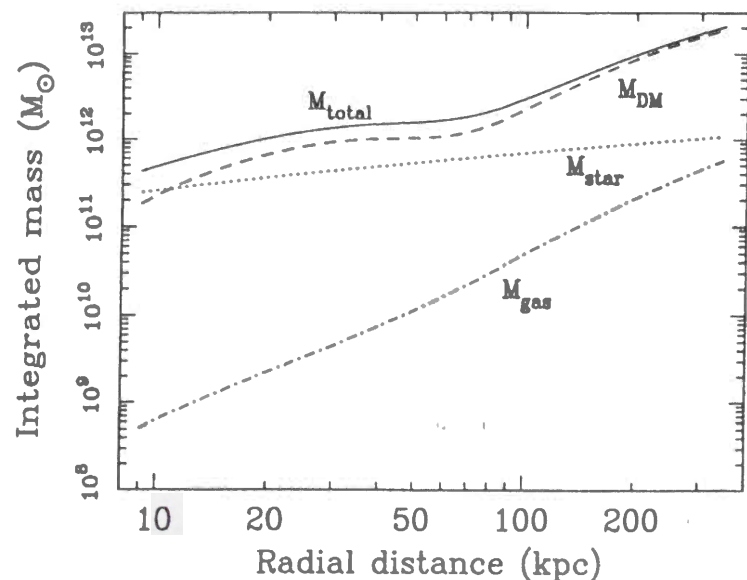


Figure 2.2: Distribution of various mass components in the Fornax cluster (Ikebe 1996).

2.2.6 Evolution of Clusters of Galaxies

The X-ray luminosity of cluster (L_X) is correlated with the temperature (T_g) as $L_X \propto T_g^3$ (Mushotzky 1984 [101]; Edge and Stewart 1991 [32]; Hatsukade [57]; David et al. 1993 [25]). This correlation is considered to be the evidence of cluster evolution (see section 2.3).

Mushotzky and Loewenstein (1997) [103] found no evolution of metal abundance from $z \sim 0.5$ till now. Furthermore, Mushotzky and Scharf (1997) [104] found no evidence for evolution in the $L_X - T_g$ relation out to $z \sim 0.5$. Similar results have been obtained by Tsuru et al. (1997a) [138] and Tsuru et al. (1997b) [139].

However, Hattori et al. (1997) [58] discovered an X-ray cluster, AXJ2019+1127 at $z=1$, which has been known as a gravitational object. Though only the two galaxies has been found in this cluster, this cluster contains iron as many as nearby cluster. Furthermore, Tsuru (1997b) [139] found that the iron masses of the two very distant clusters at $z \sim 0.8 - 1.0$ are significantly different from each other, and that the gas masses of two clusters at $z \sim 0.8 - 1.0$ and some clusters around $z \sim 0.6$ are significantly lower than those of nearby clusters. These results indicate a hint of evolution of clusters of galaxies.

2.3 Theoretical Backgrounds

In this section, we briefly summarize some physical backgrounds which relate to X-ray emissions from clusters of galaxies.

2.3.1 X-ray Emission from Thin Thermal Plasma

Because the ICM is low density ($\sim 10^{-3} \text{ cm}^{-3}$) and high temperature ($\sim 10^8 \text{ K}$) plasma, it emits most of its energy into the X-ray band. We summarize some theoretical aspects to deduce physical condition of the ICM such as temperature, metallicity, density, and so on, using the X-ray spectral information from the ICM.

Radiative processes which relate to thermal electrons in hot plasma are divided primarily into three groups based on their transitions;

1. free-free emission

A free electron emits when it is scattered by the Coulomb field of an ion. This radiation is called bremsstrahlung, or free-free emission. This mechanism contributes to X-ray continuum emission.

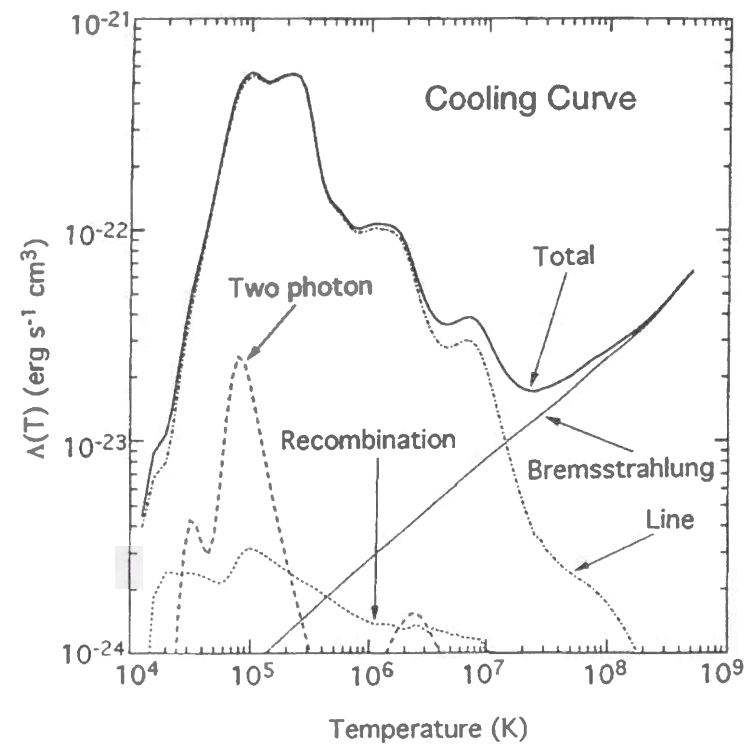


Figure 2.3: The temperature dependence of the cooling function and its components for an optically thin plasma of the cosmic abundance of Allen (1973) (Gehrels and Williams 1993).

2.3.2 Mass Distribution

We summarize below some theoretical aspects to derive the ICM mass and total gravitating mass from X-ray data.

The King Model (Distribution of Gravitating Matter)

We consider about spherically symmetric mass distribution of isothermal gravitating matter. We assume as follows;

1. Velocity distribution of particles of the gravitating matter is isotropic and independent of position.
2. The radial velocity distribution has a Gaussian profile, and the velocity dispersion is independent of position (i.e. isothermal).
3. The particle distribution is stationary.
4. Particle positions are uncorrelated.

Then we can write the particle phase-space density, $f(\vec{r}, \vec{v})$, as

$$f(\vec{r}, \vec{v}) d^3r d^3v = n(R) \times \frac{1}{(2\pi\sigma_r^2)^{3/2}} \exp\left[-\frac{1}{2}\left(\frac{v}{\sigma_r}\right)^2\right] d^3r d^3v, \quad (2.11)$$

where $\vec{r}$ and $\vec{v}$ is position and velocity, R is the three dimensional radius, σ_r is the radial velocity dispersion, and $n(R)$ is the spatial number density of particles at a distance R from the center.

If the gravitating particle is assumed to be collisionless, the phase space density f is a function of only the integrals of the motion. Because we consider the velocity distribution is isotropic, the integral of the motion cannot be the orbital angular momentum of particles, and can only be the energy per unit mass, ε , which can be expressed as

$$\varepsilon = \frac{v^2}{2} + \phi(R), \quad (2.12)$$

where $\phi(R)$ is the gravitational potential. In this case, we can express $n(R)$ as

$$n(R) = n_0 \exp\left[-\frac{\phi(R)}{\sigma_r^2}\right], \quad (2.13)$$

where n_0 is the central density. Poisson's equation for the gravitational potential is

$$\nabla\phi = 4\pi Gm \int f(\vec{r}, \vec{v}) d^3v, \quad (2.14)$$

where m is the mass per particle. Substituting Eqs. (2.11) and (2.13) for Eq. (2.14), we get

$$\frac{1}{R^2} \frac{d}{dr} \left[R^2 \frac{d\phi}{dR} \right] = 4\pi G \rho_0 \exp \left(-\frac{\phi}{\sigma_r^2} \right), \quad (2.15)$$

where $\rho_0 = n_0 m$. If we define the mass density distribution, $\rho(R)$, as

$$\rho(R) \equiv m \int f(\vec{r}, \vec{v}) d^3v \quad (2.16)$$

$$= \rho_0 \exp \left(-\frac{\phi}{\sigma_r^2} \right), \quad (2.17)$$

Eq. (2.15) becomes

$$\frac{d}{dR} \left(R^2 \frac{d \ln \rho}{dR} \right) = -\frac{4\pi G R^2 \rho}{\sigma_r^2}. \quad (2.18)$$

This differential equation has a solution of $\rho(R) = \sigma_r^2 / 2\pi G R^2$. However, we usually do not use this solution, because this function diverges at $R = 0$. The function of

$$\rho(R) = \rho_0 \left[1 + \left(\frac{R}{R_c} \right)^2 \right]^{-\frac{3}{2}}, \quad R_c \equiv \sqrt{\frac{9\sigma_r^2}{4\pi G \rho_0}} \quad (2.19)$$

was found to be a good approximation to the inner region of the numerical solution of Eq. (2.18) which is obtained with boundary conditions of $\rho(0) = \rho_0$ and $d\rho/dR = 0$ at $R = 0$. R_c is called the core radius. This function was first presented by King (1962) [74] to represent surface density distributions of globular clusters and is called King approximation or King model. In figure 2.4, we show the numerical solution of Eq. (2.18) and the King model. As can be seen from this figure, the King model is not a good approximation beyond $R/R_c \sim 5$.

