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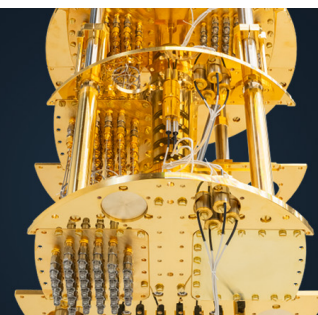
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ABSTRACT

The three-omega method offers a precise and simple technique for measuring the thermal conductivities of a wide range of materials. Utilizing nonlinear data enhances the determination of multiple thermophysical properties at the micro- and nanoscales. However, challenges such as dependence on initial guesses and convergence to local minima render nonlinear fitting processes unstable. This study introduces a machine learning-based approach that addresses these limitations by pre-learning a globally optimal solution. We developed a methodology that processes three-omega signals using machine learning to determine various thermophysical properties. The approach involved compiling results from the analytical three-omega model and augmenting them with Gaussian noise to create a robust machine learning model. Subsequently, a neural network was trained on this dataset. Testing confirmed the model's accurate predictions of volumetric heat capacity and thermal conductivity. Comparative analyses between machine learning-based and conventional fitting methods on the sample data extracted from the test set demonstrated the superior stability of the machine learning model in predicting thermophysical properties. Furthermore, experimental validation was carried out by applying our machine learning model to real-world data from glass and liquid samples. The correspondence between the predicted values and the theoretical curve of the third harmonic voltage affirmed the model's applicability and accuracy in practical scenarios. These findings validate the potential of our machine learning model for robustly predicting thermophysical properties based on actual measured data.

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The heat generation density associated with the miniaturization of semiconductor devices has emerged as a critical issue in recent years,^{1,2} emphasizing the increasingly vital role of materials' thermophysical properties in enhancing device performance. Significant advancements have been made in measurement techniques for these properties, including the transient hotwire technique,^{3,4} Raman spectroscopy,^{5,6} thermoreflectance method,^{7,8} laser flash method,⁹ and the three-omega method.¹⁰ The three-omega method is recognized for its simplicity and precision and measures the thermophysical properties of a diverse array of materials, including bulk materials,^{10–13} thin films,^{14–16} gases,^{17–19} liquids,^{20–23} and soft materials.^{13,15,24} This technique involves passing an alternating current with an angular frequency (ω) through a metal

line heater, generating a third harmonic voltage ($V_{3\omega}$) due to the resistance changes induced by temperature variations.

Our measurements focused on the third harmonic voltage to determine the material's thermophysical properties. In the low-frequency region, the relationship between the third harmonic voltage and frequency is linear, simplifying the estimation of a sample's thermal conductivity. However, for accurate measurements of micro- and nanoscale materials, nonlinear fitting-based analysis is indispensable in higher frequency regions.²² Additionally, the determination of multiple thermophysical properties, such as volumetric heat capacity or thermal boundary conductance, necessitates the use of nonlinear fitting.^{11,22} Despite its utility, nonlinear fitting poses challenges; it is time-intensive

and prone to instability, often leading to errors due to convergence to suboptimal solutions and dependence on initial guesses.

Employing a machine learning method to process measured data presents a robust solution to prevailing challenges, as it is capable of learning globally optimal solutions in advance. Extensive literature reviews and studies have explored the application of machine learning for data processing and property prediction in thermal engineering.^{25–27} For instance, deep learning techniques have been instrumental in estimating thermophysical properties, thereby enhancing our understanding of related phenomena.^{28–31} Moreover, deep learning-based techniques have been integrated into various measurement methods,^{32–35} particularly enriching the analysis capabilities within the field of thermoreflectance.^{36–39} Despite these advancements, the application of machine learning methodologies to three-omega measurements remains underexplored, indicating a significant area for further research.

In this study, a machine learning-based analytical approach was designed for the three-omega method to ensure stable analysis. We constructed machine learning models, specifically neural networks, to predict the thermophysical properties of materials. An analytical database, augmented with Gaussian noise, was employed to train these models. The effectiveness of our machine learning models was corroborated through both analytical and experimental data.

