

1 Modeling the shearing behavior of discontinuous rock mass incorporating dilation of joint aperture

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Abstract

The shearing characteristics of rock joints govern the mechanical performance of discontinuous rock masses. The present study investigated the normal compression and shear behavior of rock joints through cyclic compression tests and direct shear tests. The irreversible relationship between the normal stress and the normal closure was confirmed by cyclic compression tests on rock joints. An elastoplastic model was proposed incorporating the aperture variation. A modified version of the critical state framework was developed for modeling the shearing and dilation behavior. Specifically, the initial state of the rock joints was determined according to the stress history. The proposed model for the mechanical behavior of rock joints was validated by predicting the experimental results. A parameter analysis was also performed to highlight the difference in the shear behavior of the rock joints due to the difference in the initial apertures.

Keywords: Discontinuous rock mass, shearing behavior, joint aperture, dilation, elastoplastic, critical state theory

1 Introduction

The mechanical performance of rock masses is an overwhelmingly important research topic for the design and construction of deep underground structures, such as geological repositories for nuclear waste, underground storage facilities for resources and geothermal production well for heat energy exploitation, because these projects have high safety standards and require long-term stability. Rock joints are critical constituents in discontinuous rock masses, and their properties often govern the mechanical behavior of the fracture materials. Therefore, incorporating the joint features and correctly predicting the shear behavior are of great significance for rock mass stability analyses.

The characteristics of rock joints have been investigated for developing constitutive laws, such as the Barton-Bandies model that considers joint roughness [1], a tangent formulation that considers the dislocated shear displacement [2], the JRC-JMC model that takes account of the matching condition [3], and the Grasselli-Egger model that is based on three-dimensional surface parameters [4]. Moreover, many theories have been applied to construct shear models. Contact theory models were formulated for modeling the shear behavior, which largely depends on the topography characteristics [5, 6]. Plasticity theory models, considering asperity degradation, have been established too [7, 8]. A constitutive model, considering the specific volume of soft rock, has also been developed based on the extended critical state theory [9]. The effect of joint planes on the strength and structure of soft rock has been investigated, and

one bounding surface plasticity model was proposed [10, 11]. However, the joint aperture has not been taken into account in the modeling of the shear behavior of discontinuous rock masses despite the sensitivity of the aperture to changes in the applied load and the great influence of the aperture on the shear behavior of rock joints. Thus, the incorporation of the aperture variation is necessary for modeling the shearing behavior of discontinuous rock masses.

The joint aperture, which depends upon the matching properties and surface geometry, controls the maximum deformation of the joints and the mechanical responses of discontinuous rock masses under the normal loading process. A closed joint (e.g., rock with an interlocked joint or well-matched joint) can only cause a slight movement of the joint walls. An open joint (e.g., rock with a mismatched joint or degraded asperities) allows for a considerable amount of normal displacement of the upper half of the specimen, as the joint tends to approach the complete state [3, 12, 13]. Simultaneously, the normal stiffness is substantially larger for a perfectly matched joint with a small joint aperture than an unmatched joint with a large joint aperture [3, 12, 14, 15]. In addition, the matched and unmatched types of rock joints with different apertures both demonstrated the plastic behavior of the initial loading cycles and the elastic behavior of the subsequent loading cycles in the extensive results obtained from cyclic compressive experiments [14–20]. Hence, based on the distinct effects and the variation in joint aperture, the evolution of each aperture under cyclic normal stress needs to be carefully considered.

The initial aperture response to the matching properties of the joint walls governs the peak shear strength and dilation movement during the shear process. A smaller initial aperture usually indicates that the rock joint has a mated interface. A higher peak shear stress is then required to shave the contact asperities on the matched joint surfaces. In contrast, a larger initial aperture indicates an unmated interface. The rock joint has relatively lower peak shear strength due to the loosely interlocked asperities [3, 13, 15]. In addition, the change of joint aperture from the interlocked state to the dislocated state is closely associated with the movement of dilation during the shear process [21–24]. Moreover, an increase in the initial aperture caused by the asperity degradation has been seen to decrease the dilation in multiple shear tests conducted on the same rock joint [8, 13]. Similarly, the reduced initial porosity has been confirmed to increase the volumetric strain in quartz material [25]. Therefore, the joint aperture is a vital and sensitive parameter that influences and can be used to predict the shear and dilation behavior of rock joints in the shear process.

The present study models the shear behavior of rock joints in conjunction with the dilation of joint apertures. Cyclic loading and unloading tests were carried out to observe the aperture variation of rock joints. The elastoplastic relationship between the normal stress and the relative normal displacement was found to capture the rock joint aperture variation. A modified version of the critical state framework [26, 27] was applied to delineate the rock joint's shearing and dilation behavior in a unified manner. Moreover, the subloading surface concept [28] was

adopted to describe the plastic deformation before the critical state. The applicability of the model was validated by performing direct shear tests and comparing the results with those of the numerical modeling. Parameter analyses were conducted to discuss the effects of the initial apertures on the numerical response of the joint granite specimens.

2 Experimental evidence of compression and shear behavior of rock joint

Granite samples were analyzed to determine the mineral components, while the joint geometry was profiled to quantify the surface roughness. Then, multiple compression tests were carried out in three cycles of loading and unloading to observe the discontinuity's deformation and to calculate the rock joint's aperture. Direct shear tests were subsequently conducted under the constant normal loading condition to investigate the rock joint's shear and dilation behavior.

2.1 Material and methods

Granite specimens were sampled from a quarry located in the Inada district (specimens G1 and G2) and from a tunnel located in the Inagawa district (specimens G3 and G4), Japan. The mineral compositions of the granite specimens were determined by the X-ray diffraction (XRD) method. The Inada samples (G1 and G2) consisted of 56.75% quartz mineral, 42.00% feldspar mineral, and 1.25% biotite mineral. The Inagawa samples (G3 and G4) consisted of 30.10% quartz mineral, 33.67% feldspar mineral, and 36.23% biotite mineral. In addition, uniaxial compressive tests were conducted on intact granite to obtain the uniaxial compressive strength. Direct shear tests with different normal stress levels were conducted on rock with a flat joint

plane to obtain the frictional angle. The mechanical properties of the granite specimens are given in Table 1.

The joint granite specimens were prepared with a cross-section of 120 mm × 80 mm and a height of 120 mm. A single fracture was created along the center horizontal plane of each specimen. The profiled contour maps of the joint surfaces of one specimen (G1) are shown in Fig. 1 as an example. The specimen was placed in a shear box for vertical and horizontal loading tests. The compression and shear units were used to measure the load and displacement in the normal and shearing directions, respectively. An outline of the specimens and apparatus is given in Fig. 2.

For each specimen, the experimental procedure was repeated two times (two cases). Case-1 is the first experimental procedure. It included the surface profiling test and the enclosure of the specimen in the shear box, followed by the uniaxial compressive test and the direct shear test conducted on the specimen within the shear box. After the shear test in Case-1, the sheared rock was moved back to the original position and taken out of the shear box. The debris and gouge materials were removed, and the geometrical surfaces were profiled again. Then, the compression and shear tests were performed for Case-2. In the uniaxial compressive tests, the confining pressure was applied across the rock specimen from the initial loading stress to the final predetermined confining stress in the first loading process. Subsequently, the unloading process back to the initial stress condition was applied. The second and third loading and

unloading cycles were then performed successively under the same confining pressure process. In the following direct shear tests, the corresponding constant normal pressure was loaded on the specimen until reaching the residual state. During the shear process, the constant shear rate of 0.1 mm/min was applied within the standardized shear rate of 0.02-0.2 mm/min (ISRM 1985). The experimental conditions are shown in Table 2. The Joint Roughness Coefficient (*JRC*) value of each joint interface was calculated by the backward analytical method of the Barton-Bandies model [1] and are shown in Table 2.