The crossing time of member galaxies, $t_{cr}(R)$ can be expressed as

$$t_{cr}(R) = \frac{R}{\sigma_r} \sim 1 \times 10^9 \text{ yr} \left[\frac{R}{1 \text{ Mpc}} \right] \left[\frac{\sigma_r}{1000 \text{ km/sec}} \right]^{-1}. \quad (2.20)$$

The two body gravitational interaction time scale, t_{gr} , is estimated to be larger than 3×10^{11} years (Sarazin 1986 [116], p20). Because $t_{cr} \ll t_{gr}$, the member galaxies can be considered to be a collisionless gas. Real distribution of member galaxies in a relaxed cluster can be fitted with the King model with $R_c \sim 250$ kpc.

The β Model (Distribution of the ICM)

The sound speed in plasma which consist of hydrogen, c_s , can be expressed as

$$c_s = \sqrt{\frac{2\gamma k T_g}{m_p}} = 1.7 \times 10^8 \text{ cm/s} \left[\frac{T_g}{10^8 \text{ K}} \right]^{\frac{1}{2}}, \quad (2.21)$$

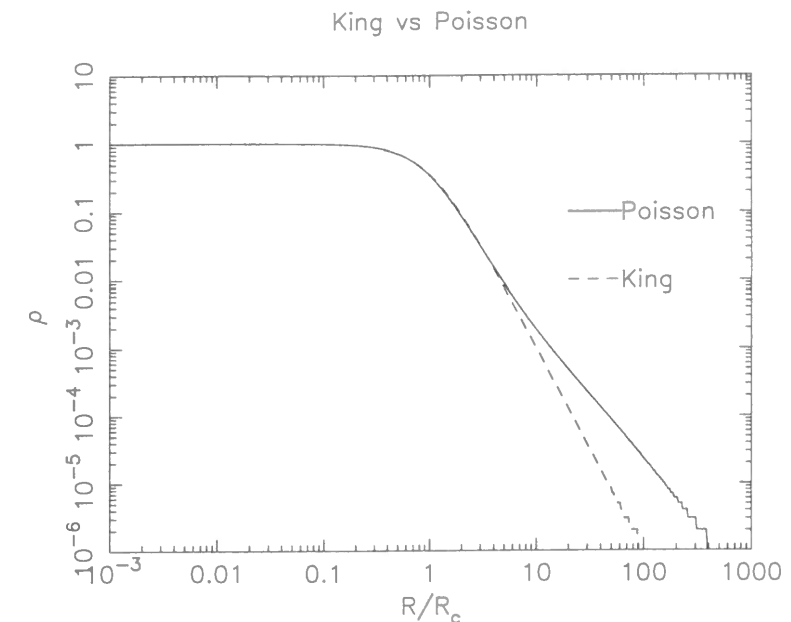


Figure 2.4: Numerical solution of Poisson's equation (solid line) and the King model (dashed line).

where γ is the ratio of specific heats (Spitzer 1962 [124], p58). Then the sound crossing time of the ICM, t_s , is given by

$$t_s \sim 5.8 \times 10^8 \text{ yr} \left[\frac{T_g}{10^8 \text{ K}} \right]^{-\frac{1}{2}} \left[\frac{D}{1 \text{ Mpc}} \right], \quad (2.22)$$

where D is the cluster diameter. The cooling time due to the free-free emission, t_{cool} , is

$$t_{cool} = 8.5 \times 10^{10} \text{ yr} \left[\frac{n_p}{10^{-3} \text{ cm}^{-3}} \right]^{-1} \left[\frac{T_g}{10^8 \text{ K}} \right]^{\frac{1}{2}}. \quad (2.23)$$

If we consider the heating of the ICM due to infall of the primordial gas into the cluster and compression, the heating time scale, t_{heat} , is equal to the free-fall time scale, and is given by

$$t_{heat} = 3.1 \times 10^9 \text{ yr} \left[\frac{D}{1 \text{ Mpc}} \right]^{\frac{3}{2}} \left[\frac{M}{10^{14} M_\odot} \right]^{-\frac{1}{2}}, \quad (2.24)$$

where M is the total mass of the cluster. Because t_s is less than the Hubble time ($\sim 10^{10}$ yr), t_{cool} and t_{heat} , the ICM can be considered to be hydrostatic:

$$\nabla P = -\rho_g \nabla \phi(R), \quad (2.25)$$

where P is the gas pressure and ρ_g is the gas mass density, which can be expressed as

$$\rho_g = n_e m_e + n_p m_p \equiv n_g \mu m_p, \quad (2.26)$$

where m_e and m_p are the masses of electron and proton, $n_g \equiv n_p + n_e$ is the gas number density, and μ is mean molecular weight. We assume $\mu = 0.6$ in this thesis. Because of the low density and high temperature, the ICM can be treated as an ideal gas, and the equation of state is given by

$$P = n_g k T_g = \frac{\rho_g k T_g}{\mu m_p}. \quad (2.27)$$

Eq. (2.25) reduces to

$$\frac{1}{\rho_g} \frac{dP}{dR} = -\frac{d\phi(R)}{dR} = -G \frac{M(< R)}{R^2}, \quad (2.28)$$

where $M(< R)$ is the total mass of the cluster within a radius R .

If we assume that the cluster gravitational potential is that of a self-gravitating isothermal sphere, we can use the King model as the mass density profile of the gravitating matter, approximately. Therefore the mass density, total cluster mass, and gravitational potential are given by

$$\rho(R) = \rho_0 (1 + x^2)^{-\frac{3}{2}} \quad (2.29)$$

$$M(< R) = 4\pi \rho_0 R_c^3 \left(\ln[x + \sqrt{1 + x^2}] - \frac{x}{\sqrt{1 + x^2}} \right) \quad (2.30)$$

$$\phi(R) = -4\pi G \rho_0 R_c^2 \frac{\ln[x + \sqrt{1 + x^2}]}{x}, \quad (2.31)$$

where $x \equiv R/R_c$. Using Eq. (2.19),

$$\sigma_r^2 = \frac{4\pi G \rho_0 R_c^2}{9} = -\frac{\phi(0)}{9}. \quad (2.32)$$

Then we consider the situation that the ICM is bounded by the gravitational potential given by equation (2.31). Substituting the equation of state (2.27) for Eq. (2.28), we get

$$\frac{d \ln \rho_g}{dR} = -\frac{\mu m_p}{k T_g} \frac{d\phi(R)}{dR}. \quad (2.33)$$

Integrating Eq. (2.33), we get

$$\rho_g(R) = \rho_{g0} \exp \left(-\frac{\mu m_p}{k T_g} [\phi(R) - \phi(0)] \right), \quad (2.34)$$

where ρ_{g0} is the central mass density of the ICM.

Substituting Eq. (2.31) for Eq. (2.34), $\rho_g(R)$ can be approximately expressed only at small radii ($R \lesssim 6R_c$) as

$$\rho_g(R) = \rho_{g0} \left[1 + \left(\frac{R}{R_c} \right)^2 \right]^{-\frac{3}{2}\beta} \quad (2.35)$$

$$\beta \equiv \frac{\mu m_p \sigma_r^2}{k T_g} = 0.73 \left[\frac{\sigma_r}{1000 \text{ km/s}} \right]^2 \left[\frac{T_g}{10^8 \text{ K}} \right]^{-1}. \quad (2.36)$$

β is the ratio of the kinematic energy of the gravitating matter per unit mass to the thermal energy of the ICM per unit mass. Equation (2.35) is called the β model. We show Eq. (2.34) and the beta model in figure 2.5. Note that the beta model is not a good approximation of Eq. (2.34) beyond $R \sim 6R_c$.

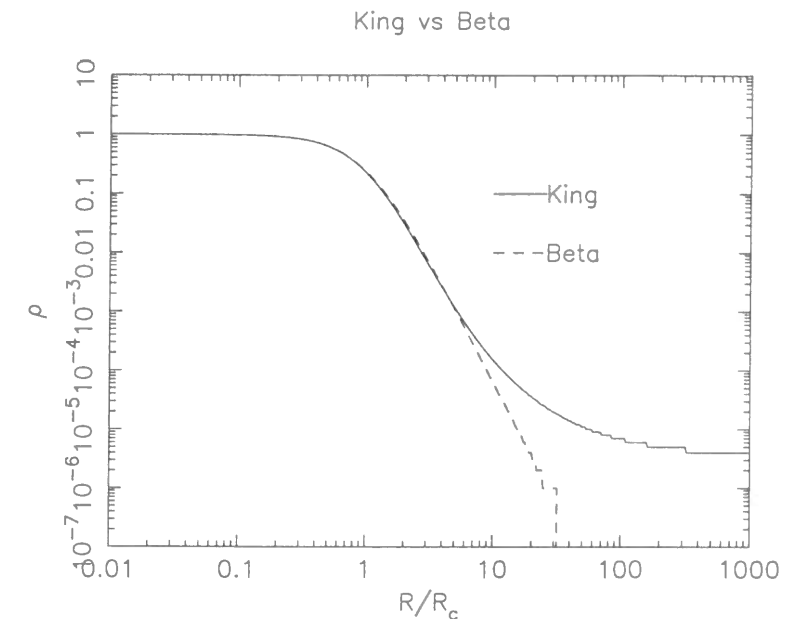


Figure 2.5: Distribution of the ICM.

Solid line shows Eq. (2.34), while dashed line shows the β model.