In the analytical phase, a test set derived from the analytical database was utilized to evaluate the precision of the machine learning models' predictions. Comparisons between conventional fitting analyses and machine learning predictions on the test set data demonstrated that machine learning offers more accurate and stable results. Additionally, we analyzed experimentally measured data from solid and liquid samples, confirming the accuracy of the predictions and the overall effectiveness of the machine learning analysis method.

In the three-omega method, an alternating current ($I_0 \cos \omega t$) with an angular frequency (ω) passes through a metal wire heater placed on a substrate, inducing Joule heating that oscillates at a frequency of 2ω . This heating causes the temperature rise of the heater (ΔT) to oscillate at 2ω , which in turn causes the resistance of the heater ($R_0 + \Delta R$) to oscillate at the same frequency. The oscillating resistance, combined with the alternating current, produces a heater voltage component at 3ω , as described by the following equation:

$$V_{3\omega} = \frac{R_0 I_0 \beta}{2} \Delta T, \quad (1)$$

where β represents the temperature coefficient of resistance. Here, note that ΔT , ΔR , and $V_{3\omega}$ are complex amplitudes.

The temperature rise in the heater is influenced by the structure and thermophysical properties of the surrounding materials and is theoretically determined using the heat conduction equation.^{12,14,40,41} In a configuration where multiple material layers are arranged in parallel, the temperature rise can be expressed as follows:

$$\Delta T = \frac{P}{2l\pi} \int_0^\infty \frac{\sin^2(mb)}{(mb)^2 k_j \sqrt{m^2 + q_j^2}} \times \frac{B^+ + B^-}{A^+ B^- - A^- B^+} dm, \quad (2)$$

where P , l , and $2b$ ($l \gg b$) represent the heating power, length, and width of the heater, respectively.¹⁶ q_i denotes the wavenumber in layer i , defined as $q_i = \sqrt{\frac{i2\omega C_i}{k_i}}$, where k_i denotes thermal conductivity and

C_i denotes volumetric heat capacity. The subscript j represents the layer in which the heater is located. In addition, A^+ , A^- , B^+ , and B^- are the elements of complex matrices $\mathbf{A}$ and $\mathbf{B}$ in the matrix formalism.⁴¹

We assume the simplest system consists of an air layer and a sample layer, as depicted in Fig. 1(a), treating both as semi-infinite in the analytical model. The heater is positioned at the interface on the sample layer, with the volumetric heat capacity assumed to be negligible. The system is also assumed to be infinite in the length direction of the heater, and heat conduction is treated as two-dimensional. To evaluate the effectiveness of machine learning model, we constructed a metal line heater on a glass substrate as depicted in Fig. 1(b). In both analytical simulations and experimental setups, the in-phase component of the third harmonic voltage was employed to estimate the thermophysical properties, as this component typically provides more reliable data in the three-omega method.¹⁰

The construction of a machine learning-based data processing system for the three-omega method is outlined in Fig. 1(c). Initially, a theoretical database of third harmonic voltage is generated using the heat conduction model. This database is then segmented into training, validation, and test sets, with respective proportions of 72.25%, 12.75%, and 15%. The machine learning algorithm is trained using the training set, evaluated using the validation set, and the best-performing model during validation is subsequently tested with the test set. It is important to note that the training process relies exclusively on the synthetic database. A detailed discussion of the implications of this approach is provided in Sec. 1 of the [supplementary material](#).