2.2 Results of compression tests and shear tests

As one example, the compression test results of specimen G1 are plotted in Fig. 3. The non-linear relationship between the normal stress-displacement in the two cases is given in Fig. 3 (a). After experiencing the compression and shear process in Case-1, the degradation of the contact asperities caused the rough surfaces to flatten. Then, the poorly matching conditions begin, and the normal displacement increases remarkably in the second compression process (Case-2). An enlarged view of the process for Case-1 is shown in Fig. 3 (b). Large irreversible displacement is observed in the first loading and unloading cycle. However, the permanent closure seems to disappear during the second and third cycles, and the ensuing loading and unloading process almost follows the same path. The discrepancy in the normal displacement between the first loading path and the latter unloading/reloading paths is attributed to the stress history. Here, the permanent closure in the initial loading process is referred to as irrecoverable

deformation. Simultaneously, the deformation of the normal displacement in the latter process is regarded as recoverable behavior.

As the normal deformation is dependent on the stress history, the maximum closure was measured in the third unloading path. As mentioned in the previous study, the compression behavior can be approximately described by a hyperbolic function [15, 29]. In our study, Fig. 4 shows that the third unloading path of Case-1 for specimen G1 can be approximately fitted as a hyperbolic curve. With the increase in normal stress, the path approaches a vertical line asymptotically. The vertical asymptote represents the maximum normal displacement or the maximum joint closure, which means the joint surfaces have been tightly matched under higher normal stress. The hyperbolic closure model of Bandies [1] was applied to characterize the relationship of the normal stress–displacement of the rock joint. This hyperbolic function is given in Eq. (1).

$$\sigma_n = \frac{v_j k_n V_{mc}}{V_{mc} - v_j} \quad (1)$$

where σ_n , v_j , k_n , and V_{mc} are the normal stress, the normal closure, the normal stiffness of the discontinuous rock mass, and the maximum closure of the joint aperture, respectively.

The joint aperture is defined as the mean distance between the adjacent joint surfaces. In the third unloading path of the compression test, the current joint aperture is calculated by subtracting the normal closure from the maximum joint closure as shown in Fig. 4. According to the fitted hyperbolic curves, the initial aperture in the shear process was regarded as the

current aperture under the corresponding confining stress. The obtained initial apertures in the first process (Case-1) and second shear process (Case-2) are given in Table 2. Comparing the initial apertures and *JRC* values in the two cases of the four joint specimens, the results show that the *JRC* value decreased and the initial aperture expanded after the shear test. After undergoing the crushing of the asperities in the shear process, the decrease in the *JRC* values indicates that the rougher surfaces are shaved to be smooth. Simultaneously, the increase in the initial apertures indicates that the originally tightly matched condition of the adjacent surfaces is declined to the later loosely matched condition. Hence, the expansion of the void space between the lower and upper surfaces is induced. Consequently, applying the same normal stress on the same specimen, enlarged initial apertures occur at the beginning of the second shear process.

The shear stress-shear displacement relationship and the dilation curves of the first shear and second shear tests on the four specimens are shown in Fig. 5. The apparent peak stress and remarkable softening behavior were observed in the first shear process of Case-1. However, the second shear process of Case-2 only shows the hardening behavior and not the salient peak shear strength, except for in the case of specimen G2. During the shear process, the dilation is assumed to equal the relative normal displacement of the upper half of the specimen. The dilation increases with the shear displacement in both the first and second shear experiments. Comparing the shear stress and dilation of the two shear cases, incorporating the initial aperture

given in Table 2, the rock joint with a small initial aperture in the first shear process exhibits higher frictional resistance and larger dilation than the rock joint with a large initial aperture in the second shear process. Therefore, the discrepancy of the shear behavior due to the difference in the initial aperture must be considered in developing a model for rock joints.

3 Elastoplastic model for rock joint considering aperture variation

The aperture variation during the compression process can be obtained according to the fitted hyperbolic curve and asymptote. The relationship between the joint aperture and normal stress can be reconstituted as a straight virgin compression line and a set of straight loading and unloading lines in a semi-logarithmic plot of normal stress and aperture. Fig. 6 shows the variation of aperture during the cyclic loading and unloading tests of Case-1 for specimen G-1.

Here, a permanent change of the aperture was observed in the first loading path; and thus, the variation in joint aperture in the first loading process was regarded as irreversible. The aperture variations in the first unloading path, second loading/unloading paths, and third loading/unloading paths were similar. The aperture variations in these paths are referred to as reversible. The aperture variation of the rock joint from irreversible to reversible behavior is similar to the volumetric transition of soil from the normal consolidation line to the swelling line. The previous study indicated that the crushing of the rock joint's asperity contributes to irreversible fracture deformation, whereas elastic deformation contributes to reversible deformation [20]. Therefore, a hypothesis was conceived whereby the rock joint possesses a

transition from elastoplastic to elastic behavior in the first and latter compression processes. Based on this hypothesis, an elastoplastic model incorporating the aperture variation was introduced for modeling the shear behavior. The repeated loading and unloading process can be simplified by the typical deformation behavior of the first cycle in the rock joint, as exhibited in Fig. 7.

It is assumed that the incremental total relative displacement of the rock joint $d\delta \left(= \begin{pmatrix} d\delta_n \\ d\delta_s \end{pmatrix} \right)$, can be decomposed into elastic component $d\delta^e \left(= \begin{pmatrix} d\delta_n^e \\ d\delta_s^e \end{pmatrix} \right)$ and plastic component $d\delta^p \left(= \begin{pmatrix} d\delta_n^p \\ d\delta_s^p \end{pmatrix} \right)$. Superscripts e and p denote the elastic and plastic parts of the deformation, respectively, and subscripts n and s denote normal and shear components, respectively.

$$d\delta = d\delta^e + d\delta^p \quad (2)$$

3.1 Elastic stress–relative displacement relationship

According to the elastic behavior of the rock joint, shown in Fig. 7, the elastic stress–relative normal displacement relationship is assumed as

$$\delta_n^e = \kappa \ln \frac{\sigma_n}{\sigma_{n0}} \quad (3)$$

where κ is the unloading compression index, σ_n is the current normal stress, and σ_{n0} is the initial normal stress where $\delta_n^e = 0$. Applying Taylor's expansion, Eq. (3) can be rewritten in the following incremental form:

$$d\sigma_n = \frac{\sigma_n}{\underbrace{\kappa}_{k_n}} d\delta_n^e \quad (4)$$

where k_n is the normal stiffness dependent on the confining pressure, σ_n . Then, an elastic relationship is assumed as

$$d\boldsymbol{\sigma} = \underbrace{\begin{bmatrix} k_n & k_{ns} \\ 0 & k_s \end{bmatrix}}_{\mathbf{D}^e} d\boldsymbol{\delta}^e \quad (5)$$

where $d\boldsymbol{\sigma} \left(= \begin{pmatrix} d\sigma_n \\ d\sigma_s \end{pmatrix} \right)$ is the incremental traction vector, $\mathbf{D}^e$ is the elastic stiffness tensor, and k_s is the shear stiffness. For the dilatant joint, the joint normal stress depends on both the normal stiffness and the shear displacement [30]. Hence, k_{ns} is proposed to describe the stiffness controlling the effect of shearing on the confining stress. Two ratios, α and μ , are introduced to link shear stiffness with normal stiffness.

$$k_s = \mu k_n \quad (6)$$

$$k_{ns} = \alpha k_n \quad (7)$$

Moreover, the joint aperture variation, Δb , is considered to be equal to the relative normal displacement during the compression tests.

$$-\Delta b_n^e = \delta_n^e \quad (8)$$

Here, the compression direction is positive for the normal elastic displacement, δ_n^e .