X-ray Surface Brightness Distribution

The X-ray surface brightness at a projected radius r is proportional to the emission measure, EM , defined as

$$EM \equiv \int n_e n_p dl, \quad (2.37)$$

where l is the distance along the line-of-sight through the cluster at a projected radius r . If we use the β model as the distribution of the ICM, the emission measure is,

$$EM = \sqrt{\pi} \left(\frac{n_{e0}}{n_{p0}} \right) n_{p0}^2 R_c \frac{\Gamma(3\beta - 1/2)}{\Gamma(3\beta)} \left[1 + \left(\frac{r}{R_c} \right)^2 \right]^{-3\beta + \frac{1}{2}} \quad \left(\beta > \frac{1}{6} \right), \quad (2.38)$$

where Γ is the gamma function and n_{p0} and n_{e0} are the central number densities of proton and electron. Therefore the X-ray surface brightness, $S(r)$, can be expressed as

$$S(r) = S_0 \left[1 + \left(\frac{r}{R_c} \right)^2 \right]^{-3\beta + \frac{1}{2}}, \quad (2.39)$$

where S_0 is the central surface brightness density. The average value of β determined by fits to the X-ray surface brightness of a large number of clusters was found to be

$$\beta_{fit} \sim 0.65 \quad (2.40)$$

(Jones and Forman 1984 [70]).

Another way to estimate β is to use Eq. (2.36) assuming the distribution of the member galaxies, ρ_{gal} , is proportional to that of the gravitating matter, which means

$$\rho_g \propto \rho_{gal}^\beta. \quad (2.41)$$

In this case, the velocity dispersion of the member galaxies can be considered to be the same as that of the gravitating matter. Substituting the velocity dispersion of the galaxies and the gas temperature deduced from the X-ray spectrum for Eq. (2.36), the average value of β is

$$\beta_{spec} \sim 1.2 \sim 2 \times \beta_{fit} \quad (2.42)$$

(Sarazin 1986 [116]). This discrepancy between β_{spec} and β_{fit} is called the β problem. Many suggestions have been made as to the origin of this discrepancy (eg. Kent and Sargent 1983 [72]; Mushotzky 1984 [101]; Henriksen and Mushotzky 1985 [60]; Bahcall and Lubin 1994 [9]). For example, this discrepancy may suggest that the velocity dispersion of the galaxies are not the same as that of the gravitating matter (Metzler and Evrard [93]).

It is important to know that both the King and β models are not good approximations beyond five times the core radius (figures 2.4 and 2.5). Therefore we have to pay attention to adopt the β profile to the whole region of the cluster.

Total Gravitating Mass

From Eq. (2.28), the total gravitating matter within a radius R can be expressed as

$$\begin{aligned} M(< R) &= -\frac{kT_g R^2}{\mu m_p G} \frac{d \ln(n_g T_g)}{dR} \\ &= -\frac{kT_g R}{\mu m_p G} \left(\frac{d \ln T_g}{d \ln R} + \frac{d \ln n_g}{d \ln R} \right) \end{aligned} \quad (2.43)$$

Therefore measurements of the gas density distribution and the temperature distribution are the key to estimate the mass of the total gravitating matter.

2.3.3 Simple Model for Cluster Evolution

We consider two simple models for evolution of the clusters of galaxies: (a) the spherical cluster containing fixed mass of gas and dark matter contracts. (b) gas and dark matter falls into the cluster with fixed radius R . The schematic view of them are shown in figure 2.6. In both cases, we assume that the gas mass is proportional to the total mass of the cluster, M .

In these cases, since $T_g \propto GM/R$, $V \propto R^3$, and $n_p \sim n_e \propto M/R^3$, Eq. (2.10) reduces to

$$L \propto \left(\frac{M}{R^3}\right)^2 R^3 \left(\frac{M}{R}\right)^{\frac{1}{2}} = M^{\frac{5}{2}} R^{-\frac{7}{2}}. \quad (2.44)$$

Eliminating R from Eq. (2.44), we get

$$L \propto T_g^{3.5} \quad (2.45)$$

for the case of (a). For the case of (b), eliminating M from Eq. (2.44), we get

$$L \propto T_g^{2.5}. \quad (2.46)$$

The real evolution is probably the intermediate between (a) and (b). Therefore the relation of $L \propto T^\alpha$ with $\alpha = 2.5 - 3.5$ is expected. Though our model is too simple, this expected value is consistent with the observation. Therefore the observed relation of $L \propto T_g^3$ can be considered to be the evidence of the evolution of clusters of galaxies.

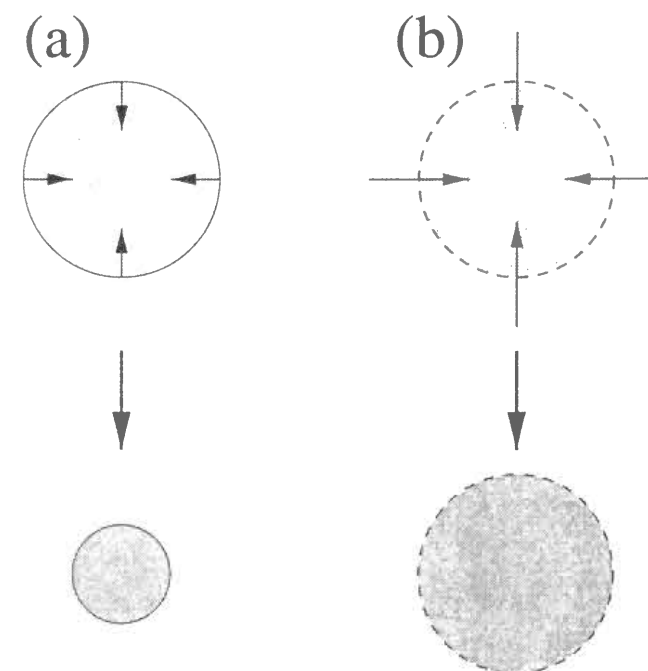


Figure 2.6: Schematic view of the simple models for the cluster evolution. (a) the total mass of the cluster is fixed. (b) the radius of the cluster is fixed.

Chapter 4

Review of the Virgo Cluster of Galaxies

4.1 Optical Properties

The Virgo cluster is the closest and best-studied cluster of galaxies, lying at a distance of approximately 15 Mpc. Cosmographically, the Virgo cluster is the nucleus of the Local Supercluster of galaxies, in whose outskirts we are situated. We can observe large numbers of galaxies of all types and luminosities in great detail in the Virgo cluster. Therefore this cluster is an ideal laboratory for the study of the systematic properties of galaxies and a fundamental stepping stone for the cosmological distance scale. Thus the Virgo cluster has been, and still is, one of the most important object for extragalactic astronomy.

We show the map of the Virgo cluster in figure 4.1. The cluster covers a large, roughly circular sky area of approximately 10° diameter. The Virgo cluster is a fairly poor, loosely concentrated, irregularly shaped cluster of galaxies. Binggeli, Sandage, and Tammann (1985) [12] cataloged 2096 galaxies and found 1277 of the cataloged galaxies are considered to be members of the Virgo cluster, and 574 to be possible members. Table 4.1 shows the number of known member galaxies. An abundance of spiral galaxies among the bright cluster members is high. This property can be seen in many clusters. Rich, dense, regularly shaped clusters whose member galaxies are dominated by E and S0 galaxies are much rarer. However, since the Virgo is the most nearest cluster, we can map it to an unsurpassed level of depth. Therefore the Virgo cluster is the richest cluster of galaxies in terms of the number of known member galaxies. As table 4.1 shows, dwarf galaxies, particularly dwarf ellipticals, numerically the cluster population.

Table 4.1: Known member galaxies if the Virgo cluster (Binggeli 1992)

Morphological Type	Number
Elliptical	30
S0	49
Spiral	128
Dwarf elliptical	828
Dwarf S0	30
Dwarf irregular	89
Dwarf irregular/elliptical	89
Other	34
Total	1277