Using Eqs. (1) and (2), the third harmonic voltage is represented by a product of an integral term, $\int_0^\infty \frac{\sin^2(mb)}{(mb)^2 k_j \sqrt{m^2 + q_j^2}} \times \frac{B^+ + B^-}{A^+ B^- - A^- B^+} dm$, and a constant term, $\frac{R_0 I_0 \beta P}{4l\pi}$, as shown below

$$V_{3\omega} = \frac{R_0 I_0 \beta P}{4l\pi} \int_0^\infty \frac{\sin^2(mb)}{(mb)^2 k_j \sqrt{m^2 + q_j^2}} \times \frac{B^+ + B^-}{A^+ B^- - A^- B^+} dm. \quad (3)$$

The parameters not involved in the integral term, such as the temperature coefficient of resistance (β), heater length (l), heater thickness (t_{heater}), electrical resistivity (ρ), and current value (I_0), were fixed, as shown in Fig. 1(c). When experimental data are inputted into the machine learning model, these data are scaled by the fixed parameters and experimental values to conform to the computational conditions of the database, as detailed in Sec. 2 of the [supplementary material](#). Conversely, parameters related to the integral term are treated as inputs to the machine learning model due to the unpredictable effects their variations can have on the signal.

In this model, the inputs for the machine learning algorithm included the third harmonic voltage ($V_{3\omega}$) and half of the heater width (b), as shown in Fig. 1(c). The alternating current frequencies were uniformly set across 100 points on a logarithmic scale, ranging from 1 to 10 000 Hz. The machine learning model outputs were the sample volumetric heat capacity (C_{sample}) and thermal conductivity (k_{sample}). The thermophysical properties of air and other constant parameters are detailed in Table SI of the [supplementary material](#). To construct the machine learning database, 500 000 data points were generated under these specified conditions, with Gaussian noise added to enhance model robustness. The noise levels were set such that the