3.2 Yield function considering the change in aperture

From the experimental evidence, the shear stiffness, shear strength, and dilation are primarily controlled by the aperture. A smaller aperture in a rock joint corresponds to larger

joint stiffness, shear strength, and dilation. A larger aperture in a rock joint results in smaller joint stiffness, shear strength, and dilation. The effects of the joint aperture on the above aspects are similar to the effects of the specific volume (void ratio) on soils/intact rocks. Moreover, an asymptotic critical state is reached at very large shear displacement. At the critical state, shear displacement increases without any further changes in the shear stress ratio and joint aperture. The shear stress ratio at the critical state is a unique, constant value specific to the rock joint. The joint aperture at the critical state is also a unique value given as a function of normal confining stress. These properties are likewise analogous to the critical state of soils and weak rocks. In the present study, the kernel concept assumes that

a) A unique critical state line in the space of confining pressure, shear stress, and aperture plays a central role in modeling a rock joint's behavior.

b) A rock joint's response is controlled by the difference of joint apertures between the current and the critical states. A joint having smaller apertures exhibits higher stiffness, strength, and dilation.

The procedure for developing the model is given below.

At a shear stress ratio, $\frac{\sigma_s}{\sigma_n}$, of zero, aperture b is assumed to stay on the first normal loading/compression line (NCL) or lower.

$$b \leq b_n - \lambda \ln \frac{\sigma_n}{p_a} \quad (9)$$

Here, b_n is the joint aperture on the first normal loading line under atmospheric pressure. λ is the slope of the first normal loading line, and p_a (= 98 kPa) is the atmospheric pressure.

After applying large shear displacement, the rock joint eventually leads to the critical state.

The aperture on the critical state line (*CSL*) is given as

$$b = b_s - \lambda \ln \frac{\sigma_n}{p_a} \quad (10)$$

where b_s is the aperture on the critical state line at $\sigma_n = P_a$.

In this study, the cyclic loading and unloading tests were conducted before the shear process. The influence of the stress history was considered in the modeling. Barton [4] claimed that the influence of the stress history on the rock joints is similar to that on the soil. The terminology “over-closed” was proposed to distinguish the normally-loaded and the pre-loaded joints, which, in concept, is close to the over-consolidated state of soil material [1, 10, 14, 31]. Here, after the cyclic loading/unloading process, the rock joint is defined at the over-closed state. Under the constant normal load condition, it finally reaches the critical state after the shear process. The aperture variation is shown in **Fig. 8**.

Aperture b_{sbs} on the state boundary surface can be obtained by

$$b_{sbs} = b_n - (b_n - b_s)\zeta(\eta) - \lambda \ln \frac{\sigma_n}{p_a} \quad (11)$$

where $\zeta(\eta)$ is an increasing function of the stress ratio. It satisfies $\zeta(0) = 0$ on the compression line and $\zeta(M) = 1$ on the *CSL*. In this study, the state function is defined as

$$\zeta(\eta) = \frac{\ln \left\{ 1 + \left(\frac{\eta}{M} \right)^2 \right\}}{\ln 2} \quad (12)$$

In the present study, the subloading surface concept was adopted to describe the plastic closure induced by the stress inside the yield surface. It is an unconventional elastoplastic model that satisfies the mechanical requirements involving the continuity condition and the smoothness condition [28]. State parameter Ω is introduced to describe the distance between the current state and the state boundary surface. Based on this concept, the stress inside the yield surface can smoothly approach the state boundary surface. **Fig. 9** illustrates the modeling of the aperture with state parameter Ω . The distance of the current aperture from the state boundary surface is represented as

$$\Omega = b_{sbs} - b = b_n - (b_n - b_s)\zeta(\eta) - \lambda \ln \frac{\sigma_n}{p_a} - b \quad (13)$$

Then, combining the subloading concept and the critical state, the arbitrary aperture is obtained by rewriting Eq. (13), as follows:

$$b = b_n - (b_n - b_s)\zeta(\eta) - \lambda \ln \frac{\sigma_n}{p_a} - \Omega \quad (14)$$

The initial aperture, b_0 , is calculated by inputting the initial normal stress as $\sigma_n = \sigma_{n0}$, the shear stress as $\sigma_s = 0$, and the stress ratio as $\eta = 0$ in Eq. (15).

$$b_0 = b_n - \lambda \ln \frac{\sigma_{n0}}{p_a} - \Omega_0 \quad (15)$$

The increment of aperture, Δb , is the magnitude from the initial state to the current state. Δb can be calculated by substituting Eq. (14) into Eq. (15).

$$\Delta b = (b_n - b_s)\zeta(\eta) - \lambda \ln \frac{\sigma_n}{\sigma_{n0}} + (\Omega - \Omega_0) \quad (16)$$

By substituting Eqs. (3), (10), and (16) into Eq. (2), plastic displacement deformation $\Delta\delta_n^p$ can be obtained.

$$\Delta\delta_n^p = (b_n - b_s)\zeta(\eta) + (\lambda - \kappa) \ln \frac{\sigma_n}{\sigma_{n0}} + (\Omega - \Omega_0) \quad (17)$$

From Eq. (17), the yield function involves the variation of aperture and can be written as follows:

$$f = (b_n - b_s)\zeta(\eta) + (\lambda - \kappa) \ln \frac{\sigma_n}{\sigma_{n0}} + (\Omega - \Omega_0) - \delta_n^p \quad (18)$$

In the condition of $d\delta_n^p = 0$, from Eq. (17), the evolution of Ω can be given as

$$d\Omega = -(b_n - b_s)\zeta(\eta) - (\lambda - \kappa) \ln \frac{d\sigma_n}{\sigma_n} \quad (19)$$

or for $d\delta_n^p \neq 0$, Ω gradually reaches zero with the plastic movement.

$$d\Omega = -R(\Omega)|d\delta^p| \quad (20)$$

where $R(\Omega)$ is a function of Ω . Parameter ω is introduced to describe the rate of plastic strain approaching the normal yield surface.

$$R(\Omega) = \omega\Omega^2 \quad (21)$$

3.3 Associated flow rule

The associated flow rule is adopted in the proposed model for simplicity. Potential plastic function g is assumed to equal yield function f . The increment in plastic displacement is calculated by

$$d\delta^p = d\Lambda \frac{\partial f}{\partial \sigma} \quad (22)$$

$$\begin{pmatrix} d\delta_n^p \\ d\delta_s^p \end{pmatrix} = d\Lambda \begin{pmatrix} \frac{\partial f}{\partial \sigma_n} \\ \frac{\partial f}{\partial \sigma_s} \end{pmatrix} \quad (23)$$

where $d\Lambda$ is a plastic multiplier.