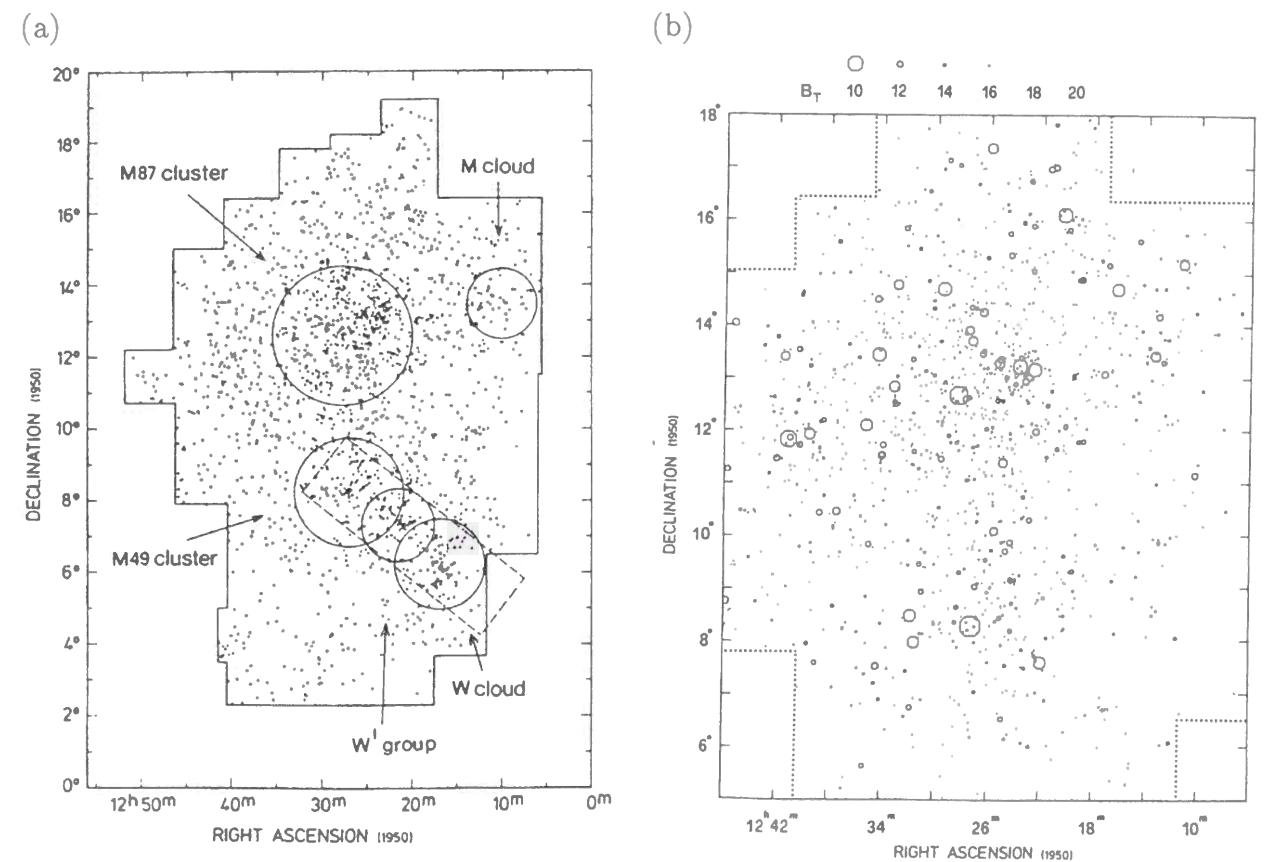


Figure 4.1: Plot of all members and possible members in the Virgo cluster: (a) Dots show the galaxies. Five main concentrations indicated by circles, are evident; (b) Luminosity-weighted map of the Virgo cluster. The symbol size (area) is proportional to the luminosity of the galaxy (Binggeli, Tammann, and Sandage, 1987).

Though the subcluster B has a lower velocity dispersion ($\sigma_r \sim 390$ km/s) than the subcluster A ($\sigma_r \sim 760$ km/s), the temperature is higher at the subcluster B, which is inconsistent with a general tendency that clusters with larger velocity dispersions have higher gas temperatures (eg. Hatsukade 1989 [57]). This may suggest that the Virgo cluster is not a dynamically relaxed system. The physical parameters are summarized in table 4.2.

Table 4.2: Physical parameters of the subcluster A and B.

	A (M87 cluster)	B (M49 cluster)
Temperature	2.2 keV	3.4 keV
$L_X^\dagger$	3×10^{43} erg/s	4×10^{42} erg/s
Gas Mass	$2 \times 10^{13} M_\odot$	$5 \times 10^{12} M_\odot$

† : X-ray luminosity in the 2 – 10 keV band.

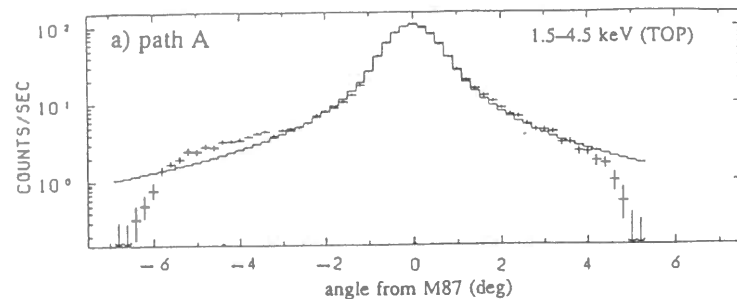


Figure 4.2: X-ray surface brightness obtained with Ginga (Takano 1990). The solid line denotes the expected profile by extrapolating the X-ray surface brightness distribution measured with the Einstein observation (Fabricant and Gorenstein (1983)).

One of the most important results of the Ginga observation is that an iron abundance rise towards the center of the Virgo cluster which is shown in figure 4.4 (Koyama, Takano, and Tawara 1991 [75]; Takano 1990 [128]). The iron abundance is at least about half the cosmic value in the innermost region of the subcluster A and significantly decreases outwards.

The Virgo region was observed with ROSAT during the ROSAT all-sky survey between November 1990 and January 1991, and the results have been already published by Böhringer et al. (1994) [16]. Figure 4.5 (a) and (b) show contour maps of the X-ray surface brightness of the Virgo cluster in a hard (0.4 – 2.4 keV) and soft (0.1 – 0.4 keV) band, respectively. The X-ray morphology is very similar to the structure in the galaxy distribution (Binggeli, Sandage, and

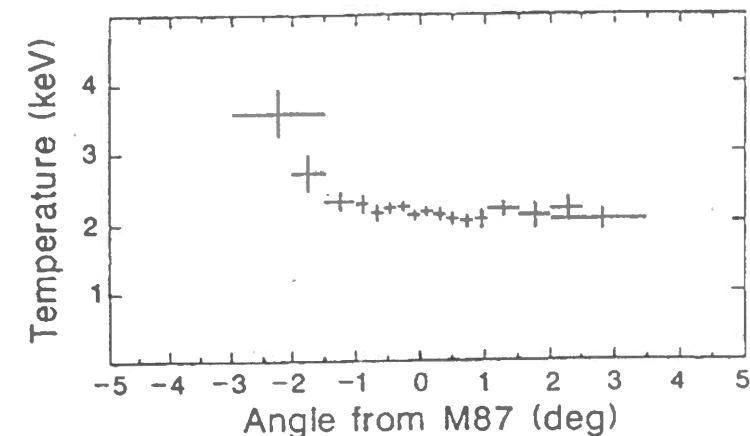


Figure 4.3: ICM temperature distribution obtained with Ginga (Koyama, Takano, and Tawara 1991).

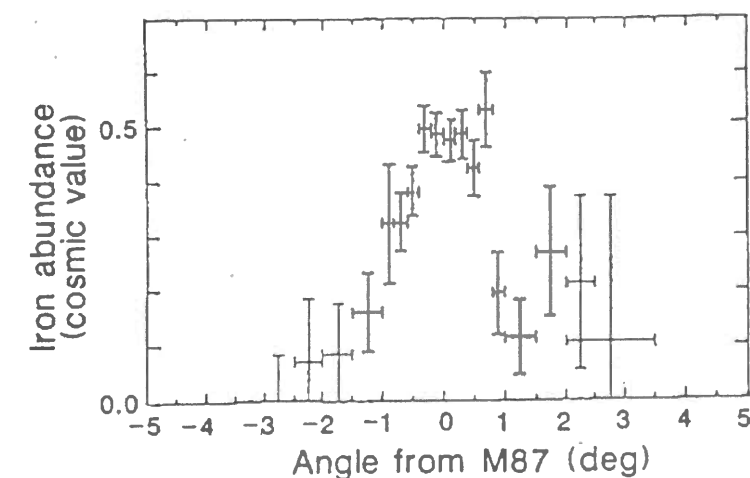


Figure 4.4: Iron abundance distribution obtained with Ginga (Koyama, Takano, and Tawara 1991).

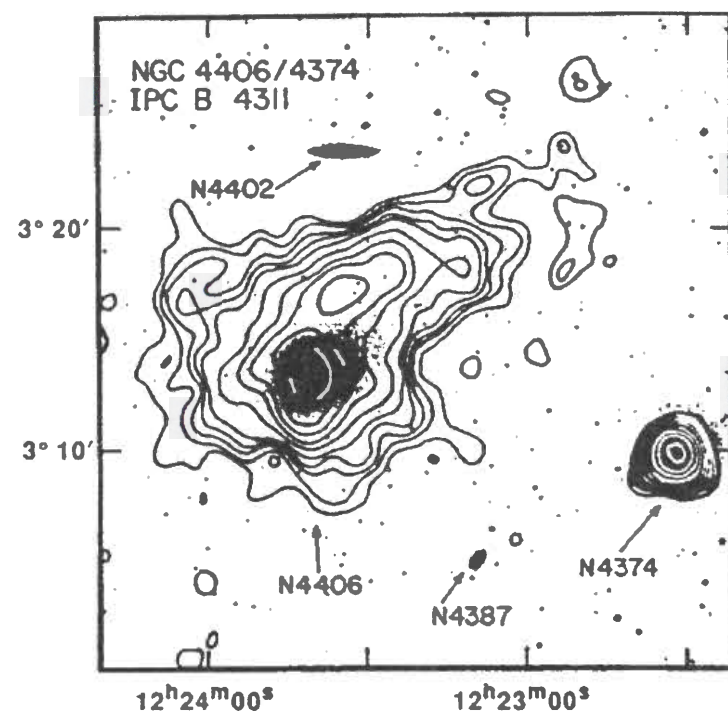


Figure 4.7: X-ray image of M86 (NGC4406) obtained with the Einstein IPC (Fabbiano, Kim and Trinchieri (1992)).

A4038 (Bowyer, Lieu, and Mittaz 1997 [18]) were also found to have the EUV emission. The emission cannot be explained by the well-known cluster gas at X-ray temperatures. Though its origin is not clear so far, Sarazin and Lieu (1997) [118] suggest that the EUV emission is inverse Compton scattering of cosmic microwave background radiation by low energy cosmic ray electrons in the ICM.