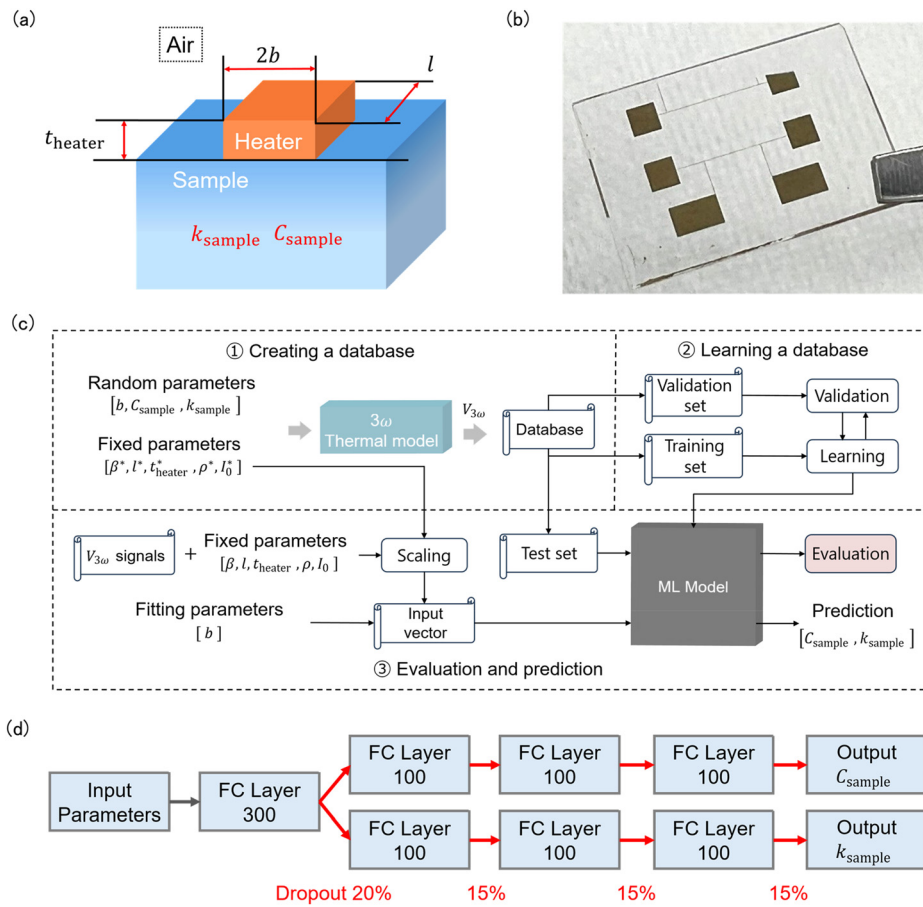


FIG. 1. (a) Configuration of the three-omega sample, consisting of two layers: an air layer and a sample layer, with a gold heater. (b) Example of samples used for experimental validation. (c) Workflow for constructing the machine learning (ML) model and performing validation. Parameters marked with an asterisk indicate fixed values used in database generation. (d) Architecture of the neural network, consisting of fully connected (FC) layers. The dropout of neurons is illustrated with red arrows, and the corresponding dropout rates are labeled.

standard deviation of the third harmonic voltage was 0.5% of the signal at 1 Hz, and for other input parameters, the standard deviation was maintained at 0.2%.

A neural network was employed due to its simplicity and strong representational capacity. To reduce overfitting, dropout^{42,43} was applied, specifically using the Monte Carlo dropout method,⁴³ which involved 1000 stochastic forward passes with dropout enabled. The mean and standard deviation of these predictions were used as the final output and its associated uncertainty, respectively. The network architecture, shown in Fig. 1(d), utilizes exponential linear unit (ELU) activation.⁴⁴ Training was conducted using the root mean squared percentage error (RMSPE) as the loss function, along with the Adam optimizer.⁴⁵ Detailed information regarding the model architecture and training procedure is provided in Sec. 3 of the [supplementary material](#).

The performance of the machine learning model was rigorously assessed using the test set. Evaluation metrics included the mean absolute percentage error (MAPE) and the coefficient of determination R^2 , defined as follows:

$$\text{MAPE} = \frac{100}{n} \sum_{i=1}^n \left| \frac{h(\mathbf{X}_i) - Y_i}{Y_i} \right|, \quad (4)$$

$$R^2 = 1 - \frac{\sum_{i=1}^n (h(\mathbf{X}_i) - Y_i)^2}{\sum_{i=1}^n (Y_i - \bar{Y})^2}, \quad (5)$$

where h represents the output of the machine learning model, $\mathbf{X}_i$, Y_i ($1 \leq i \leq n$) denote the i th input and label data, respectively, and $\bar{Y}$ is the average of the label data.

Table I presents the results of evaluating the predictions and statistical analysis of prediction uncertainty percentages for sample volumetric heat capacity and thermal conductivity using the trained machine learning model. The predicted values compared to the true values are displayed in Figs. 2(a) and 2(b), respectively, for volumetric heat capacity and thermal conductivity. According to Table I, the MAPE for both volumetric heat capacity and thermal conductivity was below 3%. Moreover, Figs. 2(a) and 2(b) demonstrate that the prediction error is less than 10% in most cases, confirming the model's capability to accurately predict the thermophysical properties.

TABLE I. Evaluation and prediction uncertainty of sample volumetric heat capacity (c_{sample}) and thermal conductivity (k_{sample}).

Parameter	Evaluation		Uncertainty %	
	R^2	MAPE %	Mean	Standard deviation
c_{sample}	0.9919	2.375	5.820	1.116
k_{sample}	0.9985	1.313	7.342	0.983