At the critical state ($\eta = M$) and under the continuous loading condition ($d\Lambda > 0$), the increment in relative plastic displacement is $d\delta_n^p = 0$. Then, b_s can be calculated by

$$b_s = b_n - \ln 2(\lambda - \kappa) \quad (24)$$

3.4 Elastoplastic stress-relative displacement relationship

During elastoplastic displacement deformation, the stress stays on the yield surface, and the yield function is equal to zero. The consistency condition is satisfied as

$$df = \frac{\partial f}{\partial \sigma} d\sigma + \frac{\partial f}{\partial \delta_n^p} d\delta_n^p + \frac{\partial f}{\partial \Omega} d\Omega = 0 \quad (25)$$

Substituting Eqs. (2), (4), (20), and (21) into Eq. (23), the plastic multiplier is calculated as

$$d\Lambda = \frac{\frac{\partial f}{\partial \sigma} : \mathbf{D}^e : d\delta}{\frac{\partial f}{\partial \sigma_n} + \frac{\partial f}{\partial \sigma} : \mathbf{D}^e : \frac{\partial f}{\partial \sigma} + R(\Omega) \left\| \frac{\partial f}{\partial \sigma} \right\|} \quad (26)$$

The elastic relationship is given by incorporating Eq. (22).

$$d\sigma = \mathbf{D}^e : (d\delta - d\delta^p) = \mathbf{D}^e : \left(d\delta - d\Lambda \frac{df}{d\sigma} \right) \quad (27)$$

Then, the elastoplastic stress-strain relationship can be expressed as

$$d\sigma = \left[\mathbf{D}^e - \frac{\mathbf{D}^e : \frac{\partial f}{\partial \sigma} \otimes \frac{\partial f}{\partial \sigma} : \mathbf{D}^e}{\frac{\partial f}{\partial \sigma_n} + \frac{\partial f}{\partial \sigma} : \mathbf{D}^e : \frac{\partial f}{\partial \sigma} + R(\Omega) \left\| \frac{\partial f}{\partial \sigma} \right\|} \right] : d\delta \quad (28)$$

Here, $\mathbf{D}^{ep}$ is the elastoplastic stiffness tensor.

$$D^{ep} = D^e - \frac{D^e : \frac{\partial f}{\partial \sigma} \otimes \frac{\partial f}{\partial \sigma} : D^e}{\frac{\partial f}{\partial \sigma_n} + \frac{\partial f}{\partial \sigma} : D^e : \frac{\partial f}{\partial \sigma} + R(\Omega) \left\| \frac{\partial f}{\partial \sigma} \right\|} \quad (29)$$

The effect of changing the aperture on the shearing behavior of joints is taken into account properly. An elastoplastic model is proposed for the interface between intact rock masses. In addition, a unified description of the stiffness, strength, and dilation characteristics can be achieved by applying the modified critical state theory. The model can be easily implemented to joint/interface elements in the FEM or FDM [32, 33]. Thus, the application of the model to practical issues is relatively easy.

3.5 Determination of constitutive parameters

Use of the constitutive model reported in this paper requires the specifications of the compression indexes, initial apertures, and critical state stress ratio. The constitutive parameters (λ , κ , and b_0) can be determined by cyclic loading and unloading tests. Loading compression index λ and unloading compression index κ are the slope of the first loading line and the slope of the first unloading line in the semi-logarithmic plot, respectively. Initial aperture b_0 can be measured from the third unloading process by subtracting the normal closure from the maximum closure. Critical state stress ratio M can be calibrated from the results of the direct shear tests.

Parameter b_n is the average aperture under atmospheric pressure that corresponds to the theoretical maximum value of the average aperture. This parameter is obtained from a backward

analysis. The value is assumed to equal the calibrated results for the aperture at the residual state. The rest of the parameters (α , μ , and ω), which control the deformation of the horizontal and vertical directions, and the rate of plastic strain, can be obtained by fitting the results of a numerically simulated test to the results of the direct shear experiment.

4 Model prediction

To validate the capability of the proposed model, the shear behavior of discontinuous rock masses was analyzed. Comparisons were made between the numerical simulation responses and the experimental results from the direct shear tests. The cases under consideration include the first shear process and the second shear process of the four granite specimens, which have different initial apertures, uniaxial compressive strength, and confining pressure.

4.1 Direct shear tests on discontinuous rock masses

The fresh joint before the shear process is seen to have a relatively smaller initial aperture than afterwards, since the upper and lower joint surfaces of the specimen match well. The first shear process was conducted on four jointed granite specimens to check the numerical simulation result. The constitutive parameters are shown in **Table 3**. **Fig. 10** presents a comparison between the first shear experimental and numerical simulation results for the four granite specimens. The comparison results demonstrated that the numerical simulation results have an excellent agreement with the experimental results for the four fresh rock joints with different initial apertures. It was confirmed that the proposed model is able to capture the

softening tendency of the shear process and the tendency of dilatancy in the discontinuous rock mass. The peak and residual shear stress can be predicted by the proposed model. Moreover, a good concordance can be observed between the experimental and numerical curves of dilation. For the fresh specimens, the peak strength in the experimental results occurs later or earlier than in the analytical prediction. These observations suggest that the fresh upper and lower surfaces need a small horizontal displacement to be tightly contacted and perfectly matched. The inaccuracies in the peak shear displacement between the experiment and the analysis stem from the initial contact condition in the shear box. The deviated displacement principally depends on the conditions of the experimental set-up.

The second shear process conducted on the four jointed granite specimens was also utilized to validate the proposed model. The constitutive parameters are shown in **Table 4**. After the first shear process, the breaking of the asperity creates a loosely matched joint and then causes an enlargement of the initial aperture. The initial apertures of the four sheared specimens increased to a certain extent more than the initial apertures of the fresh samples, respectively. Moreover, the loading/unloading compression indices also increased after the shear process. **Fig. 11** shows a comparison between the experimental and numerical simulation results of the second shear process for the four sheared specimens. The constitutive model shows a good agreement with the evolution of the dilation during the shear process. Moreover, the constitutive model can capture the hardening tendency of the sheared rock joints. The peak strength is

reasonably well predicted by the model, although specimen G2 of the second shear process still shows large peak strength in the initial shear phase. This peak strength is attributed to the presence of the remaining rough asperity on the interfaces, which is not taken into account in the proposed model.

Overall, the softening and hardening behavior in the first and second shear processes was properly described by the proposed model, respectively. The aperture dilation was also well captured during the two shear processes. Moreover, the relationship between the initial aperture and the shear strength and dilation was confirmed by the analysis model. The smaller initial aperture in the fresh rock joints tends to cause the apparent peak shear strength and larger dilation. Conversely, the larger initial aperture in the sheared rock joints demonstrates the non-salient peak shear strength and smaller dilation. The influence of the initial aperture on the mechanical behavior is discussed in the following section.

4.2 Parametric study via the proposed model

The influence of the initial aperture on the numerical shear response was investigated by applying the developed model. The constitutive parameters for specimen G1 in Case-1 and the same constant confining stress were employed to simulate the shear stress, the normal displacement, and the aperture dilation during the shear process. The analysis was performed with different initial apertures ranging from 0.01 mm to 0.12 mm. **Fig. 12** shows the effect of the different initial apertures on the shear behavior of specimen G1.