Table 6.2: The result of the thermal bremsstrahlung and narrow line model fitting to the GIS spectra.*

Radius	0'-2'	2'-4'	4'-6'	6'-8'	8'-10'	0'-10'	Identify
Brems kT (keV)	2.05 (1.90-2.21)	2.38 (2.23-2.55)	2.42 (2.26-2.58)	2.54 (2.37-2.73)	2.47 (2.28-2.68)	2.31 (2.24-2.39)	
$\chi^2/d.o.f.$	163.8/128	173.2/176	193.4/185	150.8/178	196.8/164	404.3/356	
Center (keV)	6.64 (6.59-6.69)	6.69 (6.63-6.74)	6.63 (6.57-6.69)	6.60 (6.55-6.65)	6.60 (6.54-6.67)	6.63 (6.60-6.65)	Fe xxv
Flux ($10^{-4}\text{ph cm}^{-2} \text{s}^{-1}$)	1.05 (0.86-1.23)	0.83 (0.67-1.00)	0.78 (0.62-0.94)	0.81 (0.66-0.97)	0.59 (0.45-0.74)	4.20 (3.77-4.64)	
Equivalent Width (eV)	1415 (1098-1777)	807 (617-1015)	733 (562-929)	834 (652-1031)	712 (517-926)	944 (825-1074)	
Center (keV)	7.82(fix)	7.82(fix)	7.82(fix)	7.82(fix)	7.82(fix)	7.82 (7.75-7.90)	Fe xxv and Ni xxvii
Flux ($10^{-4}\text{ph cm}^{-2} \text{s}^{-1}$)	0.30 (0.16-0.45)	0.27 (0.13-0.41)	0.30 (0.16-0.44)	0.13 (0.01-0.25)	0.16 (0.03-0.28)	1.10 (0.83-1.39)	
Equivalent Width (eV)	897 (432-1438)	521 (242-835)	580 (295-895)	276 (24-553)	388 (79-736)	527 (382-681)	

* The errors in the brackets are at 90% confidence level.

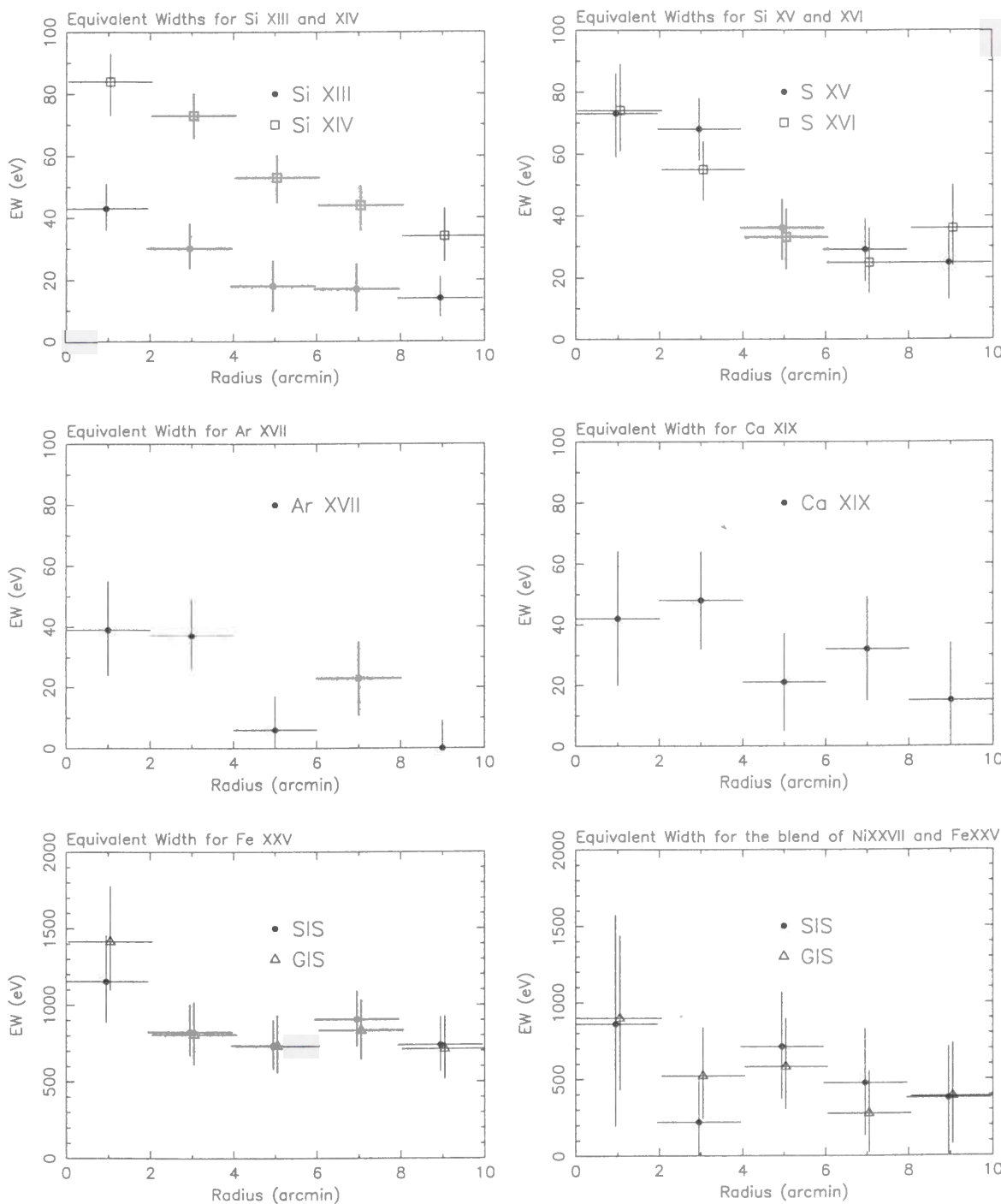


Figure 6.5: Equivalent width of emission lines plotted as a function of radius from the center of M87.

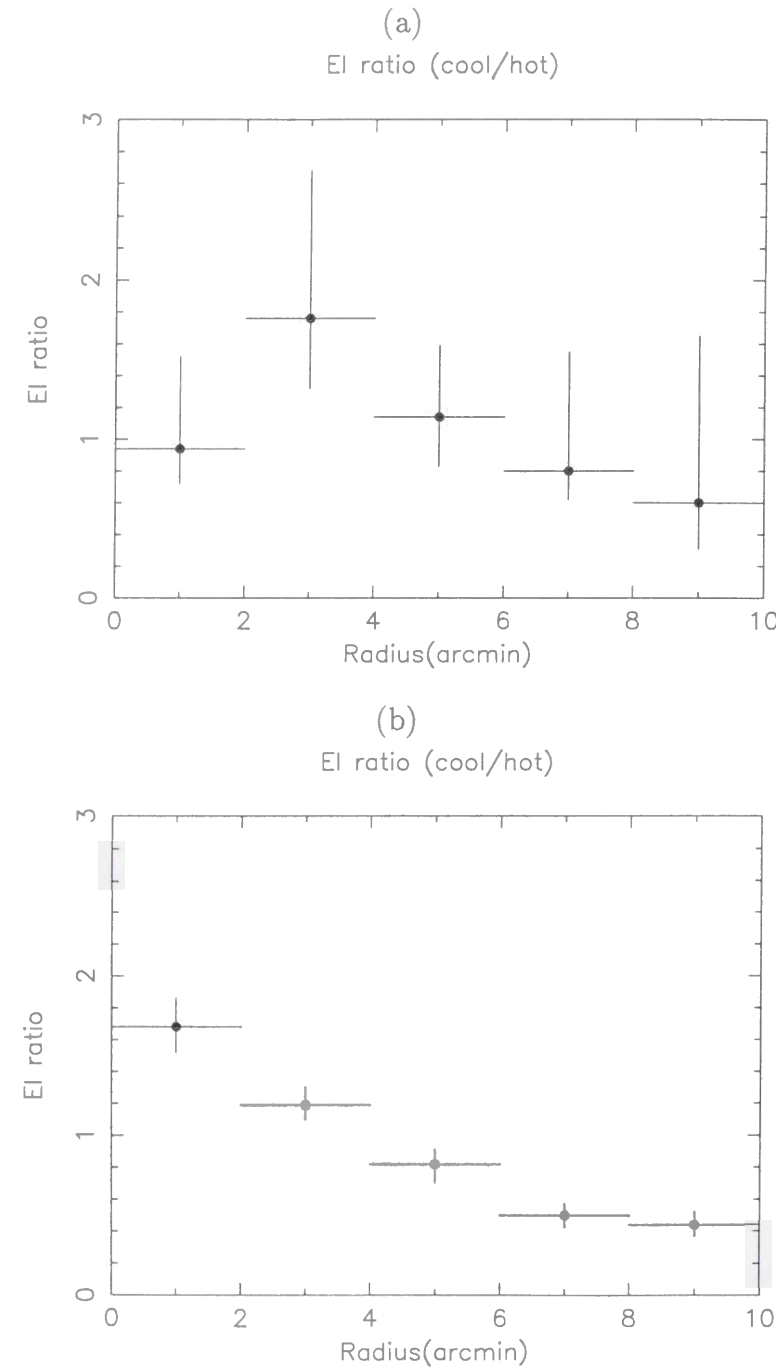


Figure 6.8: Ratio of emission integral of the cool component to that of the hot component plotted as a function of the radius from the center of M87: (a) both temperatures of the hot and cool components are free parameters, (b) temperature of the hot component is fixed to be 2.9 keV.