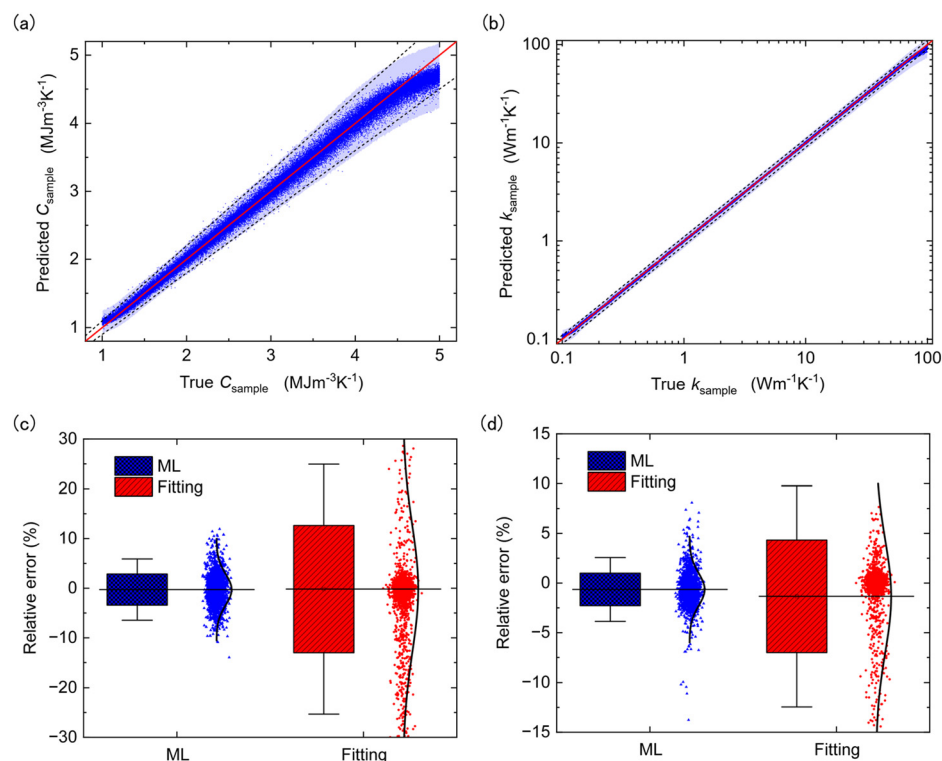


FIG. 2. Predictions from the ML model: (a) Volumetric heat capacity (C_{sample}) and (b) thermal conductivity (k_{sample}) of the sample. Accuracy is indicated when data points are near the solid red line. Black dashed lines represent the $\pm 10\%$ error. Blue shaded regions denote the 95% confidence intervals around the mean predictions. Panels (c) and (d) compare percentage errors in C_{sample} and k_{sample} between our machine learning model and conventional fitting methods. The box plots show the range within one standard deviation, with whiskers extending to the 95% confidence intervals. Individual data and corresponding normal distribution curves are displayed beside each box.

Additionally, we conducted a comparative analysis between the predictions made by our machine learning model and those derived from a conventional fitting algorithm. The comparison utilized a dataset comprising 2000 randomly sampled data points from the test set. The fitting parameters are the volumetric heat capacity (C_{sample}) and thermal conductivity of the sample (k_{sample}). Both methods were evaluated based on the relative error between the obtained and true values, allowing for a direct comparison of predictive accuracy.

Figures 2(c) and 2(d) depict the plot and distribution of the relative error for each data point in the target dataset pertaining to the volumetric heat capacity and thermal conductivity of the sample, respectively. Table II provides a statistical overview of the relative errors for predictions made using both the machine learning model

and the fitting algorithm. The predictions from the fitting algorithm can deviate significantly from the true values, as evidenced in Figs. 2(c) and 2(d). Consequently, the standard deviation, MAPE, and maximum absolute percentage error of the relative errors from our machine learning model are lower than those from the fitting algorithm for each thermophysical property. This difference can be attributed to the robustness of the machine learning-based analysis and the inherent instability of the fitting process, including its sensitivity to initial guesses and its tendency to converge to local minima. Details of the fitting procedure, along with additional simulations supporting this approach, are provided in Sec. 4 of the [supplementary material](#).

Moreover, the effectiveness of our machine learning models was further validated through the processing of actual experimental data. We conducted measurements on the third harmonic voltage from a sample composed of glass and a gold line heater, with a corresponding photograph displayed in Fig. 1(b). The experimental setup is the same as our previous work.²³ By integrating these data into the process outlined in Fig. 1(c) and applying it to our machine learning model, we were able to predict the volumetric heat capacity and thermal conductivity of the sample. The parameters used for the fitting are detailed in Table SIII of the [supplementary material](#).