From **Figs. 12 (a) and (b)**, it is observed that the initial aperture significantly affects the shear stress and the normal displacement in the numerical simulation. As with the initial aperture increasing, both the peak shear stress and the dilation of the normal displacement decrease during the shear process. Namely, the smaller initial aperture corresponds to the higher peak shear strength and the more significant dilation. This tendency coincides with the present experimental results in the first and second shear process. Meanwhile, the responses whereby the open rock joints have lower frictional resistance and small dilation than the closed rock joints were also confirmed by the previous study [13, 34]. **Fig. 12 (c)** presents the aperture evolution, with different initial values, predicted by the proposed model. In contrast with the larger initial aperture, the smaller aperture must deform greatly to reach the final aperture state.

5 Conclusion

This study highlighted the variation and the effect of the joint aperture in cyclic compression tests and repeated shear tests. An elastoplastic model was proposed for rock joints incorporating the critical state concept and the aperture variation.

The model performance was validated by predicting the experimental results of rock joints. The hardening and softening shear behavior in the first and second shear processes was successfully described by the proposed model. Moreover, the dilation behavior in the fresh and sheared rock joints was also replicated during the two shear processes. The parameter study showed that the initial aperture controls the peak shear strength and dilation of rock joints. It

was seen that a rock joint mass with a small initial aperture tends to cause the apparent peak shear stress, while a rock joint mass with a larger initial aperture usually reaches the final shear state without salient peak shear stress. In addition, it was found that a small initial aperture usually responds to the great normal displacement during the shear process.

The proposed model is an elastoplastic model for the interface between intact rock masses. A unified description of the stiffness, strength, and dilation characteristics can be achieved by applying the modified critical state theory. Thus, the developed model can be readily employed in the analysis methods by incorporating the joint aperture.

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492

List of symbols

493	σ_n, σ_{n0}	normal stress and initial normal stress
494	v_j	closure of joint aperture
495	V_{mc}	maximum closure of joint aperture
496	δ	total relative displacement
497	σ	traction vector
498	δ^e, δ^p	elastic and plastic components of total relative displacement
499	δ_n, δ_s	normal relative displacement and shear relative displacement
500	δ_n^e, δ_s^e	elastic component of normal and shear relative displacement
501	δ_n^p, δ_s^p	plastic component of normal and shear relative displacement
502	λ, κ	loading compression index and unloading compression index
503	k_n, k_s	normal stiffness and shear stiffness
504	k_{ns}	stiffness controlling effect of shearing on confining stress
505	D^e, D^{ep}	elastic stiffness tensor and elastoplastic stiffness tensor
506	μ, α	constant coefficients
507	$b, \Delta b$	joint aperture and joint aperture variation
508	b_n, b_s	joint aperture on first normal loading line and critical state line under atmospheric pressure
509	b_{sbs}	joint aperture on state boundary surface
510	$\eta, \zeta(\eta)$	stress ratio and function of stress ratio
511	M	critical state stress ratio
512	$\Omega, R(\Omega)$	distance of current joint aperture from state boundary surface and function of Ω
513	ω	rate of plastic strain approaching normal yield surface
514	f, g	yield function and potential plastic function
515	$d\Lambda$	plastic multiplier
516		

Tables and Figures

517

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544

Table 1 Mechanical properties of granite specimens

Specimen No.	Uniaxial compressive strength [MPa]	Basic friction angle [°]	Normal stiffness [MPa/mm]
G1	140.31	38.8	60.85
G2	140.31	38.8	60.85
G3	80.5	42.3	2.673
G4	80.5	42.3	2.673

Table 2 Experimental conditions

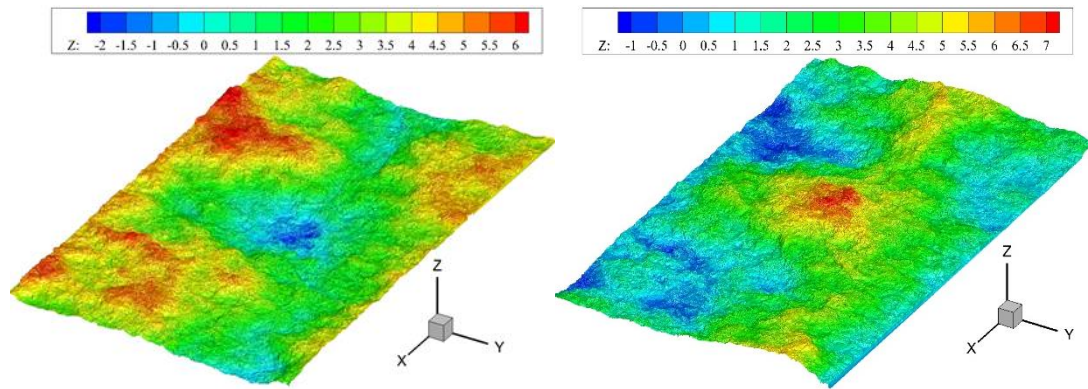
Specimen No.	Case No.	Compression test Loading stress (σ_n , MPa)	Shear test Loading stress (σ_n , MPa)	Joint roughness coefficient (<i>JRC</i>)	Initial joint aperture (b_0 , mm)
G1	Case-1	0.5-3.0	3.0	13.45	0.0285
	Case-2	0.3-3.0	3.0	3.84	0.0449
G2	Case-1	0.3-3.0	3.0	16.15	0.0043
	Case-2	0.3-3.0	3.0	8.53	0.0654
G3	Case-1	0.1-1.0	1.0	20.93	0.0147
	Case-2	0.1-1.0	1.0	9.74	0.0283
G4	Case-1	0.1-1.0	1.0	18.81	0.0243
	Case-2	0.1-1.0	1.0	8.50	0.0451

Table 3 Constitutive parameters for rock joint before shear process

Index	Parameter	G-1	G-2	G-3	G-4
λ	Loading compression index	0.0191	0.0320	0.0423	0.0560
κ	Unloading compression index	0.0021	0.0069	0.0302	0.0355
M	Critical state stress ratio	0.9459	0.9459	0.9099	0.9099
b_n	Average aperture under atmospheric pressure	1.2	1.2	1.2	1.2
b_0	Initial aperture	0.0285	0.0043	0.0147	0.0243
μ	Ratio between k_s and k_n	1	1	1	1
α	Ratio between k_{ns} and k_n	0.1	0.3	0.3	0.3
ω	Rate of the evolution	0.85	1.40	0.85	0.80

Table 4 Constitutive parameters for rock joint after shear process

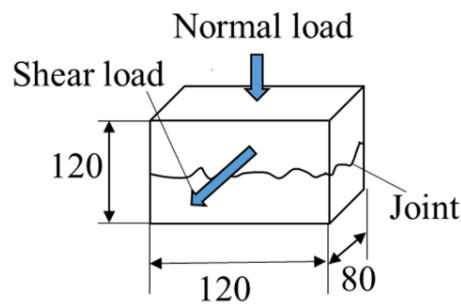
Index	Parameter	G-1	G-2	G-3	G-4
λ	Loading compression index	0.0703	0.1806	0.0763	0.0969
κ	Unloading compression index	0.0216	0.0868	0.0691	0.0895
M	Critical state stress ratio	0.9459	0.9459	0.9099	0.9099
b_n	Average aperture under atmospheric pressure	1.2	1.2	1.2	1.2
b_0	Initial aperture	0.0449	0.0654	0.0283	0.0451
μ	Ratio between k_s and k_n	1	1	1	1
α	Ratio between k_{ns} and k_n	0.2	0.5	0.2	0.2
ω	Rate of the evolution	0.01	0.60	0.10	0.10