Table 6.5: The results of the two-temperature RS model fitting. The temperature of the hot component is fixed to 2.9 keV.*

Radius	0'-2'	2'-4'	4'-6'	6'-8'	8'-10'
$N_H(\text{SIS})$ (10^{20} cm^{-2})	5.95 (5.39-6.52)	6.45 (6.02-6.89)	6.17 (5.71-6.63)	4.99 (4.49-5.49)	5.35 (4.77-5.93)
$N_H(\text{GIS})$ (10^{20} cm^{-2})	3.48 (1.97-5.02)	3.18 (1.72-4.39)	2.25 (0.85-3.65)	0.51 (<2.07)	2.80 (0.29-3.83)
$kT_1(\text{keV})$	1.25 (1.23-1.27)	1.33 (1.31-1.34)	1.39 (1.36-1.41)	1.42 (1.39-1.47)	1.40 (1.34-1.44)
$kT_2(\text{keV})$	2.9(fix)	2.9(fix)	2.9(fix)	2.9(fix)	2.9(fix)
Abundance (Solar)					
O	0.29 (0.21-0.39)	0.38 (0.29-0.46)	0.46 (0.36-0.56)	0.40 (0.29-0.52)	0.31 (0.18-0.45)
Mg	0.00 (<0.01)	0.00 (<0.01)	0.00 (<0.03)	0.00 (<0.04)	0.00 (<0.13)
Si	0.71 (0.65-0.77)	0.72 (0.67-0.77)	0.63 (0.58-0.69)	0.65 (0.58-0.73)	0.48 (0.41-0.57)
S	0.72 (0.64-0.80)	0.69 (0.62-0.76)	0.50 (0.43-0.57)	0.50 (0.41-0.58)	0.43 (0.33-0.52)
Ar	0.65 (0.42-0.88)	0.68 (0.49-0.87)	0.29 (0.10-0.48)	0.46 (0.23-0.68)	0.32 (0.07-0.57)
Ca	0.97 (0.61-1.33)	0.87 (0.60-1.15)	0.33 (0.06-0.60)	0.50 (0.20-0.80)	0.36 (0.03-0.69)
Fe	0.52 (0.49-0.55)	0.48 (0.45-0.50)	0.39 (0.36-0.41)	0.37 (0.35-0.40)	0.31 (0.28-0.33)
$\text{EI}(\text{SIS})^\S$ (10^{64} cm^{-3})	5.84 (5.52-6.16)	8.91 (8.55-9.27)	8.40 (8.06-8.74)	8.02 (7.69-8.35)	6.69 (6.38-7.04)
$\text{EI}(\text{GIS})^\S$ (10^{64} cm^{-3})	6.28 (5.94-6.61)	7.78 (7.47-8.09)	8.57 (8.23-8.92)	7.96 (7.64-8.27)	7.51 (7.17-7.85)
$\text{EI ratio}^\ddagger$ (low- kT /high- kT)	1.68 (1.52-1.86)	1.19 (1.10-1.30)	0.82 (0.71-0.91)	0.50 (0.43-0.57)	0.44 (0.37-0.52)
Cool Component					
$\text{Fx}(10^{-11} \text{ erg/s/cm}^2)^\dagger$					
SIS	3.07	3.29	2.02	1.19	0.83
GIS	3.47	3.07	2.23	1.29	0.96
$\text{Lx}(10^{41} \text{ erg/s})^{\dagger\dagger}$					
SIS	9.32	10.05	6.16	3.52	2.41
GIS	10.03	8.79	6.29	3.50	2.70
Hot Component					
$\text{Fx}(10^{-11} \text{ erg/s/cm}^2)^\dagger$					
SIS	2.42	3.66	3.39	3.26	2.61
GIS	2.68	3.34	3.64	3.45	3.06
$\text{Lx}(10^{41} \text{ erg/s})^{\dagger\dagger}$					
SIS	7.02	10.71	9.88	9.37	7.55
GIS	7.54	9.36	10.09	9.31	8.47
$\chi^2/\text{d.o.f.}$	1020/628	1131/715	974.1/725	858.9/711	852.7/681

* The errors in the brackets are at 90% confidence level.

$\S$ EI is Emission Integral of hot component.

$\ddagger$ Ratio of EI of cool component to that of hot component.

$\dagger$ X-ray flux in the 0.5 - 10 keV band from each annulus.

$\dagger\dagger$ X-ray luminosity in the 0.5 - 10 keV band from each annulus.

the errors are relatively large. There is no evidence of a gradient of S/Fe or Si/S over the entire image, and the observed Si/Fe ratio is similar to that found in clusters of galaxies (Mushotzky et al. 1996 [105]).

The obvious spectral distinctions between the “cluster gas” and the gas associated with M87 is the rise in the absolute abundance and the increasing prominence of a cooler spectral component.

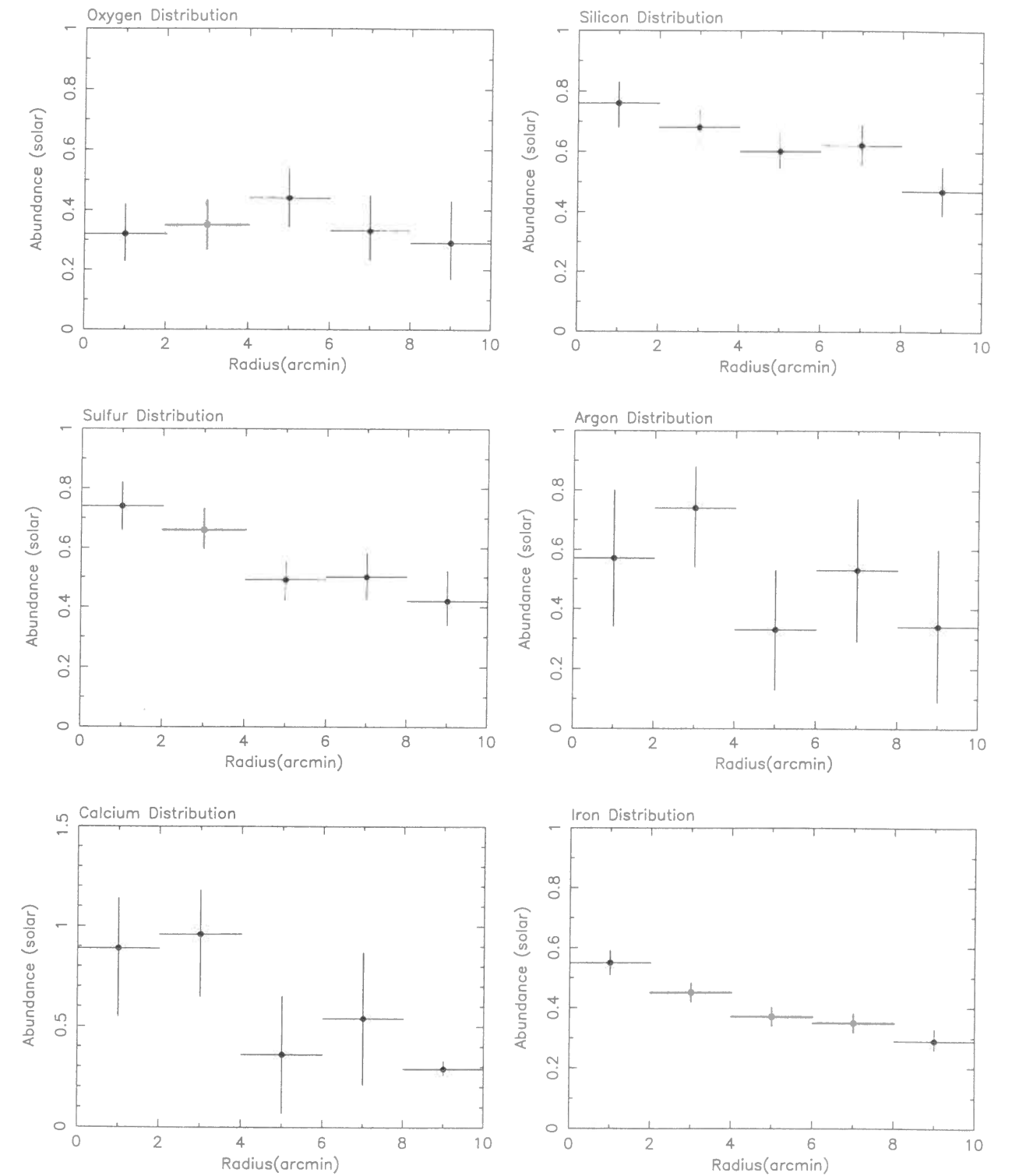


Figure 6.9: Abundance distribution of O, Si, S, Ar, Ca, and Fe. In this analysis, the temperature of each component is a free parameter.

We think the reason for this failure is that the cflow model is too simple; 1) the cflow model assumes that all of the cooling flow is within the beam of the spectrometer. Since the nominal cooling radius is larger than $10'$ (Stewart et al. 1984 [125]), this is an important effect for an analysis of the M87 data; 2) the cflow model does not take into account of a “dropping out” of mass with radius; 3) the cflow model does not include the abundance gradient; 4) the cflow model assumes that the pressure of the plasma is constant. Therefore we do not discuss about this result any further.