Figure 3 presents the third harmonic voltage measurements obtained from our experimental setup alongside the theoretical curves derived from the parameters predicted by both the machine learning model and the fitting algorithm. The predicted values for the volumetric heat capacity and thermal conductivity are enumerated in Table III. As demonstrated in Fig. 3, the theoretical curve based on predictions from the machine learning model aligns closely with the experimental data, affirming the model's applicability to real-world data.

TABLE II. Statistics of relative error for predicting sample volumetric heat capacity (C_{sample}) and thermal conductivity (k_{sample}) by machine learning (ML) and fitting algorithm, expressed in percentages.

	C_{sample}		k_{sample}	
	ML	Fitting	ML	Fitting
Mean of percentage error	−0.28	−0.184	−0.648	−1.338
MAPE	2.421	5.678	1.317	2.090
Standard deviation of relative error	3.145	12.82	1.642	5.670
Max absolute percentage error	13.95	95.18	13.77	40.99

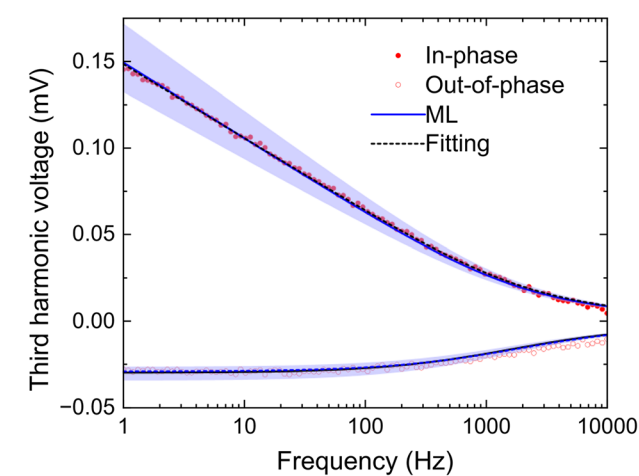


FIG. 3. Experimental signals of the third harmonic voltage. Filled markers represent in-phase component, and unfilled markers represent the out-of-phase component. The solid blue line represents the thermal model predictions based on the outputs from the ML model, while the dashed black line represents the fitting predictions. The shaded region around the solid blue line indicates the 95% confidence interval derived from prediction uncertainty.

TABLE III. Predicted results for sample volumetric heat capacity (C_{sample}) and thermal conductivity (k_{sample}) by ML model and fitting algorithm.

	ML	Fitting
C_{sample} ($\text{MJ m}^{-3} \text{K}^{-1}$)	2.136 ± 0.122	1.890
k_{sample} ($\text{W m}^{-1} \text{K}^{-1}$)	1.214 ± 0.083	1.247

The predicted values for volumetric heat capacity from the machine learning and fitting algorithms exhibited an error of approximately 10%. This variation may stem from the relatively low sensitivity of volumetric heat capacity measurements. This assertion is supported by the greater variation in predictions for volumetric heat capacity compared to thermal conductivity, as detailed in Table II. Additionally, deviations in the out-of-phase component from the theoretical model were particularly noticeable in high-frequency regions. Such deviations are likely influenced by experimental noise and the

precision of the heat conduction model employed to develop the machine learning database. To explore the implications of incorporating out-of-phase components in machine learning models, a detailed discussion is provided in Sec. 6 of the [supplementary material](#).

Furthermore, the effectiveness of the machine learning methodology was also confirmed through measurements on liquid samples using a three-omega sensor based on a parylene substrate, recently developed by our research group.²³ Figure 4(a) depicts the system configuration, which includes three layers: an air layer, a parylene substrate layer, and a sample layer. Figure 4(b) presents an example of a parylene-substrate three-omega sensor. In this setup, it is assumed that thermal boundary resistance exists between the parylene substrate and the sample layers, adding another layer of complexity to the thermal measurements.