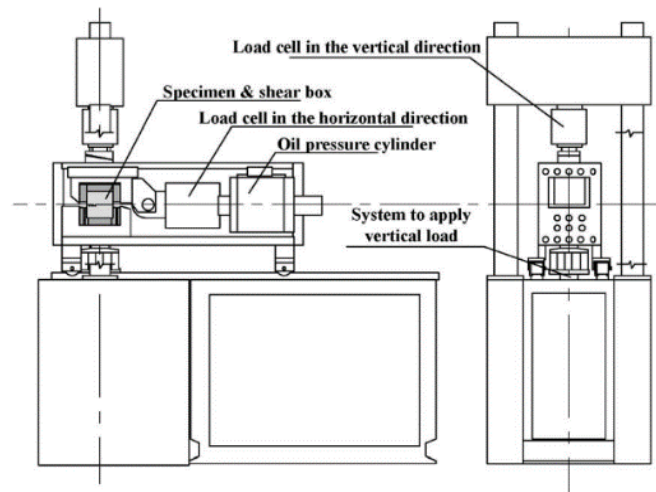
(a) Lower surface of G1

(b) Upper surface of G1

Fig. 1 Contour map of joint surface roughness of specimen G1: (a) Lower surface of G1 and (b) Upper surface of G1

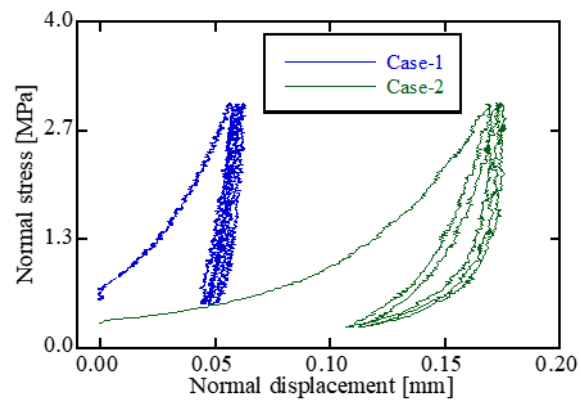


(a)

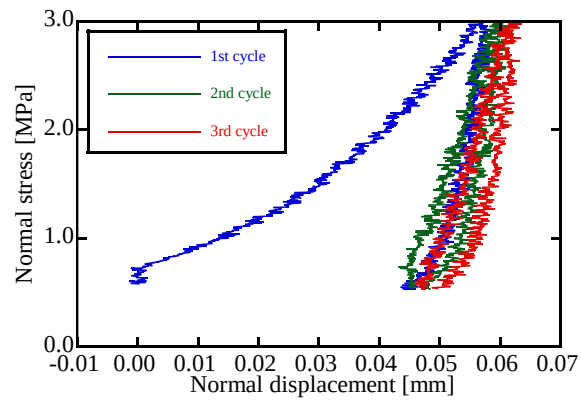


(b)

Fig. 2 Outlines of rock sample and apparatus: (a) Rock sample with single joint and (b) Apparatus including compression and shear unit [35]



(a)



(b)

Fig. 3 Normal displacement-stress relation of cyclic loading and unloading tests in granite specimen G1: (a) Overview and (b) Enlarged view of Case-1

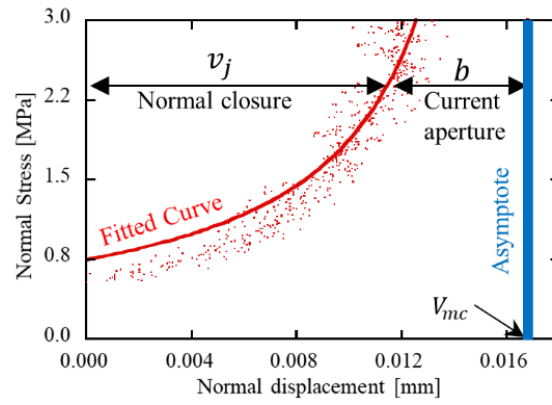
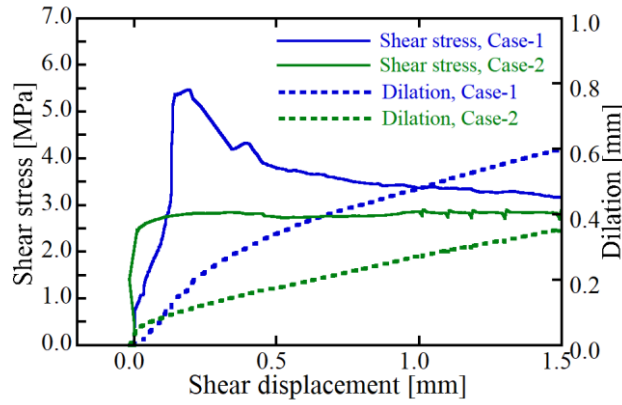
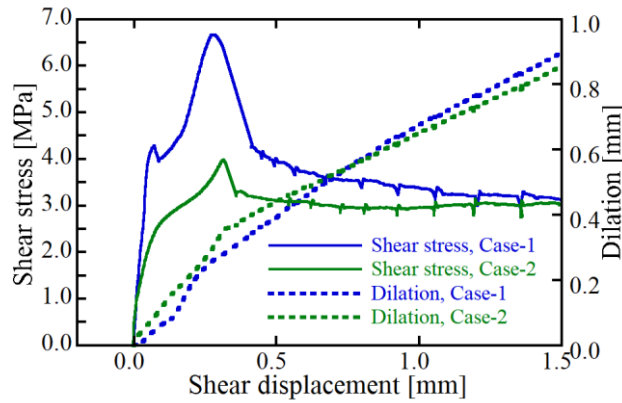


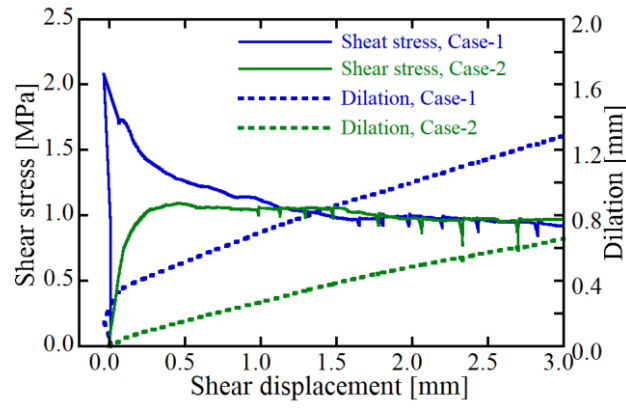
Fig. 4 Fitted hyperbolic curve of third unloading path of Case-1 in specimen G1



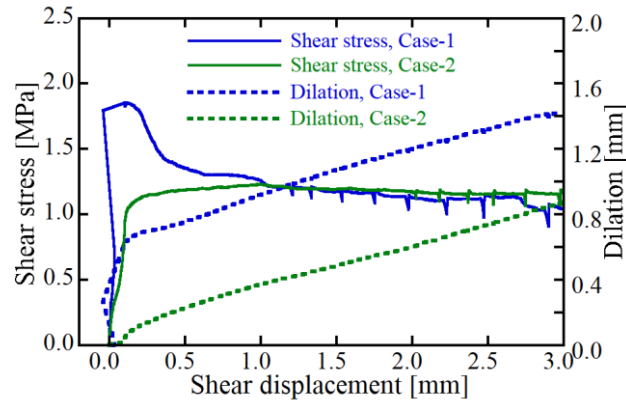
(a)



(b)



(c)



(d)

Fig. 5 Shear displacement-stress relationship of two cases in four granite specimens: (a) Case-1 and (b) Case-2