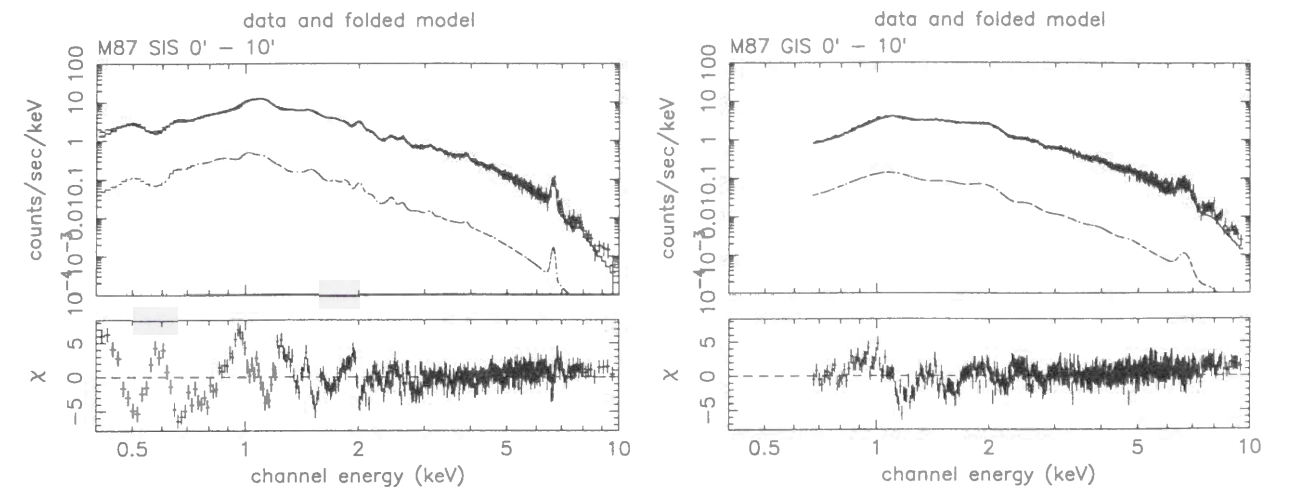


Figure 6.11: The ASCA spectrum of M87 in the $0'-10'$ region. The solid line shows the best-fitting cooling flow plus additional thermal plasma model.

Table 6.6: Results of the cflow model fitting

$N_H(\text{SIS})$ (cm^{-2})	$(6.1 \pm 0.3) \times 10^{20}$
$N_H(\text{GIS})$ (cm^{-2})	$(2.4 \pm 0.7) \times 10^{20}$
$kT_{\min}$ (keV)	0.1(fix)
$kT_{\max}$ (keV)	2.1 ± 0.01
Abundance (solar)	
O	0.68 ± 0.05
Mg	$0(<0.06)$
Si	0.69 ± 0.03
S	0.57 ± 0.04
Ar	0.40 ± 0.10
Ca	0.71 ± 0.13
Fe	0.48 ± 0.01
$\dot{M}$ (SIS) ($M_\odot/\text{yr}$)	1.0 ± 0.3
$\dot{M}$ (GIS) ($M_\odot/\text{yr}$)	1.2 ± 0.3
norm ratio [†]	0.3 ± 0.1
$\chi^2/d.o.f.$	2579/1006

The errors are at 90% confidence level.

$$\dagger \text{norm ratio} = \frac{\text{norm of additional thermal plasma model}}{\text{norm of cflow model}}$$

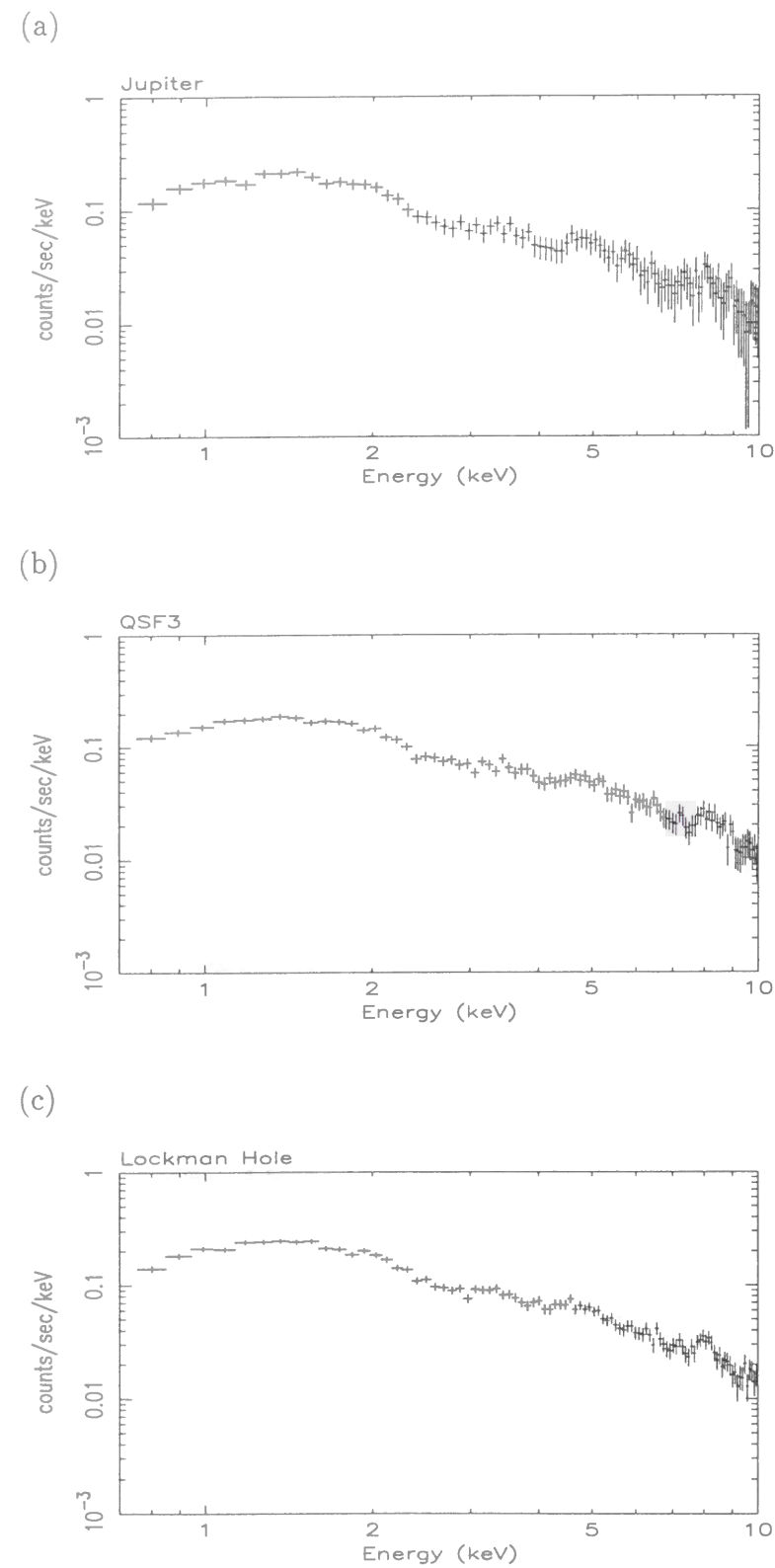


Figure 7.3: GIS spectra used as a background; (a) Jupiter, (b) QSF3, and (c) Lockman Hole.

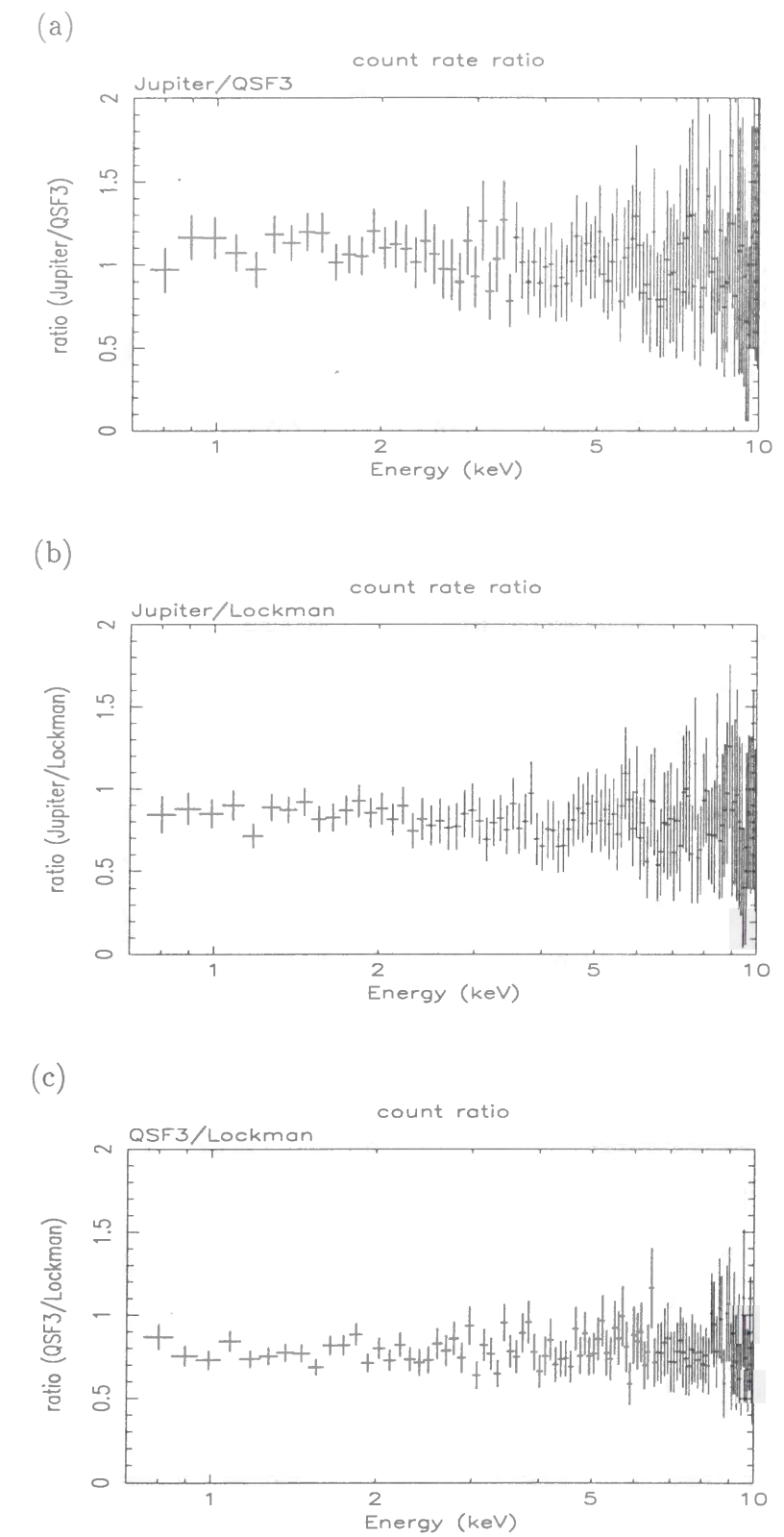


Figure 7.4: Ratio of count rate between Jupiter, QSF3, and Lockman Hole; (a) Jupiter/QSF3, (b) Jupiter/Lockman Hole, and (c) QSF3/Lockman Hole.