In this study, a machine learning model was designed to predict the thermal conductivity of a sample and the thermal boundary conductance between the parylene substrate and the sample layers. Notably, the inputs for the model included the thickness of the parylene substrate (t_{parylene}), the sample's volumetric heat capacity (C_{sample}), and half of the heater width (b). The outputs were the sample's thermal conductivity (k_{sample}) and thermal boundary conductance (G). The parameter ranges, including the thermal conductivity (k_{parylene}) and volumetric heat capacity of the parylene (C_{parylene}), and further details about the architecture of this model and its evaluation on the test set can be found in Sec. 7 of the [supplementary material](#).

The trained model was subsequently applied to experimental data from a previous study²³ on water, isopropyl alcohol (IPA), and their mixtures, as shown in Fig. 5(a). Along with theoretical predictions for thermal conductivity, the predicted values for the sample's thermal conductivity and thermal boundary conductance are shown in Fig. 5(b), and the specific values are listed in Table IV. The theoretical predictions are based on mixing theory.⁴⁶ As shown in Fig. 5(b), errors in the predicted thermal conductivity values compared to the theoretical values were less than 15%. Additionally, the predicted thermal boundary conductance showed an increase with a higher water volume fraction. However, given that parylene substrates are hydrophobic, and IPA exhibits better wettability to these substrates than water,^{47,48} the interpretation of wettability as a factor in thermal boundary conductance is inconsistent with these predictions and warrants further exploration.

This study presented a machine learning-based analytical framework for the three-omega method. An analytical dataset was

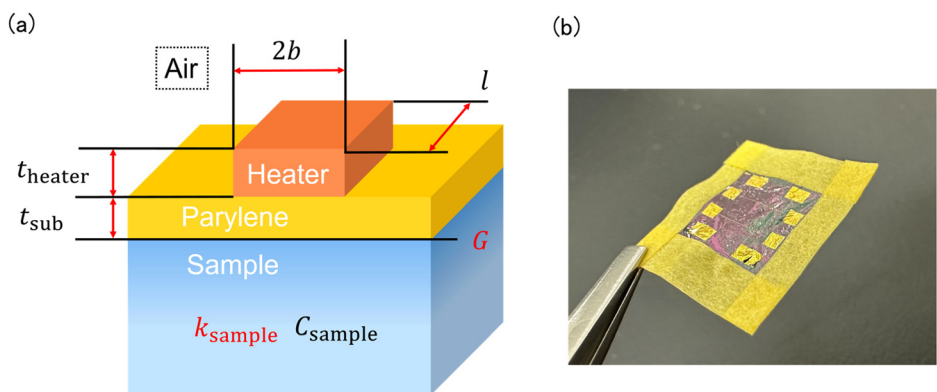


FIG. 4. (a) System configuration of the three-omega sample using a parylene substrate. The system comprises three layers: an air layer, a parylene substrate layer, and a sample layer, with a gold heater integrated. (b) An example of a three-omega sensor based on a parylene substrate.