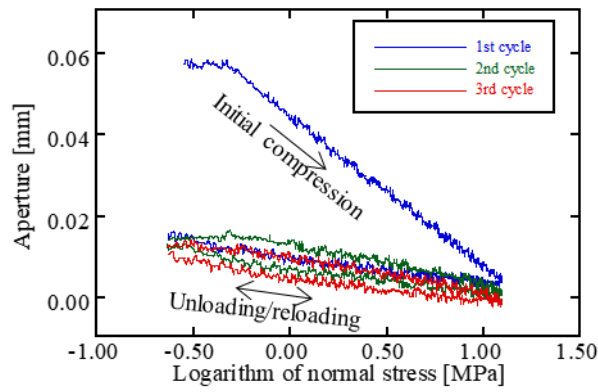


Fig. 6 Aperture evolution during compression tests of Case-1 in specimen G1

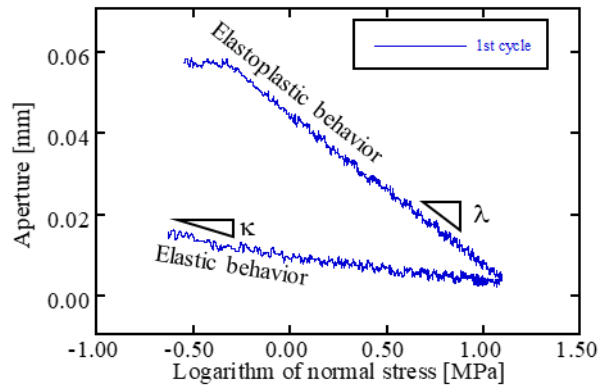


Fig. 7 Typical deformation behavior of Case-1 in specimen G1

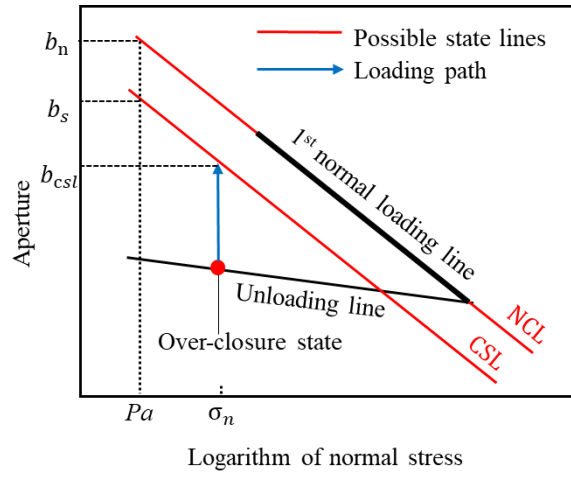


Fig. 8 Modeling of aperture in rock joint

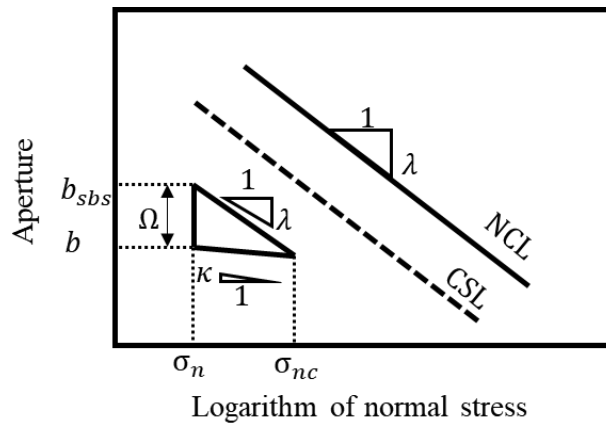
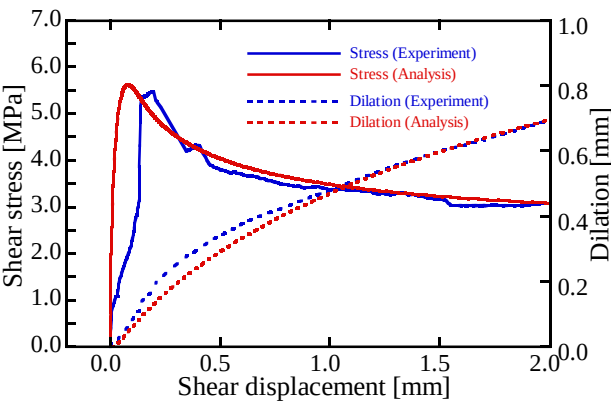


Fig. 9 Modeling of aperture in rock joint with state parameter Ω

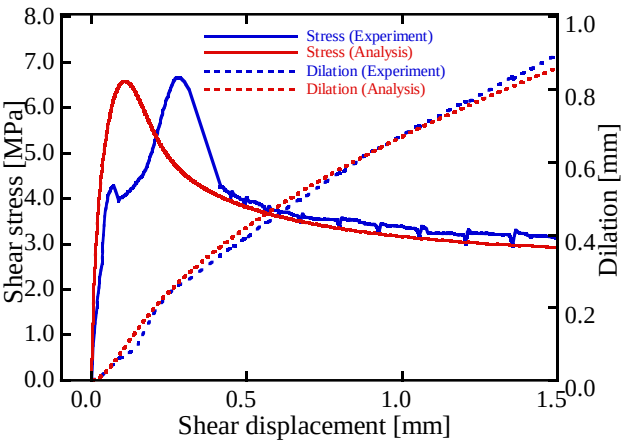
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(a)

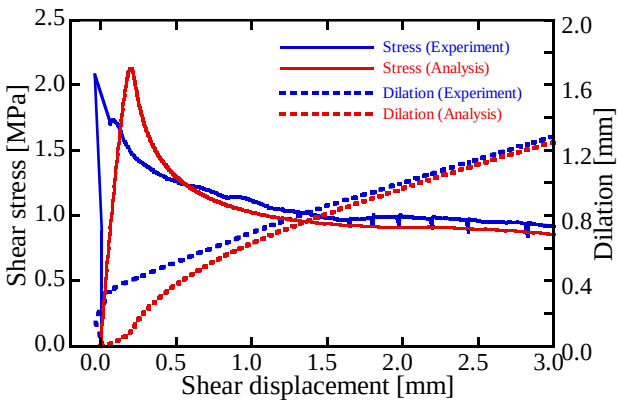


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(b)

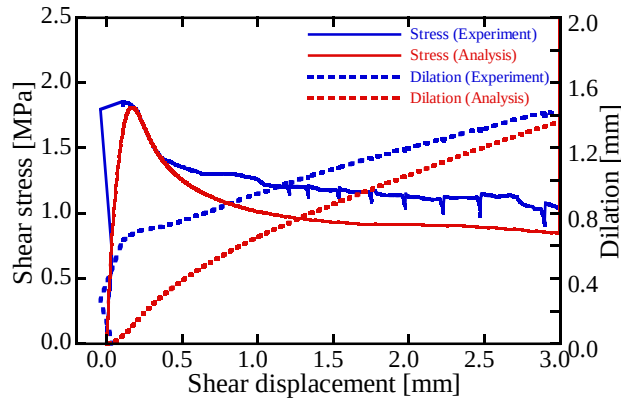


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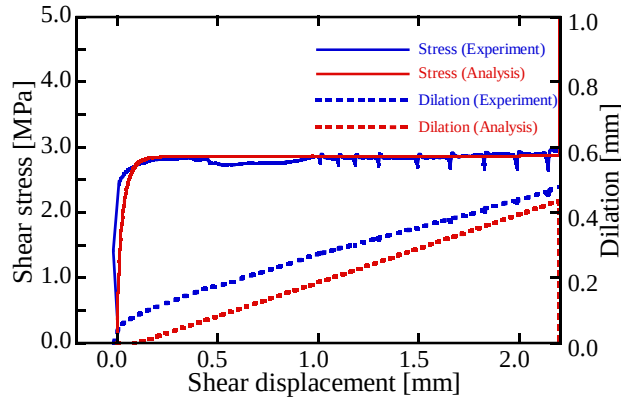
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(c)