Appendix A

ASCA spectra of M87

A.1 The spatially resolved ASCA spectra of M87

We show the spatially resolved X-ray spectra of M87 taken with the SIS and GIS. The background spectrum is subtracted from each spectrum.

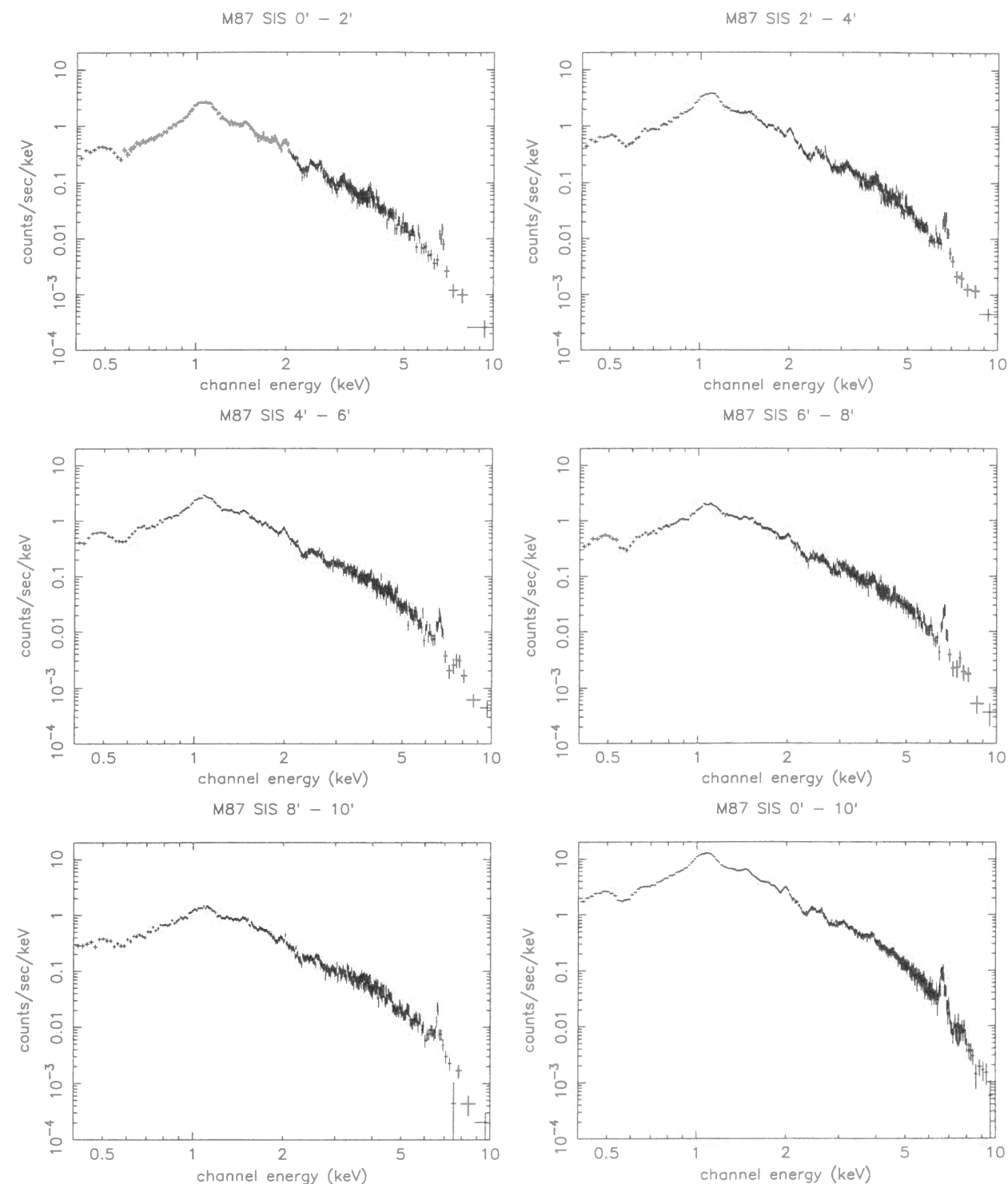


Figure A.1: The SIS spectra of M87 taken from different annular regions of the radius 0'–2', 2'–4', 4'–6', 6'–8', 8'–10', and 0'–10'.

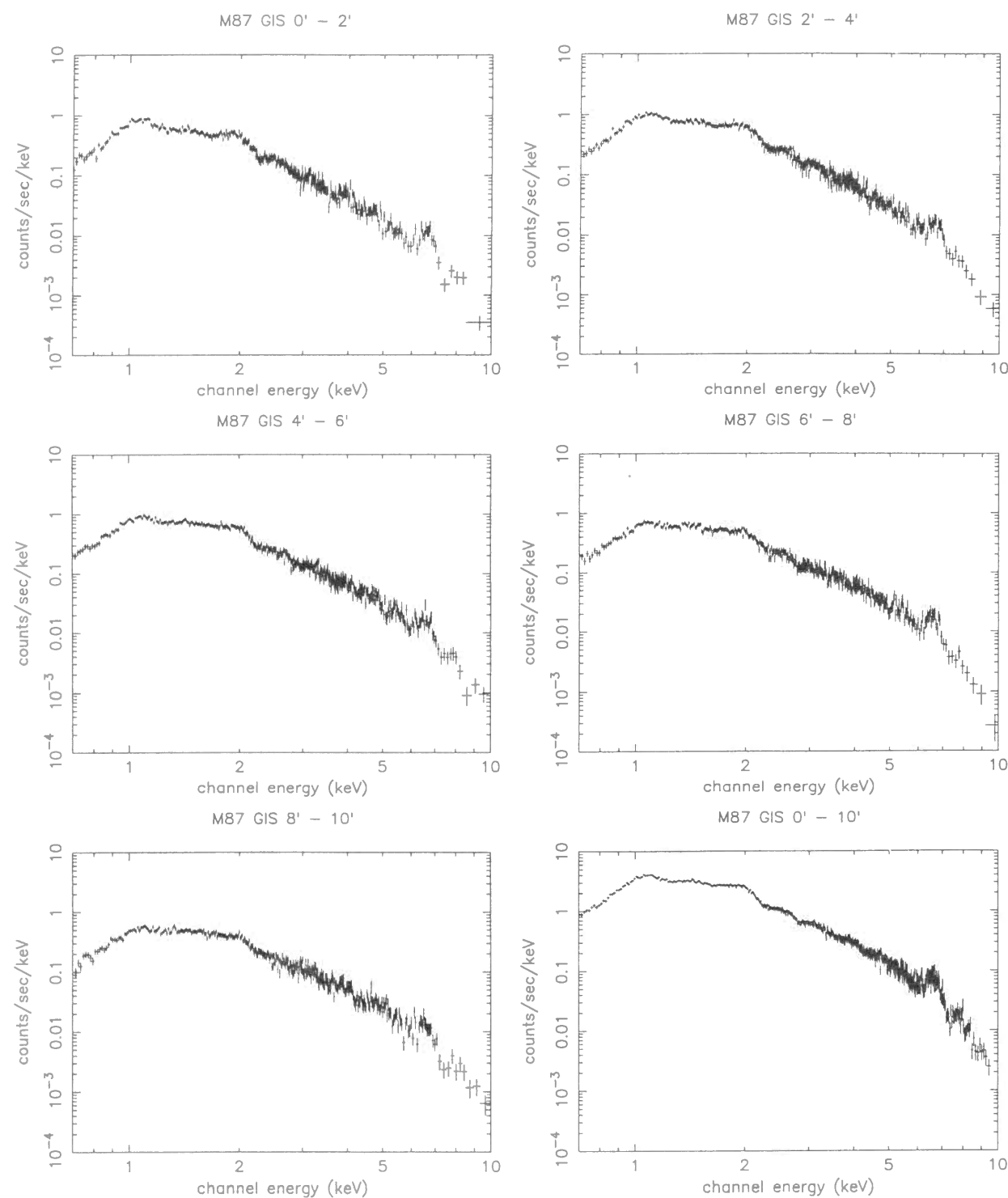


Figure A.2: The GIS spectra of M87 taken from different annular regions of the radius 0'–2', 2'–4', 4'–6', 6'–8', 8'–10', and 0'–10'.

A.2 The bremsstrahlung plus Gaussian lines model fitting

We fitted the SIS (1.6 – 10 keV) and GIS (3.0 – 10 keV) spectra of M87 with the thermal bremsstrahlung continuum and Gaussian lines model. We show the best-fit model and its residuals in figure A.3 and A.4.