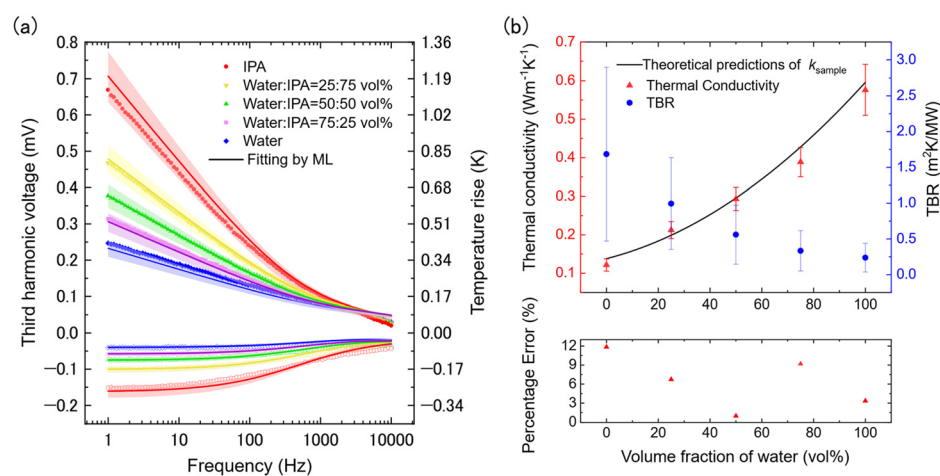


FIG. 5. Validation of predictions using an experimental dataset of water, IPA, and their mixtures. (a) Third harmonic voltage: filled markers indicate the in-phase component, and unfilled markers the out-of-phase component. Solid lines represent thermal model predictions derived from ML model outputs, with shaded regions denoting the 95% confidence intervals. (b) The upper graph shows predicted thermal conductivity (k_{sample}) and thermal boundary resistance (TBR, $1/G$) vs water volume fraction, with theoretical predictions. The lower graph shows the absolute percentage errors of the predicted thermal conductivity compared with theoretical values.

TABLE IV. Theoretical and predicted values of thermal conductivity, along with prediction uncertainties for thermal boundary conductance and thermal conductivity for the experimental dataset comprising water, isopropyl alcohol (IPA), and their mixtures.

Volume fraction of water (vol. %)		0 %	25 %	50 %	75 %	100 %
k_{sample} ($\text{W m}^{-1} \text{K}^{-1}$)	Theoretical value	0.138	0.199	0.296	0.428	0.596
	ML Prediction	0.122	0.213	0.293	0.388	0.576
	Uncertainty	0.008	0.011	0.015	0.019	0.033
G ($\text{M W m}^{-2} \text{K}^{-1}$)	ML Prediction	0.594	1.006	1.786	2.997	4.209
	Uncertainty	0.214	0.324	0.660	1.263	1.783

constructed, and neural network models were developed to predict the thermophysical properties of various samples. Model accuracy was evaluated using a designated test set from the analytical database. In comparison with conventional fitting techniques, the machine learning approach exhibited reduced variability and enhanced robustness. Application to experimental data further confirmed the reliability of the model's predictions, thereby demonstrating the practical effectiveness of the proposed method. We validated the approach by analyzing experimental data obtained from measurements on water, IPA, and their mixtures. These findings suggest that our methodology is adaptable to other systems employing the three-omega method, and we anticipate further developments and applications of this technique in the future.

See the [supplementary material](#) for detailed information about our machine learning methodology and results.

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AUTHOR DECLARATIONS

Conflict of Interest

The authors have no conflicts to disclose.

Author Contributions

Yasuaki Ikeda: Conceptualization (lead); Data curation (lead); Formal analysis (lead); Methodology (lead); Resources (lead); Software (lead); Visualization (lead); Writing – original draft (lead). **Yuki Akura:** Formal analysis (supporting); Methodology (supporting); Software (supporting); Writing – review & editing (supporting). **Ryuto Yamasaki:** Conceptualization (supporting); Formal analysis (supporting); Methodology (supporting); Resources (equal); Software (supporting). **Yuki Matsunaga:** Formal analysis (supporting); Methodology (supporting); Resources (equal). **Lijun Liu:** Conceptualization (supporting); Formal analysis (supporting); Writing – review & editing (supporting). **Masaki Shimofuri:** Conceptualization (supporting); Writing – review & editing (supporting). **Amit Banerjee:** Conceptualization (supporting); Writing – review & editing (supporting). **Toshiyuki Tsuchiya:** Conceptualization (supporting); Project administration (supporting); Writing – review & editing (supporting). **Jun Hirotani:** Conceptualization (lead); Funding acquisition (lead);

Methodology (lead); Project administration (lead); Supervision (lead); Writing – review & editing (lead).

DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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