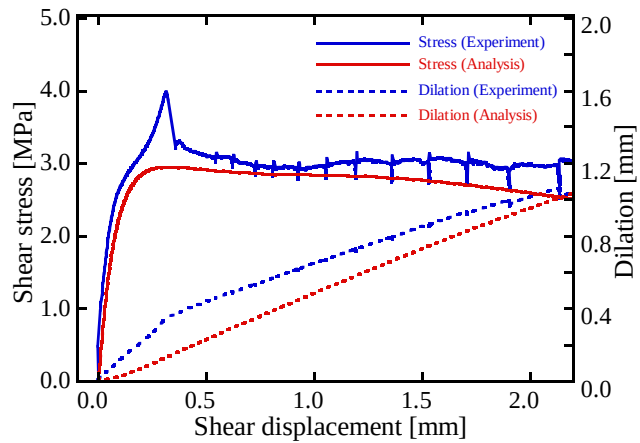


(d)

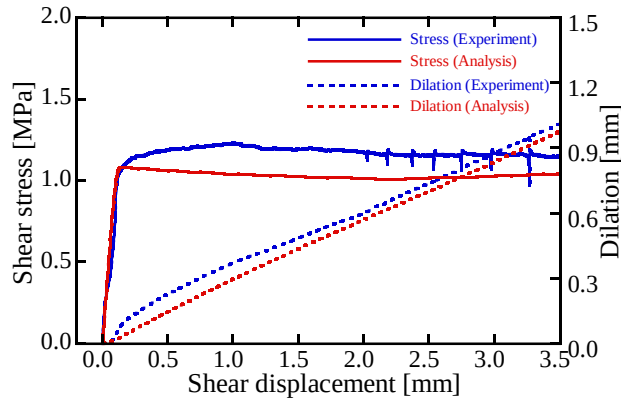
Fig. 10 Comparison of first shear experimental and numerical simulation results on four granite specimens: (a) Specimen G1 under confining stress of $\sigma_n=3$ MPa, (b) Specimen G2 under confining stress of $\sigma_n=3$ MPa, (c) Specimen G3 under confining stress of $\sigma_n=1$ MPa, and (d) Specimen G4 under confining stress of $\sigma_n=1$ MPa



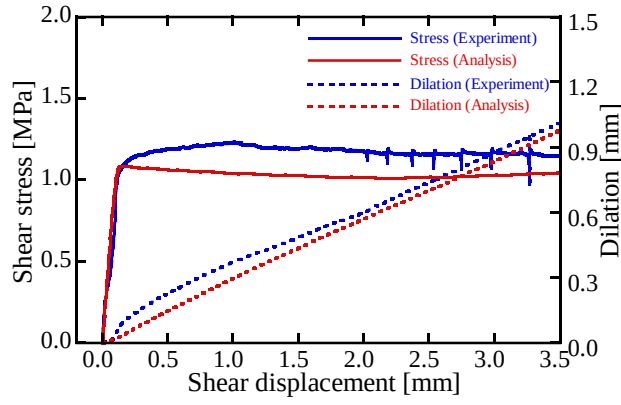
(a)



(b)

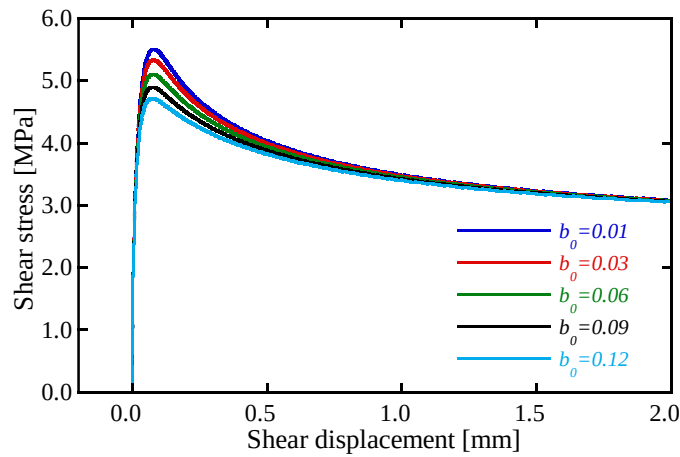


(c)

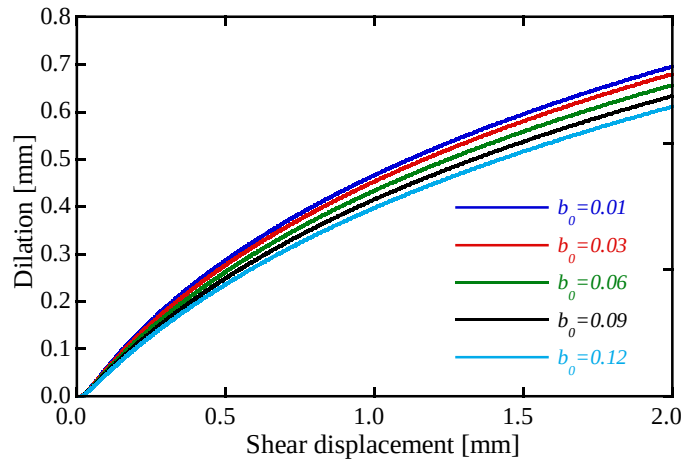


(d)

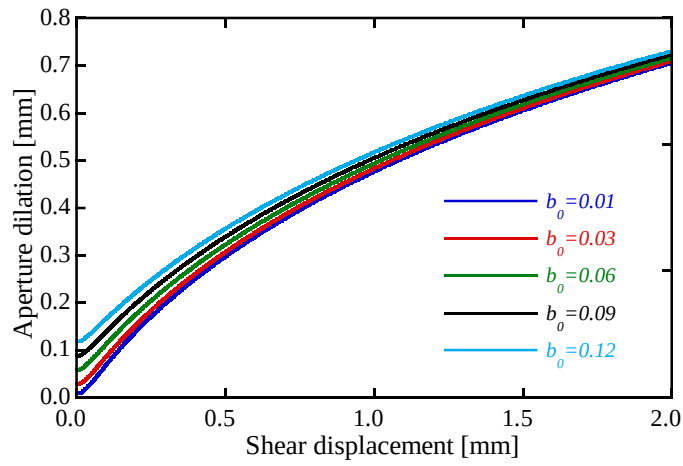
Fig. 11 Comparison of second shear experimental and numerical simulation results on four granite specimens: (a) Specimen G1 under confining stress of $\sigma_n=3$ MPa, (b) Specimen G2 under confining stress of $\sigma_n=3$ MPa, (c) Specimen G3 under confining stress of $\sigma_n=1$ MPa, and (d) Specimen G4 under confining stress of $\sigma_n=1$ MPa



(a)



(b)



(c)

Fig. 12 Simulation results of effect of initial aperture on shear behavior: (a) Influence on shear strength, (b) Influence on normal displacement, and (c) Influence on aperture dilation